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## Passive diastolic modelling of human ventricles: Effects of base movement and geometrical heterogeneity

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### ABSTRACT

Left-ventricular (LV) remodelling, associated with diastolic heart failure, is driven by an increase in myocardial stress. Therefore, normalisation of LV wall stress is the cornerstone of many therapeutic treatments. However, information regarding such regional stress-strain for human LV is still limited. Thus, the objectives of our study were to determine local diastolic stress-strain field in healthy LVs, and consequently, to identify the regional variations amongst them due to geometric heterogeneity. Effects of LV base movement on diastolic model predictions, which were ignored in the literature, were further explored. Personalised finite-element modelling of five normal human bi-ventricles was carried out using subject-specific myocardium properties. Model prediction was validated individually through comparison with end-diastolic volume and a new shape-volume based measurement of LV cavity, extracted from magnetic resonance imaging. Results indicated that incorporation of LV base movement improved the model predictions (shape-volume relevancy of LV cavity), and therefore, it should be considered in future studies. The LV endocardium always experienced higher fibre stress compared to the epicardium for all five subjects. The LV wall near base experienced higher stress compared to equatorial and apical locations. The lateral LV wall underwent greater stress distribution (fibre and sheet stress) compared to other three regions. In addition, normal ranges of different stress-strain components in different regions of LV wall were reported for five healthy ventricles. This information could be used as targets for future computational studies to optimise diastolic heart failure treatments or design new therapeutic interventions/devices.

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### 1. Introduction

Epidemiological studies reported that more than half of the patients diagnosed with heart failure (HF) have left-ventricular (LV) diastolic dysfunction with normal systolic pump function (Wang and Nagueh, 2009). LV remodelling process, associated with diastolic heart failure (HF), was identified to be driven by an increase in LV wall stress (Lee et al., 2014, Wall et al., 2006). The LV remodelling is, therefore, increasingly recognized as a potential target for therapeutic interventions, which include the use of

hydrogel injection (Lee et al., 2013a), anisotropic reinforcement (Fomovsky et al., 2012), cardiac support and resistance devices (Lee et al., 2014, Wenk et al., 2013a). The main objective of these surgical interventions was to normalise the LV wall stress at end diastole (ED). Finite element (FE) modelling, in combination with new cardiac imaging modalities and advanced simulation tools, can be used to analyse the diastolic mechanics of healthy heart and identify the normal ranges of stress-strain distribution in LV wall. Such information will provide a greater insight of the physiology and pathophysiology of HF patients, and thereby, predict their response to medical and surgical interventions.

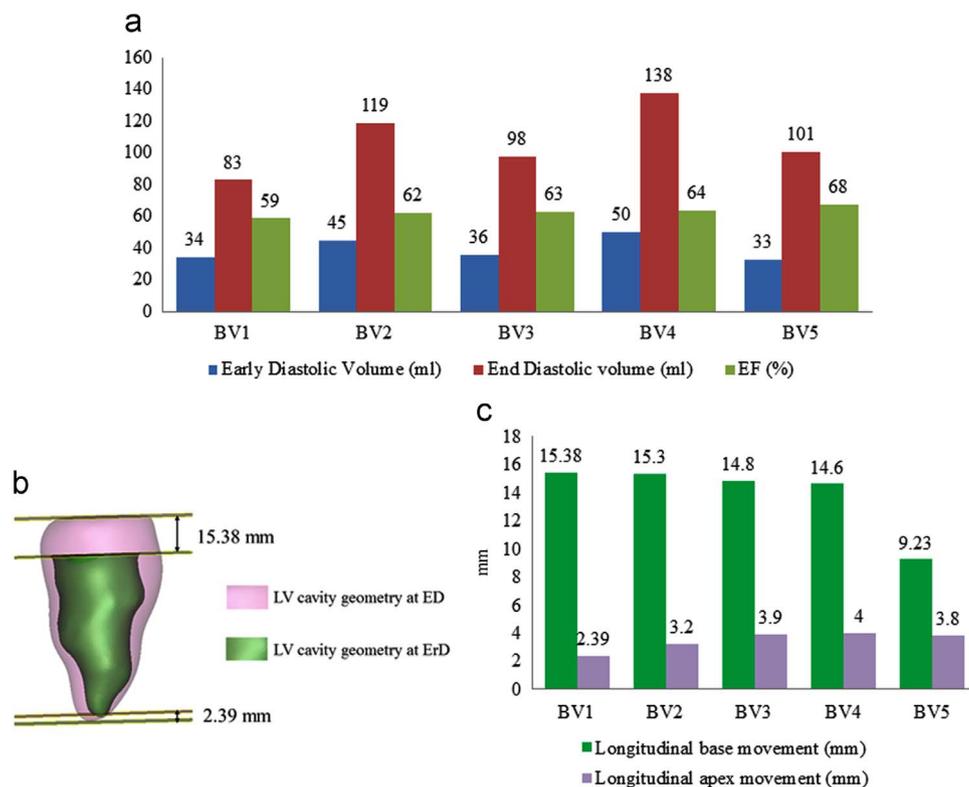
The majority of diastolic FE modelling in existing literature was based on either animal heart or idealised geometry of single LV (Guccione et al., 1995, Costa et al., 1996, Usyk et al., 2000, Vetter and McCulloch, 2000) (Table 1). With the advancement in imaging modalities over the years, subject-specific single LV geometry was used for FE modelling (Wang et al., 2013, Wang et al., 2009, Genet

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**Table 1**  
Previous work on passive diastolic modelling of LV with the key attributes considered in the study.

	Single LV		Bi-ventricle (BV)		Effect of base movement
	Animal myocardium passive properties	Human myocardium passive properties	Animal myocardium passive properties	Human myocardium passive properties	
Animal ventricle /Idealised geometry	Humphrey and Yin (1989) Guccione et al. (1995) Costa et al. (1996) Vetter and McCulloch (2000) Usyk et al. (2000) Wang et al. (2009)	-	Stevens et al. (2003)	-	-
Transversely isotropic	Humphrey and Yin (1989) Guccione et al. (1995) Costa et al. (1996) Vetter and McCulloch (2000) Wang et al. (2009)	Genet et al. (2014)	-	-	-
Human ventricle Orthotropic	Wang et al. (2013) Usyk et al. (2000)	Genet et al. (2014) -	Palit et al. (2015) Stevens et al. (2003) Palit et al. (2015) Göktepe et al. (2011)		Research in this paper
Effect of global Geometric Heterogeneity	-	Genet et al. (2014)	-		



**Fig. 1.** Subject-specific values. (a) Early Diastolic Volume (ErDV), End Diastolic Volume (EDV) and Ejection Fraction (EF) extracted from CMRI of five normal ventricles (BV1 to BV5); (b) Measurement procedure of longitudinal base and apex movement; (c) Longitudinal movement of base and apex measured for five ventricles (BV1 to BV5).

