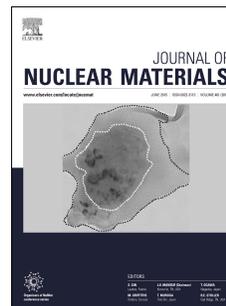


Accepted Manuscript

Precipitates in metals that dissolve on cooling and form on heating: An example with hydrogen in alpha-zirconium

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PII: S0022-3115(16)30529-3

DOI: [10.1016/j.jnucmat.2017.09.017](https://doi.org/10.1016/j.jnucmat.2017.09.017)

Reference: NUMA 50503

To appear in: *Journal of Nuclear Materials*

Received Date: 2 August 2016

Revised Date: 11 September 2017

Accepted Date: 13 September 2017

Please cite this article as: G.A. McRae, C.E. Coleman, Precipitates in metals that dissolve on cooling and form on heating: An example with hydrogen in alpha-zirconium, *Journal of Nuclear Materials* (2017), doi: 10.1016/j.jnucmat.2017.09.017.

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22 Introduction:

23 It is everyday experience that solutes precipitating from liquid solutions at constant pressure
24 form in ever increasing amounts as the temperature is lowered. When the temperature is
25 increased, these precipitates dissolve. At low temperatures, the entropy contribution to the free
26 energy, $-T\Delta S$, is small compared with the enthalpy of formation of the precipitate, whereas at
27 higher temperatures the entropy contribution favours a well-dispersed solute. The temperature
28 where the switch occurs between precipitation and dissolution is called the solvus temperature.
29 In this simple two-component two-phase constant-pressure liquid-solvent example, precipitation
30 increases with cooling and precipitates dissolve with heating.

31 When the solvent is a solid, the equivalent of pressure for liquids is hydrostatic stress, which is
32 no longer constant: there will always be internal defects, for example, dislocations, that give rise
33 to local gradients in hydrostatic stress seen by the solute. Applied stresses can lead to
34 hydrostatic stress gradients in the solvent. Both stress gradients allow precipitates to form and
35 dissolve above and below the solvus temperature.

36 Our example is hydrogen in zirconium. Hydrogen atoms move interstitially in solid solution and
37 increase the lattice parameters of the zirconium. Hydrides also expand the lattice locally, which
38 results in regions of tensile stress in the zirconium and compression in the hydride.

39 There are two hydride phases commonly seen in zirconium. These phases are the δ -phase, with
40 stoichiometry reported between $ZrH_{1.5}$ (Zr_2H_3) and $ZrH_{1.67}$ (Zr_3H_5), and the γ -phase, ZrH [1].
41 The δ -phase, with a calculated formation energy between -53 and -57 kJ/mol atom, might be
42 expected to be more stable than the γ -phase, with a formation energy of -31 to -49 kJ/mol atom
43 [2, 3], but when entropy is included, the free energy suggests that the γ -phase will be the more
44 stable, although the free energy of the two phases is very close [4]. The γ -phase forms as long
45 needles, and the δ -phase forms crystals that are platelets [5], both having sharp edges that may
46 act as local stress concentrators.

47 Gibbs' Phase Rule [6] is tested by the simultaneous observation of γ -phase and δ -phase in
48 α -zirconium: hydrogen in solution in the metal cannot simultaneously be in equilibrium with two
49 hydride phases. Gibbs' Phase Rule relates the number of components, C , and the number of
50 phases in equilibrium in gradient-free solids, P , to the number of degrees of freedom, F , that are
51 independent intensive variables that can completely describe the system thermodynamically
52 through:

$$53 \quad F = C - P + 1 \quad (1)$$

54 Hydrogen and zirconium are the two components, so $C=2$. For a single hydride phase and
55 hydrogen in solution at equilibrium, there are two phases, so $P=2$ and $F=1$. There is one degree
56 of freedom. For phase diagrams written in terms of the intensive variables concentration and
57 temperature, the Phase Rule says that only one of these variables is independent. Thus, if
58 temperature is chosen to describe the system, the concentration is given by a unique value on the
59 phase boundary curve and vice versa. But, if γ -phase, and δ -phase exist independently and
60 simultaneously with hydrogen in solution at equilibrium, then $P=3$, and $F=0$, there are no
61 degrees of freedom. In this case, there could be no variation of the equilibrium with an intensive
62 variable such as temperature or concentration, which is not observed – the phase diagram for the

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63 solvus shows unique equilibria happen for concentrations that depend on temperatures, or vice
64 versa.

65 Equilibrium between hydrogen in solution and hydrogen as hydride is dynamic: hydrogen in
66 solution in the zirconium matrix leaves solution to precipitate as hydride, and hydrogen in
67 hydrides leaves the hydrides to go into solution, the rates for these processes are equal and
68 opposite at equilibrium. For hydrogen in solid solution (SS) in equilibrium with hydride in
69 zirconium:



71 The concentration of hydrogen in solution in the metal volume adjacent to hydrides defines the
72 solvus concentration.

73 This paper presents X-ray diffraction data showing isothermal measurements of hydrogen
74 concentration in solution in zirconium, and the formation of γ -phase and δ -phase hydrides,
75 during heating and cooling. Comparisons will be made with heat flow determined using
76 Differential Scanning Calorimetry (DSC). The experimental results in this paper will be used to
77 test predictions made with the flux relation developed by Einstein for Brownian motion [7], and
78 previously used to predict delayed hydride cracking rates [8]. The results are different from
79 other applications of the Einstein flux because a solvus is crossed.

80 The focus of this paper is on precipitates dissolving during cooling and forming during heating.
81 The experimental results presented here also provide additional observations of the relationship
82 between γ -hydrides and δ -hydrides in zirconium at low hydrogen concentrations and
83 temperatures, and suggest an interpretation of the apparent hysteresis observed between the
84 temperatures at which hydrides precipitate and dissolve.

85 Background

86 Observations of γ - and δ -hydrides in zirconium

87 The phases of the zirconium-hydrogen system are controversial. Much of the reported variation
88 in the presence of each hydride phase is caused by comparing materials with a range of
89 concentrations of hydrogen, impurity and alloying elements, after various cooling rates and hold
90 times at different temperatures, various grain structures of the zirconium alloy, and different
91 temperatures of examination. The studies of the stability of the γ -phase have yielded conflicting
92 results with different explanations as the following examples demonstrate.

93 In some studies low hydrogen concentrations, < 1.3 at.% (140 ppm), favoured the formation of
94 γ -hydride [9, 10, 11] in pure zirconium and in Zircaloy-4 [12]. In [10] above 0.89 at.% (98 ppm)
95 hydrogen, a mixture of δ -hydrides and γ -hydrides was observed, while below 0.19 at.% (21 ppm)
96 hydrogen, only γ -hydride could be detected. To test the stability of the hydride phases,
97 specimens with hydrogen concentrations of 0.19 at.% (21 ppm) and 0.89 at.% (98 ppm) were
98 heated to 200 °C for two weeks and furnace-cooled. Only γ -hydrides were observed, indicating
99 that the γ -phase had not transformed to the δ -phase but vice versa. Most of the hydrides were
100 precipitated within the grains since in this test material the grain size was 500 μm whereas in
101 [13], the grain size was about ten times smaller thus providing a large area of grain boundaries,
102 where δ -hydride was found. In [11], the specimens were re-examined after three years at room
103 temperature and the γ -hydride had not converted to δ -hydride.

