



Application of fuzzy soft set in decision making problems based on grey theory

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ABSTRACT

There are many uncertain problems in practical production and life which need decisions made with soft sets and fuzzy soft sets. However, the basis of evaluation of the decision method is single and simple, the same decision problem can obtain different results from using a different evaluation basis. In this paper, in order to obtain the right result, we discuss fuzzy soft set decision problems. A new algorithm based on grey relational analysis is presented. The evaluation bases of the new algorithm are multiple. There is more information in a decision result based on multiple evaluation bases, which is more easily accepted and logical to one's thinking. For the two cases examined, the results show that the new algorithm is efficient for solving decision problems.

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1. Introduction

Molodtsov [1] proposed a completely new approach for modeling vagueness and uncertainty soft set theory. Most of its applications have already been demonstrated in [2]. Fuzzy soft set theory has been proposed [3] and has potential applications.

In recent years, soft set and fuzzy soft set theories have been proved to be useful in many different fields, such as decision making [4–14], data analysis [15], forecasting [16], simulation [17], evaluation of sound quality [18] and rule mining [19]. The study of hybrid models combining soft sets or fuzzy soft sets with other mathematical structures and new operations are emerging as an active research topic of soft set theory [20–39]. Maji et al. considered the reduct soft set with the help of rough set approach [4] and discussed soft set theory [20]. Roy et al. discussed score value as the evaluation basis to make decisions in fuzzy soft sets [5]. Zhi Kong et al. analyzed two decision evaluation bases, choice value and score value, and used a counter example to discuss the two methods [8]. Naim Çağman et al. presented soft matrix theory and uni-int decision making [6,7]. Yuncheng Jiang et al. introduced two methods, semantic decision making using ontology and intuitionistic fuzzy soft sets decision making [9,10], and extended soft sets with description logics, discussing interval-valued intuitionistic fuzzy soft set properties [27,28]. Feng Feng et al. presented an adjustable approach by means of level soft sets and interval-value fuzzy soft sets [11,12], and soft semirings and soft rough sets [22–24]. Xibei Yan et al. introduced the concept of interval-valued fuzzy soft sets and discussed its operations [13]. Ke Gong et al. discussed the bijective soft set and its operations [14]. Hacı Aktaş et al. discussed soft sets and soft groups [21]. Hailong Yang presented kernels and closures of soft set relations and soft set relation mappings [25]. Pinaki Majumdar et al. introduced generalized fuzzy soft sets [26]. Young Bae Jun et al. and Jianming Zhan et al. discussed algebras soft sets [29–33]. Wei Xu et al. presented vague soft sets and their properties [34]. Muhammad Irfan Ali et al. discussed some new operations in soft set theory and approximation space associated with each parameter in a soft set [35,36]. Babitha et al. presented soft set relations and functions [37]. Ummahan Acar et al. presented soft sets and soft rings [38]. Zhi Xiao et al. introduced exclusive soft sets [39]. Chen et al. [40] presented a definition of parameterization

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reduction in soft set theory, and compared this definition to the related concept of attributes reduction in rough set theory. Kong et al. [41] introduced the definition of normal parameter reduction to overcome adding parameters and suboptimal choice problem and an algorithm has been given.

According to the previous results for decision making in fuzzy soft sets, researchers focus on a direction as the evaluation basis, such as choice value (the sum of all membership grades for one object), score value (the number of parameters of relatively larger membership value of an object), or other evaluation bases. The evaluation methods are completely different. For the same problem, the results may be inconsistent. Decision making problems may use different factors, so it is not easy to judge which result is right. Furthermore, we don't know which method should be chosen for making decisions. Two examples (a) and (b) are listed to make decisions depending on two different evaluation bases, choice values and score values. There are 6 objects $\{o_1, \dots, o_6\}$ and we compute the choice values and score values of them, respectively. (a): choice value sequence $c = \{1.0, 1.0, 1.1, 1.2, 2.1, 2.2\}$ and score value sequence $s = \{-13, -5, -6, 2, 16, 6\}$. For problem (a), the result is o_6 with the choice value method, while the result is o_5 with the score value method. We don't know which answer is right, because the two answers are analyzed from two different factors. For objects o_5 and o_6 , we know $c_5 = 2.1$, $c_6 = 2.2$, $s_5 = 16$, $s_6 = 6$. So the values $c_5 = 2.1$ and $c_6 = 2.2$ are similar, while the values $s_5 = 16$ and $s_6 = 6$ are very different. Therefore, synthesizing two group values of o_5 and o_6 , we generally choose o_5 as the answer because of the suboptimal value $c_5 = 2.1$ and optimal value $s_6 = 6$. (b): choice value sequence $c = \{1.4, 1.3, 1.3, 1.8, 1.9, 2.9\}$ and score value sequence $s = \{-1, -7, -4, -5, 8, 7\}$. For problem (b), the result is o_6 with the choice value method, while the result is o_5 with the score value method. Because of the different evaluation bases, the results are inconsistent. Considering the choice value and score value together, for problem (b), o_6 is better.

For the above analysis, different results are obtained from using a different single evaluation basis. However, the single evaluation basis is simple, one-sided and has a shortage of information. Only one evaluation basis is considered and an extreme decision result may be obtained. To improve the decision quality many evaluation bases are comprehensively analyzed. There is more information in the decision result of multiple evaluation bases, which is more general. So we present a new algorithm to solve this problem based on grey theory. Many evaluation bases are considered in the new algorithm and a comprehensive decision result is obtained.

The key to this problem is how to operate two or more different methods together. Grey theory can help us to solve this problem. The grey relational analysis method is an important method in grey system theory, which was initiated by Deng in 1982 [42]. It is a quantitative analysis to explore the similarity and dissimilarity among factors in developing dynamic processes. The theory proposes a dependence to measure the correlation degree of factors; the more similarities develop, the more factors correlate [43]. Grey relational analysis of grey theory is a well known approach that is utilized for generalizing estimates under small samples and uncertain conditions. We apply grey relational analysis of grey theory to combine multiple evaluation methods into a single evaluation value. Finally, we use the evaluation value to make the decision.