et al., 2014). Recent study by Palit et al. (2015b) showed that the right-ventricle (RV) deformation has a significant effect on LV wall stress distribution and should be considered during ventricular modelling. Furthermore, in majority of the computational models, Fung-type transversely isotropic constitutive law was used (Guccione et al., 1995, Costa et al., 1996, Vetter and McCulloch, 2000, Wang et al., 2009, Genet et al., 2014) (Table 1). In contrast, simple shear test of pig and human myocardium (Dokos et al., 2002,

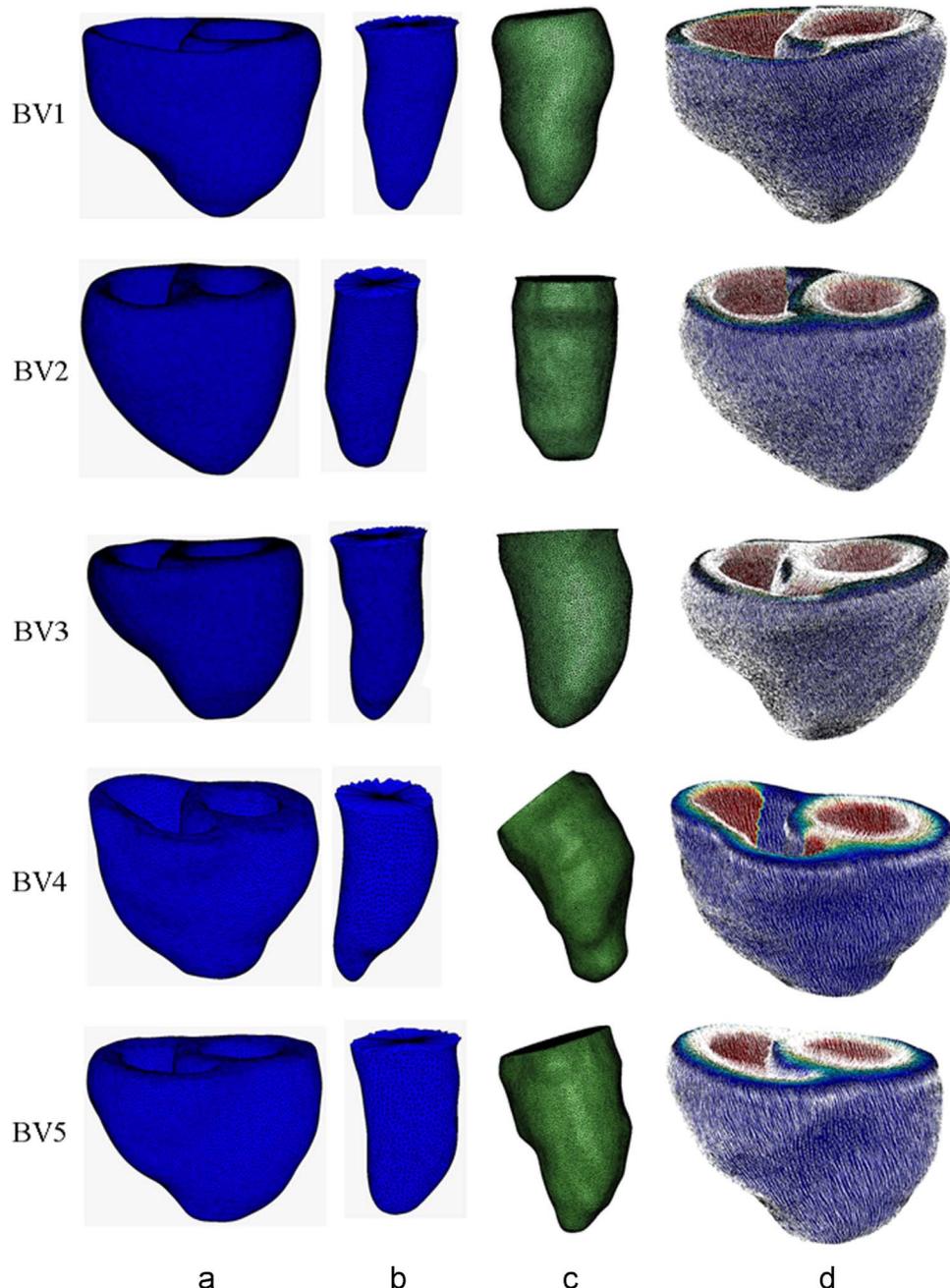
Sommer et al., 2015b, Gultekin et al., 2016) clearly exhibited orthotropic viscoelastic behaviour. Modified Fung-type (Usyk et al., 2000, Costa et al., 2001) and pole-zero law (Stevens et al., 2003) were used in diastolic modelling to incorporate material orthotropy. However, the material parameters in these orthotropic models were merely used as weighting factors, rather than any physical significance (Göktepe et al., 2011). Recently, Holzapfel and Ogden (2009) developed a constitutive law that considered the

locally orthotropic tissue architecture. The parameters of this model were closely related to the characteristic microstructure of myocardium. However, all the diastolic FE studies of human LV using Holzapfel–Ogden law used experimental data of animal myocardium which resulted in too stiff stress–strain relation, and thereby, unable to produce expected LV inflation through simulation (Wang et al., 2013, Palit et al., 2015b, Baillargeon et al., 2014). The majority of diastolic modelling of human LV used only one subject except the study conducted by Genet et al. (2014) which had limitations of using single LV model and transversely isotropic material law (Table 1). Therefore, the effect of geometrical heterogeneity in LV wall stress prediction is an important issue which is addressed in this study. There are two types of geometrical heterogeneity – (a) local geometrical heterogeneity which is present within a single LV geometry, and (b) global geometrical heterogeneity that is observed amongst different LV geometries

(amongst different subjects). In this study, the focus was mainly on the global geometrical heterogeneity although local heterogeneity was included as the geometry was developed from subject-specific MRI.

In majority of the FE models, kinematic constraints were typically used to fix longitudinal basal movement to avoid any rigid body displacement and allowed the apex to move freely (Wang et al., 2013, Genet et al., 2014, Walker et al., 2008, Eriksson et al., 2013). However, as reported by Wang et al. (2009) and observed from CMRI data, the apex of the heart did not move considerably during diastole, as opposed to the mitral valve plane (Fig. 1c).

Therefore, in the present study, personalised passive diastolic modelling of five normal human BV was carried out to address the following objectives – (1) to identify the effect of LV base movement on FE model predictions; (2) to investigate the changes in LV



**Fig. 2.** (a) Subject-specific bi-ventricular mesh geometry; (b) LV cavity at early diastole constructed from cardiac MRI; (c) LV cavity at end diastole constructed from cardiac MRI; (d) fibre orientation map using LDRF algorithm.

wall stress–strain distribution at ED due to geometric heterogeneity; and (3) to provide a reference map of regional stress–strain field in healthy LV wall at ED.