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104 The elastic strain energies of the γ - and δ -hydrides were estimated to be 6.9 kJ/mol and
 105 8.4 kJ/mol, respectively, implying that the γ -phase is expected to nucleate first from solid
 106 solution [14]. If stress-relieving accommodation dislocations are formed around the precipitates,
 107 the total strain energy declines and depends on the yield strength of the material [15]. With low
 108 strength material, ratio of yield strength/shear modulus, σ_y/μ , of 0.001, the strain energies for
 109 each hydride phase are small, <0.45 kJ/mol, and about the same size so that once γ -hydride is
 110 nucleated it continues to grow [14]. In material with high strength, σ_y/μ , of 0.01, the strain
 111 energies increase but for δ -hydride the energy required is slightly smaller than for γ -hydride,
 112 2.4 kJ/mol to 2.5 kJ/mol. The analysis assumed an absence of any significant difference in
 113 chemical formation energy. Thus after slow cooling the δ -hydride was the expected phase in
 114 strong materials, except when the hydrogen concentration was less than 100 ppm. This analysis
 115 was used to explain the presence of γ -phase in zirconium with low oxygen concentration and
 116 δ -phase when oxygen was added to the same material [14].

117 In Zircaloy-2 with about 0.90 at.% (100 ppm) hydrogen in solution, the formation of γ -hydride
 118 by fast quenching was suppressed by increasing the strength by cold-work [16]. An alternative
 119 explanation to the local difference in volume expansion for the effect of strength is that for a
 120 given concentration of hydrogen, the lower H/Zr required by γ -hydride compared with δ -hydride
 121 provides a higher number density of precipitates, $N_f^\gamma > N_f^\delta$, therefore the total strain required is
 122 greater for γ -hydride than δ -hydride. If only γ -hydride formed, the total strain, ε_T^γ , would be
 123 ($N_f^\gamma \times 0.123$), whereas if only δ -hydride formed, the total strain, ε_T^δ , would be ($N_f^\delta \times 0.172/1.6$),
 124 that is, $N_f^\delta \times 0.108$, so $\varepsilon_T^\gamma > \varepsilon_T^\delta$, thus explaining the effect of strength. If hydride nucleation at
 125 dislocations from cold-work was the controlling process, precipitation of γ -hydride would be
 126 promoted but such an increase was not observed.

- 127 • When the cooling rate was varied from brine quenching to furnace cooling, the strength
 128 effect was not observed in Zr-2.5Nb [17, 16] when the β -phase was present, which
 129 provides hydride nucleation at α/β interfaces [18, 19]. With low concentrations of
 130 hydrogen, 0.06 at.% (7 ppm), only γ -hydride was precipitated, even with furnace cooling;
 131 with a moderate concentration, 0.42 at.% (46 ppm), γ -hydride was still observed with oil
 132 quenching but δ -hydride was detected after air cooling; a mixture of γ - and δ -hydrides
 133 was found after all coolings when the hydrogen concentration was 1.3 at.% (140 ppm);
 134 only δ -phase was observed with air cooling and furnace cooling with a hydrogen
 135 concentration of 2.7 at.% (300 ppm).
- 136 • With hydrogen concentrations of 1.8 at.% (200 ppm) and 4.4 at.% (500 ppm) in pure Zr,
 137 γ -hydrides from water quenching transformed almost completely to δ -hydride after aging
 138 at 200 °C for 3 weeks. Aging at 150 °C only partially converted the γ -hydride to δ -
 139 hydride after 3 weeks. After furnace cooling from the solution temperature only δ -
 140 hydrides were detected and these precipitates did not change with aging [20].
- 141 • Lanzani and Ruch [21] added between 1.56 at.% (174 ppm) and 12.15 at.% (1514 ppm)
 142 hydrogen to Zircaloy-4 by corrosion then subjected specimens to storage at room
 143 temperature for various hold times totalling 37 months, with an intermediate heating to
 144 148 °C for 2212 h. No γ -phase was detected by X-ray diffraction.
- 145 • Synchrotron evaluations at room temperature of Zircaloy containing up to 21.5 at.%
 146 (3000 ppm) hydrogen revealed mostly δ -hydrides, with traces of γ -hydride. ε -hydride

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- 147 was detected in hydride layers containing about 35 at.% (6 000 ppm) hydrogen on the
148 rim of cladding [22, 23].
- 149 • Specimens of pure Zr containing up to 60 at.% (16 000 ppm) contained a mixture of γ -
150 and δ -hydrides after cooling from the β -phase [24]. After furnace cooling the δ -hydride
151 dominated whereas after water quenching γ -hydride was prominent. After aging for 6.5
152 months at room temperature, in the water-quench materials, the volume of the γ -hydride
153 increased at the expense of the δ -hydride and approached ZrH at 50 at.% (11 000 ppm)
154 hydrogen. The stability of the γ -phase at room temperature was indicated by the
155 decoration of δ -hydride with γ -hydride in pure Zr containing 55.5 at.% (13 500 ppm)
156 hydrogen after holding for 174 days following a furnace cool from 500°C [25]; γ -hydride
157 in the matrix remained unchanged.
 - 158 • With high concentrations of hydrogen, 48 at.% to 60 at.% (10 000 ppm to 16 000 ppm),
159 the material mostly consisted of a mixture of γ -hydride and δ -hydride [24, 26, 27].
160 Heating to over 250 °C (523 K) converted all the γ -hydride to δ -hydride.
 - 161 • In Zircaloy-2 containing 0.9 at.% (100 ppm) hydrogen, electron energy loss spectroscopy
162 showed that the composition of a hydride could vary from ZrH at the tip to ZrH_{1.7} in the
163 core of the hydride [28].
 - 164 • No γ -hydride was observed in specimens of Zr-1.15Cr-0.1Fe containing 27.7 at.%
165 (4200 ppm) hydrogen [29]; heating for 2200 h at 220 °C – 20 °C below a suspected
166 transformation temperature – yielded no γ -hydride.

167
168 Studies of hydrogen in annealed Zircaloy using diffraction of X-rays from a synchrotron have
169 used the δ -phase to represent hydrides during temperature cycling [30, 31, 32]. These
170 experiments explored the solubility limits of hydrogen in Zr, the kinetics of hydride nucleation
171 and growth and the crystallographic features of reoriented hydrides. The common features of the
172 experiments are large hydrogen concentrations, 0.72 at.% to 5.2 at.% (80 ppm to 600 ppm), and
173 continuous temperature changes between 5 °C/s and around 10 °C/minute.

174
175 Neutron diffraction measurements have shown that the γ -phase is the stable hydride at room
176 temperature in the strong alloy Zr-2.5Nb. During heating of a specimen containing 0.783 at.%
177 (87 ppm) hydrogen isotopes, about 60% of the γ -phase signal was lost and δ -phase formed at
178 about 180 °C [33]. During cooling from well above this temperature the first phase detected was
179 δ -hydride. The formation of γ -hydride at room temperature was slow, with a characteristic time
180 scale of the order of months [34, 35]. As shown for hydrides in pure Zr [25], the γ -hydride
181 consumed the δ -hydride precipitate from outside-in, and after a further year of storage only a
182 small island of δ -hydride remains [35], Figure 1.

183 Although most phase diagrams omit the γ -phase, preferring to consider it a metastable phase,
184 some of the above results and observations suggest there is a transformation to γ -hydride at low
185 temperatures within the phase field between the $\alpha/(\alpha+\delta)$ and $(\alpha+\delta)/\delta$ boundaries with a
186 transformation temperature between 180 °C to 250 °C. Two studies showed that a difference in
187 strength could affect which hydride formed, either because their plastic strain energies were
188 similar [14] or because their composition determined their number density [16]. Atomic-scale
189 calculations of the properties of the Zr–H system [36, 37] indicate that the formation energies of
190 the hydrides are about 5 to 15 times larger than the strain energies and the difference between the
191 formation energies of γ - and δ -hydrides is 15% and 25%, with δ -hydrides being the more stable.
192 These results suggest that because of the modest differences between each of the contributions to

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193 the energies of the precipitation of the two hydrides, when embedded within the zirconium
194 matrix their relative stabilities may depend on mechanical and thermal contributions to their free
195 energies, modified by slight variations in composition and fabrication of the component.
196 Whether γ -hydride or δ -hydride or both are present in a material depends on the hydrogen
197 concentration, zirconium alloy composition and the thermomechanical treatments, and time at
198 the low temperature.