In this paper, we take choice value evaluation and score value evaluation as an example. Here we combine the two evaluation methods to make decisions in a fuzzy soft set based on grey relational analysis and compute the correlation degree for every object. Finally, we use the relational grade as the evaluation basis. In this paper, a new algorithm is presented based on evaluation bases. Applying the new algorithm, the above two problems can be solved well.

The new algorithm in this paper is suitable for soft set and fuzzy soft set decision making problems and unconstrained for evaluation methods. Whatever kind of evaluation methods we choose, as long as every evaluation sequence is given, such as choice value sequence, score value sequence, or other sequences, then we can make the decision using this new algorithm. The evaluation sequence associates to a kind of evaluation method, so this new algorithm is a hybrid evaluation method for comprehensive evaluation. Also, this new algorithm is objective, numerical and accurate, and we can compare the value to obtain the optimal choice, suboptimal choice, and so on.

The paper is organized as follows. In Section 2, we provide some basic definitions in soft sets and fuzzy soft sets. In Section 3, we discuss the present two methods in decision making problems in fuzzy soft sets, and two examples are listed to illustrate the two problems. In Section 4, a new algorithm is presented to solve the two problems. In Section 5, an example is analyzed using the uni-int decision making method and the new algorithm. In Section 6, we end this paper with some conclusions.

2. Definitions and notation

In this section, we review useful notions of soft sets and fuzzy soft sets. Let U be an initial universe set and let E be a set of parameters.

Definition 2.1 (See [2]). A pair (F, E) is called a soft set (over U) if and only if F is a mapping of E into the set of all subsets of the set U , i.e., $F : E \rightarrow P(U)$, where $P(U)$ is the power set of U , and E is a set of parameters.

The soft set is a parameterized family of subsets of the set U . Every set $F(\varepsilon)$, $\varepsilon \in E$, from this family may be considered as the set of ε -elements of the soft set (F, E) , or as the ε -approximate elements of the soft set. As an illustration, some examples such as fuzzy sets and topological spaces were listed in [2]. The way of setting (or describing) any object in soft set theory differs in principle from the way it is used in classical mathematics. In classical mathematics, a mathematical

Table 1
Soft set table.

U	e_1	e_2	e_3	e_4	Choice value
h_1	1	1	1	0	3
h_2	0	1	0	1	2
h_3	1	0	1	1	3
h_4	1	0	0	1	2

Table 2
Fuzzy soft set table.

U	e_1	\dots	e_m
o_1	o_{11}	\dots	o_{1m}
\dots	\dots	\dots	\dots
o_n	o_{n1}	\dots	o_{nm}

model of an object is usually constructed for which it is too complicated to find the exact solution. Therefore the notion of an approximate solution has been introduced in soft set theory, whose approach is the opposite of classical mathematics.

The absence of any restrictions on the approximate description in soft set theory makes it very convenient and easy to apply in practice. We can use any parameterization with the help of words and sentences, real numbers, functions, mappings, and so on.

To illustrate this idea, let us consider the following example.

Example 2.1. Let universe $U = \{h_1, h_2, h_3, h_4\}$ be a set of houses, $E = \{e_1, e_2, e_3, e_4\}$ be a set of statuses of houses, which stand for the parameters “beautiful”, “cheap”, “in green surroundings”, and “in good location” respectively. Consider the mapping F to be a mapping of E into the set of all subsets of the set U . Now consider a soft set (F, E) that describes the “attractiveness of houses for purchase”. According to the data collected, the soft set (F, E) is given by

$$\{F, E\} = \{(e_1, \{h_1, h_3, h_4\}), (e_2, \{h_1, h_2\}), (e_3, \{h_1, h_3\}), (e_4, \{h_2, h_3, h_4\})\},$$

where $F(e_1) = \{h_1, h_3, h_4\}$, $F(e_2) = \{h_1, h_2\}$, $F(e_3) = \{h_1, h_3\}$, and $F(e_4) = \{h_2, h_3, h_4\}$. In order to store a soft set in computer, a two-dimensional table is used to represent the soft set (F, E) . Table 1 is the table form of the soft set (F, E) . If $h_i \in F(e_j)$, then $h_{ij} = 1$, otherwise $h_{ij} = 0$, where h_{ij} are the entries.

Suppose that Mr. X is interested in buying a house on the basis of his choice parameters “beautiful”, “cheap”, “in green surroundings”, etc. According to the choice value, Mr. X can choose h_1 or h_3 .

Definition 2.2 (See [5]). Let $\Psi(U)$ denote the set of all fuzzy sets of U , E be a set of parameters. Let $A_i \subset E$. A pair (F_i, A_i) is called a fuzzy soft set over U , where F_i is the mapping given by $F_i : A_i \rightarrow \Psi(U)$.

Definition 2.3 (See [5]). For two fuzzy soft sets (F, A) and (G, B) over a common universe U , (F, A) is a fuzzy soft subset of (G, B) if (i) $A \subset B$, and (ii) $\forall \varepsilon \in A$, $F(\varepsilon)$ is a fuzzy subset of $G(\varepsilon)$. We write $(F, A) \widetilde{\subset} (G, B)$. (F, A) is said to be a fuzzy soft super set of (G, B) , if (G, B) is a fuzzy soft subset of (F, A) . We denote it by $(F, A) \widetilde{\supset} (G, B)$.

The tabular representation of a fuzzy soft set is given in Table 2. o_{ij} is the membership degree of o_i in a parameter set $\{e_j\}$, $o_{ij} \in [0, 1]$. At present there are many methods to make decisions by fuzzy soft set theory. In this paper, two main methods are introduced, one uses choice value as the evaluation basis, the other uses score value as the evaluation basis. In Section 3, the two methods are described in detail.