## 2. Material and methods

### 2.1. Construction of subject-specific bi-ventricular geometry

ECG gated, breathe hold, steady state free precession (SSFP) cardiac magnetic resonance imaging (CMRI) was performed to capture the images of five normal human ventricles at UHCW, Coventry, UK. BSREC ethics approval and patient consents were obtained to carry out the research on anonymised human data. Details of the mesh geometry construction were described in (Palit et al., 2015b; Palit et al., 2014). The early-diastolic volume (ErDV), EDV and ejection fraction (EF), were calculated from CMRI (Fig. 1a). Average longitudinal movement of base and apex during diastole were measured from constructed LV cavity geometry (Fig. 1b). It was observed that the average longitudinal movement of base was considerably higher than the movement of apex for all five ventricles during diastole (Fig. 1c). Fig. 2a–c shows the early diastolic BV mesh geometries, early and end diastolic LV cavities respectively, constructed from CMRI. Detailed CMRI scanning protocol and demographic information of the subjects are enclosed in Appendix A.

### 2.2. Construction of rule-based fibre-sheet orientation

Myocardial fibre-sheet orientation was implemented by 'Laplace–Dirichlet-Region growing-FEM' (LDRF) based algorithm (Palit et al., 2014, Wong and Kuhl, 2014). Based on previous studies (Streeter et al., 1969, Arts et al., 2001, Rohmer et al., 2007, Sommer et al., 2015a, Holzapfel and Ogden, 2009), the fibre orientation was defined by a linear variation of helix angle from  $-70^\circ$  in the sub-epicardium and RV septal endocardium to almost  $0^\circ$  in the mid-wall to  $+70^\circ$  at sub-endocardium and RV free wall endocardium for all five ventricles (Fig. 2d). The sheet direction was assumed to be aligned with local radial direction as it has very little effect on passive stress–strain distribution of LV wall (Wang et al., 2013).

### 2.3. Constitutive law for passive myocardium

The Holzapfel–Ogden material law (Eq. (1)) was used to define myocardium (Holzapfel and Ogden, 2009). Appendix B includes a detailed description of the strain energy function. Table 2 shows the material parameters used in this study. A brief description of the material parameter identification is included in Appendix C.

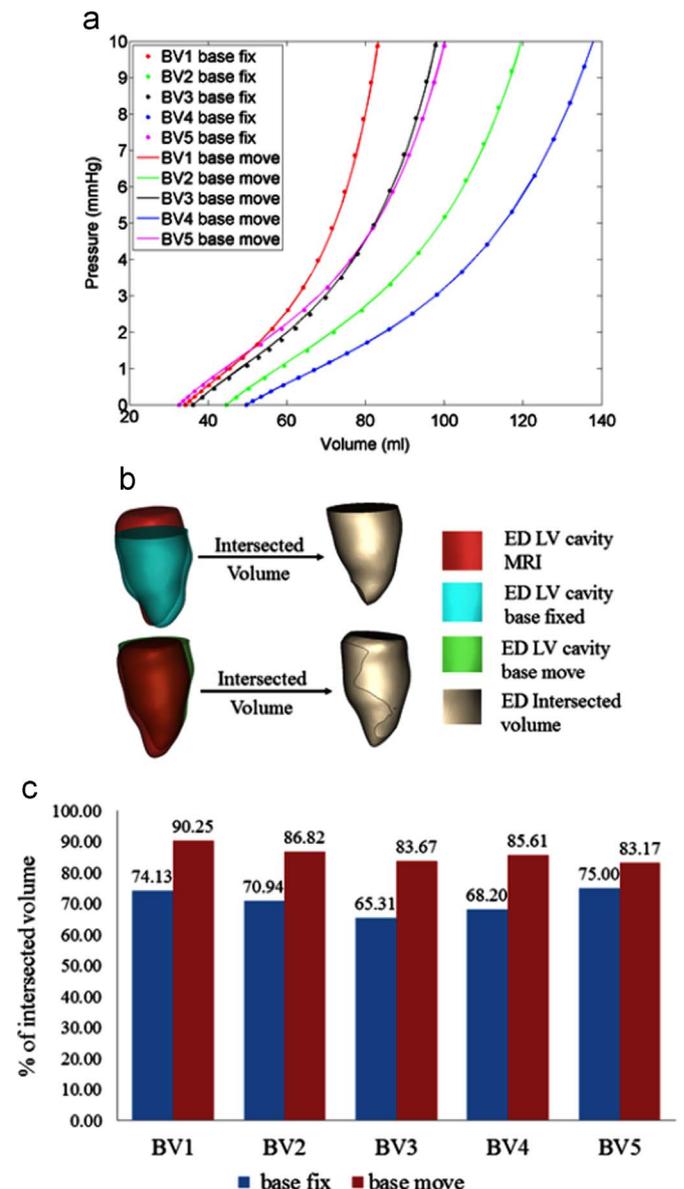
$$\Psi = K \left( \frac{I^2 - 1}{2} - \ln J \right) + \frac{a}{2b} \exp[b(\bar{I}_1 - 3)] + \sum_{i=f,s} \frac{a_i}{2b_i} \left\{ \exp[b_i(\bar{I}_{4i} - 1)^2] - 1 \right\} + \frac{a_{fs}}{2b_{fs}} \left\{ \exp[b_{fs}(\bar{I}_{8fs})^2] - 1 \right\} \quad (1)$$

### 2.4. Finite element model of passive LV mechanics

Early-diastolic (ErD) BV mesh geometry was constructed from ErD CMRI of human ventricle. According to state-of-the-art, ErD is assumed as initial stress free configuration since the ventricular pressure is lowest at this point, and therefore, stress is minimum (Usyk et al., 2000, Genet et al., 2014, Palit et al., 2015b, Sun et al., 2009, Wenk et al., 2011b, Wenk et al., 2011a, Palit et al., 2015a). Due to the unavailability of subject-specific ventricular pressure, which requires invasive measurement, LV EDP was considered 10 mmHg (Genet et al., 2014, Wang et al., 2013, Lee et al., 2013b, Lee et al., 2013a). One third of the LV blood pressure was applied on the RV endocardium (Palit et al., 2015b). Traditionally, the longitudinal movement of the base and the circumferential displacement of epicardial wall at the base were suppressed whereas apex was set free (Lee et al., 2014, Wang et al., 2013, Genet et al., 2014, Palit et al., 2015b, Eriksson et al., 2013, Wenk et al., 2011b, Dorri, 2004). However, as reported by Wang et al. (2009) and observed from CMRI (Fig. 1b and c), the upward basal movement was greater compared to the movement of

apex during diastole. Therefore, two cases were considered for all five BVs to explore the effect of base movement. Case-1 used the traditional method of constraining the longitudinal movement of base and allowing the apex to move free (Lee et al., 2014, Wang et al., 2013, Genet et al., 2014, Palit et al., 2015b, Eriksson et al., 2013, Dorri, 2004, Wenk et al., 2011b). In case-1, the circumferential displacement of epicardial wall at the base is also constrained along with the longitudinal movement of base as described in Sun et al. (2009), Wenk et al. (2013a), and Wang et al. (2013). Case-2 followed the method of Wang et al. (2009) in order to include the base movement to match the data from the CMRI. Average longitudinal displacement (Fig. 1c) was prescribed in all the basal nodes except the basal endocardial nodes (Wang et al., 2009). The movement of apex and the circumferential displacement of epicardial wall at base was suppressed in order to avoid any rigid body displacement (Wang et al., 2009). Radial direction was assumed to be free to deform (Wang et al., 2013, Wenk et al., 2013a) for both cases.

