

# Soil moisture deficit estimation using satellite multi-angle brightness temperature



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## SUMMARY

Accurate soil moisture information is critically important for hydrological modelling. Although remote sensing soil moisture measurement has become an important data source, it cannot be used directly in hydrological modelling. A novel study based on nonlinear techniques (a local linear regression (LLR) and two feedforward artificial neural networks (ANNs)) is carried out to estimate soil moisture deficit (SMD), using the Soil Moisture and Ocean Salinity (SMOS) multi-angle brightness temperatures ( $T_{bs}$ ) with both horizontal (H) and vertical (V) polarisations. The gamma test is used for the first time to determine the optimum number of  $T_{bs}$  required to construct a reliable smooth model for SMD estimation, and the relationship between model input and output is achieved through error variance estimation. The simulated SMD time series in the study area is from the Xinjiang hydrological model. The results have shown that LLR model is better at capturing the interrelations between SMD and  $T_{bs}$  than ANNs, with outstanding statistical performances obtained during both training ( $NSE = 0.88$ ,  $r = 0.94$ ,  $RMSE = 0.008$  m) and testing phases ( $NSE = 0.85$ ,  $r = 0.93$ ,  $RMSE = 0.009$  m). Nevertheless, both ANN training algorithms (radial BFGS and conjugate gradient) have performed well in estimating the SMD data and showed excellent performances compared with those derived directly from the SMOS soil moisture products. This study has also demonstrated the informative capability of the gamma test in the input data selection for model development. These results provide interesting perspectives for data-assimilation in flood-forecasting.

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## 1. Introduction

Although soil moisture comprises only 0.01% of the total amount of water on our planet, its existence plays an important role in influencing the water and energy exchanges at the land surface/atmosphere interface. There is abundant evidence that hydrological processes are significantly conditioned by a river catchment's antecedent wetness state (Massari et al., 2014; Trambly et al., 2012). In particular the surface soil wetness is an important variable in hydrological modelling because it controls key processes such as runoff and evapotranspiration, and is a vital parameter for flood modelling (Draper et al., 2011; Han et al., 2012)

The Earth thermal emission at microwave bands depends essentially on the soil temperature and the soil water content (Al-Yaari et al., 2014; Rodríguez-Fernández et al., 2015). Recent research activities indicate rising interest in the operational monitoring of the global soil moisture remote sensing. In particu-

lar, the data acquired by lower microwave frequencies (e.g., L-band at 1.20–1.41 GHz), both active and passive, have been utilised to provide detailed surface soil moisture fluctuations in recent years (Calvet et al., 2011). The launch of the Soil Moisture and Ocean Salinity (SMOS; (Kerr et al., 2001)) mission in November 2009 and the Soil Moisture Active/Passive mission (SMAP; (Entekhabi et al., 2010)) in January 2015 clearly demonstrates the significance and determination of an advanced global surface soil moisture monitoring system. SMOS is the first mission dedicated to monitoring direct surface soil moisture and sea surface salinity on a global scale (Kerr et al., 2010), and has a longer period of data record since its launch in 2009. Therefore, SMOS is chosen in this study.

The SMOS soil moisture operational algorithm utilises a direct or forward model and an optimal estimation method: a radiative transfer model (e.g., LMEB model is used in the SMOS algorithm (Wigneron et al., 2007)) is applied to estimate L-band brightness temperatures (hereafter  $T_{bs}$ ) for a set of physical parameters, soil composition, and moisture content and vegetation opacity (Rodríguez-Fernández et al., 2015). In order to estimate soil moisture, the simulated  $T_{bs}$  are compared with those measured by SMOS

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using an iterative process to minimise the difference between them. This approach then requires in-situ observation data for soil moisture evaluation (Al-Yaari et al., 2014; Al Bitar et al., 2012). However most areas do not have in-situ sensors because they are expensive to set up and impractical to maintain; and they are too sparse for catchment-scale studies (Al-Shrafany et al., 2013; Srivastava et al., 2013b, 2013c; Walker et al., 2004; Wang and Qu, 2009). Since the presence of vegetation can reduce the brightness temperature sensitivity to soil moisture, in the aforementioned method decoupling the effects of soil and vegetation on brightness temperature can pose a major challenge for useful application under such circumstances.

In order to retrieve accurate soil wetness information that can be directly used in a hydrological model and avoid aforementioned shortcomings, a data-driven model is desirable, which could effectively link the inputs to the desired output and is not computationally intensive. This can be achieved by building an inverse model that provides soil moisture information (i.e., soil moisture deficit (SMD) in this study, which is a key soil moisture variable in hydrological models (Zhuo et al., 2015a)) directly from a given set of satellite measured  $T_b$ s. Among the data-driven models, nonlinear regression models such as Local Linear Regression (LLR) and Artificial Neural Networks (ANNs) are widely recognised and used as efficient inverse models. Therefore both LLR and ANNs are used in this study.

The foremost objective of this study is therefore to build an inverse model for the first time that can simulate the relevant hydrological SMD data directly from the SMOS brightness temperatures using various nonlinear modelling techniques. In this study, the SMD is estimated instead of the normal soil moisture because in hydrological modelling the excess runoff is closely linked with SMD, but not directly with the normal soil moisture (i.e., the volumetric soil moisture). The SMD refers to the amount of water needed to bring the soil moisture back to field capacity. Since SMD is directly relevant to hydrology, it is the main purpose of this study. SMOS is the first radiometer in space with full-polarisation and multangular capabilities (Rodríguez-Fernández et al., 2015). Hence, a dedicated retrieval scheme has to be studied. An LLR model and two ANN models are trained and tested for their valuation in SMD retrieval. The modelled SMD values using different techniques are then compared against the Xinanjiang simulated SMD as the target. Furthermore, a well-proven and widely applied computing algorithm called the gamma test (GT) is employed to find the optimal combination of data inputs for SMD calculation. Noori et al. (2011) and Remesan et al. (2008) applied the GT data selection method in hydrological studies, for daily solar radiation estimation and monthly streamflow prediction, and both reported positive performances. In contrast to the conventional allocation method of the training and the testing data, the *M*-test is adopted to find the optimal training dataset which has sufficient information for training any regression models. This will avoid wasting time and effort in allocating excessive training data or using inadequate training data. Therefore, no predefined training and testing data will be specified at the early stage of the study. Finally, the SMD estimates from the aforementioned nonlinear methods are compared with those directly derived from the SMOS soil moisture products (i.e., two different SMOS products are used: one is from the SMOS Barcelona Expert Centre (SMOS-BEC) (SMOS-BEC, 2015) and the other is from the Centre Aval de Traitement des Données SMOS (SMOS-CATDS) (Jacquette et al., 2010)).

## 2. Study area and data

Pontiac is a medium-sized catchment (1500 km<sup>2</sup>) in the Vermilion River, located in the central Illinois area of the U.S. The