Definition 2.4 (See [2]). Assume that we have a binary operation, denoted by $*$, for subsets of the set U . Let (F, A) and (G, B) be soft sets over U . Then, the operation $*$ for soft sets is defined in the following way: $(F, A) * (G, B) = (H, A \times B)$, where $H(\alpha, \beta) = F(\alpha) * G(\beta)$, $\alpha \in A$, $\beta \in B$, and $A \times B$ is the Cartesian product of the sets A and B .

3. Fuzzy soft set in decision making problems

At present there are two methods to handling decision making problems in fuzzy soft sets. In [5] the decision depends on the score s_i , where s_i signifies the number of parameters of relatively larger membership value of object o_i . In [8] the decision depends on choice value c_i , where c_i signifies the sum of the membership values of all parameters of object o_i . The decision that results is not always the same according to the two methods, the score value and choice value. However, sometimes the same decision may be obtained. The reason is that, for an object, possibly the more the number of parameters of the relatively larger membership values is, the greater the probability of the membership sum values of all parameters is. The algorithm for decision making problems in fuzzy soft sets [5] is as follows.

Algorithm [5].

1. Input the fuzzy-soft-set (F, A) , (G, B) and (H, C) .
2. Input the parameter set P as observed by the observer.

Table 3
Fuzzy soft set table of case 1.

U	e_1	e_2	e_3	e_4	e_5	Choice value
o_1	0.1	0.1	0.1	0.1	0.6	$c_1 = 1.0$
o_2	0.3	0.2	0.1	0.2	0.2	$c_2 = 1.0$
o_3	0.1	0.3	0.1	0.1	0.5	$c_3 = 1.1$
o_4	0.3	0.2	0.2	0.2	0.3	$c_4 = 1.2$
o_5	0.1	0.3	0.4	0.4	0.9	$c_5 = 2.1$
o_6	0.9	0.2	0.1	0.2	0.8	$c_6 = 2.2$

Table 4
Comparison table of case 1.

	o_1	o_2	o_3	o_4	o_5	o_6
o_1	5	2	4	1	1	1
o_2	4	5	3	3	1	3
o_3	4	3	5	2	2	2
o_4	4	5	3	5	1	3
o_5	5	4	5	4	5	4
o_6	5	5	4	4	1	5

Table 5
Score table of case 1.

	Row sum	Column sum	Score value
o_1	14	27	−13
o_2	19	24	−5
o_3	18	24	−6
o_4	21	19	2
o_5	27	11	16
o_6	24	18	6

3. Compute the corresponding resultant-fuzzy-soft-set (S, P) from the fuzzy soft sets (F, A) , (G, B) and (H, C) and place it in tabular form.
4. Construct the Comparison table of the fuzzy-soft-set (S, P) and compute r_i and t_i for o_i , $\forall i$.
5. Compute the score of o_i , $\forall i$.
6. The decision is S_k if $S_k = \max_i S_i$.
7. If k has more than one value then any one of o_k may be chosen.

Algorithm [8].

From Step 4 the algorithm is revised as below: c_{ij} and r_i should be redesigned as

$$c_{ij} = \sum_{k=1}^m (f_{ik} - f_{jk})$$

$$r_i = \sum_{j=1}^m c_{ij}$$

where f_{ik} is the membership value of object o_i for the k^{th} parameter, m is the number of parameters. Step 5: the decision is k if $r_k = \max_i r_i$.

The above two methods in decision making problems are considered from different aspects. Consider the following two cases. Let $U = \{o_1, o_2, \dots, o_n\}$ be the object set, $C = \{c_1, c_2, \dots, c_n\}$ be the choice value sequence, $S = \{s_1, s_2, \dots, s_n\}$ be the score sequence. Suppose c_i is the optimal value, c_j is the suboptimal value in the choice value sequence; s_j is the optimal value, s_i is the suboptimal value in the score sequence. Case 1: if the choice values of two objects are almost equal ($c_i > c_j$), but the scores differ widely ($s_j > s_i$), in general, one usually chooses o_j as the optimal object, not o_i . Case 2: if the scores of two objects are almost equal, but the choice values differ widely, in general, one usually chooses o_i as the optimal object, not o_j .

However, when we want to make a decision based on choice value and score, which one is the optimal object? In this section, the problem is discussed. There are two examples in the following.

Let $U = \{o_1, o_2, o_3, o_4, o_5, o_6\}$ be the set of objects. The parameter set $E = \{e_1, e_2, e_3, e_4, e_5\}$. The tabular representation of the fuzzy soft set and corresponding choice values of objects are as follows.

Example 3.1. See Table 3.

The choice value is $c_i = \sum_{j=1}^5 o_{ij}$. The Comparison table of the above fuzzy-soft-set is given in Table 4.

Table 6

Fuzzy soft set table of case 2.

U	e_1	e_2	e_3	e_4	e_5	Choice value
o_1	0.2	0.3	0.2	0.3	0.4	$c_1 = 1.4$
o_2	0.6	0.2	0.3	0.1	0.1	$c_2 = 1.3$
o_3	0.1	0.2	0.4	0.2	0.4	$c_3 = 1.3$
o_4	0.6	0.1	0.1	0.9	0.1	$c_4 = 1.8$
o_5	0.5	0.3	0.4	0.3	0.4	$c_5 = 1.9$
o_6	0.1	0.9	0.9	0.9	0.1	$c_6 = 2.9$

Table 7

Comparison table of case 2.

	o_1	o_2	o_3	o_4	o_5	o_6
o_1	5	3	4	3	3	2
o_2	2	5	2	4	1	2
o_3	2	4	5	3	2	2
o_4	2	3	2	5	2	3
o_5	5	4	5	3	5	2
o_6	3	4	4	4	3	5

Table 8

Score table of case 2.