199 Terminal Solid Solubility

200 An alternative interpretation of 'Terminal Solid Solubility' (TSS) is presented in this paper. TSS
201 refers to the equilibrium phase boundary between hydrogen in solution in the metal, and
202 hydrogen in hydride. This equilibrium phase boundary is known as the solvus. In the standard
203 interpretation, this phase boundary is not unique because it depends on whether it is approached
204 by heating or cooling. Hence, 'equilibrium', in the standard interpretation of the solvus, is
205 meant in a 'restricted and dynamic' sense depending on whether the sample is heated or cooled:
206 the solvus where hydrides precipitate upon cooling is labeled TSSP, and the solvus where
207 hydrides dissolve upon heating is labeled TSSD.

208 The cooling-heating cycle often used to explain the standard interpretation is shown in Figure 2
209 along with representative TSSP (upper) and TSSD (lower) curves. The cooling-heating cycle
210 starts at Point A where all of the hydrogen is in solution (*i.e.*, Point A is below the TSSD
211 concentration and above the TSSD temperature). For this example, the total hydrogen
212 concentration is 1 at.% (110 ppm) and the starting temperature is 360 °C. As the alloy is cooled,
213 the hydrogen concentration in solution remains at 1 at.% (110 ppm) until Point B is reached.
214 During cooling from Point A to Point B, there is no observable effect of crossing the TSSD line -
215 the TSSD line is not apparent during cooling. Upon further cooling, hydrides can nucleate.
216 Once hydrides form, the concentration of hydrogen in solution follows the TSSP line as the alloy
217 is cooled to Point C. In the heating portion of the cycle, the alloy is first heated from Point C to
218 Point D. During heating the TSSP line is not apparent, but now the TSSD line is. On heating,
219 the solvus line is given by TSSD. Between Points C and D, the temperatures are below the
220 TSSD temperature and, hence, the concentration of hydrogen in solution does not change until
221 Point D, which is where the horizontal line between Points C and D intersects with the TSSD
222 curve. At Point D, the hydrides begin to dissolve with further heating, and the hydrogen
223 concentration in solution follows the TSSD line until Point E, which is where all the hydrides
224 have dissolved and where the concentration in solution is again 1 at.% (110 ppm). The
225 concentration of hydrogen in solution stays at 1 at.% (110 ppm) as the temperature is raised to
226 the starting value.

227 The standard interpretation is that the hydrogen concentration in solution is the lesser of [38, 39]:

- 228 • The total hydrogen content;
- 229 • The composition of the solvus for hydride dissolution during heating;
- 230 • The composition of the solvus for hydride precipitation during cooling.

231 In addition, when switching between cooling and heating there is a hiatus where the
232 concentration does not change because of a hysteresis [40], *i.e.*, the horizontal line between
233 Points C and D in Figure 2.

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234 In the standard interpretation, both TSSP and TSSD are solvus lines, and both represent
235 equilibrium conditions, albeit in the ‘restricted sense’ of while the temperature is changing -
236 cooling for TSSP and heating for TSSD. These solvus lines do not exist at the same time,
237 because you cannot cool and heat simultaneously, but they do exist at the same location. During
238 heating, all locations within the alloy see TSSD as the solvus, and during cooling all locations
239 see TSSP as the solvus. The shift of the solvus between TSSP and TSSD is called the hysteresis
240 [40], which is interpreted to mean that the concentration of hydrogen in solution for hydride
241 dissolution is less than for hydride precipitation, or, equivalently, the temperature for hydride
242 dissolution is greater than for hydride formation. The temperature hysteresis between hydride
243 precipitation, given by TSSP, and dissolution, given by TSSD, can be as large as 60 °C for the
244 same concentration, depending on which features of the experimental measurements are used to
245 indicate precipitation and dissolution.

246 For thermodynamic equilibrium, according to the Phase Rule, composition and temperature
247 cannot be changed independently for two phases to be present in a binary alloy. At the same
248 composition, hydrides should dissolve and precipitate at the same temperature independent of
249 heating or cooling. The presence of two values of the solubility limit suggests that one or both
250 the values do not represent equilibrium and the hysteresis and values are therefore indicated as
251 “apparent”. In dynamic measurements, values of apparent TSS by heating or cooling are clearly
252 distinguishable and reproducible even if strictly invalid as equilibrium values. They are of
253 practical use for evaluating reactor components and experiments.

254 Experimental Work:

255 Compact toughness specimens (2 mm thick, 10 mm square) were machined from a 20% cold-
256 worked and stress-relieved Zircaloy-2 pressure tube that was originally manufactured in the
257 1960s (Sn 1.47 wt.%, Fe 0.12 wt.%, Cr 0.11 wt.%, Ni 0.06 wt.%, O 1010 wt.ppm, H 12 wt.ppm,
258 balance Zr); the notch was not examined in this experiment. The microstructure comprised flat
259 α -grains with thickness of about 1 μm , elongated to about 10 μm in the axial and transverse
260 directions. The zirconium crystals had a preferred orientation with respect to the principal
261 directions of the tube, axial (A), radial (R) and transverse (T) directions, with Kearns’ factors
262 [41] for (0001) of $f_A = 0.046$, $f_R = 0.376$, and $f_T = 0.578$. Tensile properties of the Zircaloy-2
263 material were obtained in the transverse direction using ASTM Standard methods [42, 43]. The
264 yield strength was found to obey the empirical relation: $959 - 1.95T + 2.77 \times 10^{-3}T^2$ [MPa] for
265 temperatures, T(°C), between 100 °C and 350 °C.

266 Hydrogen was added gaseously to two Zircaloy-2 specimens to concentrations of 0.6 at.% and
267 1 at.%. A third reference specimen was fabricated, but without added hydrogen; its as-received
268 hydrogen concentration was 0.1 at.%. At the conclusion of the X-ray experiments described
269 below, each specimen was completely sectioned into six separate samples. Differential Scanning
270 Calorimetry (DSC) (TA Instruments) was used to measure the heat flow during heating and
271 cooling at 10 °C/min about the expected solvus values for each sample. Typical DSC curves for
272 the specimen with 1 at.% hydrogen in Zircaloy-2 are shown in Figure 3. The heat flow shows
273 the endothermic energy, interpreted as that required to dissolve hydrides on heating, passed
274 through a minimum at $315 \text{ °C} \pm 7 \text{ °C}$, and the onset of exothermic energy released, interpreted as
275 that emitted when hydrides precipitate on cooling, occurred at $278 \text{ °C} \pm 4 \text{ °C}$. Similar
276 measurements for the 0.6 at.% specimen showed the minimum heat flow on heating occurred at

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277 282.4 °C ± 2 °C, and the onset temperature on cooling was 255.3 °C ± 2 °C; the corresponding
278 temperatures for the 0.1 at.% specimen were 172 °C ± 9 °C and 141 °C ± 3 °C. The temperature
279 differences for dissolution and precipitation for these specimens range from 27 °C to 37 °C.
280 Reported DSC temperatures are averages and standard deviations determined from three runs for
281 each of the six sectioned samples of each specimen. Hydrogen concentrations were measured
282 with Hot Vacuum Extraction Mass Spectroscopy (HVEMS) [44]. The determined average
283 atomic percent concentrations and standard deviations for hydrogen were 1.02±0.04, 0.57±0.04,
284 and 0.11±0.03, corresponding to ppm by weight values 113±4, 63±4, and 12±3, respectively.