In order to study the stress–strain distribution of the LV wall, three short-axis slices were considered: (1) basal slice positioned 10 mm below the base; (2) equatorial slice located 20 mm below the basal slice; and (3) apical slice positioned 20 mm above the apex. In addition, two long-axis slices were defined. The s–l slice, passing through the septum and lateral wall, divided both RV and LV in the middle. The a–p slice, passing through anterior and posterior wall, divided the LV



**Fig. 3.** Effect of base movement on diastolic model prediction. (a) EDPVRs of LV for both cases (i.e. base fix vs base move) show that the EDPVR remains same even with the inclusion of base movement; (b) Procedure to calculate intersected volume to incorporate the shape-volume relevancy at ED; (c) Percentage of intersected volume between original and simulated LV cavity at ED; it shows that the better model prediction is achieved when base movement is included.

**Table 2**

Subject-specific values of Holzapfel–Ogden material parameters used in this study.

Subject	Passive material properties							
	$a$ (kPa)	$b$	$a_r$ (kPa)	$b_r$	$a_s$ (kPa)	$b_s$	$a_{fs}$ (kPa)	$b_{fs}$
BV1	0.080	6.00	2.951	5.893	0.492	3.393	0.070	3.929
BV2	0.092	4.800	2.647	5.323	0.441	3.065	0.063	3.548
BV3	0.089	4.760	2.579	5.000	0.430	2.879	0.061	3.333
BV4	0.060	4.450	2.500	4.853	0.417	2.794	0.059	3.235
BV5	0.048	4.380	2.466	5.000	0.411	2.879	0.058	3.333

cavity in the middle. In addition, each short-axis location was divided in four regions such as: anterior, lateral, posterior, and septum.

### 3. Results

#### 3.1. Model validation

Validation of Holzapfel–Ogden material model implementation in FE framework was detailed in Palit (2015). A shape-volume based validation procedure was introduced, for the first time, instead of comparing only LV EDV. The geometry of LV cavity at ED, constructed from CMRI, was attributed as 'original' shape (Fig. 2c). The geometry of LV cavity at ED, resulted from simulation, was considered as 'predicted' shape. The intersected volume between 'original' and 'predicted' geometry was calculated to incorporate shape-volume relevancy (Fig. 3b), and consequently, to check the accuracy of the model predictions. This is performed in 3-matic by importing both the .stl files of 'original' and 'predicted' LV cavity, and thereafter, by using the intersected volume option. Fig. 3c shows that the 'predicted' LV cavity is able to produce  $85.91 \pm 2.84\%$  shape-volume similarities when compared with 'original' LV cavity at ED (case-2).

#### 3.2. Effect of base movement

Two separate simulations (case-1 and case-2) were carried out for each BV to investigate the effect of base movement on FE model prediction. Three different parameters were compared.

First, the LV EDV was compared by plotting the LV end diastolic pressure volume relation (EDPVR) for both the cases (Fig. 3a). It was observed that the base movement did not affect the EDPVR of LVs, and therefore, both cases achieved same LV EDV as measured from CMRI. Second, although both the cases produced same LV EDPVR, the shape-volume relevancy was better for case-2 for all subjects ( $85.91 \pm 2.84\%$  in case-2 compared to  $70.72 \pm 4.05\%$  in case-1) (Fig. 3c). Third, a qualitative comparison in fibre stress–strain distribution in LV wall (BV1) at ED for both cases was carried out (Fig. 4). It was identified that the following areas experienced higher fibre stress in case-2: anterior and posterior regions of basal and equatorial locations, LV endocardium and near epicardium. The fibre stress distribution at apical location was completely different between the cases (Fig. 4). Moreover, the entire LV wall experienced higher fibre strain in case-2.

#### 3.3. Stress–strain amongst the different wall locations of the five ventricles

Fig. 5 shows that the LV endocardium experiences higher fibre stress compared to the LV epicardium. The average fibre stress was marginally higher in the equatorial location compared to the basal and the apical location (except for BV3). Both sheet and sheet-normal stresses were greater in the basal location and minimal in the apical location for all five ventricles (Fig. 6b). Variations in fibre and sheet stresses in the apical location were higher in comparison with the other locations (Fig. 6a). In contrast, the variation in sheet-normal stress was greater in the basal location. The average