	Row sum	Column sum	Score value
o_1	20	19	1
o_2	16	23	-7
o_3	18	22	-4
o_4	17	22	-5
o_5	24	16	8
o_6	23	16	7

The Comparison table is a square table in which the number of rows and number of columns are equal, the rows and columns both are labelled by the object names o_1, o_2, \dots, o_6 of the universe, and the entries are c_{ij} , $j = 1, 2, \dots, 6$. c_{ij} indicates a numerical measure, which is an integer and o_i dominates o_j in c_{ij} number of parameters out of k parameter [5]. Next we compute the row sum, column sum, and the score for each o_i as shown in Table 5.

The row sum of an object o_i is denoted by r_i and is calculated by using the formula $r_i = \sum_{j=1}^6 c_{ij}$. r_i indicates the total number of parameters in which o_i dominates all the numbers of U . The column sum of an object o_j is denoted by t_j and may be computed as $t_j = \sum_{i=1}^6 c_{ij}$. The score value $s_i = r_i - t_i$ [5].

Example 3.2. See Table 6.

The Comparison table of the above fuzzy-soft-set is given in Table 7.

Next we compute the row sum, column sum, and the score for each o_i as shown in Table 8.

4. Algorithm

From Tables 3–5, we see the choice value sequence is $\{c_1, c_2, \dots, c_6\} = \{1.0, 1.0, 1.1, 1.2, 2.1, 2.2\}$ and the score sequence is $\{s_1, s_2, \dots, s_6\} = \{-13, -5, -6, 2, 16, 6\}$, where $c_5 = 2.1$, $c_6 = 2.2$, $s_5 = 16$, $s_6 = 6$. In general, o_5 is the optimal choice when considering the choice value and score value together. From Tables 6–8, we see the choice value sequence is $\{c_1, c_2, \dots, c_6\} = \{1.4, 1.3, 1.3, 1.8, 1.9, 2.9\}$ and the score sequence is $\{s_1, s_2, \dots, s_6\} = \{1, -7, -4, -5, 8, 7\}$, where $c_5 = 1.9$, $c_6 = 2.9$, $s_5 = 8$, $s_6 = 7$. In general, o_6 is the optimal choice. We now present an algorithm to solve the above problems.

Algorithm.

Step 1.

Input some kind of evaluation requirements, for example, the choice value sequence $\{c_1, c_2, \dots, c_n\}$ and the score sequence $\{s_1, s_2, \dots, s_n\}$, where c_i and s_i are associate with object o_i .

Step 2.

Grey relational generating

$$c'_i = \frac{c_i - \text{Min}\{c_i, i = 1, \dots, n\}}{\text{Max}\{c_i, i = 1, \dots, n\} - \text{Min}\{c_i, i = 1, \dots, n\}},$$

$$s'_i = \frac{s_i - \text{Min}\{s_i, i = 1, \dots, n\}}{\text{Max}\{s_i, i = 1, \dots, n\} - \text{Min}\{s_i, i = 1, \dots, n\}}.$$

Step 3.

Reorder sequence. $\{c'_1, s'_1\}, \dots, \{c'_n, s'_n\}$, where $\{c'_i, s'_i\}$ is associated with object o_i .

Step 4.

Difference Information.

$$\begin{aligned} c_{\max} &= \text{Max}\{c'_i, i = 1, \dots, n\}, & s_{\max} &= \text{Max}\{s'_i, i = 1, \dots, n\}, & \Delta c'_i &= |c_{\max} - c'_i|, & \Delta s'_i &= |s_{\max} - s'_i|. \\ \Delta_{\max} &= \text{Max}\{\Delta c'_i, \Delta s'_i, i = 1, \dots, n\}, & \Delta_{\min} &= \text{Min}\{\Delta c'_i, \Delta s'_i, i = 1, \dots, n\}. \end{aligned}$$

Step 5.

Grey relative coefficient.

$$\begin{aligned} \gamma(c, c_i) &= \frac{\Delta_{\min} + \xi * \Delta_{\max}}{\Delta c'_i + \xi * \Delta_{\max}}, \\ \gamma(s, s_i) &= \frac{\Delta_{\min} + \xi * \Delta_{\max}}{\Delta s'_i + \xi * \Delta_{\max}}, \end{aligned}$$

where ξ is the distinguishing coefficient, $\xi \in [0, 1]$. The purpose of the distinguishing coefficient is to expand or compress the range of the grey relational coefficient. In this paper, $\xi = 0.5$.

Step 6.

Grey relational grade. $\gamma(o_i) = (\omega_1 * \gamma(c, c_i) + \omega_2 * \gamma(s, s_i))$, where $\omega_i, i = 1, 2$ is the weight of evaluation factor, $\omega_1 + \omega_2 = 1$. In this paper, $\omega_1 = \omega_2 = 0.5$.

Step 7.

Decision making. The decision is o_k if $o_k = \max \gamma(o_k)$. Optimal choices have more than one object if there are more objects corresponding to the maximum.

Using the above algorithm, we discuss [Examples 3.1](#) and [3.2](#) in the following.

Decision for [Example 3.1](#).

Step 1.

The choice value sequence $\{c_1, c_2, \dots, c_6\} = \{1.0, 1.0, 1.1, 1.2, 2.1, 2.2\}$ and the score sequence is $\{s_1, s_2, \dots, s_6\} = \{-13, -5, -6, 2, 16, 6\}$.