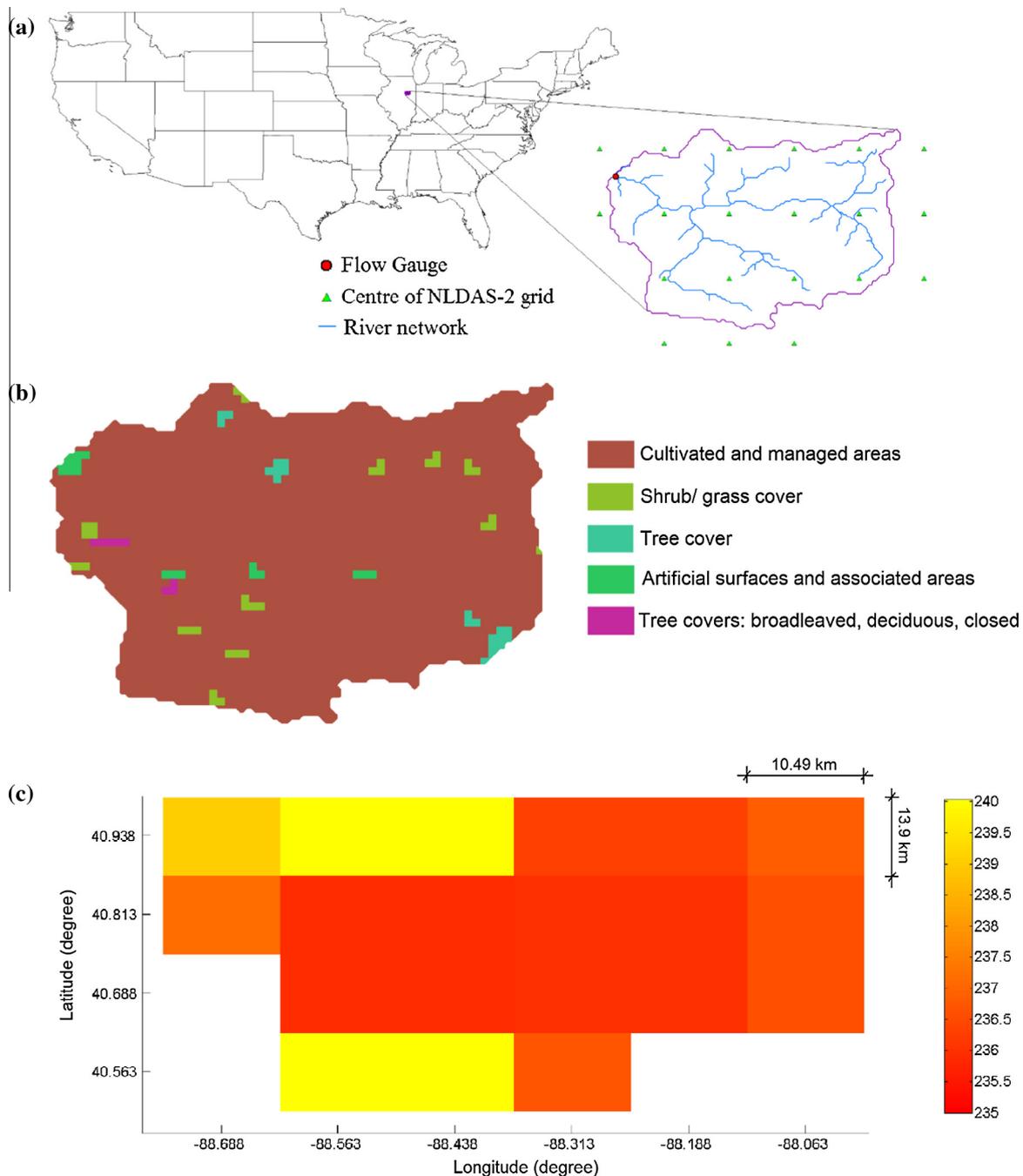
catchment's topography is flat and mainly used for cultivation purpose as illustrated in Fig. 1b (Bartholomé and Belward, 2005; Hansen et al., 1998). Based on the Global Soil Regions map (USDA, 2005), its soil is predominately Mollisols. The catchment is dominated mainly by hot summer continental climate (Peel et al., 2007). The layout of the Pontiac catchment is shown in Fig. 1a along with the location of its flow gauge, river network, and the North American Land Data Assimilation Systems Phase 2 (NLDAS-2) grid points (i.e., the marked grid points are located at the central of each 0.125° × 0.125° NLDAS-2 grids). The spatial variations of an extracted SMOS  $T_b$  dataset (H polarisation) at an incidence angle of 32.5° is shown in Fig. 1c (it has been transformed into NLDAS-2 grid spacing at 0.125° for easier analysis). It can be seen from this retrieved image, the central catchment area has lower  $T_b$  values (i.e., relatively wetter soil), while the western upper and lower parts show slightly higher  $T_b$  values (i.e., relatively drier soil). This could partially be explained by the location of the river network as indicated in Fig. 1a: the majority of the water concentrates at the central area (i.e., the mainstream) and then flows to the catchment outlet (so the soil can be replenished with water more easily); whereas the soil around the small substream areas has less water availability and tends to be drier. It should be noted that soil moisture does not solely correlate with the variation of brightness temperature but also with other factors such as vegetation cover, local soil properties, and surface roughness.

The Xinanjiang (XAJ) model's hydrological forcing is obtained from the NLDAS-2 (Mitchell et al., 2004). The datasets comprise precipitation (Daly et al., 1994) and potential evapotranspiration at the 0.125° spatial resolution and daily temporal resolution (converted from hourly resolution). Both datasets have been transformed into the catchment-scale using the weighted average method to operate the lumped XAJ model. Readers are referred to Xia et al. (2012) and Zhuo et al. (2015c) for a full description of the NLDAS-2 data products. The observed daily flow data for this study is provided by the U.S. Geological Survey. The observations cover a total period of 24-months from January 2010 to December 2011. The reason for using these two-year data is due to the discontinuity of flow observations in the selected catchment.

### 2.1. SMOS data

SMOS retrieves the thermal emission from the Earth at the frequency of 1.4 GHz in both polarisations and for incidence angles from 0° to 60°. It is dedicated to providing global surface soil moisture information at an accuracy of 0.04 m<sup>3</sup>/m<sup>3</sup> (Kerr et al., 2012). SMOS has a Y-shaped antenna structure, which comprises 69 small antennas (a diameter of 16.5 cm) and 4.5-m long arms to perform interferometry and synthesise an aperture of ~7.5 m (McMullan et al., 2008; Rodríguez-Fernández et al., 2015). The projection of the synthesised beam on the Earth surface is generally presented as an ellipse whose axis ratio and orientation depend on the observed point position (Rodríguez-Fernández et al., 2015). The retrieved observations have a spatial resolution of 35–50 km (Kerr et al., 2010). SMOS follows a sun-synchronous polar orbit with a global coverage at the equator crossing the times of 6:00 A.M. at the local solar time (LST) (ascending) and 6:00 P.M. (LST, descending).

In order to estimate SMD from SMOS  $T_b$ s, the Level-3 brightness temperature data from the CATDS is used (Jacquette et al., 2010). This daily global brightness temperature data contains SMOS  $T_b$ s in the reference frame of 0.25° EASE grid (Brodzik and Knowles, 2002) on the Earth surface. It provides  $T_b$ s measurements acquired at all incidence angles in a given day (averaged in 5° – width angle bins) which have been transformed into the ground polarisation reference frame (i.e., H, and V polarisations). Hence, the quantity



**Fig. 1.** (a) Geographical location of the study area with river network, flow gauge and NLDAS-2 grids; (b) GIS extracted GLC2000 land-use map; (c) spatial variations of the retrieved SMOS brightness temperature (in kelvins) data on 13/01/2010 at the ascending overpass, with the H polarisation and incidence angle of  $32.5^\circ$  for the catchment area (it has been transformed into NLDAS-2 grids at  $0.125^\circ \times 0.125^\circ$  grid spacing for easier analysis).

of the input data can be as high as 24 (12 angle bins per polarisation), with the centre of the first angle bin at  $2.5^\circ$  in both polarisations (Rodríguez-Fernández et al., 2014). In this catchment, the only angle range that gives the most available record of data is from  $27.5^\circ$  to  $57.5^\circ$  (i.e., 7 for H and 7 for V polarisation), which is therefore chosen for the model development. In order to better understand the sensitivity of SMOS  $T_b$ s to the SMD, the Pearson correlation coefficients ( $r$ ) are calculated and illustrated in Fig. 2. It can be seen that the correlation decreases for H polarisation when the incidence angle rises (from  $r \sim 0.55$  to  $r \sim 0.45$ ); whereas the correlation for V polarisation is more stable and fluctuates around 0.6–0.65. This phenomenon agrees with the general

trend of the theoretical effect of H–V polarisations at different incidence angles (Wei et al., 2014).

Additionally, the Level-3 soil moisture products from the CATDS (SMOS-CATDS) and the BEC (SMOS-BEC) are also obtained for a comparison study. The main difference between these two products is that they are made from different data inputs. The SMOS-BEC utilises the Level-2 Soil Moisture User Data Product (UDP) generated by ESA as its Level-3 data inputs, while SMOS-CATDS goes in a rather unusual way by using brightness temperature products in the Fourier domain (L1B) as input for the Level-3 processor. The detailed comparison between these two products is beyond the scope of this paper, and the interested readers are referred to

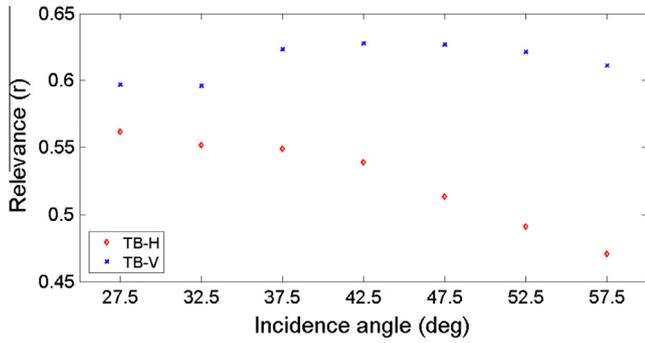


Fig. 2. Correlations  $r$  between the SMOS multangular brightness temperatures with H and V polarisations and the XAJ SMD.

Elsa et al. (2013) and SMOS-BEC (2015) for full descriptions. All acquired SMOS products cover the period between January 2010 and December 2011 and have been converted into a catchment-scale dataset by the weighted average method. Furthermore, they have been re-scaled by mapping the mean to zero and the standard deviation to 0.5. This normalisation step is able to equalise the relative numerical difference among the input variables and better aid the GT feature selection routine (Remesan et al., 2008). It is noted that the re-scaled data is only for the GT routine and the  $M$ -test, and normal data are used for SMD estimation.

