



Revealing the stability and efficiency enhancement in mixed halide perovskites $\text{MAPb}(\text{I}_{1-x}\text{Cl}_x)_3$ with *ab initio* calculations

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HIGHLIGHTS

- VCA method was applied to investigate the mixed iodide-chloride perovskites.
- Lattice constant and dielectric constant decrease linearly as increasing Cl content.
- Band gap and exciton binding energy increase quadratically as increasing Cl content.
- Exciton binding energy has the minimum at 7% Cl content.
- Chemical decomposition changes from exothermic to endothermic at 7% Cl content.

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ABSTRACT

A little addition of Cl to MAPbI_3 has been reported to improve the material stability as well as light harvesting and carrier conducting properties of organometal trihalide perovskites, the key component of perovskite solar cell (PSC). However, the mechanism of performance enhancement of PSC by Cl addition is still unclear. Here, we apply the efficient virtual crystal approximation method to revealing the effects of Cl addition on the structural, electronic, optical properties and material stability of $\text{MAPb}(\text{I}_{1-x}\text{Cl}_x)_3$. Our *ab initio* calculations present that as the increase of Cl content cubic lattice constants and static dielectric constants decrease linearly, while band gaps and exciton binding energies increase quadratically. Moreover, we find the minimum of exciton binding energy at the Cl content of 7%, at which the chemical decomposition reaction changes coincidentally to be from exothermic to endothermic. Interactions among constituents of compound and electronic charge transferring during formation are carefully discussed. This reveals new prospects for understanding and designing of stable, high efficiency PSCs.

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1. Introduction

The world has been searching for inexpensive, renewable and clean energy sources with growing concerns on more and more energy demands, global warming and serious climate change. Among various options for such energy sources, solar power should have undoubtedly the greatest potential due to its most abundance and eternal nature, despite the drawbacks such as being variable in time and widespread in space, which require to create new

technologies for effective solar energy harvesting. Recently, photovoltaic (PV) technology, known to be a promising route for harnessing solar power, has attained the new prosperity since a breakthrough occurred by an invention of perovskite solar cell (PSC) using organometal trihalide perovskite (OTP) as a light harvester [1,2]. A great attraction of PSCs comes from remarkably low energy cost compared with other conventional solar cells. The reduction of energy cost in PSCs may be associated with low cost of substrate materials, easy manufacturing process, and high performance of device given by efficiency and stability [3,4], which promise for PV energy to become competitive with fossil fuels [5,6]. This is due to the unique optoelectronic properties of OTPs, typically methylammonium lead trihalide perovskite MAPbX_3

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(MA = CH₃NH₃, X = Cl, Br, I) that is the key component of PSC, such as large light absorption coefficients [7], optimal band gaps [8], large and balanced carrier mobilities [9], large carrier diffusion length [10,11], and small exciton binding energies [12,13].

However, there are still major challenges for OTPs such as poor material stability [14–16] and toxicity of the lead [17], which hinder practical use of PSCs. In particular, the issues of degradation of OTPs and stability of PSCs should be urgently resolved to achieve a long lifetime of PSCs with high conversion efficiency. Although PSCs consist of multilayers including light harvesting materials, electron and hole transport layers, counter electrodes, etc., the key problem of degradation is that MAPbI₃(s), the most popular OTP, may be readily decomposed into PbI₂(s) and MAI(aq) or further CH₃NH₂(aq) and HI(aq) under different ambient conditions during operation, such as moisture [18,19] or oxygen in air [20], ultraviolet light [21,22], and thermal effect [23,24]. In spite of the very importance and urgency, the mechanism of degradation by each of external actions or synergy action is not yet fully understandable.

In order to resolve poor material stability of MAPbI₃, any modification in the position of component ions could be thought [15,16]. One successful technique is to replace organic MA cation with larger size organic cation like formamidinium ion (FA⁺ = HC(NH₂)₂⁺), which was found to increase the material stability [25,26]. When replacing Pb with Sn, however, the stability reduces significantly due to a possible oxidation of Sn²⁺, although some merits like non-toxicity are expected [17]. Then, the most widely studied substitution could be in halogen ion position; the stability of MAPbI₃ can be remarkably improved when mixing with a small fraction of Br or Cl [27–29]. In the case of MAPb(I_{1-x}Br_x)₃, a high resistivity to humidity was found at $x \geq 0.2$ from experiments [27,30] and density functional theory (DFT) calculations [31–33]. This might be associated with their compact and stable structures, since the replacement of larger I ions (2.20 Å) with smaller Br ions (1.96 Å) leads to a reduction in the lattice constant and a phase transition from the tetragonal to the cubic [30]. A similar effect was observed when mixing with much smaller Cl ions (1.81 Å) [2,34–38]. The resulting compact structure of MAPb(I_{1-x}Cl_x)₃ could increase the resistivity of the material to moisture, light and temperature thanks to its higher binding compared to MAPbI₃. Nevertheless, there is no clear evidence of the role of chlorine insertion to enhance stability. In addition, these modifications using appropriate substitutions could improve other material properties of the perovskite related with efficiency, such as band gaps, light absorption coefficients and carrier mobilities. The insertion of Cl into MAPbI₃, for instance, improves the uniformity of its layer and results in an increase of recombination lifetime of carriers and electron diffusion length from 100 nm to 1 μm [10,11]. Although mixing halide in OTPs seems to have beneficial effects in terms of performance, the questions of what is the optimal Cl content in MAPb(I_{1-x}Cl_x)₃ and why is still in debate due to a lack of systematic investigation.

In this work, we report an *ab initio* study on the mixed iodide-chloride perovskites MAPb(I_{1-x}Cl_x)₃ using the virtual crystal approximation (VCA) [32,39] method within DFT. As increasing the Cl content x , we first optimize the lattice parameters of cubic phases, and then, using the determined structures, calculate optoelectronic properties such as band gaps, effective masses of charge carriers, exciton binding energies and light absorption coefficients, which are used to demonstrate the advantages of charge carrier generation and transportation in these materials. At the end, we attempt to give a reason for the stability enhancement by mixing chlorine as well as a precise value of Cl content to enhance performance with a careful analysis of the calculated formation enthalpies and charge density differences.

2. Computational methods

The *ab initio* calculations were carried out by applying the pseudopotential plane wave package ABINIT (version 7.10.2) [40] using generalized gradient approximation (GGA) parameterized by Perdew-Burke-Ernzerhof (PBE) [41] with the semi-empirical van der Waals correction (vdW-D2) [42]. The optimized norm-conserving, designed nonlocal pseudopotentials were generated with the OPIUM package [43,44], using the following valence electronic configurations of atoms: H–1s¹, C–2s²2p², N–2s²2p³, Cl–3s²3p⁵, I–5s²5p⁵, and Pb–5d¹⁰6s²6p². For the virtual atoms I_{1-x}Cl_x from $x = 0$ to 1 with an interval of 0.1, we applied the Yu-Emmerich extended averaging approach (YE²A²) [39] to constructing their pseudopotentials, as it was proved for this method to give reasonable results for the mixed iodide-bromide perovskites [32]. A plane wave cutoff energy of 40 Ha and a $4 \times 4 \times 4$ k -point grid were used, confirming the total energy convergence to be 5 meV per cell. When calculating the optoelectronic properties, a denser k -point mesh of $10 \times 10 \times 10$ was used. We determined the optimal lattice parameters by calculating the total energies versus volumes of the unit cells, allowing the atomic relaxation with a force tolerance of 0.01 eV Å⁻¹, and then fitting the total energy-cell volume (E - V) data into the Birch-Murnaghan equation of state (EOS) [45].