285 X-ray diffraction experiments were performed with the Advanced Photon Source Synchrotron at
286 Argonne National Laboratory on beamline 1-ID. The beam was calibrated with a ceria standard;
287 the wavelength was 14.42 pm; it was rectangular (200 μm x 50 μm) and incident normal to the
288 square surface of the specimen in the radial direction of the original tube. The transverse
289 direction of the original tube was vertical and the specimen was held stationary with a 10 N load
290 used to secure it in the load frame. The beam passed through the specimen sampling about
291 200 000 α-grains. The test temperatures were obtained with a furnace that surrounded the
292 specimens and grips, and the temperature was measured and controlled with a thermocouple spot
293 welded to the side of the specimen [45]. An illustration of the experimental arrangement is
294 shown in Figure 4.

295 Diffraction rings were collected on an amorphous silicon detector located 2 m behind the
296 specimen to magnify the region where γ- and δ-hydride signals are expected with d-spacings
297 between 0.26 nm and 0.28 nm corresponding to {111}. Figure 5 shows that the intensities of the
298 zirconium diffraction rings varied with angle around the ring because of the underlying
299 crystallographic texture of the zirconium lattice. The majority of basal-plane normals in the
300 specimens were aligned in the vertical direction, which is the transverse direction in the original
301 tube, and the prism plane normals were aligned horizontally. The major intensities of diffraction
302 from the zirconium (0002) were at the top (0°) and bottom (180°) of the diffraction rings.

303 Figure 6 shows room temperature zirconium metal diffraction peaks obtained by integrating the
304 intensity around the diffraction rings for the 0.1 at % (12 ppm) hydrogen specimen. Diffraction
305 lines associated with the basal (0002) plane and prism {10 $\bar{1}$ 0} plane are labeled in the spectrum;
306 for the diffraction pattern obtained at each location in the specimen, the intensity is normalized to
307 the strongest line, which is the pyramidal {10 $\bar{1}$ 1}. Zirconium metal has a hexagonal-close-
308 packed crystal structure with lattice parameters measured in this work at 25 °C: $a_0 = 0.323$ nm
309 and $c_0 = 0.515$ nm, as expected [46].

310 Hydrogen in solution expands the zirconium proportional to the concentration: for example, at
311 450 °C, 1 at.% hydrogen increased the a-lattice spacing by 1.13×10^{-4} nm and the c-lattice
312 spacing by 2.95×10^{-4} nm, providing an anisotropy factor of 2.61 [47]. Thus, changes in
313 zirconium lattice spacings are a measure of both changes in the concentration of hydrogen in
314 solution and thermal expansion.

315 Hydrogen can leave solution to form hydride phases in the zirconium lattice, and additional
316 peaks appear in the diffraction spectrum. In this work, hydride peaks were seen because of the
317 face-centered-cubic δ-phase, with a lattice parameter at room temperature of 0.478 nm [48, 49],

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318 and the γ -phase, which has a face-centred-tetragonal ($c/a > 1$) structure, and reported lattice
319 parameters at room temperature $a = 0.460$ nm and $c = 0.497$ nm [48, 49] and $a = 0.459$ nm and
320 $c = 0.495$ nm [50]. Consequently, at room temperature hydrides expand the zirconium lattice
321 locally by 12% to 17% [51, 52]. Figure 7 shows the region of the diffraction spectrum where
322 peaks associated with diffraction from $\{111\}$ planes of γ - and δ -hydrides can be found for the
323 three hydrogen concentrations of this study at room temperature. The d-spacing for the $\{111\}$
324 peaks calculated from the lattice parameters [53] are 0.276 nm for δ -hydrides, and 0.272 nm and
325 0.271 nm, respectively, for γ -hydrides. The d-spacings in Figure 7 are lower than these
326 calculated values because in this study the X-rays traverse the specimen so that the hydrides
327 diffracting the beam are in compression in the metal interior. X-ray diffraction patterns seen in
328 reflection have higher d-spacings from hydrides closer to the metal surface where any
329 compressive stress will be relieved. Similar low d-spacings of the $\{111\}$ δ -hydride peak in
330 Zircaloy-4 have been reported in another synchrotron transmission X-ray diffraction study [45].

331 The amounts of γ - and δ -hydride were determined by integrating the intensity of the diffraction
332 peaks from $\{111\}$ planes of each hydride phase around the circumference of the diffraction rings,
333 and in two angular ranges around the diffraction rings: 0° to 20° and 55° to 75° counterclockwise
334 from the top. The amounts of hydrides were assumed to be proportional to the areas of the
335 diffraction peaks.

336 Diffraction spectra were obtained under isothermal conditions at temperature intervals between
337 room temperature and 330°C . The specimens were heated and cooled at $10^\circ\text{C}/\text{min}$ between
338 temperature intervals of 10°C or 5°C between 200°C and 330°C , followed by an isothermal
339 hold of 3 minutes before spectra were collected every 0.5 s for 18 s. The isothermal hold
340 facilitates both thermal equilibrium and equilibrium between hydrogen in solution and hydrides,
341 but equilibrium is not required to interpret these isothermal diffraction spectra with dynamic
342 DSC heat flow measurements. The data obtained during cooling were gathered after the data
343 obtained during heating, which included annealing at 550°C for an hour that ensured all of the
344 hydrides were dissolved.

345 Theory:

346 The Einstein relation for Brownian motion [7] is used to describe diffusion when velocities of
347 particles are limited to terminal values, such as ions moving in liquids under applied electric
348 potential gradients (*i.e.*, Nernst-Einstein equation), particles moving in viscous liquids under
349 gravitational potential gradients (*i.e.*, Stokes-Einstein equation) and the drift current in
350 semiconductors. Solute atoms moving in solid solutions reach terminal velocities, v , that are
351 proportional to forces derived from negative gradients in chemical potential: $v = -\Gamma \nabla \mu$. The
352 proportionality constant is the mobility, Γ . The chemical potential is written using the definition
353 of relative activity of the solute, a , via $\mu = \mu^\circ + RT \ln a$, where T is temperature in K, R is the
354 Ideal Gas Constant, 8.314 J/mol.K, and μ° is a reference state for the chemical potential [54].
355 The activity is approximated by concentration, C , in the limit of ideal dilute solute, which will be
356 assumed in accord with the solute (hydrogen) in the solid solvent (zirconium) being less than
357 1 at.% in this study. The chemical potential includes an additional term to account for the work
358 done to expand the solvent (e.g. by the solute), so that regions of tension lower the chemical
359 potential; this work is the product of the hydrostatic pressure, σ , and the partial molar volume, V ,
360 of the solute. The flux of solute, J , is the product of the velocity and the concentration. The flux

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361 reduces to the empirical equation of Fick [55] when there are no temperature or stress gradients
 362 (*i.e.*, $J = -D\nabla C$, which defines the diffusion constant, D); the equivalence of the flux and Fick's
 363 equation leads to the Einstein relation between the mobility and the diffusivity: $\Gamma = D/RT$. Thus,
 364 Fick's Law is derived from the chemical potential. Inserting the gradient of the chemical
 365 potential into the equation for the velocity, multiplying by the concentration to give the flux, and
 366 substituting the Einstein relation for the mobility, yields the Einstein flux in a hydrostatic stress
 367 gradient at constant temperature in terms of the diffusivity [8]:

$$368 \quad J = -D(\nabla C + \frac{CV}{RT} \nabla \sigma). \quad (3)$$

369 The flux of solute atoms, J , contains a diffusion current, which depends on concentration
 370 gradients as in Fick's Law, and a drift current, which depends on stress gradients. Equilibrium is
 371 defined when the chemical potential of hydrogen is the same in all phases, which is equivalent to
 372 $J = 0$. Equilibrium is temperature dependent because the drift current and diffusivity both vary
 373 with temperature.