### 3. Methodology

#### 3.1. XAJ model

The XAJ model developed by Zhao (1980, 1992) and Zhao and Liu (1995) is a widely used conceptual rainfall–runoff model. The model has been proven in many publications to be effective for both operational and offline simulation purposes in humid, semi-humid regions (Chen et al., 2013; Shi et al., 2011; Zhao, 1992; Zhao and Liu, 1995; Zhuo et al., 2015b, 2015c) as well as dry areas (Gan et al., 1997) around the world. The main hypothesis used in the model development is the runoff generation on repletion of its storage capacity, which means that runoff is not generated until the soil water reaches the field capacity (Zhao, 1992). In this study, the XAJ model is used for SMD estimation through an improved soil moisture accounting scheme (Zhuo and Han, 2016a, 2016b). Further details on calibration and validation of the XAJ model and the SMD are discussed by Zhuo et al. (2015a) and Zhuo et al. (2016).

#### 3.2. Gamma test and $M$ -test

An appropriate selection of the incidence angles of the SMOS observations is important to ensure the best SMD estimation. In this study, a well-developed GT algorithm (Koncar, 1997; Stefánsson et al., 1997) is adopted because it has been proven to be efficient in selecting model inputs (Durrant, 2001; Jaafar and Han, 2011; Noori et al., 2011; Remesan et al., 2008; Tsui et al., 2002). It is a near-neighbour data analysis routine which allows efficient estimation of the minimum mean-squared error ( $MSE$ ) that can be achieved when modelling the input-output data using nonlinear models. This calculation is called the gamma statistics and represented as  $\Gamma$ . The inspiration of GT came from the *Delta test* (Pi and Peterson, 1994). Only a brief introduction on GT is provided here and the interested readers are referred to the aforementioned papers for further explanations. For simplicity a case is introduced where a set of data samples is given in the form of:

$$\{(x_i, y_i), 1 \leq i \leq M\} \quad (1)$$

where the input vectors  $x_i \in R^m$  are confined to a closed bounded set  $C \in R^m$ , and without loss of generality, the outputs  $y_i \in R$  are scalars. The vectors  $x$  comprise predictively useful information that controls the output  $y$ . The only assumption made is that the underlying relationship of the system is from the following equation:

$$y = f(x_1 \dots x_m) + r \quad (2)$$

where  $f$  is a smooth function and  $r$  is an indeterminable variable that is regarded as noise. Without loss of generality, the mean of the  $r$  distribution is assumed to be zero (because any constant bias has been considered in the unknown function  $f$ ) and that the variance of the noise  $Var(r)$  is bounded. The domain of a potential model is now restricted to the class of smooth functions which have bounded first partial derivatives. The  $\Gamma$  is an estimate of the model's output variance that cannot be accounted for by a smooth data model.

The GT is based on  $N[i, k]$ , which are the  $k$ th ( $1 \leq k \leq p$ ) nearest neighbours  $x_{N[i, k]}$  ( $1 \leq k \leq p$ ) for each vector  $x_i$  ( $1 \leq i \leq M$ ).  $p$  is a fixed integer. GT is calculated from the *Delta* function of the input vectors:

$$\delta_M(k) = \frac{1}{M} \sum_{i=1}^M |x_{N[i, k]} - x_i|^2 \quad (1 \leq k \leq p) \quad (3)$$

where  $|\dots|$  is Euclidean distance, and the related gamma function of the output values:

$$\gamma_M(k) = \frac{1}{2M} \sum_{i=1}^M |y_{N[i, k]} - y_i|^2 \quad (1 \leq k \leq p) \quad (4)$$

where  $y_{N[i, k]}$  is the corresponding output value with  $x_{N[i, k]}$ . To compute  $\Gamma$  a least-squared regression line for the  $p$  points ( $\delta_M(k), \gamma_M(k)$ ) is built as in the following equation:

$$\gamma = A\delta + \Gamma \quad (5)$$

where  $\Gamma$  is the intercept on the vertical axis (i.e.,  $\delta = 0$ ), as can be explained as:

$$\gamma_M(k) \rightarrow Var(r) \text{ in probability as } \delta_M(k) \rightarrow 0 \quad (6)$$

This gives an estimation of the optimal  $MSE$  value achievable utilising a modelling method for unknown smooth functions. The derived gradient  $A$  is also a useful indicator in showing information on the complexity of the system under investigation (the larger the  $A$  value the more complexity the model is required). The merit of GT is that it can provide valuable guidance about the system regardless of the subsequent modelling technique choice. A formal mathematical proof of the GT can be found in Evans and Jones (2002). In practice, the GT can be carried out through the winGamma™ software (Durrant, 2001).

A general practice in nonlinear modelling (e.g., LLR and ANNs) is to divide the dataset into two parts, i.e., training and testing. However many studies hastily adopted the size of their training dataset without proper examination, and this could result in unsatisfactory modelling performance. Therefore in order to determine the best training data size that can give a stable and reliable  $\Gamma$  statistics, an  $M$ -test is carried out. The  $M$ -test is accomplished by computing the  $\Gamma$  for increasing  $M$  value (indicating the effect of the training data size) and through analysing the resulting graph to determine whether the  $\Gamma$  approaches a stable asymptote (this way is easier than defining a complex algorithm). Such a procedure is useful in avoiding wasteful model-fitting attempts when the  $MSE$  from the training phase is already smaller than the  $Var(r)$ , and hence preventing the overfitting problem.

### 3.3. Nonlinear models

The modern statistical approach to nonlinear model building has led to techniques such as LLR, support vector machines, principal component analysis, feedforward ANNs, and radial basis function networks. In this study, the LLR and the ANNs are used. Only brief theoretical backgrounds relevant to the study are explained.

#### 3.3.1. Local linear regression (LLR)

LLR is a widely researched nonparametric regression methodology that has been applied in low-dimensional forecasting and smoothing problems (Liu et al., 2011; Pinson et al., 2008; Remesan et al., 2008; Sun et al., 2003). However to our knowledge it has rarely been used in soil moisture estimation, especially those simulated from the remote sensing technology. The advantages of LLR are that it can locally provide reliable statistical modelling based on a small amount of data sample, is less computationally demanding, and is able to give accurate estimations in regions of high data density in the input space. Furthermore, LLR can make an initial prediction with only three data points, and any newly updated data are used for further predictions. LLR performs local linear regression through the  $p_{max}$  nearest points to a query point, to give a linear model in the locality of the query point. This process is repeated across the training data to produce a piecewise linear model. One of the methods of choosing  $p_{max}$  is called influence statistics and is explained below (Durrant, 2001; Remesan et al., 2008).

Given a neighbourhood of  $p_{max}$  points, the following linear matrix equation needs to be calculated

$$Xm = y \quad (7)$$

where  $X$  is a  $p_{max} \times d$  matrix of the  $p_{max}$  input points in  $d$  dimensions,  $x_i$  ( $1 \leq i \leq p_{max}$ ) are the nearest neighbour points,  $y$  is a column vector at the length  $p_{max}$  of the associated outputs, and  $m$  is a column vector of parameters that has to be determined to provide the best mapping solution from  $X$  to  $y$ , such that

$$\begin{pmatrix} x_{11} & x_{12} & x_{13} & \cdots & x_{1d} \\ x_{21} & x_{22} & x_{23} & \cdots & x_{2d} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ x_{p_{max}1} & x_{p_{max}2} & x_{p_{max}3} & \cdots & x_{p_{max}d} \end{pmatrix} \begin{pmatrix} m_1 \\ m_2 \\ \vdots \\ m_d \end{pmatrix} = \begin{pmatrix} y_1 \\ y_2 \\ \vdots \\ y_{p_{max}} \end{pmatrix} \quad (8)$$

The rank of the matrix  $X$  is the number of linearly independent rows, which affects the existence or uniqueness of the solutions for  $m$ .

If the matrix  $X$  is square and non-singular then the unique solution to Eq. (7) is  $m = X^{-1}y$ . However if  $X$  is not square or singular, Eq. (7) needs to be modified and  $m$  is determined by minimising the following equation:

$$|Xm - y|^2 \quad (9)$$

as has been proved by Penrose (1955), the distinct solution to this problem is:

$$m = X^\#y \quad (10)$$

where  $X^\#$  is a pseudo-inverse matrix (Penrose, 1955, 1956).

One of the various methods available to organise the input training data is the  $k$ -dimensional tree ( $k$ - $d$  tree), with a time complexity in the order  $O(M \log M)$ . A  $k$ - $d$  tree is a space partitioning data structure for organising points in a  $k$ -dimensional space so that the LLR algorithm can be implemented using the least number of direct evaluations (Remesan et al., 2008).