Step 2.

$$\begin{aligned} \text{Min}\{c_i, i = 1, \dots, 6\} &= 1.0, & \text{Max}\{c_i, i = 1, \dots, 6\} &= 2.2, & c'_i &= (c_i - 1.0)/1.2. \\ \{c'_1, c'_2, \dots, c'_6\} &= \{0, 0, 0.083, 0.167, 0.917, 1\}. & \{s'_1, s'_2, \dots, s'_6\} &= \{0, 0.276, 0.241, 0.517, 1, 0.655\}. \end{aligned}$$

Step 3.

$$\begin{aligned} \{c'_1, s'_1\} &= \{0, 0\}, & \{c'_2, s'_2\} &= \{0, 0.276\}, & \{c'_3, s'_3\} &= \{0.083, 0.241\}, & \{c'_4, s'_4\} &= \{0.167, 0.517\}, \\ \{c'_5, s'_5\} &= \{0.917, 1\}, & \{c'_6, s'_6\} &= \{1, 0.655\}. \end{aligned}$$

Step 4.

$$\begin{aligned} c_{\max} &= 1, & s_{\max} &= 1, & \Delta c'_1 &= 1, & \Delta c'_2 &= 1, & \Delta c'_3 &= 0.917, & \Delta c'_4 &= 0.833, & \Delta c'_5 &= 0.083, \\ \Delta c'_6 &= 0; & \Delta s'_1 &= 1, & \Delta s'_2 &= 0.724, & \Delta s'_3 &= 0.759, & \Delta s'_4 &= 0.483, & \Delta s'_5 &= 0, & \Delta s'_6 &= 0.345. \\ \Delta_{\max} &= 1, & \Delta_{\min} &= 0. \end{aligned}$$

Step 5.

$$\begin{aligned} \gamma(c, c_1) &= 0.333, & \gamma(c, c_2) &= 0.333, & \gamma(c, c_3) &= 0.353, & \gamma(c, c_4) &= 0.375, & \gamma(c, c_5) &= 0.858, \\ \gamma(c, c_6) &= 1; & \gamma(s, s_1) &= 0.333, & \gamma(s, s_2) &= 0.408, & \gamma(s, s_3) &= 0.397, & \gamma(s, s_4) &= 0.509, \\ \gamma(s, s_5) &= 1, & \gamma(s, s_6) &= 0.529. \end{aligned}$$

Step 6.

$$\begin{aligned} \gamma(o_1) &= 0.333, & \gamma(o_2) &= 0.371, & \gamma(o_3) &= 0.375, & \gamma(o_4) &= 0.442, & \gamma(o_5) &= 0.929, \\ \gamma(o_6) &= 0.796. \end{aligned}$$

Step 7. The decision is o_5 .

For [Example 3.2](#), with the same steps we can obtain.

Step 1. The choice value sequence $\{c_1, c_2, \dots, c_6\} = \{1.4, 1.3, 1.3, 1.8, 1.9, 2.9\}$ and the score sequence is $\{s_1, s_2, \dots, s_6\} = \{1, -7, -4, -5, 8, 7\}$.

Step 2.

$$\begin{aligned} \min\{c_i, i = 1, \dots, 6\} &= 1.3, & \max\{c_i, i = 1, \dots, 6\} &= 2.9. \\ c'_i &= (c_i - 1.3)/1.6, & \{c'_1, c'_2, \dots, c'_6\} &= \{0.063, 0, 0, 0.313, 0.375, 1\}. \\ \{s'_1, s'_2, \dots, s'_6\} &= \{0.533, 0, 0.2, 0.133, 1, 0.933\}. \end{aligned}$$

Step 3.

$$\begin{aligned} \{c'_1, s'_1\} &= \{0.063, 0.533\}, & \{c'_2, s'_2\} &= \{0, 0\}, & \{c'_3, s'_3\} &= \{0, 0.2\}, & \{c'_4, s'_4\} &= \{0.313, 0.133\}, \\ \{c'_5, s'_5\} &= \{0.375, 1\}, & \{c'_6, s'_6\} &= \{1, 0.933\}. \end{aligned}$$

Step 4.

$$\begin{aligned} c_{\max} &= 1, & s_{\max} &= 1, & \Delta c'_1 &= 0.937, & \Delta c'_2 &= 1, & \Delta c'_3 &= 1, & \Delta c'_4 &= 0.687, & \Delta c'_5 &= 0.625, \\ \Delta c'_6 &= 0; & \Delta s'_1 &= 0.467, & \Delta s'_2 &= 1, & \Delta s'_3 &= 0.8, & \Delta s'_4 &= 0.867, & \Delta s'_5 &= 0, & \Delta s'_6 &= 0.067. \\ \Delta_{\max} &= 1, & \Delta_{\min} &= 0. \end{aligned}$$

Step 5.

$$\begin{aligned} \gamma(c, c_1) &= 0.348, & \gamma(c, c_2) &= 0.333, & \gamma(c, c_3) &= 0.333, & \gamma(c, c_4) &= 0.421, & \gamma(c, c_5) &= 0.444, \\ \gamma(c, c_6) &= 1; & \gamma(s, s_1) &= 0.517, & \gamma(s, s_2) &= 0.333, & \gamma(s, s_3) &= 0.385, & \gamma(s, s_4) &= 0.366, \\ \gamma(s, s_5) &= 1, & \gamma(s, s_6) &= 0.882. \end{aligned}$$

Step 6.

$$\begin{aligned} \gamma(o_1) &= 0.433, & \gamma(o_2) &= 0.333, & \gamma(o_3) &= 0.359, & \gamma(o_4) &= 0.393, & \gamma(o_5) &= 0.722, \\ \gamma(o_6) &= 0.941. \end{aligned}$$

Step 7. The decision is o_6 .

5. Example

The primary motivation for designing the algorithm is to solve decision making problems by using grey theory. To illustrate the basic idea of the algorithm, we apply it to soft set based decision making problems. Let us consider Example 4 in [7].

Example 4 [7]. Assume that a company wants to fill a position. There are 48 candidates who fill in a form in order to apply formally for the position. There are two decision makers; one of them is from the department of human resources and the other one is from the board of directors. They want to interview the candidates, but it is very difficult to do this for all of them. Therefore, by using the uni-int decision making method, the number of candidates are reduced to a suitable one.

Assume that the set of candidates is $U = \{u_1, u_2, \dots, u_{48}\}$, which may be characterized by a set of parameters $E = \{x_1, x_2, \dots, x_7\}$. For $i = 1, 2, \dots, 7$, the parameters x_i stand for “experience”, “computer knowledge”, “training”, “young age”, “higher education”, “marriage status” and “good health”, respectively. See Table 9.