374 The simple no-flux solution to Equation 3 is for no gradients in concentration and stress. This
 375 solution can be used to define the solvus, which is a unique temperature and concentration of
 376 hydrogen in solid solution in dynamic equilibrium with hydrogen at a hydride surface in the
 377 volume adjacent to the surface in the limit where any stress gradients are zero. Similar
 378 approaches are used to truncate the stresses at the tip of a sharp crack, which defines an event
 379 horizon to avoid a singularity [56, 57]. The hydrides that form will be under compression, and
 380 the adjacent metal lattice will be under tension. Between these regions of compression and
 381 tension is the neutral stress region, where the stress gradient is zero, and, by Equation 3, where
 382 there will be no concentration gradient at equilibrium. These two conditions define the solvus in
 383 terms of the concentration of hydrogen in solution in the volume adjacent to the hydride surface
 384 in the limit where any stress gradients are zero.

385 Consider cooling gradient-free zirconium alloy containing hydrogen completely in solution. Just
 386 before precipitation there are no concentration gradients, and there are no stress gradients
 387 associated with matrix hydrides, because there are none. The onset of precipitation will be used
 388 to approximate the temperature for the no-gradients condition that defines the solvus temperature
 389 associated with only one concentration. This concentration is the solvus, or the terminal solid
 390 solubility, C_{TSS} . This value was used to predict the maximum in delayed hydride cracking
 391 growth rates in zirconium alloys [8] and will be used to explain the observations of this work.

392 Additional no-flux solutions to Equation 3 occur when the two gradient terms are equal and
 393 opposite. Thermal fluctuations can lead to transient local concentration gradients in embryonic
 394 condensations of hydrogen clouds, and accompanying stress gradients because of the hydrostatic
 395 stress from the hydrogen atoms, but these structures will be dissipated by thermal agitation until
 396 hydrides form. When hydrides are present, stress gradients will form as the metal is expanded
 397 because of the larger volume of metal hydrides compared with the metal. Stable stress gradients
 398 also form in response to internal defects and external loads. When stable hydrides are present,
 399 there will be regions where local concentrations are stabilized at the solvus concentration;
 400 concentration gradients within the hydrogen clouds will terminate with the solubility limit.
 401 Equilibrium concentrations of hydrogen in solution in the presence of hydrides and stress

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402 gradients are determined by setting the flux of hydrogen in Equation 3 to zero and integrating
403 with one concentration limit equal to C_{TSS} . There are two possibilities:

$$404 \quad \int_{C_-}^{C_{TSS}} \left(\frac{\nabla C}{C} \right) = -\int \frac{V \nabla \sigma}{RT}; \quad \int_{C_{TSS}}^{C_+} \left(\frac{\nabla C}{C} \right) = -\int \frac{V \nabla \sigma}{RT}. \quad (4)$$

405 At these limits, the difference in hydrostatic stress is negatively proportional to the yield stress,
406 σ_y , for tensile stress gradients. The proportionality constant is the elastic stress concentration
407 factor, K , which is expected to vary between 1 and 2.4, the latter being the value in the plain-
408 strain limit, appropriate for needle-like γ -hydrides, in a lattice that deforms in a perfectly plastic
409 manner [56-59]. The two solutions for tension depend on the ordering of the integration limits:

$$410 \quad C_-(T) = C_{TSS}(T) \exp\left(\frac{-KV\sigma_y}{RT}\right); \quad (5)$$

$$411 \quad C_+(T) = C_{TSS}(T) \exp\left(\frac{+KV\sigma_y}{RT}\right). \quad (6)$$

412 Different values of K may be possible for different internal defects, for example, dislocations,
413 that give rise to local gradients in hydrostatic stress seen by the solute. For example, Equations 5
414 and 6 are plotted in Figure 8 for $K = 2$.

415 Equation 5 corresponds to when the hydrogen concentration in solution equals C_{TSS} at the stress
416 riser and C_- in the neighbouring matrix, which first happens at T_+ when cooling from a
417 temperature where all the hydrogen is in solution (Figure 8). The hydrogen flux also equals zero
418 when the hydrogen concentration in solution equals C_{TSS} at the stress riser and C_+ in the
419 neighbouring matrix. At temperature T_- shown in Figure 8, the concentration of hydrogen in
420 solution in the matrix neighbouring the stress riser equals the total hydrogen concentration. The
421 hydrogen in solution in the matrix neighbouring the stress riser can form equilibria with
422 subsequent neighbouring regions when the concentrations satisfy $J = 0$. For concentrations and
423 temperatures bounded by the expressions for C_+ and C_- , the flux of hydrogen, J , is negative and
424 hydrogen moves from the surrounding matrix to the hydride, otherwise J is positive and the
425 hydrides lose hydrogen to the solution. Thus, hydrides are predicted to be stabilized against
426 dissolution above the solvus temperature until T_+ , and destabilized and dissolve below T_- . The
427 drift current directed towards tensile stresses emanating from lattice imperfections such as
428 dislocations or from hydrides already formed, can inhibit dissolution, which can lead to hydride
429 precipitation above the phase boundary, and hydride dissolution below the phase boundary.
430 These solutions given by Equations 5 and 6 do not yield a solvus, by definition, because the
431 concentration of hydrogen in solution is not unique due to the concentration gradient.
432 Concentration varies with location, notably one concentration at the stress riser and a second
433 concentration far-field in the matrix.

434 Equation 5 has been proposed before to explain how delayed hydride cracking can occur above
435 the solvus on cooling from temperatures where all of the hydrogen is in solution: hydrides are
436 stabilized at the crack tip by the drift current once T_+ is reached (see Figure 6 in [8] where T_+ is
437 called T_5). Equation 6 is proposed in this work to represent the concentration of a hydrogen

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438 cloud formed at a stress concentration or a Cottrell atmosphere of hydrogen in solution at a
439 dislocation [60]. The concentration in the hydrogen cloud or Cottrell atmosphere can be higher
440 than the solvus concentration when it is stabilized by the drift current, and can be destabilized for
441 concentrations and temperatures above the line for C_+ , Equation 6.

442 Results:

443 The areas of hydride diffraction peaks were found to increase as hydrides precipitated and
444 decrease as hydrides dissolved, and spacings of the zirconium lattice were found to expand and
445 contract in accord with hydrogen moving in and out of solution. Figure 9 shows the areas of
446 hydride peak intensities integrated around the circumference of the diffraction ring for the
447 specimen with 1 at.% hydrogen, (113±4) ppm. On cooling from a temperature where all of the
448 hydrogen is in solution (370 °C), γ -hydride diffraction peaks were observed at 330 °C. The area
449 of these γ -hydride diffraction peaks decreased to a minimum value at ≈ 315 °C, coincident with
450 the minimum heat-flow temperature on heating shown in Figure 3, and T_+ . With further cooling,
451 the areas of the γ -hydride diffraction peaks increased as the temperature was lowered past the
452 onset of precipitation temperature (*i.e.*, the solvus or TSS: 280 °C, Figure 3), and reached a
453 maximum value at ≈ 245 °C, which is coincident with T_- . (The calculation of T_+ and T_- is
454 described in the Discussion.) δ -hydrides were not observed during cooling until 230 °C. On
455 heating, γ -hydride peak intensities integrated around the ring were not discernible from the
456 variability in the background. The areas of δ -hydride peak intensities integrated around the ring
457 were seen to rise with heating to a maximum value at 230 °C, and then fall with further heating.
458 For temperatures above 280 °C, the δ -hydride peaks were not distinguishable from the variability
459 in the background.

460 The large intensities of adjacent zirconium diffraction peaks makes it difficult to see small
461 hydride peaks. This large confounding background can be reduced with a judicious choice of
462 viewing angles for the hydrides between the regions where the texture makes the zirconium lines
463 intense. The hydrides can be seen relatively free of zirconium interference between 0° to 20° and
464 55° to 75° from the top of the diffraction rings.