#### 3.3.2. Artificial neural networks (ANNs)

ANNs are models that learn from a training data set mimicking the human-learning ability (Zurada, 1992). They are able to identify noisy data and approximate multivariate nonlinear relations among the variables (Ahmad et al., 2010). They have been widely used in many disciplines, including water resources and hydrology research such as for river level forecasting, rainfall runoff modelling, daily evaporation estimation, rainfall forecasting and groundwater modelling (Dehghani et al., 2014; Han et al., 2007; Ireland et al., 2015; Islam et al., 2012; Srivastava et al., 2013a; Tehrany et al., 2014). Multilayer feedforward neural networks (NNs) are universal approximators (Hornik et al., 1989) and explored in this study to determine their effectiveness in relating a number of inputs to the SMD. Specifically, an ANN can exploit the synergy of different input variables due to its truly multivariate nature and its nonlinear capabilities (Aires et al., 2011). The supervised ANN is the most widely applied ANN, where the inputs are presented to the ANN along with the targeted output. For each neuron in the hidden layers, the input vector (including a unity element, the *bias*) is multiplied by a vector of weights using a scalar product. Although the most commonly used learning algorithm in ANN is the backpropagation algorithm (fitted with gradient descent and gradient descent with momentum), it is often time-consuming for a practical point of view as it requires low learning rates for stable learning. Whereas algorithms such as conjugate gradient, quasi-Newton, and Levenberg-Marquardt provide alternative ways which are faster yet efficient. Two-hidden-layers have been thought as the most effective ANN architecture (Jones, 2004), therefore, it is used in this study. For each input vector containing a combination of SMOS  $T_b$ s, there is an associated target containing an SMD value. The output of the ANN is compared with the desired value, and the weights are adjusted by minimising a cost function (i.e., *MSE*). The minimisation has been achieved by the Broyden-Fletcher-Goldfarb-Shanno (BFGS) neural network training algorithm (Fletcher, 2013), and the conjugate gradient training algorithm (Bishop, 1995). The BFGS algorithm is a *variable metric* or *quasi-Newton* method, where the quadratic error function evaluated at  $w$  near to the minimum  $w^*$  is considered as the following equation:

$$E(w) = E(w^*) + \frac{1}{2}(w - w^*)^T H(w - w^*) \quad (11)$$

By differentiating Eq. (11), the location of the minimum  $w^*$  can be calculated as:

$$g \equiv \nabla E(w) = H(w - w^*) = 0 \quad (12)$$

The minimum  $w^*$  can therefore be calculated as:

$$w^* = w - H^{-1}g \quad (13)$$

where the vector  $-H^{-1}g$  is the *Newton direction* and when validated at any  $w$  on a quadratic error surface, it will direct to the minimum of the error function  $w^*$ .

For the conjugate gradient training algorithm, to achieve consecutive conjugate search directions, the gradient  $g \equiv \nabla E(w)$  of the error surface at the next point must be a minimum in the current search direction  $d_j$ , which is achieved when:

$$d_{j+1}Hd_j = 0 \quad (14)$$

where  $H$  is the Hessian matrix appraised at the point  $w_{j+1}$ . This direction search method is called *conjugate*. Full mathematical descriptions of the two training algorithms used in this study can be found in the aforementioned literature.

## 4. Results

In this study, four performance indicators are used: Pearson product moment correlation coefficient ( $r$ ), Mean squared error ( $MSE$ ), Nash-Sutcliffe Efficiency ( $NSE$ ) (Nash and Sutcliffe, 1970), and Root Mean Square Error ( $RMSE$ ).

### 4.1. Time series plots of XAJ SMD and SMOS soil moisture observations

We have selected the days on which both the SMOS-BEC and the SMOS-CATDS have available soil moisture data. This selection is to make a fair judgement between the two products because during the same time period SMOS-CATDS has more available data than SMOS-BEC. The time series plots of the XAJ SMD and the two soil moisture products are presented in Fig. 3. It can be seen that the SMD demonstrates a high variability with seasons, with nadir (lower SMD indicates wetter soil) often occurring in winter where evapotranspiration demand is the lowest. On the other hand during the summer season, the hot temperature and increased evapotranspiration lead to an overall drier surface soil (i.e., high SMD). For the two satellite soil moisture products, it is clear to observe that they are slightly discriminated from each other. In order for a better visualisation, two enlarged time series plots (i.e., during a winter period and a summer period, respectively) are presented in Fig. 4. Interestingly during the winter period (Fig. 4a) when the soil is frozen, SMOS-BEC observations are significantly less available than the SMOS-CATDS's. In order to appraise the hydrological values of the SMOS-CATDS frozen soil moisture data, the correlation coefficient is calculated against the XAJ SMD ( $r = -0.76$ ). This high correlation value indicates that even under the frozen condition, some of the satellite retrieved  $T_b$ s data are still useful for soil moisture estimation. Due to the limited availability of the SMOS-BEC data during the winter season, its correlation is not calculated here. During the summer period (Fig. 4b), data availability for both products is higher than in the winter period, and their soil moisture values are closer to each other. It can be seen from both products in the two enlarged plots that the summer soil (averagely around  $0.15 \text{ m}^3/\text{m}^3$ ) is generally drier than the winter soil (averagely around  $0.25 \text{ m}^3/\text{m}^3$ ), which agrees with the XAJ SMD fluctuations. The results of SMD estimation directly from the two SMOS soil moisture products are presented in the later section of the paper.

### 4.2. SMD estimation using SMOS brightness temperature as input

#### 4.2.1. Input data selection

As discussed in Section 3.2, an appropriate selection of incidence angles of the SMOS brightness temperature observations is necessary to ensure the best SMD retrieval. In this study, data selection is carried out by using a full embedding (embedding means a selection of inputs from all the possible inputs) calculation with the gamma ( $\Gamma$ ) from the GT as a metric. This approach tests every combination of data inputs to determine which combination yields the smallest absolute gamma value. If there are  $m$  scalar inputs then there are  $2^m - 1$  possible embeddings (i.e., 16,383 embeddings in this case). Although this method is more time consuming, it is more comprehensive. The full embedding result is demonstrated by a histogram plot in Fig. 5, which shows the frequency of embeddings with a given gamma statistic. It can be seen that the histogram tends to be a Gaussian distribution, indicating that the choice of embedding is largely driven by statistical variations in the data (Jones, 1998). The best inputs combination is from the embedding that gives the lowest gamma value, which is the combination of H polarisation at the incidence angles of  $32.50^\circ$ ,  $37.50^\circ$ ,  $47.50^\circ$ ,  $52.50^\circ$ ,  $57.50^\circ$  and V polarisation at the incidence angles of  $27.50^\circ$ ,  $32.50^\circ$ ,  $37.50^\circ$ ,  $42.50^\circ$ ,  $57.50^\circ$ . Although Fig. 2 shows that incidence angle  $27.50^\circ$  at H polarisation is more correlated with the SMD, it may contain some duplicated features with other angles (called redundancy) and is therefore excluded. There is a similar reason for those angles that also have a high correlation with the SMD, but are not selected after the full embedding test. The gamma statistic given by this combination is  $\Gamma = 0.048$ , and the gradient utilised to calculate the gamma statistic is  $0.51 (A)$  which roughly indicate that the output SMD is a relatively simple function of the ten  $T_b$ s inputs. A model with low  $\Gamma$  and low  $A$  is considered to be the best scenario for modelling. Therefore using the selected ten brightness temperature data solely should be efficient in modelling the SMD variations.

The quantity of the training data to predict the desirable output is again analysed by the  $M$ -test, which is useful in deciding whether there is sufficient data to provide an asymptotic gamma estimate and subsequently a reliable model. The results of the  $M$ -test are presented in Fig. 6. To select the most suitable training-data length, a trade-off between the best gamma and standard error results, and the longest testing-data length is made. As a

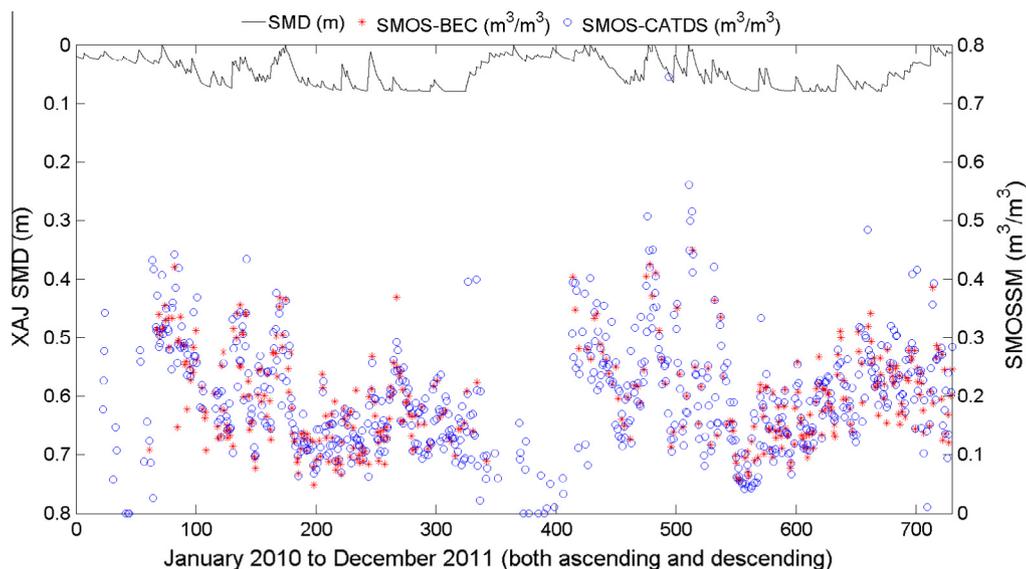


Fig. 3. Time series plots of the XAJ SMD and the two SMOS soil moisture products (indicated as SMOSSM in the y-axis label) from CATDS and BEC, respectively.