It was found from experiments that at room temperature, bulk MAPbI₃ forms a tetragonal structure (space group $I4/mcm$) (and transforms into a cubic phase ($Pm\bar{3}m$) above $\sim 56^\circ$ C), whereas MAPbCl₃ forms the cubic structure ($Pm\bar{3}m$) (and transforms into the tetragonal phase ($P4/mmm$) below -96° C) [46,47]. After the incorporation of Cl⁻ into MAPbI₃, the cubic phase MAPb(I_{1-x}Cl_x)₃ always occurred in meso-porous substrate [38,48], although the tetragonal phase was occasionally found on compact TiO₂ substrate [49]. It is worth noting that there is no critical difference between the tetragonal and cubic phases, except a slight rotation of PbI₆ octahedra along the c -axis, and thus, the tetragonal phase can be treated as a pseudo-cubic phase (Pm) with $a^* = a/\sqrt{2}$, $c^* = c/2$ [26]. Based on these arguments, we treated the pseudo-cubic phase for all solid solutions MAPb(I_{1-x}Cl_x)₃ ($x = [0, 1]$) in this work.

The macroscopic dielectric functions including the effect of electron-hole interaction, $\epsilon_M(\omega) = \epsilon_1(\omega) + i\epsilon_2(\omega)$, were calculated within the Bethe-Salpeter approach [50] as implemented in the ABINIT code. Those were used to determine the photo-absorption coefficient, using the following equation:

$$\alpha(\omega) = \frac{2\omega}{c} \sqrt{\frac{[\epsilon_1^2(\omega) + \epsilon_2^2(\omega)]^{1/2} - \epsilon_1(\omega)}{2}}, \quad (1)$$

where c is the speed of light in vacuum. The static dielectric constants (ϵ_s) extracted at zero-frequency limit, together with effective masses of electron (m_e^*) and hole (m_h^*), were used to estimate the exciton binding energy within the weak Mott-Wannier model, using the following equation [32,51]:

$$E_b^{\text{ex}} = \frac{m_e e^4}{2(4\pi\epsilon_0)^2 \hbar^2} \frac{m_r^*}{m_e} \frac{1}{\epsilon_s^2} \approx 13.56 \frac{m_r^*}{m_e} \frac{1}{\epsilon_s^2} \text{ (eV)}, \quad (2)$$

where $1/m_r^* = 1/m_e^* + 1/m_h^*$ for effective reduced mass m_r^* . This model is validated when the exciton radius $a_0^* = \epsilon_s \frac{m_e}{m_r^*} a_0$, where a_0 is Bohr radius, is larger than the lattice constant.

3. Results and discussion

3.1. Structure related properties

It was confirmed that there exist vdW interactions between the organic molecule and the inorganic matrix in the OTPs and they play a certain role in the description of material properties within the DFT framework [33,52,53]. Accordingly, we first checked the validity of vdW inclusion by comparing the computed lattice constants from the PBE functional without vdW correction, with semi-empirical vdW correction (vdW-D2) and vdW functional (vdW-optPBE) to the experimental data of MAPbI₃ and MAPbCl₃. As mentioned above, MAPbX₃ (X = I_{1-x}Cl_x, x = [0, 1]) crystals were modeled with a pseudo-cubic phase with [101] orientation of MA cation, as identified from experiments [26,46,47] and verified to be the lowest energy configuration by our previous work [32,33] (Fig. 1(a)).

We calculated the total energies of unit cells at fixed volume which varies from 0.9V₀ to 1.1V₀ with 10 intervals, while allowing full atomic relaxation, and then performed fittings of the (*E* – *V*) data into the Birch-Murnaghan EOS, determining the equilibrium lattice constant and bulk modulus. To roughly estimate the structural stability, we analyzed the averaged Pb–X bond length, and the cohesive energy calculated as the difference between the total energy of bulk MAPbX₃ and the sum of isolated constituent atoms' like $E_c = E(\text{MAPbX}_3) - \sum_i E(i)$. The calculated equilibrium lattice constants, bulk moduli, averaged Pb–X bond lengths, and cohesive energies for MAPbI₃, MAPbCl₃ and their solid solution MAPb(I_{0.5}Cl_{0.5})₃ are summarized in Table 1. It was found that, while the PBE overestimates the lattice constant as usual for other inorganic semiconductors, the vdW-D2 outputs the closest values compared to experiment and optPBE in between. Based on this check, the PBE + vdW-D2 method was used for further calculations. We see that, whatever the type of XC functional is, going from I to Cl, the lattice constant and Pb–X bond length decrease, while the bulk modulus and the magnitude of cohesive energy increase. However, there is no significant change in C–N bond length, indicating that the change of lattice does not affect the intramolecular behaviour of MA molecule but the Pb–X and PbX₆–MA bonding.

By repeating the above procedure for pseudo-cubic MAPb(I_{1-x}Cl_x)₃ as increasing the Cl content *x*, we obtained the systematic change of lattice constants and bulk moduli, as shown in Fig. 1(b) (EOS curves in Fig. S1). They are of almost linear functions of Cl content without any anomaly in the middle, $a(x) = 6.310 - 0.716x$ (Å) for lattice constants and $B(x) = 10.627 + 5.492x$ (GPa) for bulk moduli, showing a satisfaction of the Vegard's law for lattice constants. This indicates that mixing chloride with

Table 1

Lattice constant *a* (Å), bulk modulus *B* (GPa), averaged Pb–X bond length *d*_{Pb–X} (Å) and cohesive energy *E*_c (eV).

Material	Property	PBE	optPBE	vdW-D2	Exp.[46]
MAPbI ₃	<i>a</i>	6.358	6.354	6.311	6.328
	<i>B</i>	14.61	13.53	10.94	
	<i>d</i> _{Pb–I}	3.266	3.266	3.200	
	<i>E</i> _c	–3.72	–3.37	–3.58	
MAPb(I _{0.5} Cl _{0.5}) ₃	<i>a</i>	6.078	6.113	5.915	
	<i>B</i>	17.66	18.21	13.21	
	<i>d</i> _{Pb–X}	3.071	3.100	2.991	
	<i>E</i> _c	–3.78	–3.44	–3.65	
MAPbCl ₃	<i>a</i>	5.868	5.801	5.649	5.675
	<i>B</i>	19.35	22.56	16.44	
	<i>d</i> _{Pb–Cl}	3.044	2.934	2.860	
	<i>E</i> _c	–3.97	–3.66	–3.85	

The bold values are the closest ones to the experimental values.

iodide perovskite induces a shrinking of lattice and an increase of bulk modulus, resulting in a strengthening of Pb–X bond and thus chemical stability.

3.2. Electronic properties

The electronic structures are crucial factors for solar cell application, since the light harvesting capability of the key materials, which mainly governs the performance of the solar cell, can be determined just from those. Accordingly, we investigated the electronic band structures and density of states (DOS) systematically as the increase of Cl content. As can be seen in Fig. 2(a) and Fig. S2, the band structures of the mixed perovskites MAPb(I_{1-x}Cl_x)₃ from *x* = 0.0 to *x* = 1.0 are quite similar in overall with gradual increase of band gaps, which is in direct mode at the R point in the first Brillouin zone (1BZ). It is worth noting that the next direct band gap can occur at the M point in 1BZ (Fig. S2). The symmetry analysis of the electronic states at the R and M points with group theory implies that the optically allowed electron transitions are at the R point between A_{1g} valence band (VB) and 3-fold degenerated T_{1u} conduction band (CB) or T_{1g} VB and T_{1u} CB, and at the M point between A_{1g} VB and 2-fold degenerated E_u CB, as depicted in Fig. 2(c) [51].