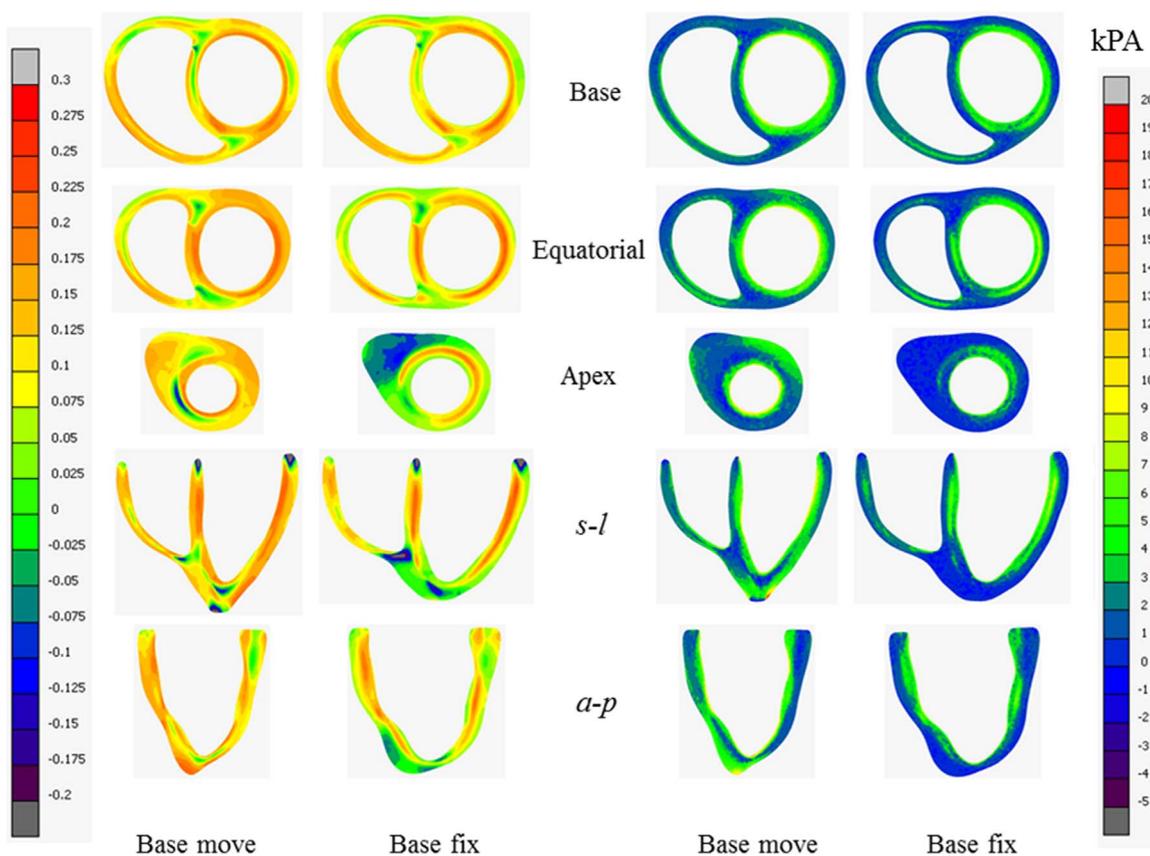
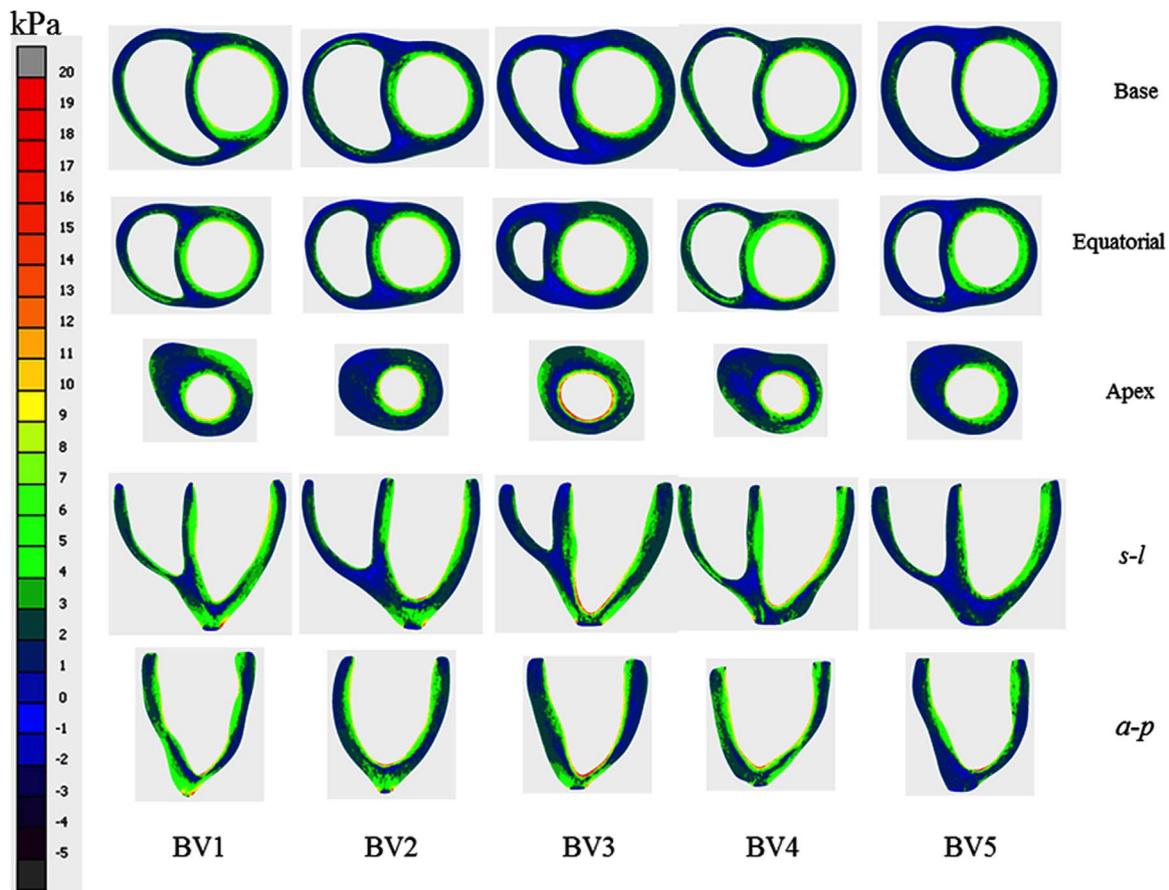


Fig. 4. Comparison between fibre stress (Cauchy) and fibre strain (logarithmic) predictions between the two cases (base move vs base fix) for BV1. The location definition of the images are described in Section 2.4.



**Fig. 5.** Subject-specific fibre stress (Cauchy stress) at three short axis (base, equatorial and apex) and two long-axis (*s-l* and *a-p*) locations. The location definition of the images are described in Section 2.4.

fibre stress at ED was higher compared to sheet and sheet-normal stresses. The ranges of fibre, sheet and sheet-normal stresses were approximately in the range of 0–6 kPa, –1.5 to +1.5 kPa and –1 to +5 kPa respectively for all locations (Fig. 6a).

Figs. 6c and d show the average GL strain in local cardiac coordinate ( $\mathbf{e}_c$ ,  $\mathbf{e}_z$ ,  $\mathbf{e}_n$ ) (Palit et al., 2014, Wang et al., 2013). The circumferential and radial strains were higher in the basal and the equatorial locations compared to the apical location, whereas the longitudinal strain was higher in the apical location and lowest in the equatorial location. The circumferential GL strain was greater in comparison with longitudinal and radial strain (Fig. 6c).