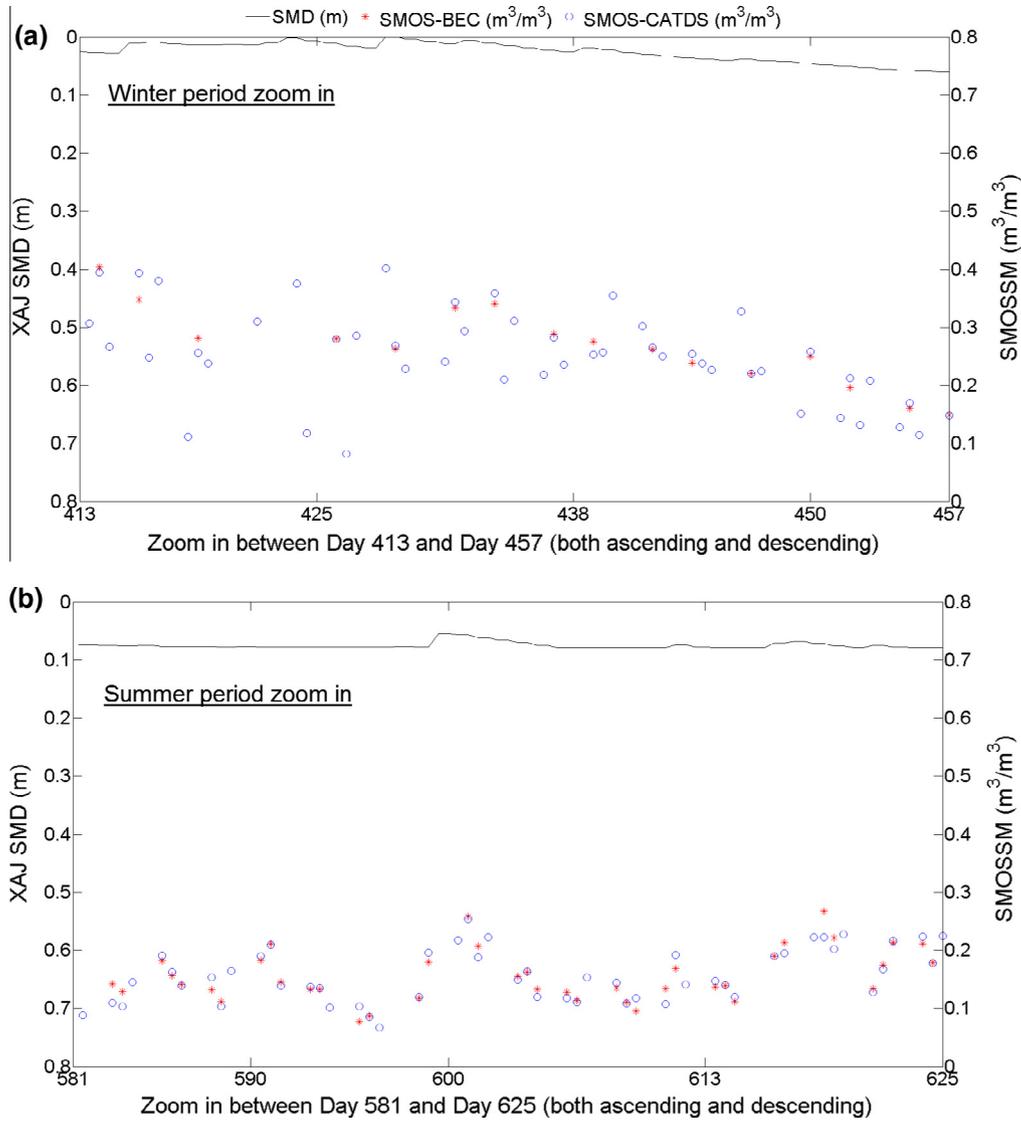


Fig. 4. Two enlarged time series plots of the XAJ SMD and the two SMOS soil moisture products (indicated as SMOSSM in the y-axis label) from CATDS and BEC, respectively: (a) between Day 413 and Day 457 (a winter period), and (b) between Day 581 and Day 625 (a summer period).

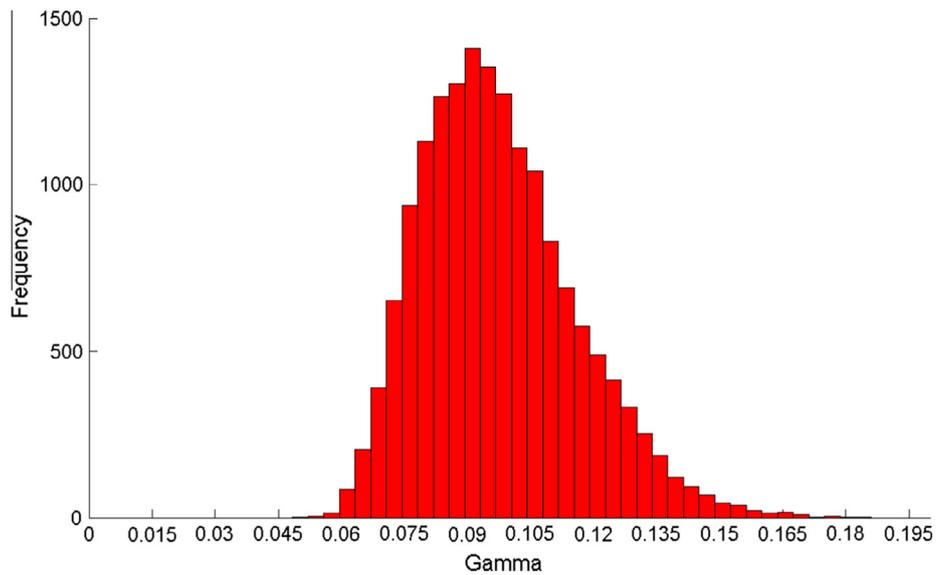


Fig. 5. The histogram of the full embedding calculation, with the gamma ( $r$ ) from the gamma test as a metric.

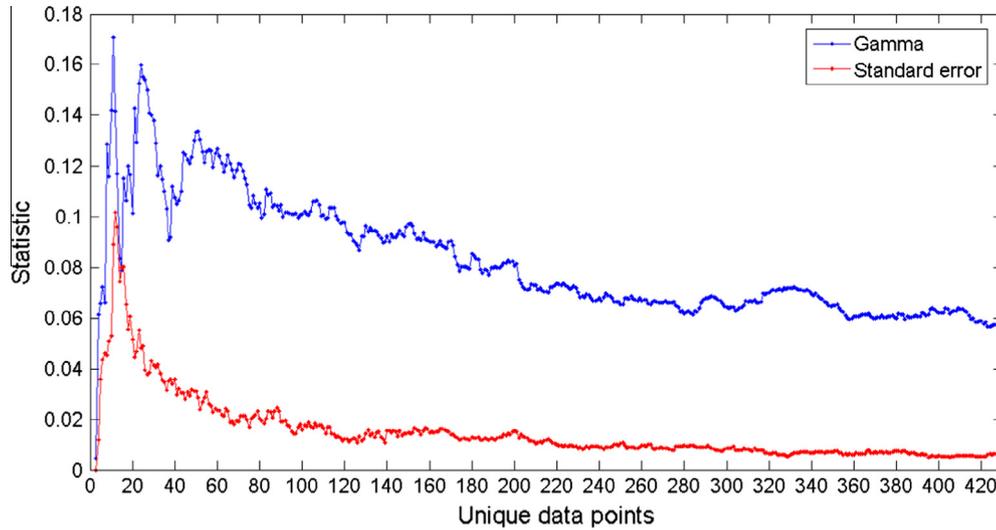


Fig. 6. *M*-test results. It indicates an asymptotic convergence of the gamma ( $\Gamma$ ) to a value of 0.061 at 356 data length, and the corresponding standard error at the convergent point is 0.0062.

result, the 356 data length produces the best trade-off result. The corresponding gamma and standard error are 0.061 and 0.0062, respectively. The small values of both statistics illustrate that the gamma test is relatively accurate. The results of the aforementioned tests give a clear image that it is possible to build a nonlinear predictive model utilising 356 data points.