Now, apply the uni-int- \wedge as follows:

Step 1: The decision makers consider the sets of parameters, $A = \{x_1, x_2, x_4, x_7\}$ and $B = \{x_1, x_2, x_5\}$, respectively, to evaluate the candidates.

Step 2: The decision makers seriously investigate the CV of the candidates. After a serious discussion each candidate is evaluated from the point of view of the goals and the constraint according to a chosen subset $A, B \subseteq E$. Then the decision makers construct the following two soft sets over U according to their parameters, respectively.

$$\begin{aligned} F_A &= \{(x_1, \{u_4, u_7, u_{13}, u_{21}, u_{28}, u_{31}, u_{32}, u_{36}, u_{39}, u_{41}, u_{43}, u_{44}, u_{48}\}), \\ &\quad (x_2, \{u_1, u_3, u_{13}, u_{18}, u_{19}, u_{21}, u_{22}, u_{24}, u_{28}, u_{32}, u_{36}, u_{42}, u_{44}, u_{46}\}), \\ &\quad (x_4, \{u_2, u_3, u_{13}, u_{15}, u_{18}, u_{23}, u_{25}, u_{28}, u_{30}, u_{33}, u_{36}, u_{38}, u_{42}, u_{43}\}), \\ &\quad (x_7, \{u_1, u_5, u_{12}, u_{13}, u_{17}, u_{20}, u_{24}, u_{28}, u_{29}, u_{34}, u_{36}, u_{41}, u_{45}, u_{47}\})\}. \\ F_B &= \{(x_1, \{u_3, u_4, u_5, u_8, u_{14}, u_{21}, u_{22}, u_{26}, u_{27}, u_{34}, u_{35}, u_{37}, u_{40}, u_{42}, u_{46}\}), \\ &\quad (x_2, \{u_1, u_4, u_7, u_{10}, u_{11}, u_{13}, u_{15}, u_{21}, u_{29}, u_{30}, u_{32}, u_{36}, u_{42}, u_{43}, u_{45}\}), \\ &\quad (x_5, \{u_2, u_4, u_8, u_9, u_{12}, u_{13}, u_{14}, u_{16}, u_{17}, u_{21}, u_{23}, u_{28}, u_{36}, u_{42}, u_{44}\})\}. \end{aligned}$$

Step 3: Now, we can find the \wedge -production $F_A \wedge F_B$ of the soft sets F_A and F_B as follows:

$$\begin{aligned} &\{((x_1, x_1), \{u_4, u_{21}\}), ((x_1, x_2), \{u_4, u_7, u_{13}, u_{21}, u_{32}, u_{36}, u_{43}\}), \\ &\quad ((x_1, x_5), \{u_4, u_{13}, u_{21}, u_{28}, u_{36}, u_{44}\}), ((x_2, x_1), \{u_3, u_{21}, u_{22}, u_{42}, u_{46}\})\}, \\ &\{((x_2, x_2), \{u_1, u_{13}, u_{21}, u_{32}, u_{36}, u_{42}\}), ((x_2, x_5), \{u_{13}, u_{21}, u_{28}, u_{36}, u_{42}, u_{44}\})\}, \\ &\{((x_4, x_1), \{u_3, u_{42}\}), ((x_4, x_2), \{u_{13}, u_{15}, u_{30}, u_{36}, u_{42}, u_{43}\})\}, \\ &\{((x_4, x_5), \{u_2, u_{13}, u_{23}, u_{28}, u_{36}, u_{42}\}), ((x_7, x_1), \{u_5, u_{34}\})\}, \\ &\{((x_7, x_2), \{u_1, u_{13}, u_{29}, u_{36}, u_{45}\}), ((x_7, x_5), \{u_{12}, u_{13}, u_{17}, u_{28}, u_{36}\})\}. \end{aligned}$$

Table 9

Score table A and B.

	u_1	u_2	u_3	u_4	u_5	u_6	u_7	u_8	u_9	u_{10}	u_{11}	u_{12}	u_{13}	u_{14}	u_{15}	u_{16}	u_{17}	u_{18}	u_{19}	u_{20}	u_{21}	u_{22}	u_{23}	u_{24}
c_{Ai}	2	1	2	1	1	0	1	0	0	0	0	1	4	0	1	0	1	2	1	1	2	1	1	2
c_{Bi}	1	1	1	3	1	0	1	2	1	1	1	1	2	2	1	1	1	0	0	0	3	1	1	0
	u_{25}	u_{26}	u_{27}	u_{28}	u_{29}	u_{30}	u_{31}	u_{32}	u_{33}	u_{34}	u_{35}	u_{36}	u_{37}	u_{38}	u_{39}	u_{40}	u_{41}	u_{42}	u_{43}	u_{44}	u_{45}	u_{46}	u_{47}	u_{48}
c_{Ai}	1	0	0	4	1	1	1	2	1	1	0	4	0	1	1	0	2	2	2	2	1	1	1	1
c_{Bi}	0	1	1	1	1	1	0	1	0	1	1	2	1	0	0	1	0	3	1	1	1	1	0	0

Table 10

Grey relational generation table A and B.