### 3.4. Stress–strain amongst the different wall regions of the five ventricles

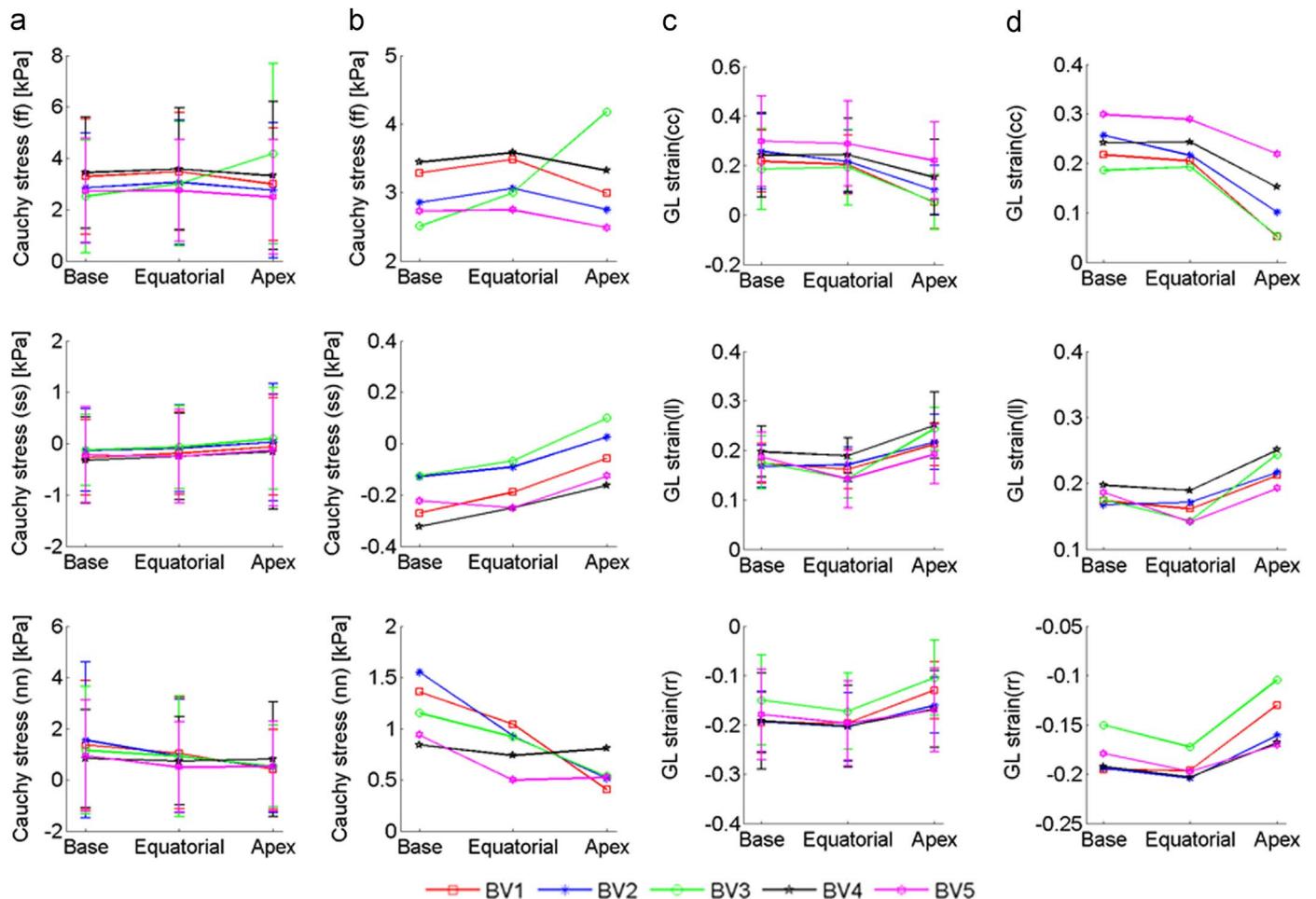
The lateral region of LV in all the short-axis locations was experienced comparatively higher fibre stress for all the ventricles (except BV4 in equatorial location) whereas the septum in the apical location experienced lower fibre-stress (Fig. 7b). Compressive sheet stress was greater in the lateral region of the equatorial and the apical locations. Sheet-normal stress was higher in the posterior region of the equatorial location whereas the lateral wall experienced comparatively lower sheet-normal stresses (except BV3 sheet-normal stress). Moreover, the variation in fibre-stress amongst the regions was less in the basal and the equatorial locations compared to the variation in the apical location. The ranges of stresses, experienced by different regions of LV wall in different short-axis location, are shown in Fig. 7a.

The ranges of different GL strain components are plotted in Fig. 8a. High circumferential GL strain was experienced by the lateral wall at the basal location, and the posterior region of the equatorial and the apical locations (Fig. 8b). The anterior and the septum wall received comparatively lower circumferential GL strain. The longitudinal GL strain was less in the posterior region of the basal and the equatorial locations.

## 4. Discussion

### 4.1. Comparison with state-of-the-art

Passive diastolic modelling was carried out for five human ventricles to investigate the effect of base movement and geometrical heterogeneity on LV wall stress–strain distributions. Authors' previous work (Palit et al., 2015b) included the effect of fibre orientation and right ventricle (RV) on LV mechanics using porcine myocardium data, and without considering base movement. The current study aimed to explore the effect of global geometrical heterogeneity and base movement on LV mechanics using human myocardium properties. The previous study was conducted by implementing different fibre orientation on single ventricular geometry, whereas in this study, five BV geometries were used with similar fibre structure to find the effect of global geometrical heterogeneity. Several improvements were incorporated in the present study over state-of-the-art for better model prediction. Firstly, BV geometries were used in the study to consider the effect of RV deformation. Palit et al. (2015b) reported that



**Fig. 6.** (a) Range and (b) average values of the fibre (ff), sheet (ss) and sheet-normal (nn) stresses at base, equatorial and apical locations of each BV; (c) Range and (b) average values of the circumferential (cc), longitudinal (ll) and radial (rr) strains at base, equatorial and apical locations of each BV.

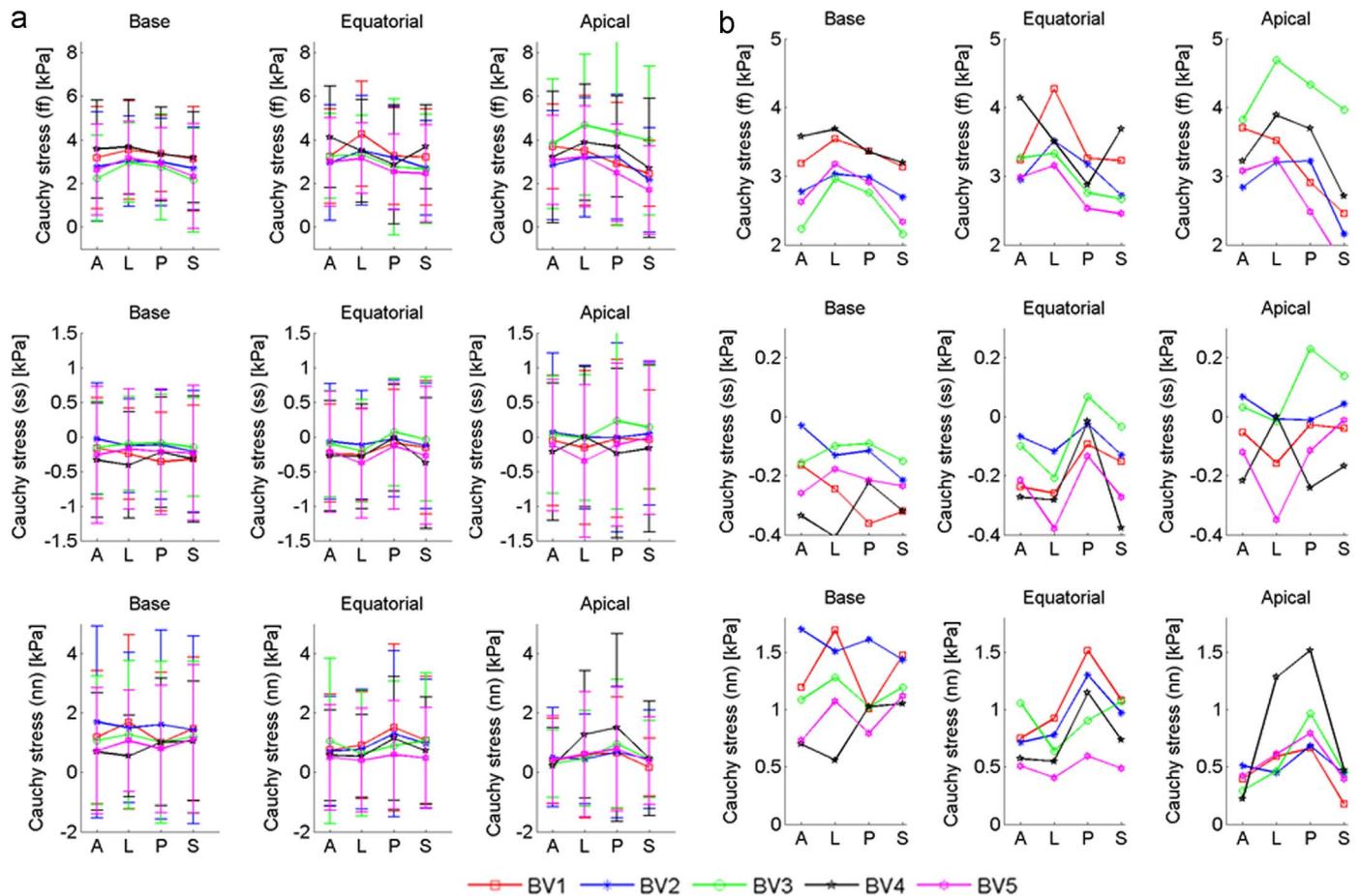
the inclusion of RV deformation in computational model not only changed the stress-strain distribution pattern but also increased LV wall stress-strain during diastole. The majority of previous studies used only single LV geometry (Genet et al., 2014, Wang et al., 2013, Wang et al., 2009), and therefore, the effects of RV deformation were not considered. Secondly, subject-specific passive orthotropic material properties for human myocardium were used instead of transversely isotropic properties (Genet et al., 2014). Thirdly, LV base movement was included in diastole to predict more accurate shape-volume changes of ventricles during diastole. Although Wang et al. (2009) included base movement in their model, the effect was first investigated in this study. Fourthly, a new shape-volume based validation procedure was introduced to measure the model prediction accuracy. Finally, the variation of fibre, sheet and sheet-normal stresses (and strains) amongst different wall regions and locations of the five normal ventricles were reported.