4.2.2. SMD estimation using LLR model

After selection of the input data, the LLR model is trained (between the 1st–356th data points) and tested (between the 357th–434th data points) on the simulated SMD data from XAJ. It is important to choose the optimal number of nearest neighbours ( $p_{max}$ ) in LLR so that the best model performance can be achieved. This has been identified by the trial and error method. The procedure is carried out by repeating the training and testing processes for another four times over different training-testing data combinations using the 4-fold cross-validation (i.e., shifting the data by 108 each time) so that there is a total of five training-testing data combinations (including the training-testing data combination obtained from the *M*-test). In this way, all the data are tested at least once instead of just using the original testing data. The trial and error results (not normalised) are presented in Table 1. It is observed that the *MSE* varies with different  $p_{max}$  values and divided groups, indicating that both factors are important in controlling the LLR modelling performance. The generally low *MSE* values observed in group 1 clearly reveal the usefulness of the *M*-test. It

is still difficult to judge the most appropriate  $p_{max}$  value based on those individual case results. Therefore, it is necessary to average them so that a smooth trial and error curve can be obtained (Fig. 7). The close *MSE* values between the testing and the training demonstrate that the LLR model is quite stable in simulating the SMD values from the selected  $T_{bs}$  inputs. The LLR model with  $p_{max}$  at three generally gives the lowest *MSE* value and is therefore implemented hereafter.

The performance of the LLR technique is measured by three global statistics (*NSE*, *r*, and *RMSE*). Fig. 8 shows the scatter plots of the LLR computed and the XAJ simulated SMD during the training and testing periods. LLR shows a rather satisfactory performance (*NSE* = 0.88, *r* = 0.94, *RMSE* = 0.008 m) during the training phase in estimating the SMD. The majority of the data points are saturated around the 45° line (dotted line) indicating that the model is well trained. Points far above the bisector line signify over-estimation whereas points far below the dotted line mean under-estimation. The training outcome illustrates the degree to which the LLR model explains SMD variation as a function of the ten  $T_{bs}$  inputs, while the effectiveness of the model is judged during the testing phase. It is clear to see that the LLR model performs very well during the testing phase (*NSE* = 0.85, *r* = 0.93, *RMSE* = 0.009 m). A large number of saturated data points around the dotted line signifies that there is a surprisingly excellent match between the modelled SMD and the XAJ SMD. The used LLR algorithm has been double checked by disrupting the SMD target in the testing datasets and

Table 1  
Trial and error results of finding the best number of nearest neighbours ( $p_{max}$ ) in the LLR model.

$p_{max}$	Group 1		Group 2		Group 3		Group 4		Group 5		Mean	
	Training	Testing										
1	8.1E-05	1.3E-04	1.4E-04	1.4E-04	1.0E-04	8.4E-05	8.4E-05	1.1E-04	1.1E-04	7.3E-05	1.0E-04	1.1E-04
2	7.6E-05	1.1E-04	1.2E-04	1.4E-04	6.4E-05	9.0E-05	6.8E-05	5.6E-05	8.9E-05	7.0E-05	8.3E-05	9.3E-05
3	7.1E-05	7.6E-05	1.0E-04	1.1E-04	6.0E-05	9.2E-05	6.9E-05	1.0E-04	1.0E-04	6.7E-05	8.1E-05	9.0E-05
4	6.1E-05	8.6E-05	9.6E-05	1.1E-04	7.5E-05	1.1E-04	7.8E-05	1.4E-04	1.1E-04	6.4E-05	8.3E-05	1.0E-04
5	7.3E-05	7.9E-05	1.1E-04	1.0E-04	1.1E-04	1.1E-04	9.3E-05	1.6E-04	1.2E-04	8.8E-05	1.0E-04	1.1E-04
6	6.7E-05	1.0E-04	1.2E-04	1.4E-04	1.4E-04	6.8E-05	1.3E-04	2.0E-04	1.2E-04	9.2E-05	1.2E-04	1.2E-04

Note: The performance is measured by the mean squared error (*MSE* is in the unit of  $m^2$ ). The datasets (i.e., 434 in total) have been divided into five groups so that all of them can be tested at least once. Group 1 comprises the training data of 1–356, and testing data of 357–434 from the *M*-test; group 2 comprises the training data of 1–326, and testing data of 327–434; group 3 comprises the training data of 109–434, and testing data of 1–108; group 4 comprises the training data of 1–107, 216–434, and testing data of 108–215; group 5 comprises the training data of 1–216, 326–434, and testing data of 217–325. The mean *MSE* results are used to determine the optimal  $p_{max}$  value in LLR model.

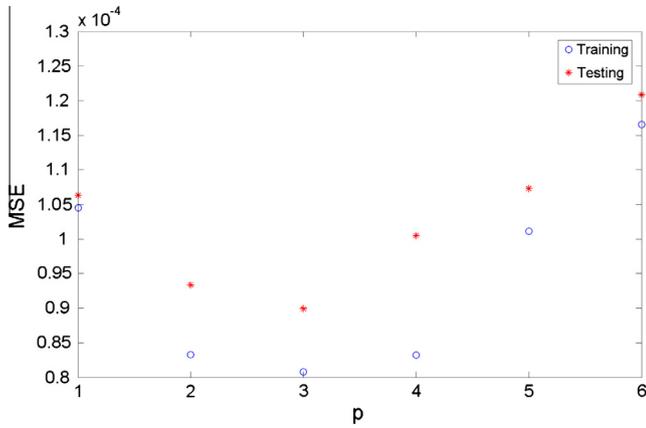


Fig. 7. Trial and error result to find the optimal  $p_{max}$  value in the LLR modelling.

changing the input file, and its performance remains the same. Therefore, it is believed that LLR model is rather suitable for estimating SMD from  $T_b$ s. Fig. 9 shows that the median of the XAJ simulated SMD is higher than the LLR modelled. Nevertheless, the LLR model performs well for both low and high SMD values as the 5/25% and 75/95% percentiles of the XAJ and the model estimated SMD match well.

4.2.3. SMD estimation using ANN models

The LLR model is then compared with two ANN models (i.e., the BFGS training algorithm ANN and the conjugate gradient training algorithm ANN, respectively). The feedforward network used in this work has two hidden layers. Various tests have been done to determine the optimal ANN architecture. In the ANN conjugate gradient model, above 5 neurons in the hidden layer, the results do not improve anymore, therefore 10-5-5-1 ANN structure is adopted. For the ANN BFGS model, the feedforward 10-8-8-1

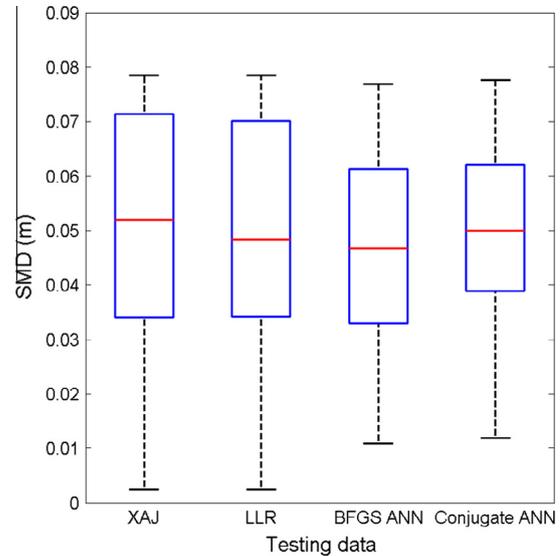


Fig. 9. The statistical plot of the XAJ simulated SMD and the models estimated SMD during the testing phase. The boxes indicate 25–75% percentiles. The whiskers extend from 5% to 95% percentile values. The red line represents the median value of the data. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

ANN is found to be the most suitable. The size of the sufficient training dataset has been determined as 356 through the  $M$ -test, and the target  $MSE$  has been identified as 0.061 (normalised) to avoid the potential overtraining problem. Scatter plots of the two ANN models during the training and testing phases are illustrated in Fig. 10, and their statistical performances are indicated accordingly in the figure. It is seen in the statistics summary table (Table 2), that the SMDs estimated by ANNs are inferior to the estimates by the LLR model for both the training and testing parts. Box plots comparing the spread of the ANN estimated SMDs with