	u_1	u_2	u_3	u_4	u_5	u_6	u_7	u_8	u_9	u_{10}	u_{11}	u_{12}	u_{13}	u_{14}	u_{15}	u_{16}	u_{17}	u_{18}	u_{19}	u_{20}	u_{21}	u_{22}	u_{23}	u_{24}
c'_{Ai}	0.5	0.25	0.5	0.25	0.25	0	0.25	0	0	0	0	0.25	1	0	0.25	0	0.25	0.5	0.25	0.25	0.5	0.25	0.25	0.5
c'_{Bi}	0.33	0.33	0.33	1	0.33	0	0.33	0.67	0.33	0.33	0.33	0.33	0.67	0.67	0.33	0.33	0.33	0	0	0	1	0.33	0.33	0
	u_{25}	u_{26}	u_{27}	u_{28}	u_{29}	u_{30}	u_{31}	u_{32}	u_{33}	u_{34}	u_{35}	u_{36}	u_{37}	u_{38}	u_{39}	u_{40}	u_{41}	u_{42}	u_{43}	u_{44}	u_{45}	u_{46}	u_{47}	u_{48}
c'_{Ai}	0.25	0	0	1	0.25	0.25	0.25	0.5	0.25	0.25	0	1	0	0.25	0.25	0	0.5	0.5	0.5	0.5	0.25	0.25	0.25	0.25
c'_{Bi}	0	0.33	0.33	0.33	0.33	0.33	0	0.33	0	0.33	0.33	0.67	0.33	0	0	0.33	0	1	0.33	0.33	0.33	0.33	0	0

Step 4: Finally, we can find a decision set $\text{uni-int}(F_A \wedge F_B)$ as follows:

$$\begin{aligned}
 \text{uni}_x \text{int}_y(F_A \wedge F_B) &= \bigcup_{x \in A} (\bigcap_{y \in B} (f_{A \wedge B}(x, y))) \\
 &= \bigcup \left\{ \begin{aligned} &\cap \{ \{u_4, u_{21}\}, \{u_4, u_7, u_{13}, u_{21}, u_{32}, u_{36}, u_{43}\}, \\ &\quad \{u_4, u_{13}, u_{21}, u_{28}, u_{36}, u_{44}\} \}, \\ &\cap \{ \{u_3, u_{21}, u_{22}, u_{42}, u_{46}\}, \{u_1, u_{13}, u_{21}, u_{32}, u_{36}, u_{42}\}, \\ &\quad \{u_{13}, u_{21}, u_{28}, u_{36}, u_{42}, u_{44}\} \}, \\ &\cap \{ \{u_3, u_{42}\}, \{u_{13}, u_{15}, u_{30}, u_{36}, u_{42}, u_{43}\}, \\ &\quad \{u_2, u_{13}, u_{23}, u_{28}, u_{36}, u_{42}\} \}, \\ &\cap \{ \{u_5, u_{34}\}, \{u_1, u_{13}, u_{29}, u_{36}, u_{45}\}, \\ &\quad \{u_{12}, u_{13}, u_{17}, u_{28}, u_{36}\} \}. \end{aligned} \right\} \\
 &= \cup \{ \{u_4, u_{21}\}, \{u_{21}, u_{42}\}, \{u_{42}\}, \emptyset \} = \{u_4, u_{21}, u_{42}\}
 \end{aligned}$$

and

$$\begin{aligned}
 \text{uni}_y \text{int}_x(F_A \wedge F_B) &= \bigcup_{y \in B} (\bigcap_{x \in A} (f_{A \wedge B}(x, y))) \\
 &= \bigcup \left\{ \begin{aligned} &\cap \{ \{u_4, u_{21}\}, \{u_3, u_{21}, u_{22}, u_{42}, u_{46}\}, \{u_3, u_{42}\}, \{u_5, u_{34}\} \}, \\ &\cap \{ \{u_4, u_7, u_{13}, u_{21}, u_{32}, u_{36}, u_{43}\}, \{u_1, u_{13}, u_{21}, u_{32}, u_{36}, u_{42}\}, \\ &\quad \{u_{13}, u_{15}, u_{30}, u_{36}, u_{42}, u_{43}\}, \{u_1, u_{13}, u_{29}, u_{36}, u_{45}\} \}, \\ &\cap \{ \{u_4, u_{13}, u_{21}, u_{28}, u_{36}, u_{44}\}, \{u_{13}, u_{21}, u_{28}, u_{36}, u_{42}, u_{44}\}, \\ &\quad \{u_2, u_{13}, u_{23}, u_{28}, u_{36}, u_{42}\}, \{u_{12}, u_{13}, u_{17}, u_{28}, u_{36}\} \}. \end{aligned} \right\} \\
 &= \cup \{ \emptyset, \{u_{13}, u_{36}\}, \{u_{13}, u_{28}, u_{36}\} \} = \{u_{13}, u_{28}, u_{36}\}.
 \end{aligned}$$

Hence, the decision makers to make interviewing invite the candidates which are the elements of the following uni-int decision set.

$$\begin{aligned}
 \text{uni-int}(F_A \wedge F_B) &= \text{uni}_x \text{int}_y(F_A \wedge F_B) \cup \text{uni}_y \text{int}_x(F_A \wedge F_B) = \{ \{u_4, u_{21}, u_{42}\} \cup \{u_{13}, u_{28}, u_{36}\} \} \\
 &= \{ \underline{u_4}, u_{13}, u_{21}, u_{28}, u_{36}, u_{42} \}.
 \end{aligned}$$

Note: Underline marked sets in the above algorithm process are revised because of clerical error in Example 4 of paper [7]. Therefore, one of $u_4, u_{13}, u_{21}, u_{28}, u_{36}, u_{42}$ is the optimal choice.

Now, suppose the decision makers evaluate the parameter sets $A = \{x_1, x_2, x_4, x_7\}$ and $B = \{x_1, x_2, x_5\}$ using choice values and apply soft set decision making based on grey theory as follows:

Step 1. Input two kinds of evaluation criteria.

Step 2. Grey relational generating (see Table 10).

Step 3. Reorder sequence. $\{c'_{A1}, c'_{B1}\}, \dots, \{c'_{A48}, c'_{B48}\}$.

Step 4. Difference information (see Table 11).

Step 5. Grey relative coefficient (see Table 12).

Step 6. Grey relational grade. $\omega_1 = \omega_2 = 0.5$ (see Table 13).

Step 7. Decision making. From the grey relational grade, we can see u_{13} and u_{36} are the optimal choices.