465 Figure 10 shows stacked plots of integrated intensity from 0° to 20° and 55° to 75°, from the top
466 of the diffraction rings, obtained with the specimen containing 1 at.% hydrogen for a series of
467 isothermal measurements made at progressively higher temperature in the region where γ - and
468 δ -hydride peaks are found. The temperatures of the stacked spectra range from 220 °C to 310 °C
469 (top to bottom) in steps of +10 °C, with each spectrum offset vertically from the low temperature
470 spectrum. Both the γ - and δ -hydride peaks persisted to temperatures above the onset
471 precipitation temperature, and disappeared when the temperature reached the minimum
472 heat-flow temperature determined during heating with DSC.

473 Figure 11 shows stacked plots of diffraction spectra obtained with the specimen containing
474 1 at.% H for a series of isothermal measurements made at progressively lower temperature. The
475 temperatures of the stacked spectra range from 330 °C to 230 °C (top to bottom) in steps
476 of -5 °C, with each spectrum offset vertically from the low temperature spectrum. Prior to these
477 measurements the specimen was heated to 550 °C for an hour to ensure all of the hydrides were
478 dissolved. Figure 11 shows the integrated intensity from 0° to 20° and 55° to 75° from the top of
479 the diffraction rings. Common to both views in these figures, there is no indication of δ -hydride

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480 until the lowest temperature of 230 °C is reached. In both angular views, the γ -hydride peak seen
481 at the starting temperature, 330 °C, decreases as the temperature is lowered to ≈ 315 °C, then rises
482 to a maximum value at an intermediate temperature that depends on the view, before falling
483 again as the temperature is lowered to 230 °C.

484 Figure 12 shows stacked plots of diffraction spectra obtained with the 0.6 at.% H specimen for a
485 series of isothermal measurements made at progressively lower temperature. The temperatures
486 of the stacked spectra range from 300 °C to 200 °C (top to bottom) in steps of -5 °C, with each
487 spectrum offset vertically from the low temperature spectrum. Prior to these measurements the
488 specimen was heated to 550 °C for an hour to ensure all of the hydrides were dissolved.
489 Figure 12 shows the integrated intensity from 0° to 20° and 55° to 75° from the top of the
490 diffraction rings. There is no indication of δ -hydride on cooling until 205 °C. The γ -hydride
491 peak in the 0° to 20° view is first seen on cooling at 280 °C; the peak grows reaching a maximum
492 value on further cooling, and then disappears by ≈ 235 °C. Compared with the specimen
493 containing 1 at.% H, for the 0.6 at.% H specimen there is no indication of γ -hydride in the 55° to
494 75° view, outside of the limits inferred for the background, and, in the 0° to 20° view, signals
495 associated with δ -hydrides at low temperatures are difficult to distinguish from the background.

496 The diffraction lines for 0.6 at.% H in Zircaloy-2 shown in Figure 12 confirm features seen in
497 Figure 11 for 1 at.% H: on cooling, γ -hydrides are seen to form above the DSC onset
498 precipitation temperature in the 0° to 20° view; the diffraction lines associated with these
499 γ -hydrides grow reaching maximum values below the onset precipitation temperature, and then
500 decline, and disappear in the 0.6 at.% H specimen, before δ -hydrides are seen in both views,
501 which happens 50 °C below the onset precipitation temperature.

502 Figure 13 shows how the areas under the diffraction peaks from {111} planes of the γ -hydrides
503 and δ -hydrides (subsequently called area) vary with temperature during cool-down, and heat-up
504 for the specimen with 1 at.% H. These plots show qualitatively how the amounts of various
505 hydrides change as they precipitate and dissolve at various temperatures. The areas of the
506 γ -hydride lines on cooling have been normalized to their maximum values on cooling, and the
507 areas of δ -hydride lines on heating are normalized to their maximum values on heating.

508 The d-spacings for the $\{10\bar{1}0\}$ and (0002) alpha zirconium lines, with thermal expansion
509 subtracted, determined from the specimen containing 0.1 at.% H, are depicted in Figure 14.
510 These plots corroborate hydrogen moving into and out of solution; d-spacings increase or
511 decrease when hydrogen moves into or out of solution. In both plots, the values were raised and
512 lowered so that the high temperature results overlapped. The values after cooling were lower
513 than those for heating presumably because of the stress relief within the specimen after the
514 550 °C heat-treatment. Similar results were seen for the zirconium lines of the specimen
515 containing 0.6 at.%. The cooling results for the specimen containing 1 at.% H are discussed
516 first.

517 Figure 13a shows that on cooling from temperatures where all of the hydrogen is in solution,
518 γ -hydride diffraction lines are observed to form above the temperature of minimum endothermic
519 heat-flow seen on heating (315 °C; Figure 3), and at both diffraction-ring viewing ranges
520 between 55° and 75° and between 0° and 20° from the top of the diffraction ring. These
521 γ -hydrides are clearly visible in the diffraction data, appear to be transient and they do not appear
522 to contribute to the heat flow measured with DSC during cooling (Figure 3). The hydrides

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523 diffracting between 0° and 20° grow below 315°C and, because they continue not to contribute
524 to the heat flow, at least until 280°C , they are labeled with the superscript 'a' to connote that
525 these hydrides are apparently athermal.

526 On cooling a further 35°C , at diffraction-ring angles between 55° and 75° , γ -hydride diffraction
527 lines again become visible at the temperature of the first indication, or onset (TSS), of
528 exothermic heat flow observed in the DSC experiment (280°C , Figure 3) and continue to grow
529 on cooling; they are called 'thermal' γ -hydrides, and labelled γ^t , even though these hydrides were
530 apparently athermal for temperatures above 315°C for the isothermal X-ray diffraction
531 measurements shown in Figure 13a.

532 The different diffraction-ring angles where γ^a and γ^t are observed suggests these hydrides
533 precipitate on different planes in the textured zirconium matrix. Although the amount of
534 γ^a -hydride might appear to be large in Figure 13a, recall that these areas have been normalized,
535 and the intensities in the angular collection ranges are not necessarily similar. The amount of
536 hydrogen leaving solution inferred from the changes in zirconium lattice spacings integrated
537 around the ring shown in Figure 14 provides a better indication of the relative amounts of γ^a and
538 γ^t for the measurement temperatures. The amount of γ^a -hydride should provide an exothermic
539 signal but it is too small to resolve with the current DSC instrument.

540 On further cooling, γ^a and γ^t precipitation reaches maximum amounts at 260°C and at 245°C ,
541 respectively. On still further cooling, the areas for these γ -hydrides decrease. These hydrides are
542 dissolving and hydrogen is going into solution as indicated by the increase in zirconium lattice
543 parameter in Figure 14 starting at 250°C . The γ -hydrides dissolve at temperatures above where
544 δ -hydrides appear suddenly at 230°C in both viewing angles (Figure 13a). The sudden
545 appearance of δ -hydrides is shown in Figure 15 by the time-dependent growth of the δ'' -hydride
546 peak between 55° and 75° ; the γ^t -phase peak decreases over the same time. Unlike the decline of
547 the γ^t -phase, the increase in δ'' -phase did not reach equilibrium in the 18 s observation time,
548 which occurred after cooling from 235°C to 230°C , at $10^\circ\text{C}/\text{min}$, and then waiting for 3 min
549 (Figure 16). The α -phase lattice parameter declined when the specimen was cooled from 235°C
550 to 230°C (Figure 14), but it remained constant over the 18 s observation time of Figures 15 and
551 16, which suggests prior hydrogen accumulation in the regions where δ -hydride precipitated. No
552 extra heat was detected by DSC at the temperature where the δ -phase started to precipitate
553 between 235°C and 230°C , Figure 3.