Atomic resolved and partial DOSs are shown in Fig. 2(b) and Fig. S3. The top of the valence band at the R and M points is composed of strong antibonding coupling of Pb 6s with X 3/5p orbitals, making upper VBs dispersive. On the other hand, the bottom of the conduction band at the R and M points is predominantly Pb 6p orbitals with negligible antibonding coupling with X 3/5s orbitals, indicating the ionicity of MAPbX₃. In addition, the

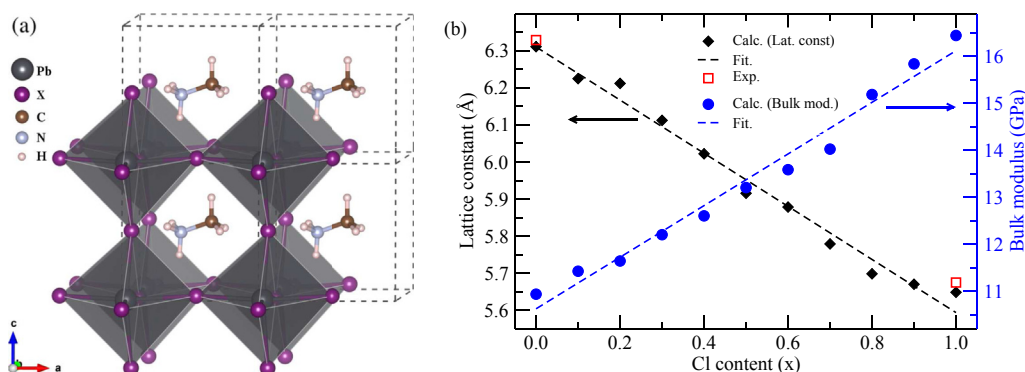


Fig. 1. (a) The crystalline structure of pseudo-cubic MAPbX₃ (space group *Pm*) with [101] orientation of MA cation. (b) Lattice constants and bulk moduli as linear functions of Cl content *x* in MAPb(I_{1-x}Cl_x)₃. Dashed lines denote the fitting lines and Exp. data is from Ref. [46].

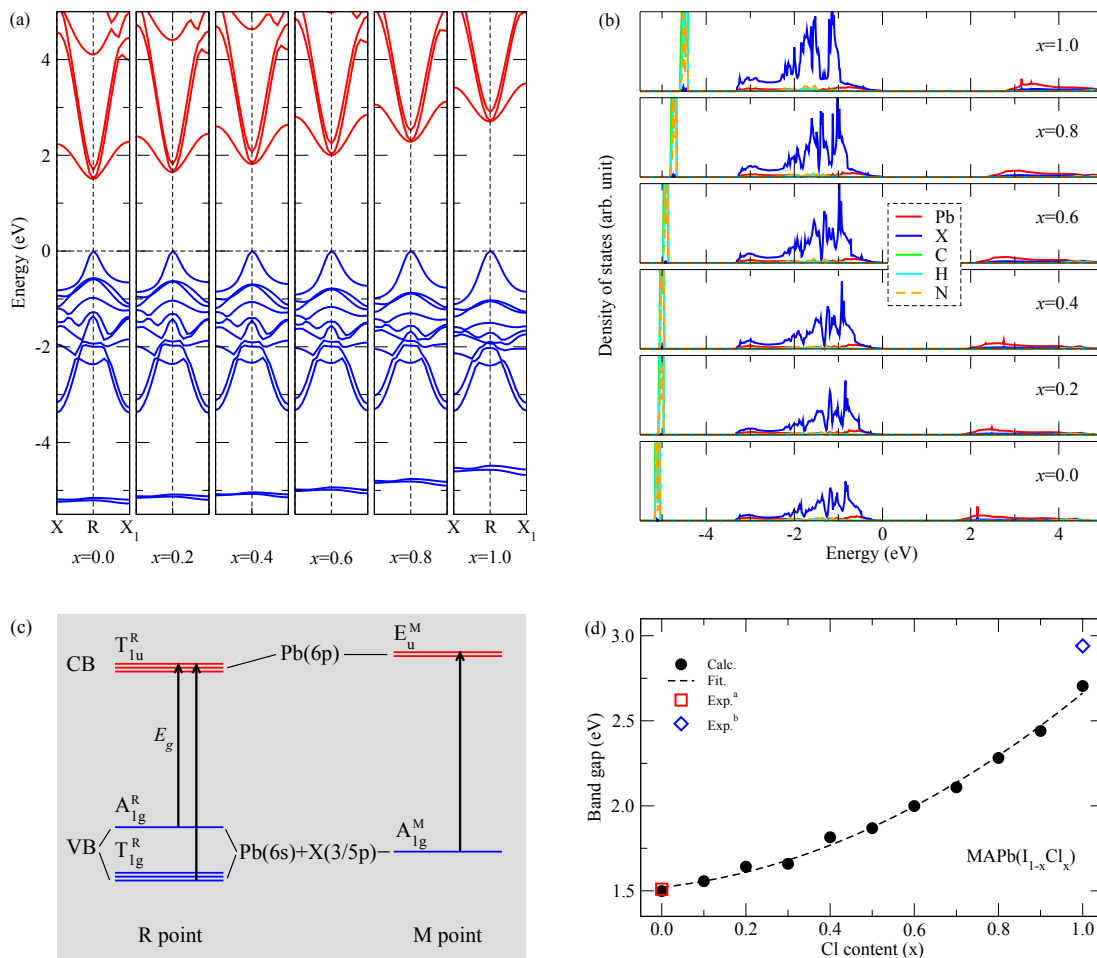


Fig. 2. Systematic change in electronic properties of $\text{MAPb}(\text{I}_{1-x}\text{Cl}_x)_3$ ($x = [0, 1]$). (a) Electronic band structures around R point and (b) atomic resolved density of states, setting the valence band maximum to be zero. (c) Schematic energy level diagram depicted at R and M points with irreducible representations of the group and atomic contributions to the levels, and (d) band gaps with quadratic fitting line (dashed line). Exp^a and Exp^b are from Ref. [54] and ref. [29], respectively.

occupied molecular orbitals of MA cation, found deep ~ 5 eV below the VB maximum, have no significant coupling with other orbitals, which reminds the aforementioned weak vdW interaction between organic MA cation and the inorganic PbX_6 matrix. When increasing the Cl content in the mixed MAPbX_3 , moreover, the molecular orbitals of MA cation get closer to the hybridized orbitals of PbX_6 matrix due to getting stronger MA– PbX_6 interaction [52], which may cause an upward shift of the CB orbitals, resulting in the increase of band gaps from MAPbI_3 to MAPbCl_3 .

From the band structure, the direct band gap of pseudo-cubic MAPbI_3 is estimated to be 1.50 eV at the R point, which is in good agreement with the experimental data [54]. It is well known that this agreement is accidental coincidence thanks to the compensation of GGA underestimation by the lack of SOC [51,52,55,56]. In fact, the large SOC of lead atom can induce a split of the CB into a 2-fold degenerated $E_{1/2g}$ and a 4-fold degenerated $F_{3/2u}$ state at the R point, making the band gap energy reduced to be like 0.5 eV [51]. Although this severe underestimation by the SOC effect can be cured by linking with GW method in defiance of heavy computational cost [57], we could be satisfied with the results from the PBE + vdW-D2 without SOC. When replacing I atom with lighter Cl atom, i.e., for MAPbCl_3 , the SOC effect seems to become weaker, leading to a slight underestimation of the band gap (2.70 eV) compared to the experimental value (2.94 eV) [29] (Table 2).

With the gradual increase of the Cl content in the mixed

Table 2

Band gap (eV) and effective masses of electron and hole.

Material	Band gap		Effective mass			
	Calc.	Exp.	m_e^*	m_e^{*c}	m_h^*	m_h^{*c}
MAPbI_3	1.50	1.50 ^a	0.19	0.23	0.24	0.29
$\text{MAPb}(\text{I}_{0.5}\text{Cl}_{0.5})_3$	1.87		0.27		0.34	
MAPbCl_3	2.70	2.94 ^b	0.34		0.47	

^a Ref. [54].

^b Ref. [29].