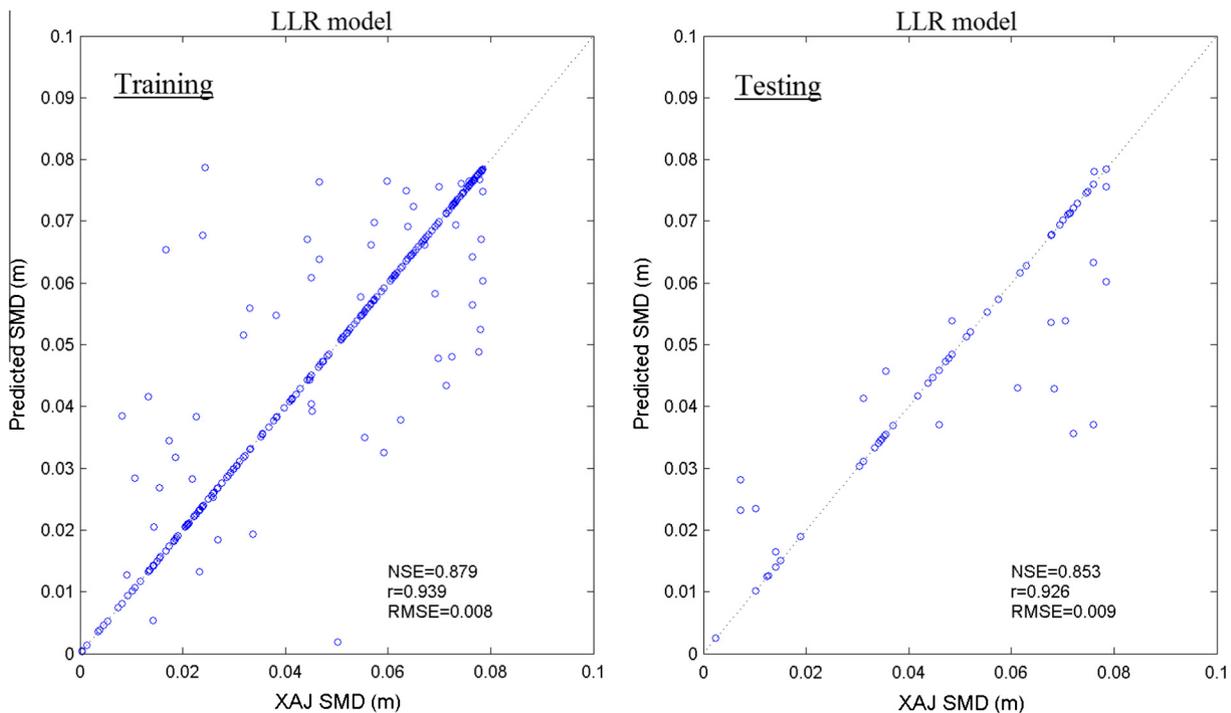
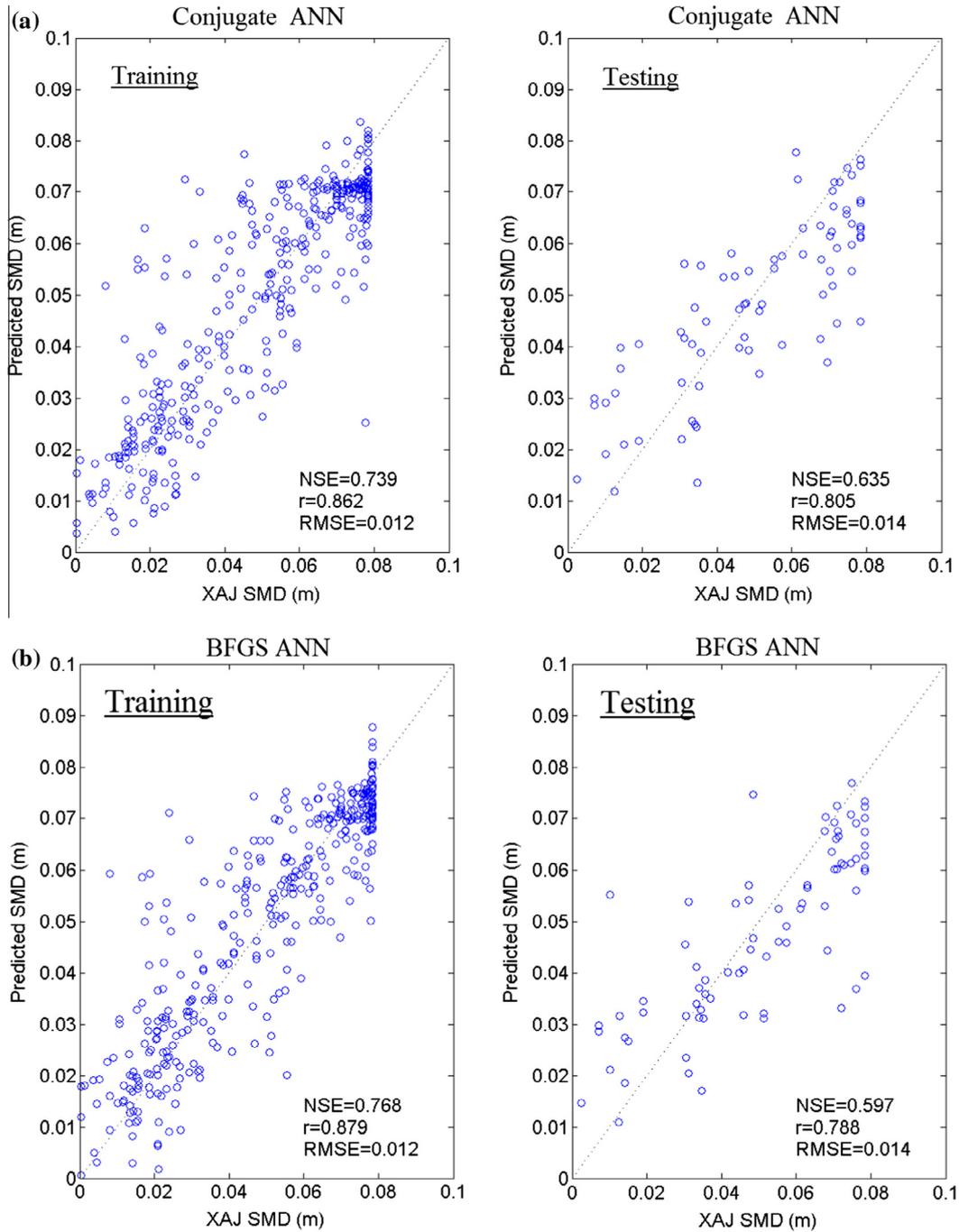


Fig. 8. SMD simulated by the LLR model. It shows the scatter plots of the LLR computed and the XAJ simulated SMD during the training and testing periods. It is noted that RMSE is in the unit of metre.



**Fig. 10.** SMD simulated by the ANN models. (a) shows the scatter plots of the conjugate ANN computed and the XAJ simulated SMD during the training and testing periods; (b) presents the scatter plots of the BFGS ANN computed and the XAJ simulated SMD during the training and testing periods. It is noted that RMSE is in the unit of metre.

**Table 2**  
Summary of the model performances.

	Training			Testing		
	NSE	r	RMSE (m)	NSE	r	RMSE (m)
LLR	0.88	0.94	8.0E-3	0.85	0.93	9.0E-3
ANN-conjugate	0.74	0.86	1.2E-2	0.64	0.81	1.4E-2
ANN-BFGS	0.77	0.88	1.2E-2	0.60	0.79	1.4E-2
SMOS-BEC	0.55	0.74	1.5E-2	0.34	0.60	1.8E-2
SMOS-CATDS	0.53	0.73	1.5E-2	0.35	0.61	1.8E-2

the XAJ simulated are also shown in Fig. 9. The plot indicates that both ANN models do not capture the extreme low SMD values well (the 5% whiskers), but they perform acceptably in estimating extreme high SMD values (the upper 95% whiskers). In addition, both ANN models are comparatively poorer in modelling high SMD values (75% percentile) than LLR. The ANN-BFGS is able to simulate low SMD well (25% percentile), while the ANN-conjugate shows less capability in this aspect. On the other hand, the ANN-conjugate's simulation is able to produce the closest mean SMD value to the XAJ's, while the ANN-BFGS's mean is more deviated. Generally, the statistics results of the study indicate that

the SMD predictive capability by the ANN-conjugate is stronger than the ANN-BFGS.

#### 4.3. SMD estimation using SMOS soil moisture as input

To further evaluate the proposed method, a comparison study is carried out to derive the SMD directly from the two SMOS soil moisture products. LLR model is adopted for this purpose because this is a mono-variable regression problem (i.e., to derive from one of the SMOS soil moisture products into the SMD). If ANN is used it will have only one input node which makes the ANN model ineffective. The quantities of the training and the testing data are again analysed by the *M*-test. The *M*-test results show that the most suitable training data period for the SMOS-BEC and the SMOS-CATDS is 1st–216th and 1st–220th, respectively, and the rest of the data are

used as the testing dataset. The optimal number of  $p_{max}$  in LLR model is found to be 13 in both data input cases. The SMD estimation results are illustrated in Fig. 11. The goodness of fit is indicated by *NSE*, *r*, and *RMSE* statistics. The statistical performances between the two cases are close to each other, indicating there is no significant difference between the two soil moisture products. The poor results during both the training and the testing phases reveal that those soil moisture products generated using the in-situ soil moisture networks and the numerical weather modelling outputs as the evaluating target are not hydrologically suitable. Although both ANN models are not capable of surpassing the LLR technique, their SMD estimations are still much better than those derived from the SMOS soil moisture directly (as shown in Table 2). Therefore, the proposed method using the SMOS multi-angle brightness temperatures is a more efficient way.