554 Figure 13b shows that on heating from 220°C , the γ^t -hydride areas increase as the temperature is
555 increased (thus hydrides are forming), reaching a maximum around 265°C , and then dropping to
556 a low value at $\approx 280^\circ\text{C}$. The δ' -hydride areas increase until 240°C (these hydrides are also
557 forming during heating), but then dissolve and are gone by $\approx 315^\circ\text{C}$. The δ'' -hydride areas
558 decrease monotonically with heating. The γ^a -hydride areas are difficult to quantify in Figure 10
559 (bottom plot): although the peak intensities are changing, with the peak widths increasing above
560 $\approx 280^\circ\text{C}$, the peak areas seem almost constant over the temperature range. Figure 14 shows that
561 the d-spacings of the zirconium lines increase monotonically with increase in temperature: there
562 is no hiatus.

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563 Discussion

564 The T_{\pm} temperature limits shown in Figures 9, 13 and 14 were calculated with the temperature
 565 dependence of the solvus (TSSP in [61]), the partial molar volume of hydrogen [45], and the
 566 yield strength determined in this work. For the current solvus (TSS) temperature, which is equal
 567 to the DSC onset temperature for precipitation on cooling (280 °C, Figure 3), the calculated
 568 plain-strain perfectly-plastic upper limit for T_{+} is 320 °C, which agrees well with the temperature
 569 where hydrides disappear on heating, and γ^{α} -hydrides appear on cooling, ≈ 315 °C (Figure 13).

570 The plain-strain perfectly-plastic lower limit for T_{-} is calculated to be 237 °C. Experimentally
 571 the temperature where the γ^{β} -hydrides dissolve (Figure 13a) and hydrogen goes into solution
 572 (Figure 14) is between 245 °C and 250 °C. If instead the K factor multiplying the yield stress is
 573 reduced from the plain-strain perfectly-plastic value of 2.4 to 2.0, then T_{+} becomes 314 °C and T_{-}
 574 becomes 245 °C, which agree with the observed experimental temperatures; these temperatures
 575 are indicated as vertical lines in Figures 9, 13 and 14. Equations 5 and 6 are plotted in idealized
 576 form in Figure 8 along with the T_{\pm} temperature limits calculated with $K = 2$. Crack-tip stresses in
 577 the plain strain limit have been characterized with similar values of multiples of the yield stress
 578 [63] suggesting that the stress fields around hydrides are similar to those found at crack tips in
 579 plain strain. Figure 8 indicates the regions where the flux of hydrogen is initially positive
 580 (leading to hydride dissolution) or negative (leading to hydride formation) during heating and
 581 cooling when hydrides are present or can form given time – these positive and negative fluxes
 582 are not general, they correspond to specific examples described below. An example where the
 583 initial flux designations in Figure 8 would not apply is for temperatures well above T_{+} , where the
 584 initial flux will be negative and hydrogen will flow to regions of tension, but no stable hydrides
 585 would form. Eventually, the flux would go to zero when equilibrium is achieved. Hydrogen
 586 concentration gradients without precipitates have been observed in zirconium bars subjected to
 587 bending stresses [62].

588 Hydride precipitation and dissolution during cooling and heating is controlled by the
 589 concentrations C_{+} , C_{TSS} , and C_{-} . At a constant temperature, equilibrium is when the
 590 concentration of hydrogen in solution at the hydride surface is C_{TSS} and surrounding layers have
 591 concentrations of C_{+} , C_{TSS} , or C_{-} (i.e., $J = 0$). When the temperature first changes during heating
 592 or cooling, the local concentrations do not change instantly, which on Figure 8 would be
 593 represented by moving concentrations along horizontal lines, so the concentrations C_{+} and C_{-}
 594 that were present at the equilibrium temperature will move either into regions where $J > 0$ or
 595 $J < 0$. For cooling, the initial C_{-} moves into a $J < 0$ region and is stabilized. The initial C_{+}
 596 concentration moves into a $J > 0$ region and would dissolve except for the stress has been
 597 relieved by the influx of hydrogen forming a hydrogen cloud. This initial state is stable on
 598 cooling until the initial C_{TSS} intersects with the C_{+} line, demonstrated with the top horizontal line
 599 in Figure 8; this intersection happens at the TSS (solvus) temperature. The initially formed
 600 hydrides dissolve at this point, and new hydrides appear in unstressed regions of the matrix.
 601 These events are ultimately controlled by the C_{+} line.

602 For heating from an initial equilibrium state, the reverse happens, and the events are ultimately
 603 controlled by the C_{-} line. When heating from an initial equilibrium, C_{-} moves into a $J > 0$ region
 604 and dissolution occurs. Heating moves C_{+} into a $J < 0$ region, and the C_{+} concentration grows

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605 because the stress gradient diminishes, perhaps reaching sufficient values for condensation of
606 hydrogen. This initial state is stable on heating until the initial C_{TSS} intersects with the C_- line.

607 On cooling: hydrides can form and dissolve

608 It follows that the first hydrides to form on cooling, the athermal γ^a -hydrides, must be
609 precipitating in regions where there are prior stress gradients and concentration gradients,
610 because they form above the solvus temperature. We propose that hydrides observed below
611 315 °C between 0° and 20° around the diffraction ring are associated with dislocations. Hydrides
612 are suggested to form when hydrogen trapped by tensile stresses at crystal imperfections (e.g.
613 dislocations) attain concentrations sufficient to precipitate hydrides. Metals contain
614 imperfections in the lattice that produce local tensile stress gradients, and there are many sites of
615 residual stresses, for example from intergranular differential thermal expansion, that will
616 encourage hydrogen to flow and form precipitates in the same way as to a crack tip under an
617 applied tensile stress [8]. The internal stresses would activate the drift current and promote
618 precipitation above the solvus temperature, hence γ^a -hydrides are predicted.

619 Figure 17 shows hydrides decorating dislocations is possible. The precipitates form well above
620 the onset temperature in Figure 3 and appear to be athermal. If kinetic energy of the hydrogen is
621 lost when associating with the imperfection, then the chemical energy released might appear to
622 be small. The aggregation of hydrogen atoms in the tensile region relieves hydrostatic stresses
623 when the elastic dilation caused by the dislocation has been replaced by the dilation associated
624 with the different atomic volumes of solute and solvent: Cottrell atmosphere [60].

625 When hydrides form, the concentration of hydrogen in solution at the hydride edge will be at the
626 solubility limit, C_{TSS} , for the formation temperature. Hydride formation introduces additional
627 stress and further hydrogen movement to form an additional hydrogen cloud with concentration
628 C_+ that surrounds the region at C_{TSS} . As the temperature is lowered, hydride growth is stunted:
629 initially hydrogen moves towards the hydride because $J < 0$, until the additional stress associated
630 with the hydride is relieved, at which point $J = 0$ and there is no hydrogen flux to grow the
631 hydride. These hydrides once formed do not grow when cooled, until a temperature is reached
632 where $J > 0$ at the periphery of the second hydrogen cloud so that the hydrogen in solution
633 trapped at the hydride edge can diffuse away and the hydride will dissolve. A consequence of
634 hydrides being unable to grow when cooled is that they form into arrays of platelets, which are
635 discussed later.

636 The γ^a -hydrides that form above the solvus temperature are predicted to dissolve in the order
637 they were formed as the temperature is lowered below the solvus temperature, and be gone by T_- .
638 The result is that a maximum amount of γ^a -hydrides should be seen between the solvus
639 temperature and T_- . The sequence of events is depicted in Figure 8. γ^a -hydrides that form above
640 the solvus temperature will decline following C_+ below the solvus (seen as the intersection of the
641 horizontal grey lines with C_+). The γ^a -hydrides that form below the solvus temperature will
642 increase with cooling as do the vertical grey lines seen in Figure 8 below the solvus. The net
643 difference predicts a maximum hydride diffraction peak area at 260 °C, which agrees with the
644 observed maximum temperature.