The shape-volume based validation procedure is easy to implement without the use of extra scanning operation or higher computational cost, yet provides a great way to compare the prediction of FE modelling. As tag-MRI is not a routine clinical practice in majority of the hospitals, cine MRI could be used to calculate strain. Cine images are 2D, and thus, out of plane motion cannot be easily estimated (Gao et al., 2015). In addition, due to lack of patterns/features in cine images, higher uncertainties presents while estimating pixel-wise strain. Gao et al. (2014) showed that the regional circumferential strains could be estimated correctly from cine images. However, greater discrepancies exists

during the estimation of regional radial strains, and therefore, could not be used in FE modelling (Gao et al., 2015). Even with tag-MRI, the radial strain cannot be measured with adequate accuracy (Declerck et al., 2000, Denney et al., 2003, Sun et al., 2009). Therefore, when short axis images are used, only single parameter (circumferential strain) could be used for validation which is not sufficient to compare the global deformed shape. Also, it is difficult to estimate strain in late diastole due to the fading of tag data (Gao et al., 2014, Xu et al., 2010) (however, DENSE MRI does not have this issue). It leads to complex and additional computational time. In addition, some studies used (Genet et al., 2014, Gao et al., 2015, Sun et al., 2009) tag MRI in FE modelling without considering the longitudinal basal movement. However, it is evident from the present study that the inclusion of base movement is mandatory for better model prediction. Therefore, shape-volume based validation should be performed along with strain-based validation for improved model prediction.

#### 4.2. Effect of base movement

The EDPVRs of LV did not alter due to the inclusion of longitudinal base movement, and therefore, same subject-specific EDV was achieved for both the cases. However, it was observed that the shape-volume prediction was better ( $85.91 \pm 2.84\%$  compared to  $70.72 \pm 4.05\%$ ) when longitudinal movement of base was included in the model. It showed that the LV wall expanded more in the radial direction in the fixed base case, and consequently led to inaccurate shape. In addition, including base movement



**Fig. 7.** (a) Range and (b) average values of the fibre (ff), sheet (ss) and sheet-normal (nn) stresses at anterior (A), lateral (L), posterior (P) and septum (S) regions of each locations (i.e. base, equatorial and apical) of each BV.

increased the average fibre strain in the LV. These observations indicated two aspects which should be incorporated in any future computational studies of cardiac mechanics. Firstly, the longitudinal base movement should be included in the model; otherwise the model would provide accurate volume estimation with inaccurate geometrical shape. Any surgical simulations with such inconsistency could result in imprecise model prediction, and therefore, lead to the selection of wrong surgical treatment. Secondly, the traditional method of validating the diastolic model prediction only by comparing the LV EDV (Genet et al., 2014, Lee et al., 2013a), would not be sufficient. Future studies should also compare the geometrical shape to provide precise model estimation for diastole and systole.

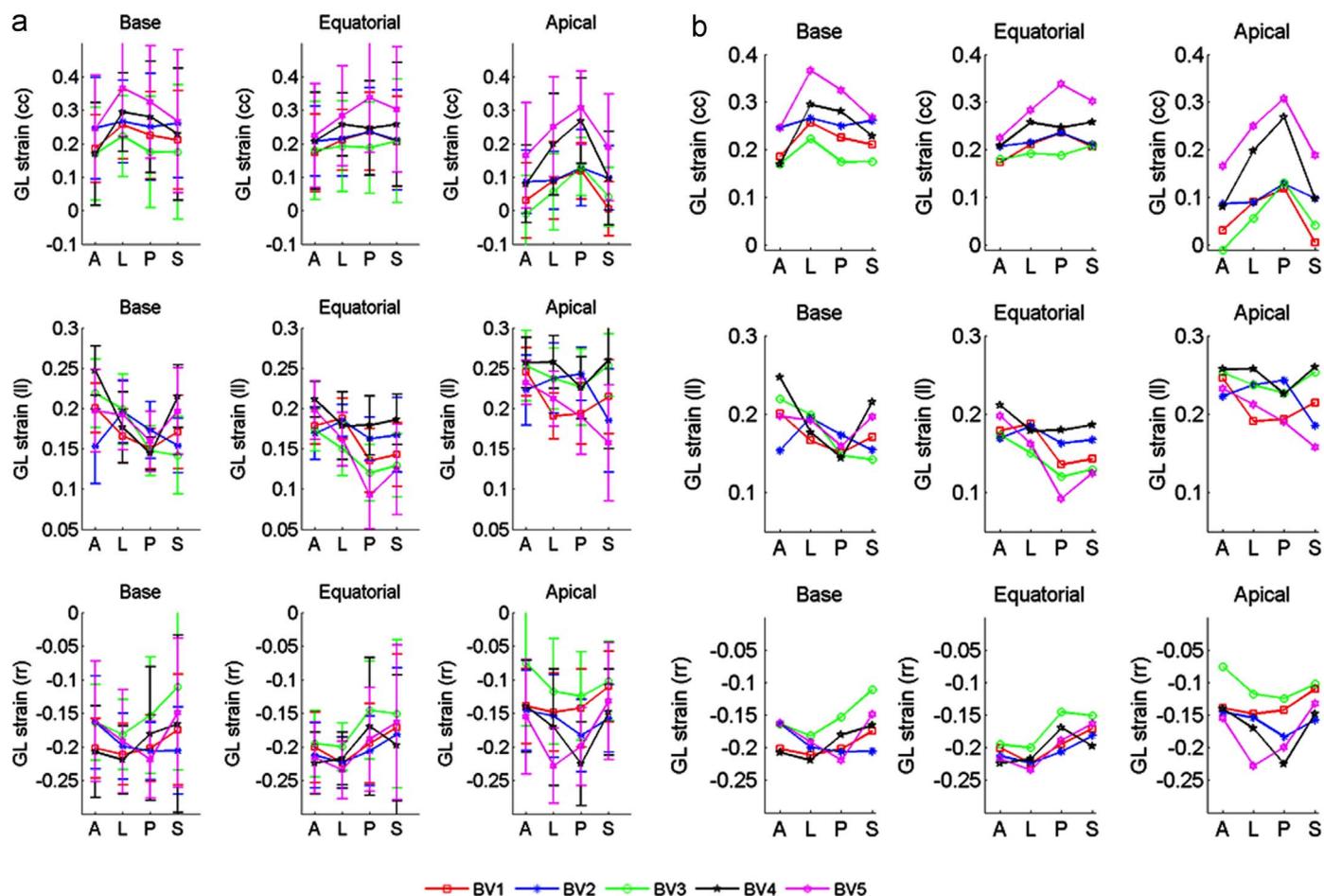
#### 4.3. Stress-strain amongst the different wall locations and regions of five ventricles