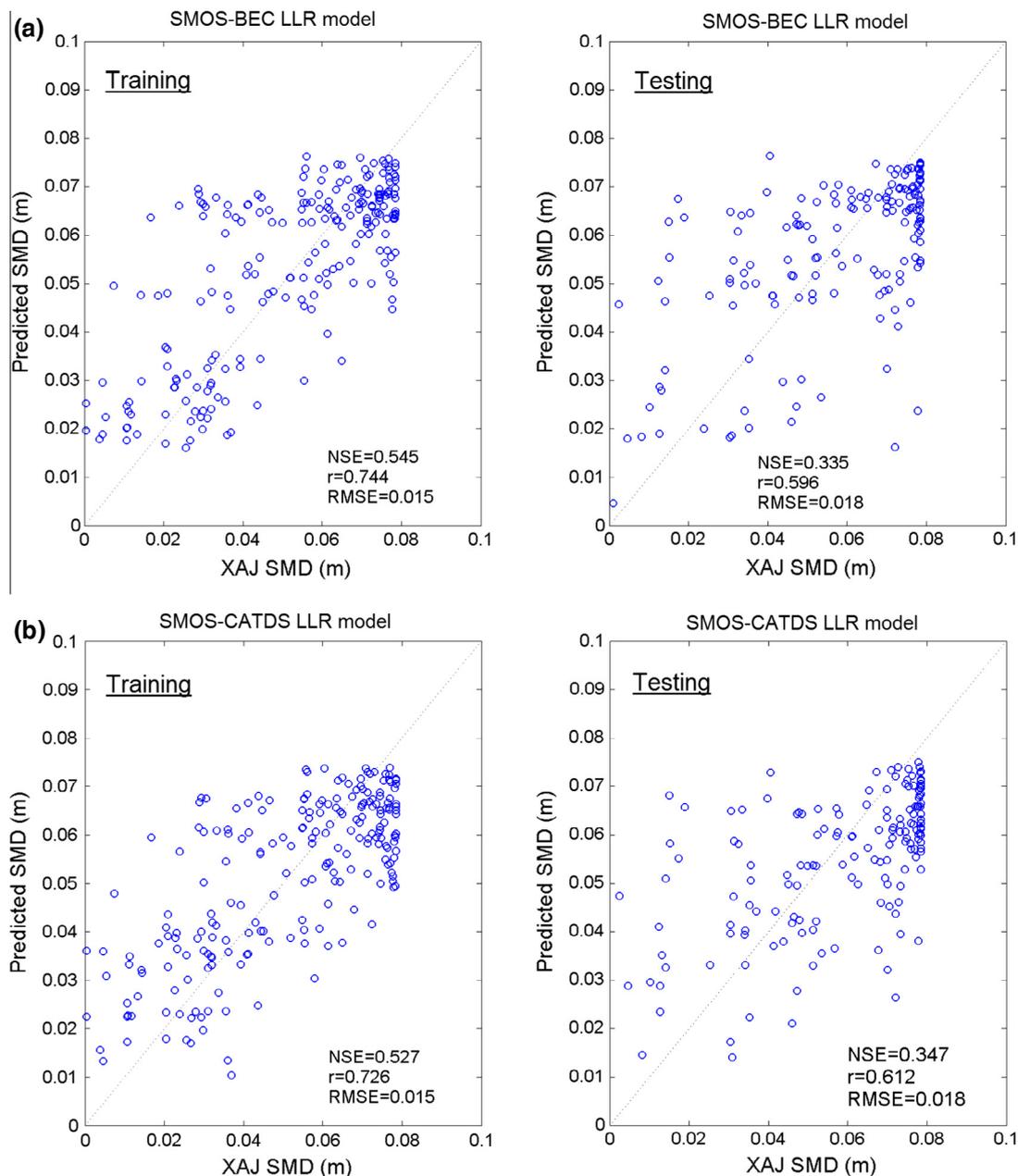


Fig. 11. SMD estimation using LLR model and SMOS soil moisture input: (a) from SMOS-BEC; (b) from SMOS-CATDS. It is noted that *RMSE* is in the unit of metre.

## 5. Discussion and conclusions

This paper describes a novel approach for the first time to estimate hydrological SMD directly from the SMOS multi-angle brightness temperatures with both the H and V polarisations using nonlinear modelling techniques. A well-proven gamma test is also employed to further improve the input data feature selection process. The use of LLR and ANNs with the BFGS NN training algorithm and the conjugate gradient training algorithm have been presented in this study. Both the radial BFGS ANN training algorithm and the conjugate gradient training algorithm perform well in estimating the SMD data, yet both fail to achieve the highest possible results. On the other hand, the training and testing results demonstrate that the LLR model is surprisingly good at capturing the interrelations between SMD and  $T_{bs}$  over ANNs. All the SMD values estimated from the proposed nonlinear methods achieve outstanding accuracies compared with those derived from the standard SMOS soil moisture products (both from the SMOS-BEC and the SMOS-CATDS).

The results from the LLR model are quite puzzling due to a large number of data points perfectly matching with the predicted SMD values, in both the training phase and the testing phase. One obvious suspicion is the model overfits the training data, however this has been excluded using the combination of the training data and the testing data because an over-trained model cannot perform well in the testing phase. Our explanation is such a phenomenon is caused by two nearby points which have identical or almost the same SMD values. This happens if the distance between them is very small, and is more likely to happen with LLR model which is local in comparison with other global models such as ANN. A local model breaks the whole data points into local groups. For a special case when  $p_{max} = 1$ , a value to be estimated at a certain point will be totally decided by its nearest neighbour. If its nearest neighbour is close enough a zero error could be achieved. However if the local data points are very sparse then its nearest neighbour will be quite far away, and the estimated value will have a large error. This explains why there are so many points on the perfectly matched line, while there are still many data points off it. The overall results indicate that the LLR technique has a huge potential to provide hydrologists with valuable information on the application of satellite brightness temperature for SMD estimation, which has not been explored before. The current study could form the basis for efficient satellite data assimilation into real-time flood forecasting systems. The LLR model evaluated in this paper is numerically very efficient and is capable of retrieving SMD fast enough to be assimilated into such systems.

In this study the 'ground truth' is based on the SMD simulation from the XAJ model. One may argue that a hydrological model's soil moisture state variable has no physical meaning and its purpose is purely to facilitate a model's flow simulation, hence it has no direct connection with the real-field soil moisture. Moreover, as Keith Beven states in Beven (2012) there are many models with different parameter values which could produce equally good flow simulations (called the equifinality effect) because those models are all optimised with the same flow simulation. As a result, models with similar flow simulation accuracy could have very distinct values in their soil moisture state variables. To explore this argument, we have carried out some numerical experiments to demonstrate that although the absolute SMD values could vary greatly between different model parameter sets, their response patterns to soil moisture changes are almost identical because they are driven by the same precipitation and evapotranspiration processes with the identical physical response mechanisms. Therefore, the SMD pattern is the true reflection of the soil moisture changes in the real field, and this justifies the usage of SMD derived from the hydrological model as the 'ground truth' for assessing soil moisture data quality. However, the SMD and the real-field soil

moisture represent different aspects of the soil moisture condition. A regression formula is needed to convert the satellite observations into hydrological SMD as shown in Figs. 8 and 10 (to derive hydrological SMD from the SMOS raw data using ANN and LLR) and Fig. 11 (to convert from the SMOS soil moisture product into hydrological SMD). To make a fair comparison, the regression formulas with the similar complexity are used in both cases.

The accuracy of the SMD estimation is largely dependent on the relationship of the training dataset with the target output. The presence of erroneous values and under/over estimation in the training dataset hampers the model performance. Although larger training data sizes generally yield better results, it is challenging to decide what size is large enough, especially when the analysed data period is short. At the moment, the rule of two-third data for training and one-third data for testing is still popular albeit such a method lacks consideration of the data characteristics. In addition, there is no commonly recognised method for input data feature selection and quality check, which has hampered many modelling developments. This is because some input data sets carry duplicated features (high redundancy), which can make the model over-complicated (over-fitting). Also, if the inherent errors in the input data exceed the model's capability, it is rather difficult for the model to perform well, even the model itself is good enough. This study demonstrates the informative capability of the GT and the  $M$ -test in the input data selection for nonlinear model constructions. It is hoped that this approach could be generalised to benefit various research areas including hydrology, meteorology and where input data feature selection is needed.

The mismatch between the satellite footprint and catchment scale is an important issue that should be considered in the hydrological application of soil moisture products. In this study, the chosen catchment has a compatible size with the satellite footprint, therefore the mismatch is not an issue in this case. The effect of larger or smaller catchments should be explored in future studies. Since the adopted LLR model is data based, the optimal model could change for various soil type, catchment size, land cover and climate regions. The proposed scheme has to be applied to individual catchments with their own model development for SMD estimation. With more studies using the proposed method, it could be feasible to build a look-up table in which users can search for the model structure and parameters so that it can be utilised in ungauged catchments as well. Finally, it should be noted that the SMD produced from this paper cannot be directly used in agricultural management or other disciplines because there is no universal soil moisture product for all purposes. Nevertheless, for any specific application field, the proposed method can be easily adopted to it by changing the targeted soil moisture (e.g., to change SMD to volumetric soil moisture to be used in agriculture).

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