^c PBE + SOC calculation [56].

perovskites MAPbX_3 , the band gaps are likely to increase quadratically as shown in Fig. 2(d). The data can be interpolated into the following quadratic function [32]:

$$E_g(x) = E_g(0) + [E_g(1) - E_g(0) - b]x + bx^2 \quad (3)$$

with $E_g(0) = 1.521$ eV, $E_g(1) = 2.663$ eV, and $b = 0.873$ eV for the bowing parameter. Since the bowing parameter reflects the fluctuation degree in the crystal field and the nonlinear effect from the anisotropic binding [27], its larger value compared to 0.33 eV in $\text{MAPb}(\text{I}_{1-x}\text{Br}_x)_3$ [32] indicates larger compositional disorder and low miscibility between MAPbI_3 and MAPbCl_3 . The replacement of some I ions by Cl ions with smaller ionic radius leads to an

enhancement of interaction between Pb and X within PbX_6 octahedra, resulting in the contraction of lattice as well as the decrease of Pb–X bond length. This causes the increase of band gaps and thus a spoil of the light harvesting properties on the increment of Cl content.

Within the parabolic approximation, we calculated the effective masses of electron (m_e^*) around the top of VB and hole (m_h^*) around the bottom of CB at the R point by numerically processing the band structures. As listed in Table 2 and shown in Fig. S4, they increase linearly from 0.19 to $0.34m_e$ for electrons and from 0.24 to $0.47m_e$ for holes as the increase of Cl content, indicating a reduction of carrier mobilities upon the Cl addition to MAPbI_3 . The linear fitting produces the formulas $m_e^*(x) = (0.199 + 0.140x)m_e$ for electrons and $m_h^*(x) = (0.231 + 0.203x)m_e$ for holes, respectively.

3.3. Optical properties

In order to estimate the optical properties such as the exciton binding energy and photo-absorption coefficient, we first determined the macroscopic dielectric constants as functions of incident photon energy by solving the Bethe-Salpeter equation (BSE) including the electron-hole interaction (i.e., excitonic effect) with or without local field effect (LFE) (see Fig.S5(a) and (b)) [50]. Then the static dielectric constants are extracted from those at the zero photon energy, and they, together with the effective masses of carriers as discussed above, are utilized to determine the exciton binding energy using Eq. (2). The obtained static dielectric constants and exciton binding energies as functions of Cl content in MAPbX_3 are shown in Fig. 3.

For MAPbI_3 , the static dielectric constant 5.6 in this work is in good agreement with the recent theoretical values of ~ 4 calculated by quantum molecular dynamics (QMD) method [12] and 5.4 by PBE calculation within density functional perturbation theory (DFPT) [32], and the experimental values of 7–10 measured at 10^{12} Hz (~ 0.01 eV) [13]. However, larger values were also derived from theoretical calculations, such as ~ 15 by nonadiabatic QMD [12] and 18–24 by DFPT with PBEsol functional [58]. It should be noted that the Bethe-Salpeter approach considering the excitonic and many-body effects in this work gives the almost identical dielectric constants with those from DFPT, which includes the effect of atomic displacements. Using the calculated static dielectric constant and effective masses of electron and hole for MAPbI_3 , the exciton binding energy is calculated to be 45 meV, with an effective exciton Bohr radius of 2.8 nm, which is comparable with the experimental values of 50 meV [59] and 16–45 meV [60] (see Ref. [6] for review). These are low enough to be comparable with the inorganic thin-

film semiconductors (< 50 meV). Nonetheless, taking larger dielectric constants from other theoretical works, the exciton binding energy can drop to 12 meV [12] or 10 meV [13], evidencing the existence of free carriers in MAPbI_3 .

It was found in this work that, as the increase of Cl content in MAPbX_3 , the static dielectric constants decrease linearly with a function of $\epsilon_s(x) = 5.698 - 2.593x$, and accordingly, the exciton binding energies increase quadratically with a function of $E_b^{\text{ex}}(x) = 0.055 - 0.036x + 0.253x^2$ (eV). In the explanation of these variation tendencies, the role of MA cation should be emphasized. In fact, the low frequency regime of the macroscopic dielectric functions can be dominated by rotational motion of MA molecule that has intramolecular dipole, while the high frequency behaviour is related to vibrational polar phonons of the lattice [51]. Here, the MA molecular dipoles can screen the Coulombic interaction between photo-excited electrons and holes in the Pb and I sublattices [12], leading to a reduction of exciton binding. Considering that MA cation is placed in a cuboctahedral cage formed by the nearest 12 halogen atoms, the size of this cage reduces when I atom is replaced by Cl atom (-25%). This induces a restriction of molecular motion, resulting in a decrease of static dielectric constant (reduction of exciton screening) and inversely a sizable increase of exciton binding energy. Here, it is the most interesting that the minimum of exciton binding energy is found at $x \approx 0.07$ unlike in the case of $\text{MAPb(I}_{1-x}\text{Br}_x)_3$ where it increases linearly [32]. This indicates an enhancement of the light harvesting efficiency when adding a small amount of Cl atom ($\sim 7\%$) to MAPbI_3 .

Next, using the macroscopic dielectric functions, we obtained the photo-absorption coefficients of mixed iodide-chloride perovskites MAPbX_3 , direct estimation of light harvesting capability of PSC, as shown in Fig. 4 with relevant photon energy range and in Fig.S5(c) with full photon energy range. It should be noted that the absorption lines in Fig. 4 are from BSE with no LFE for the sake of clear view of variation tendency, while those with LFE for MAPbI_3 and MAPbCl_3 are shown in Fig.S5(c) for comparison. As can be expected from the band gaps discussed above, when increasing the Cl content in MAPbX_3 , the absorption onset and first peak shift to a higher photon energy, i.e., a shorter wavelength light, implying a lowering of power conversion efficiency.

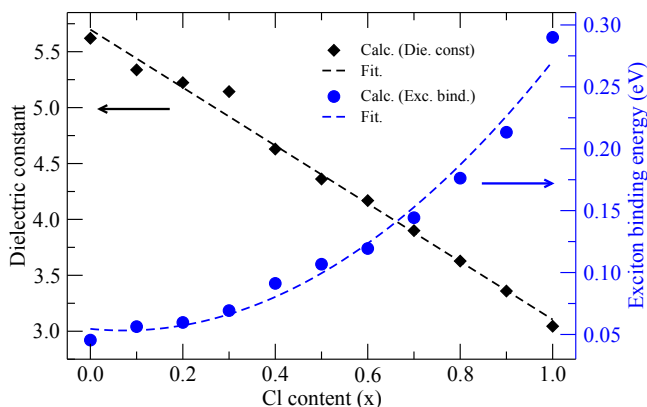


Fig. 3. Static dielectric constants and exciton binding energies as functions of Cl content x in $\text{MAPb(I}_{1-x}\text{Cl}_x)_3$.

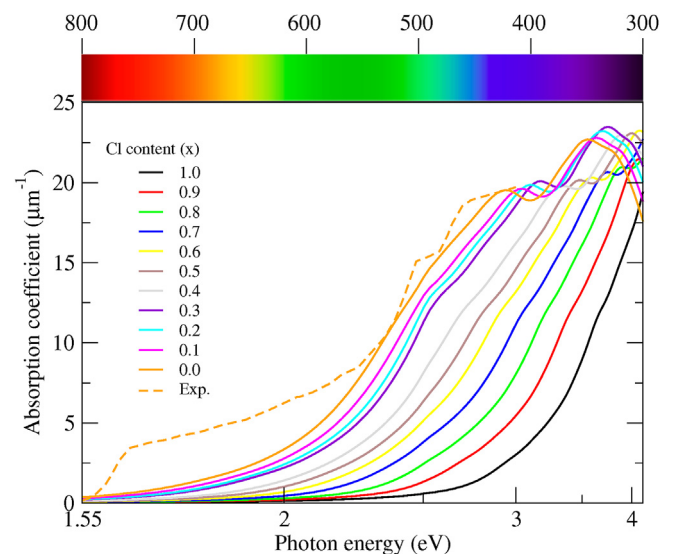
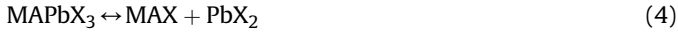


Fig. 4. Photo-absorption coefficients of mixed halide perovskites $\text{MAPb(I}_{1-x}\text{Cl}_x)_3$ with different Cl content. For comparison, experimental absorption spectrum on MAPbI_3 from Ref. [61] is shown.