Table 11

Difference information table A and B.

	u_1	u_2	u_3	u_4	u_5	u_6	u_7	u_8	u_9	u_{10}	u_{11}	u_{12}	u_{13}	u_{14}	u_{15}	u_{16}	u_{17}	u_{18}	u_{19}	u_{20}	u_{21}	u_{22}	u_{23}	u_{24}
$\Delta c'_{Ai}$	0.5	0.75	0.5	0.75	0.75	1	0.75	1	1	1	1	0.75	0	1	0.75	1	0.75	0.5	0.75	0.75	0.5	0.75	0.75	0.5
$\Delta c'_{Bi}$	0.67	0.67	0.67	0	0.67	1	0.67	0.33	0.67	0.67	0.67	0.67	0.33	0.33	0.67	0.67	0.67	1	1	1	0	0.67	0.67	1
	u_{25}	u_{26}	u_{27}	u_{28}	u_{29}	u_{30}	u_{31}	u_{32}	u_{33}	u_{34}	u_{35}	u_{36}	u_{37}	u_{38}	u_{39}	u_{40}	u_{41}	u_{42}	u_{43}	u_{44}	u_{45}	u_{46}	u_{47}	u_{48}
$\Delta c'_{Ai}$	0.75	1	1	0	0.75	0.75	0.75	0.5	0.75	0.75	1	0	1	0.75	0.75	1	0.5	0.5	0.5	0.5	0.75	0.75	0.75	0.75
$\Delta c'_{Bi}$	1	0.67	0.67	0.67	0.67	0.67	1	0.67	1	0.67	0.67	0.33	0.67	1	1	0.67	1	0	0.67	0.67	0.67	0.67	1	1

Table 12

Grey relative coefficient table A and B.

	u_1	u_2	u_3	u_4	u_5	u_6	u_7	u_8	u_9	u_{10}	u_{11}	u_{12}	u_{13}	u_{14}	u_{15}	u_{16}	u_{17}	u_{18}	u_{19}	u_{20}	u_{21}	u_{22}	u_{23}	u_{24}
$\gamma(c, c_{Ai})$	0.5	0.4	0.5	0.4	0.4	0.33	0.4	0.33	0.33	0.33	0.33	0.4	1	0.33	0.4	0.33	0.4	0.5	0.4	0.4	0.5	0.4	0.4	0.5
$\gamma(c, c_{Bi})$	0.43	0.43	0.43	1	0.43	0.33	0.43	0.6	0.43	0.43	0.43	0.43	0.6	0.6	0.43	0.43	0.43	0.33	0.33	0.33	1	0.43	0.43	0.33
	u_{25}	u_{26}	u_{27}	u_{28}	u_{29}	u_{30}	u_{31}	u_{32}	u_{33}	u_{34}	u_{35}	u_{36}	u_{37}	u_{38}	u_{39}	u_{40}	u_{41}	u_{42}	u_{43}	u_{44}	u_{45}	u_{46}	u_{47}	u_{48}
$\gamma(c, c_{Ai})$	0.4	0.33	0.33	1	0.4	0.4	0.4	0.5	0.4	0.4	0.33	1	0.33	0.4	0.4	0.33	0.5	0.5	0.5	0.5	0.4	0.4	0.4	0.4
$\gamma(c, c_{Bi})$	0.33	0.43	0.43	0.43	0.43	0.43	0.33	0.43	0.33	0.43	0.43	0.6	0.43	0.33	0.33	0.43	0.33	1	0.43	0.43	0.43	0.43	0.33	0.33

Table 13

Grey relation grade table A and B.

	u_1	u_2	u_3	u_4	u_5	u_6	u_7	u_8	u_9	u_{10}	u_{11}	u_{12}	u_{13}	u_{14}	u_{15}	u_{16}	u_{17}	u_{18}	u_{19}	u_{20}	u_{21}	u_{22}	u_{23}	u_{24}
$\gamma(u_i)$	0.46	0.41	0.46	0.7	0.41	0.33	0.41	0.47	0.38	0.38	0.38	0.41	0.8	0.47	0.41	0.38	0.41	0.42	0.37	0.37	0.75	0.41	0.41	0.42
	u_{25}	u_{26}	u_{27}	u_{28}	u_{29}	u_{30}	u_{31}	u_{32}	u_{33}	u_{34}	u_{35}	u_{36}	u_{37}	u_{38}	u_{39}	u_{40}	u_{41}	u_{42}	u_{43}	u_{44}	u_{45}	u_{46}	u_{47}	u_{48}
$\gamma(u_i)$	0.37	0.38	0.38	0.72	0.41	0.41	0.37	0.46	0.37	0.41	0.38	0.8	0.38	0.37	0.37	0.38	0.42	0.75	0.46	0.46	0.41	0.41	0.41	0.37

Remark. If we select $\gamma(u_i) \geq 0.5$, the objects $u_4 = 0.7$, $u_{13} = 0.8$, $u_{21} = 0.75$, $u_{28} = 0.72$, $u_{36} = 0.8$ and $u_{42} = 0.75$ meet the requirements, which is consistent with the result of the uni-int decision making method. But the uni-int decision making method is a preprocessing method and cannot give the final decision. Furthermore, the uni-int decision making method can only deal with soft set decision problems. For fuzzy soft set decision problems, it does not work well. The algorithm in this paper is suitable for soft set and fuzzy soft set decision making problems and unconstrained for evaluation methods. Whatever kind of evaluation methods we choose, as long as every evaluation sequence is given, such as choice value sequence, score value sequence, or other sequences, then we can make the decision using this new algorithm. The evaluation sequence associates to a kind of evaluation method, so this new algorithm is a hybrid evaluation method for comprehensive evaluation. Also, this new algorithm is objective, numerical and accurate, and we can compare the value to obtain the optimal choice, suboptimal choice, and so on.

6. Conclusions

In this paper, we use multiple evaluation bases to make decisions. A new algorithm for multiple evaluation bases for the fuzzy soft set decision making problem is presented based on grey theory. Using this new algorithm the decision result is general and efficient.

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