It was identified that the endocardium region experienced higher fibre stress compared to the epicardium of LV wall at ED. Similar observation was identified by Genet et al. (2014) using scaled myocardium properties for human LV, and by Wenk et al. (2013b) using animal myocardium properties and different constitutive law (fung-type law). Genet et al. (2014) reported that the volume-averaged fibre stress at ED was  $2.21 \pm 0.58$  kPa. In the present study, it was identified that the average fibre stress was in the range of 2–3.5 kPa (Fig. 6b). Due to the lack of diastolic strain measurement for human myocardium, the circumferential and radial strain values in the present study were compared with the strain values provided for animal heart in the literature. It was reported that the circumferential strain for animal heart was 0.07–

0.15 (Sinusas et al., 2001), 0.07–0.22 (Veress et al., 2005), 0.09–0.15 (Guccione et al., 1991) and 0.05–0.22 (Omens et al., 1991). In this study, the circumferential strain was in the range of 0.1–0.3 (from apex to base), which agreed excellently with the literature. In addition, radial strain for animal heart was reported as 0.15–0.25 (Sinusas et al., 2001), 0.09–0.14 (Veress et al., 2005), 0.19–0.34 (Guccione et al., 1991) and 0.12–0.18 (Omens et al., 1991). The absolute value of radial strain was also in the similar range (0.1–0.2). Due to the lack of published data on transmural stress-strain distributions in the human LV at ED where human myocardial properties were used (see Table 1), and given the differences in subjects, more detailed quantitative comparisons do not seem merited. Although the average fibre stress was comparatively higher in the equatorial location, the differences were not considerable. Furthermore, the sheet and sheet-normal stresses and circumferential strain were higher in the basal location compared to the equatorial and the apical locations. Therefore, it was concluded that the LV wall near base location experienced higher stress-strain. In addition, it was observed that the lateral region of LV wall experienced higher fibre and sheet stress. These results were mostly consistent for all five normal human ventricles.

#### 4.4. Limitations and future work

First of all, rule-based fibre-sheet orientation was used instead of subject-specific ones. Precise fibre-sheet orientation can be measured only ex-vivo and feasibility of in-vivo diffusion tensor imaging (DTI) for subject-specific fibre-sheet orientation is still an open question (Wang et al., 2009, Genet et al., 2014). The LV EDP was considered 10 mmHg due to the unavailability of subject-



**Fig. 8.** (a) Range and (b) only average values of the circumferential (cc), longitudinal (ll) and radial (rr) strains at anterior (A), Lateral (L), posterior (P) and septum (S) regions of each location (i.e. base, equatorial and apical) of each BV.

specific EDP, which requires invasive measurements. Due to such ethical and technical limitations, studies of human ventricular mechanics assumed physiologically reasonable values of ventricular pressure in computational model (Genet et al., 2014, Wang et al., 2013, Lee et al., 2013b, Lee et al., 2013a). The third limitation was the assumption of an initial stress-free state, which was present in all the previous simulations study (Usyk et al., 2000, Genet et al., 2014, Palit et al., 2015b, Sun et al., 2009, Wenk et al., 2011b, Wenk et al., 2011a). Wang et al. (2014) reported that the effects of such initial (residual) stresses are relatively small in late diastole when pressure is higher. In contrast, a recent study observed measurable effect of pre-stress during diastole (Genet et al., 2015). Therefore, it is still an open question and future studies will be carried out to compute personalised diastolic mechanics by considering physiological pre-stress condition.

From the perspective of myocardial physiology and ventricular blood pressure, the structure–functional relations of normal human heart are very complex. It was not claimed that the computational model of BV being able to realistically simulate all the coupled phenomena with inadequate clinical data. However, the model realistically simulated only a limited scope of local LV diastolic mechanics, and within that scope, the model was state-of-the-art in their pragmatism and consistent with which they were validated.

## 5. Conclusions

In the present study, personalised passive diastolic modelling of human LV was carried out to identify the changes in regional stress–strain distributions in LV wall at ED due to geometrical heterogeneity and base movement. The improvements of the current study over the state-of-the-art as follows. (1) Subject-specific passive orthotropic material properties of human myocardium was used for better model prediction, instead of previously used animal myocardium data with transversely isotropic properties. (2) Personalised computational models of five healthy human ventricles were carried out instead of using single human heart. (3) A new shape–volume based validation procedure was introduced along with traditionally used EDV based comparison. (4) Subject-specific base movement, which was not considered by the majority of previous studies, was included, and consequently, the effect of such movement on model prediction was explored. (5) Bi-ventricular model was considered to include RV deformation. Results indicated that only EDV based validation was not sufficient for accurate model prediction, and therefore, shape–volume relevancy should be compared. Including base movement increased the shape–volume relevancy of LV cavities, and consequently, improved the model prediction. The endocardium of LV wall was experienced high fibre stress compared to the epicardium wall. The LV wall near base location was experienced greater stress and

strain compared to the other locations. In general, the lateral LV wall experienced higher stress-strains compared to the other three regions. In addition, a detailed measurement of different stress-strain components amongst different locations and regions of LV wall was reported for five healthy ventricles. These could be used as a reference map for future computational studies or could serve as targets for in-silico design of therapeutic interventions for diastolic heart failure treatments.

### Conflict of interest statement

The authors have no conflict of interest.

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### Appendix A. Supporting information

Supplementary data associated with this article can be found in the online version at <http://dx.doi.org/10.1016/j.jbiomech.2016.12.023>.

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