3.4. Material stability

We have already discussed the material stability of mixed iodide-chloride perovskites $\text{MAPb}(\text{I}_{1-x}\text{Cl}_x)_3$ in subsection 3.1 using lattice related properties such as lattice constant, Pb-X bond length, bulk modulus and cohesive energy. However, it might be thought that these data can not give a direct estimation of material stability. Therefore, we now study their stability by calculating the formation enthalpy ΔH with respect to the following chemical reaction:



Here, the formation enthalpy can be calculated as follows:

$$\Delta H_f = H(\text{MAPbX}_3) - [H(\text{MAX}) + H(\text{PbX}_2)] \quad (5)$$

Considering that $H = E + PV$ and the PV term for solid at the atmospheric pressure is in order of ~ 0.1 meV, we can write $\Delta H \approx \Delta E$ in safe. It is worth noting that the accuracy of the formation enthalpy could be improved to be 0.1 meV per cell due to a cancellation of errors. Although different chemical reactions are thought to be possible such as further reaction of $\text{CH}_3\text{NH}_3\text{PbX}_3 \leftrightarrow \text{CH}_3\text{NH}_2 + \text{HX} + \text{PbX}_2$ [15,62] or even $\text{CH}_3\text{NH}_3\text{PbX}_3 \leftrightarrow \text{NH}_4\text{X} + \text{H}_2\text{C} + \text{PbX}_2$ [63], we preferred the reaction Eq. (4) based on the majority of experimental procedures for synthesis of OTPs.

We assumed that PbX_2 can be crystallized in rhombohedral structure with space group $\bar{P}3m1$ [62], which can be characterized by a two-dimensional structure consisting of PbX_2 edge sharing octahedron in a hexagonal arrangement, as shown in Fig. 5(a). On the other hand, MAX can be crystallized in rocksalt structure, which should be also pseudo-cubic with space group Pm due to the existence of MA cation and its orientational freedom like in MAPbX_3

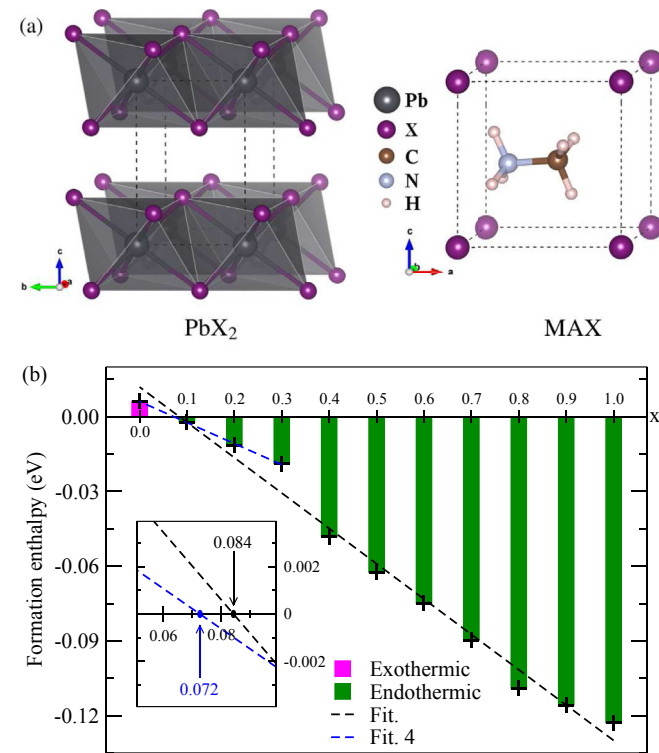


Fig. 5. (a) The crystalline structures of rhombohedral PbX_2 and pseudo-cubic MAX. (b) Formation enthalpy of $\text{MAPb}(\text{I}_{1-x}\text{Cl}_x)_3$ from their components PbX_2 and MAX as the increase of Cl content, where the inset shows the intersection points of fitting (dashed) lines with X-axis.

(Fig. 5(a)). Therefore, we performed the structural optimization, maintaining the cubic symmetry and taking account of the MA orientation to confirm the lowest energy configuration. In the context of structural characteristics of both phases, the vdW correction should be considered; the semi-empirical vdW function (vdW-D2) was used. To make it clear that such decomposition of the OTPs causes the deterioration of PSC, we calculated the band gaps of PbX_2 (Fig. S6) and MAX. They are 2.5–3.1 eV in PbX_2 and ~ 4 eV in MAX, indicating a blue-shift of light absorption onset.

The calculated formation enthalpies for MAPbX_3 as the increase of Cl content are presented with the bar diagram in Fig. 5(b). It turns out that only the MAPbI_3 has the positive formation enthalpy, while all other compounds treated in this work have negative values, increasing in the magnitude as almost linear function of Cl content. This result directly indicates that in the former case the phase decomposition reaction is exothermic, while in the latter cases they are endothermic. This means that the phase decomposition of MAPbI_3 into MAI and PbI_2 may occur spontaneously without application of any extrinsic factors such as moisture, oxygen, UV light and elevated temperature, but for other mixed iodide-chloride perovskites the decompositions are thermodynamically unfavorable. It should be noted that in spite of exothermicity of phase decomposition of MAPbI_3 the kinetic barrier can hinder the reaction, explaining its stable existence in a certain period [62]. When compared with other recent PBE/vdW calculations (0.111/0.119 eV f.u.⁻¹ (formular unit) for MAPbI_3 and $-0.040/-0.004$ eV f.u.⁻¹ for MAPbCl_3) [62], our results (0.006 and -0.109 eV, respectively) are in reasonable agreement with them. Moreover, our results are consistent with the experimental findings by Buin et al. [64], reporting that time evolution of the main XRD (X-ray diffraction) peak of MAPbI_3 shows the PbI_2 peak as soon as MAPbI_3 is formed, while MAPbCl_3 does not give any evidence of PbCl_2 peak.

We also performed fitting of the calculated formation enthalpies into linear function. This process outputs the linear functions $\Delta H_f(x) = 0.0062 - 0.0846x$ (eV f.u.⁻¹) for the first four data from $x = 0.0$ to $x = 0.3$ (dashed blue line in Fig. 5(b)) as well as $\Delta H_f(x) = 0.0120 - 0.1419x$ (eV f.u.⁻¹) for the whole range of Cl content (dashed black line). As shown in the inset of Fig. 5(b), these lines intersect with X-axis at 0.072 and 0.084, respectively. These are turning points at which the phase decomposition reaction becomes to be endothermic from exothermic. Here we should stress that the turning point ~ 0.07 is consistent with what we have found for the minimum of exciton binding energy as discussed in subsection 3.3. Therefore, it can be concluded that at the mixing ratio of Cl ~ 0.07 into MAPbI_3 the best efficiency could be realized with the positive material stability. We should note that it is much smaller than the one in $\text{MAPb}(\text{I}_{1-x}\text{Br}_x)_3$ (~ 0.2) [32], and this small ratio value reasonably corresponds to the experimentally observed Cl doping ratio 3–4% into MAPbI_3 [48].

The material stability can be related with the strength of chemical bonds between the constituents of the compound. As discussed in subsection 3.1, the strength of chemical bonds increase as the increase of Cl content due to the contraction of lattice constant and Pb-X bond length. Besides, since the strength of chemical bond can be inspected by electronic charge transfer in the formation of compound from its components, we estimated the electronic charge density difference between the MAPbX_3 and PbX_3 framework plus MA molecule as follow:

$$\Delta n(\mathbf{r}) = n_{\text{MAPbX}_3}(\mathbf{r}) - [n_{\text{PbX}_3}(\mathbf{r}) + n_{\text{MA}}(\mathbf{r})] \quad (6)$$

For the sake of clear comparison, the electronic charge density differences only at the Cl contents of $x = 0.0, 0.5$ and 1.0 are shown in Fig. 6. It is observed that a charge accumulation occurs in the interspatial region surrounding the halogen atoms, while a charge

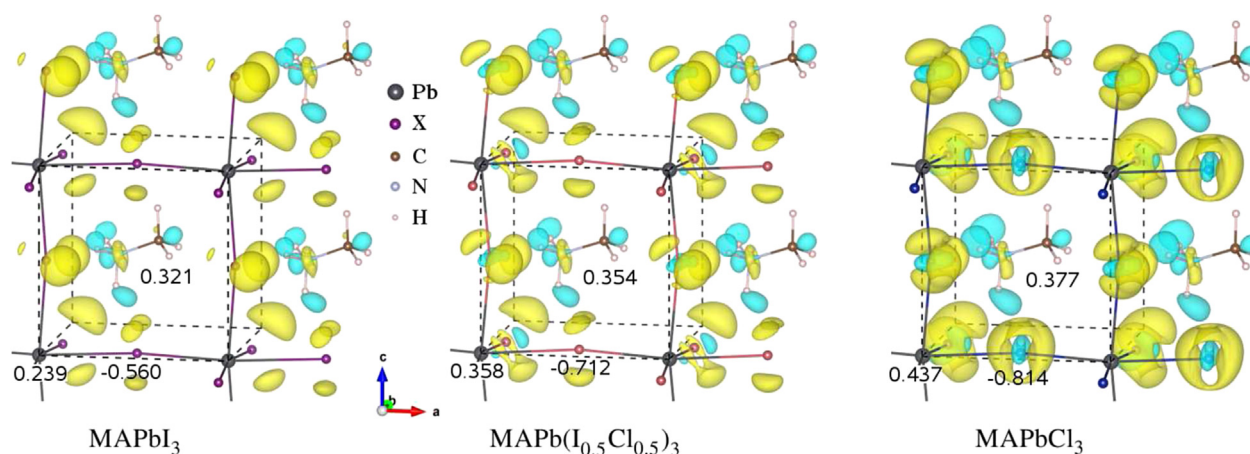


Fig. 6. Electronic charge density difference in MAPbX_3 at the Cl contents of $x = 0.0, 0.5, 1.0$. The 3D isosurfaces are plotted at the value of $\pm 0.0017 |e| \text{ \AA}^{-3}$, where the yellow (cyan) colour represents the positive (negative) value indicating electron accumulation (depletion). Numbers denote the transferred electronic charges for Pb, X₃ and MA molecule calculated by using the Hirshfeld method.

depletion occurs around the hydrogen atoms of MA cation and the lead atoms, being enhanced from iodide to chloride. This indicates that electrons are in general transferred from MA cation and Pb atom to halogen atoms, making the chemical bond strong, and the chemical bond gets stronger going from iodide to chloride. To quantitatively estimate the charge transfer, we calculated the net charges (q_n) of atoms with the Hirshfeld method, using the equation $q_n = q_r - q_H$ meaning q_r and q_H the reference and Hirshfeld charge. Thus the positive value indicates the lose of electron, while the negative value the gain of electron. As shown in Fig. 6 and Table S1, going from $x = 0.0$ to $x = 0.5$ and to $x = 1.0$, Pb atom loses electron of 0.239, 0.358 and 0.437, MA molecule also loses electron of 0.321, 0.354 and 0.377, while halogen atoms gain electron of $-0.560, -0.712$ and -0.814 , again indicating the enhancement of charge transfer when mixing chloride with MAPbI_3 . It should be noted that carbon and nitrogen atoms inside MA molecule also gain electrons.

4. Conclusions

With *ab initio* calculations using the vdW-D2 functional and the efficient VCA method, the effects of Cl addition on structural, electronic, optical properties and material stability of mixed iodide-chloride perovskites $\text{MAPb}(\text{I}_{1-x}\text{Cl}_x)_3$ were systematically investigated. As the increase of Cl content, the pseudo-cubic crystalline lattice contracts, seeing the decrease of lattice constants according to the linear function of $a(x) = 6.310 - 0.716x$ (Å) and the increase of bulk modulus with the linear function of $B(x) = 10.627 + 5.492x$ (GPa), which indicates the enhancement of chemical stability. The electronic structure calculations show the increase of band gaps with the quadratic function of $E_g(x) = 1.521 + 0.269x + 0.873x^2$ (eV) and the almost linear increase of effective masses of carriers. By solving the Bethe-Salpeter equation with local field effect and using the Mott-Wannier model, we have found that the static dielectric constants decrease linearly according to the function of $\epsilon_s(x) = 5.698 - 2.593x$, while the exciton binding energies increase quadratically according to the function of $E_b^{\text{ex}}(x) = 0.055 - 0.036x + 0.253x^2$ (eV) with the minimum of 0.054 eV at $x \approx 0.071$. Furthermore, this Cl content $\sim 7\%$ is consistent with the turning point at which the decomposition reaction changes to be from exothermic to endothermic, indicating that the best performance can be realized at the Cl addition of $\sim 7\%$ to MAPbI_3 . This work provides the evidence why a little addition of Cl

to MAPbI_3 enhances the stability as well as the efficiency of PSC and thus reveals new prospects for designing of stable, high efficiency PSCs.

Notes

The authors declare no competing financial interest.

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Appendix A. Supplementary data

Supplementary data related to this article can be found at <http://dx.doi.org/10.1016/j.jpowsour.2017.03.038>.

References

- [1] A. Kojima, K. Teshima, Y. Shirai, T. Miyasaka, Organometal halide perovskites as visible-light sensitizers for photovoltaic cells, *J. Am. Chem. Soc.* 131 (2009) 6050–6051.
- [2] M. Liu, M.B. Johnston, H.J. Snaith, Efficient planar heterojunction perovskite solar cells by vapour deposition, *Nature* 501 (2013) 395–398.
- [3] T.-B. Song, Q. Chen, H. Zhou, S. Luo, Y. Yang, J. You, Y. Yang, Unraveling film transformations and device performance of planar perovskite solar cells, *Nano Energy* 12 (2015) 494–500.
- [4] Z. Xiao, Y. Yuan, Q. Wang, Y. Shao, Y. Bai, Y. Deng, Q. Dong, M. Hu, C. Bi, J. Huang, Thin-film semiconductor perspective of organometal trihalide perovskite materials for high-efficiency solar cells, *Mater. Sci. Eng. R* 101 (2016) 1–38.
- [5] S. Luo, W.A. Daoud, Recent progress in organic-inorganic halide perovskite solar cells: mechanisms and materials design, *J. Mater. Chem. A* 3 (2015) 8992–9010.
- [6] T.C. Sum, N. Mathews, Advancements in perovskite solar cells: photophysics behind the photovoltaics, *Energy Environ. Sci.* 7 (2014) 2518–2534.
- [7] R. Lindblad, D. Bi, B. w. Park, J. Oscarsson, M. Gorgoi, H. Siegbahn, M. Odelius, E.M.J. Johansson, H. Rensmo, Electronic structure of $\text{TiO}_2/\text{CH}_3\text{NH}_3\text{PbI}_3$ perovskite solar cell interfaces, *J. Phys. Chem. Lett.* 5 (2014) 648–653.
- [8] J.M. Frost, K.T. Butler, F. Brivio, C.H. Hendon, M. van Schilfgaarde, A. Walsh, Atomistic origins of high-performance in hybrid halide perovskite solar cells, *Nano Lett.* 14 (2014) 2584–2590.
- [9] E. Edri, S. Kirmayer, S. Mukhopadhyay, K. Gartsman, G. Hodes, D. Cahen,

- Elucidating the charge carrier separation and working mechanism of $\text{CH}_3\text{NH}_3\text{PbI}_{3-x}\text{Cl}_x$ perovskite solar cells, *Nat. Commun.* 5 (2014) 3461.
- [10] G. Xing, N. Mathews, S. Sun, S.S. Lim, Y.M. Lam, M. Grätzel, S. Mhaisalkar, T.C. Sum, Long-range balanced electron- and hole-transport length in organic-inorganic $\text{CH}_3\text{NH}_3\text{PbI}_3$, *Science* 342 (2013) 344–347.
 - [11] S.D. Stranks, G.E. Eperon, G. Grancini, C. Menelaou, M.J.P. Alcocer, T. Leijtens, L.M. Herz, A. Petrozza, H.J. Snaith, Electron-hole diffusion lengths exceeding 1 μm in an organometal trihalide perovskite absorber, *Science* 342 (2013) 341–344.
 - [12] T. Hakamata, K. Shimamura, F. Shimojo, R.K. Kalia, A. Nakano, P. Vashishta, The nature of free-carrier transport in organometal halide perovskites, *Sci. Rep.* 6 (2016) 19599.
 - [13] S.D. Stranks, H.J. Snaith, Metal-halide perovskites for photovoltaic and light-emitting devices, *Nat. Nanotechnol.* 10 (2015) 391–402.
 - [14] D. Wang, M. Wright, N.K. Elumalai, A. Uddin, Stability of perovskite solar cells, *Sol. Energy Mater. Sol. Cells* 147 (2016) 255–275.
 - [15] G. Niu, X. Guo, L. Wang, Review of recent progress in chemical stability of perovskite solar cells, *J. Mater. Chem. A* 3 (2015) 8970–8980.
 - [16] T.A. Berhe, W.-N. Su, C.-H. Chen, C.-J. Pan, J.-H. Cheng, H.-M. Chen, M.-C. Tsai, L.-Y. Chen, A.A. Dubaleb, B.-J. Hwang, Organometal halide perovskite solar cells: degradation and stability, *Energy Environ. Sci.* 9 (2016) 323–356.
 - [17] N.K. Noel, S.D. Stranks, A. Abate, C. Wehrenfennig, S. Guarnera, A.-A. Haghighirad, A. Sadhanala, G.E. Eperon, S.K. Pathak, M.B. Johnston, A. Petrozza, L.M. Herz, H.J. Snaith, Lead-free organico-inorganic tin halide perovskites for photovoltaic applications, *Energy Environ. Sci.* 7 (2014) 3061–3068.
 - [18] Y. Han, S. Meyer, Y. Dkhissi, K. Weber, J. Pringle, U. Bach, L. Spiccia, Y.-B. Cheng, Degradation observations of encapsulated planar $\text{CH}_3\text{NH}_3\text{PbI}_3$ perovskite solar cells at high temperatures and humidity, *J. Mater. Chem. A* 3 (2015) 8139–8147.
 - [19] J.A. Christians, P.A.M. Herrera, P. Kamat, Transformation of the excited state and photovoltaic efficiency of $\text{CH}_3\text{NH}_3\text{PbI}_3$ perovskite upon controlled exposure to humidified air, *J. Am. Chem. Soc.* 137 (2015) 1530–1538.
 - [20] H. Zhou, Q. Chen, G. Li, S. Luo, T.-B. Song, H.-S. Duan, Z. Hong, J. You, Y. Liu, Y. Yang, Interface engineering of highly efficient perovskite solar cells, *Science* 345 (2014) 542–546.
 - [21] T. Leijtens, G.E. Eperon, S. Pathak, A. Abate, M.M. Lee, H.J. Snaith, Overcoming ultraviolet light instability of sensitized TiO_2 with meso-superstructured organometal tri-halide perovskite solar cells, *Nat. Commun.* 4 (2013) 2885.
 - [22] J. Song, E. Zheng, J. Bian, X.-F. Wang, W. Tian, Y. Sanehira, T. Miyasaka, Low-temperature SnO_2 -based electron selective contact for efficient and stable perovskite solar cells, *J. Mater. Chem. A* 3 (2015) 10837–10844.
 - [23] C. Bi, Y. Shao, Y. Yuan, Z. Xiao, C. Wang, Y. Gao, J. Huang, Understanding the formation and evolution of interdiffusion grown organolead halide perovskite thin films by thermal annealing, *J. Mater. Chem. A* 2 (2014) 18508–18514.
 - [24] A. Dualeh, P. Gao, S.I. Seok, M.K. Nazeeruddin, M. Grätzel, Thermal behavior of methylammonium lead-trihalide perovskite photovoltaic light harvesters, *Chem. Mater* 26 (2014) 6160–6164.
 - [25] S. Aharon, A. Dymshits, A. Rotem, L. Etgar, Temperature dependence of hole conductor free formamidinium lead iodide perovskite based solar cells, *J. Mater. Chem. A* 3 (2015) 9171–9178.
 - [26] G.E. Eperon, S.D. Stranks, C. Menelaou, M.B. Johnston, L.M. Herz, H.J. Snaith, Formamidinium lead trihalide: a broadly tunable perovskite for efficient planar heterojunction solar cells, *Energy Environ. Sci.* 7 (2014) 982–988.
 - [27] J.H. Noh, S.H. Im, J.H. Heo, T.N. Mandal, S.I. Seok, Chemical management for colorful, efficient, and stable inorganic-organic hybrid nanostructured solar cells, *Nano Lett.* 13 (2013) 1764–1769.
 - [28] M.M. Lee, J. Teuscher, T. Miyasaka, T.N. Murakami, H.J. Snaith, Efficient hybrid solar cells based on meso-superstructured organometal halide perovskite, *Science* 338 (2012) 643–647.
 - [29] L. Dimesso, M. Dimamay, M. Hamburger, W. Jaegermann, Properties of $\text{CH}_3\text{NH}_3\text{PbX}_3$ ($X = \text{I}, \text{Br}, \text{Cl}$) powders as precursors for organic/inorganic solar cells, *Chem. Mater* 26 (2014) 6762–6770.
 - [30] S. Aharon, B.E. Cohen, L. Etgar, Hybrid lead halide iodide and lead halide bromide in efficient hole conductor free perovskite solar cell, *J. Phys. Chem. C* 118 (2014) 17160–17165.
 - [31] E. Mosconi, A. Amat, M.K. Nazeeruddin, M. Grätzel, F.D. Angelis, First-Principles modeling of mixed halide organometal perovskites for photovoltaic applications, *J. Phys. Chem. C* 117 (2013) 13902–13913.
 - [32] U.-G. Jong, C.-J. Yu, J.-S. Ri, N.-H. Kim, G.-C. Ri, Influence of halide composition on the structural, electronic, and optical properties of mixed $\text{CH}_3\text{NH}_3\text{Pb}(\text{I}_{1-x}\text{Br}_x)_3$ perovskites calculated using the virtual crystal approximation method, *Phys. Rev. B* 94 (2016) 125139.
 - [33] C.-J. Yu, U.-G. Jong, M.-H. Ri, G.-C. Ri, Y.-H. Pae, Electronic structure and photo absorption property of pseudo-cubic perovskites $\text{CH}_3\text{NH}_3\text{PbX}_3$ ($X = \text{I}, \text{Br}$) including van der Waals interaction, *J. Mat. Sci.* 51 (2016) 9849–9854.
 - [34] J. Liu, J. Lin, Q. Xue, Q. Ye, X. He, L. Ouyang, D. Zhuang, C. Liao, H.L. Yip, J. Mei, W.M. Lau, Growth and evolution of solution-processed $\text{CH}_3\text{NH}_3\text{PbI}_{3-x}\text{Cl}_x$ layer for highly efficient planar-heterojunction perovskite solar cells, *J. Power Sources* 301 (2016) 242–250.
 - [35] N. Tripathi, M. Yanagida, Y. Shirai, T. Masuda, L. Han, K. Miyano, Hysteresis-free and highly stable perovskite solar cells produced via a chlorine-mediated interdiffusion method, *J. Mater. Chem. A* 3 (2015) 12081–12088.
 - [36] M.H. Du, Efficient carrier transport in halide perovskites: theoretical perspectives, *J. Mater. Chem. A* 2 (2014) 9091–9098.
 - [37] C.-C. Chueh, C.-Y. Liao, F. Zuo, S.T. Williams, P.-W. Liang, A.K.Y. Jen, The roles of alkyl halide additives in enhancing perovskite solar cell performance, *J. Mater. Chem. A* 3 (2014) 9058–9062.
 - [38] A.E. Williams, P.J. Holliman, M.J. Carnie, M.L. Davies, D.A. Worsley, T.M. Watson, Perovskite processing for photovoltaics: a spectro-thermal evaluation, *J. Mater. Chem. A* 2 (2014) 19338–19346.
 - [39] C.-J. Yu, H. Emmerich, An efficient virtual crystal approximation that can be used to treat heterovalent atoms, applied to $(1-x)\text{BiScO}_3-x\text{PbTiO}_3$, *J. Phys. Condens. Matter* 19 (2007) 306203.
 - [40] X. Gonze, B. Amadon, P.M. Anglade, J.-M. Beuken, F. Bottin, et al., ABINIT: first-principles approach to material and nanosystem properties, *Comput. Phys. Commun.* 180 (2009) 2582–2615.
 - [41] J.P. Perdew, K. Burke, M. Ernzerhof, Generalized gradient approximation made simple, *Phys. Rev. Lett.* 77 (1996) 3865.
 - [42] S. Grimme, Semiempirical GGA-type density functional constructed with a long-range dispersion correction, *J. Comput. Chem.* 27 (2006) 1787–1799.
 - [43] A.M. Rappe, K.M. Rabe, E. Kaxiras, J.D. Joannopoulos, Optimized pseudopotentials, *Phys. Rev. B* 41 (1990) 1227–1230.
 - [44] N.J. Ramer, A.M. Rappe, Designed nonlocal pseudopotentials for enhanced transferability, *Phys. Rev. B* 59 (1999) 12471–12478.
 - [45] F. Birch, Finite elastic strain of cubic crystal, *Phys. Rev.* 71 (1947) 809–824.
 - [46] A. Poglitsch, D. Weber, Dynamic disorder in methylammonium-trihalogenoplumbates (ii) observed by millimeter-wave spectroscopy, *J. Chem. Phys.* 87 (1987), 6383–6378.
 - [47] T. Baikie, Y.N. Fang, J.M. Kadro, M. Schreyer, F.X. Wei, S.G. Mhaisalkar, M. Grätzel, T.J. White, Synthesis and crystal chemistry of the hybrid perovskite $(\text{CH}_3\text{NH}_3)\text{PbI}_3$ for solid-state sensitised solar cell applications, *J. Mater. Chem. A* 1 (2013) 5628–5641.
 - [48] S. Colella, E. Mosconi, P. Fedeli, A. Listorti, F. Gazza, F. Orlandi, P. Ferro, T. Besagni, A. Rizzo, G. Calestani, G. Gigli, F.D. Angelis, R. Mosca, $\text{MAPbI}_{3-x}\text{Cl}_x$ mixed halide perovskite for hybrid solar cells: the role of chloride as dopant on the transport and structural properties, *Chem. Mater* 25 (2013) 4613–4618.
 - [49] P. Docampo, F. Hanusch, S.D. Stranks, M. Döblinger, J.M. Feckl, M. Ehrensperger, N.K. Minar, M.B. Johnston, H.J. Snaith, T. Bein, Solution deposition-conversion for planar heterojunction mixed halide perovskite solar cells, *Adv. Energy Mater* 4 (2014) 1400355.
 - [50] G. Onida, L. Reining, A. Rubio, Electronic excitations: density-functional versus many-body Green's-function approaches, *Rev. Mod. Phys.* 74 (2002) 601–659.
 - [51] J. Even, L. Pedesseau, C. Katan, Analysis of multivalley and multibandgap absorption and enhancement of free carriers related to exciton screening in hybrid perovskites, *J. Phys. Chem. C* 118 (2014) 11566–11572.
 - [52] C. Motta, F. El-Mellouhi, S. Kais, N. Tabet, F. Alharbi, S. Sanvito, Revealing the role of organic cations in hybrid halide perovskite $\text{CH}_3\text{NH}_3\text{PbI}_3$, *Nat. Commun.* 6 (2015) 7026.
 - [53] W. Geng, L. Zhang, Y.-N. Zhang, W.-M. Lau, L.-M. Liu, First-Principles study of lead iodide perovskite tetragonal and orthorhombic phases for photovoltaics, *J. Phys. Chem. C* 118 (2014) 19565–19571.
 - [54] H.S. Kim, C.R. Lee, J.H. Im, K.B. Lee, T. Moehl, A. Marchioro, S.J. Moon, R. Humphry-Baker, J.H. Yum, J.E. Moser, M. Grätzel, N.G. Park, Lead iodide perovskite sensitized all-solid-state submicron thin film mesoscopic solar cell with efficiency exceeding 9%, *Sci. Rep.* 2 (2012) 591.
 - [55] J. Even, L. Pedesseau, J.-M. Jancu, C. Katan, Importance of spin-orbit coupling in hybrid organic/inorganic perovskites for photovoltaic applications, *J. Phys. Chem. Lett.* 4 (2013) 2999–3005.
 - [56] G. Giorgi, J.-I. Fujisawa, H. Segawa, K. Yamashita, Small photocarrier effective masses featuring ambipolar transport in methylammonium lead iodide perovskite: a density functional analysis, *J. Phys. Chem. Lett.* 4 (2013) 4213–4216.
 - [57] P. Umari, E. Mosconi, F.D. Angelis, Relativistic GW calculations on $\text{CH}_3\text{NH}_3\text{PbI}_3$ and $\text{CH}_3\text{NH}_3\text{SnI}_3$ perovskites for solar cell applications, *Sci. Rep.* 4 (2014) 4467.
 - [58] F. Brivio, A.B. Walker, A. Walsh, Structural and electronic properties of hybrid perovskites for high-efficiency thin-film photovoltaics from first-principles, *APL Mater* 1 (2013) 042111.
 - [59] V. D'Innocenzo, G. Grancini, M.J.P. Alcocer, A.R.S. Kandada, S.D. Stranks, M.M. Lee, G. Lanzani, H.J. Snaith, A. Petrozza, Excitons versus free charges in organo-lead tri-halide perovskites, *Nat. Commun.* 5 (2014) 3486.
 - [60] A. Miyata, A. Mitoglu, P. Plochocka, O. Portugall, R.J. Nicholas, Direct measurement of the exciton binding energy and effective masses for charge carriers in an organic-inorganic tri-halide perovskite, *Nat. Phys.* 11 (2015) 582–587.
 - [61] S.D. Wolf, J. Holovsky, S.J. Moon, P. Loper, B. Niesen, M. Ledinsky, F.J. Haug, J.H. Yum, C. Balif, Organometallic halide perovskites: sharp optical absorption edge and its relation to photovoltaic performance, *J. Phys. Chem. Lett.* 5 (2014) 1035–1039.
 - [62] Y.-Y. Zhang, S. Chen, P. Xu, H. Xiang, X.-G. Gong, A. Walsh, S.-H. Wei, Intrinsic instability of the hybrid halide perovskite semiconductor $\text{CH}_3\text{NH}_3\text{PbI}_3$, *arXiv* (1506) 01301.
 - [63] F. El-Mellouhi, E.T. Bentría, S.N. Rashkeev, S. Kais, F.H. Alharbi, Enhancing intrinsic stability of hybrid perovskite solar cell by strong, yet balanced, electronic coupling, *Sci. Rep.* 6 (2016) 30305.
 - [64] A. Buin, R. Comin, J. Xu, A.H. Ip, E.H. Sargent, Halide-dependent electronic structure of organolead perovskite materials, *Chem. Mater* 27 (2015) 4405.