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645 On further cooling below T_+ , and to the left of the (C_+ , $J=0$) line in Figure 8, the flux becomes
646 positive and hydrides dissolve. In Figure 13a, around 250 °C, we see the areas for γ^t -hydrides
647 decreasing, and in Figure 14 the zirconium lattice-spacing increasing, which confirms the
648 hydrides are dissolving during cooling and hydrogen is going into solution. The γ^t -hydrides
649 continue to dissolve, and a peak is seen in zirconium lattice spacing at a temperature below T_+ .
650 Then formation of δ -hydrides intervenes. The γ -hydrides cannot simply transform to δ -hydrides;
651 the large stoichiometry difference has to be overcome and there is not enough hydrogen in the
652 (ZrH) γ -hydrides to form (ZrH_{1.5-1.67}) δ -hydrides. The γ -hydrides would have to collapse to a
653 smaller volume while rearranging hydrogen bonding if the δ -hydrides were formed strictly from
654 solid-state conversion of γ -hydrides. In addition, if γ -hydrides were transforming into δ -hydrides
655 by solid-state conversion, the rates of change of the areas of hydride diffraction peaks would sum
656 to zero. Figure 16 shows that during the 18 s observation period after the cooldown to 230 °C
657 and hold, the γ -hydride signal remains almost constant after ≈ 10 s while the area of the δ -hydride
658 peak continues to grow, hence, solid-state conversion is not supported by the time dependence of
659 the hydride diffraction signals.

660 Instead, the γ -hydrides dissolve putting hydrogen into solution, including into the surrounding
661 hydrogen cloud and into the metal matrix. This hydrogen is available when the higher
662 stoichiometric δ -hydrides form as the temperature reaches 230 °C for the specimen containing
663 1 at.% H. The ratios of C_+ to C_{TSS} calculated from Equation 6 vary from 1.6 to 1.7 as the
664 temperature is reduced from 280 °C to 230 °C provide the range of stoichiometry for the
665 δ -hydride. The concentration of hydrogen in solution drops suddenly as the δ -hydride forms, as
666 demonstrated by the last of the cooling points in Figure 14 showing the decrease in lattice
667 parameter for the zirconium lines between 235 °C to 230 °C, and the sequential growth of the
668 δ -hydride peaks shown in Figure 15 and Figure 16. Consistent with hydrogen condensing from
669 the local hydrogen cloud, there was no further movement of the zirconium diffraction lines
670 during the sequential growth showing that the required amount of hydrogen in solution had
671 already moved to the regions where the δ -hydride formed in the time between the start of cooling
672 from 235 °C and the start of the measurement at 230 °C. The amounts of γ -hydride and
673 δ -hydride may vary in this concerted way with further cooling.

674 In the specimen with 0.6 at.% H, on cooling, δ -hydrides were observed to form suddenly well
675 below the solvus temperature in a similar manner as observed for the specimen with 1 at.% H.
676 Figure 12 shows the process seen for 1 at.% H is repeated in the specimen with 0.6 at.% H,
677 except the formation of δ -hydrides occurs at 205 °C. The lower temperature (205 °C versus
678 230 °C) is in accord with the lower solvus temperature (255.3 °C \pm 2 °C versus 278 °C \pm 4 °C)
679 because of the lower concentration (0.6 at.% H versus 1 at.% H) in the specimen. For both
680 specimens, γ -hydrides formed above the solvus temperature on cooling, and then on further
681 cooling δ -hydrides formed 50 °C below the solvus temperature after γ -hydrides dissolved. For
682 both specimens, hydrogen moving in and out of solution was corroborated by the change in
683 d-spacings observed for the zirconium lines.

684 Figure 7 shows that the room-temperature proportions of γ -hydride and δ -hydride in the
685 Zircaloy-2 specimens of this study changed in a similar manner as reported for low hydrogen
686 concentrations in pure zirconium [9, 10, 11] and in Zircaloy-4 [12] and in Zr-2.5Nb [16-19] (See
687 the background in the Introduction). At low concentrations, 0.1 at.% H, only γ -hydrides were

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688 observed. For 0.6 at.% H and 1 at.% H, both γ -hydrides and δ -hydrides were observed, with a
689 greater proportion of δ -hydrides for the larger total hydrogen concentration. The areas of the
690 γ -hydride peaks are similar for the three concentrations. If the events leading to the precipitation
691 of δ -hydrides seen in Figures 11, 12, 13 and 14 can serve as a template, then hydride formation
692 starts with γ -hydride precipitation, and follows with dissolution of some γ -hydrides at
693 temperatures below the solubility limit, and then δ -hydrides precipitate below T_- . The
694 dissolution of γ -hydrides will take longer for lower total concentrations of hydrogen because the
695 diffusion rates are lower because the temperatures are lower. The preponderance of γ -hydrides at
696 low temperatures for low total hydrogen concentrations could result from insufficient time for
697 the γ -hydrides to dissolve so that δ -hydrides can precipitate, for example, during an experiment.
698 For higher total hydrogen concentrations, for which temperatures are also higher, the diffusion
699 times will be shorter. The implication is that γ -hydrides are expected to dominate for low
700 concentrations, and δ -hydrides dominate for high concentrations, in specimens with similar
701 cooling when compared at room temperature.

702 The decreasing and then increasing of the lattice spacings in Figure 14 during cooling, and then
703 the drop once δ -hydrides precipitate shows that the concentration of hydrogen in solution below
704 onset precipitation temperatures cannot be captured with a simple universal function (e.g.
705 exponential). For instance, specimens with low total hydrogen concentrations need to be cooled
706 to low temperatures to instigate precipitation, but diffusion is slow at low temperature, and
707 precipitation of δ -hydrides might be indeterminately delayed. Hence, the concentration of
708 hydrogen in solution could be higher than expected from extrapolation of TSS precipitation onset
709 values determined with DSC at higher temperatures. A disproportionately small, or absent,
710 δ -hydride peak could indicate hydrogen frozen in solution. The implication is that models of
711 phenomena that depend on the concentration of hydrogen in solution, such as delayed hydride
712 cracking [8], could under-predict rates at low temperatures and low concentrations. There are
713 indications that TSSP features change with temperature history [64], seemingly suggesting
714 complicated precipitation, whereas the current results show both precipitation and dissolution
715 behaviour, Figures 13 and 14. In contrast, experimentally determined TSSD concentrations vary
716 smoothly with temperature on heating, like the lattice spacings for the zirconium lines in
717 Figure 14.

718 Figure 13 show hydrides on cooling above T_+ , for reasons that are not yet clear. The zirconium
719 lattice contracts when cooled squeezing hydrogen into regions of relative tension where the
720 concentration could locally exceed C_- , even though the average concentration would not. Thus,
721 a second 'rainbow' line (C_-) could be defined below C_- . Similarly, hydrides above T_+ also
722 suggests additional no-flux conditions with different values for K . Regions of compression will
723 likewise lead to no-flux equations like those for tension (Equation 4). Compressive yield
724 strengths can be higher than tensile yield strengths, and could be different depending on direction
725 for a textured matrix.

726 On heating: hydrides can dissolve and precipitate

727 Figure 13b shows the areas of δ' -hydride diffraction peaks decrease as the temperature is raised;
728 hydrides in this view were previously labelled thermal. The areas of δ' -hydride diffraction peaks
729 increased with heating from 220 °C, and reached a maximum at ≈ 240 °C. Figure 8 suggests the
730 maximum should occur at 250 °C, which is the temperature where a horizontal line from TSS at

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731 220 °C intersects the C_+ line. δ' -hydrides are seen in the view associated with imperfections such
732 as dislocations. When heating first starts, the simultaneous increase of δ' -hydride and decrease
733 of δ'' -hydride combine to reduce the rate of increase of the amount of hydrogen entering
734 solution, and a slow rise in d-spacings is seen initially in Figure 14 reminiscent of the horizontal
735 line connecting Points C and D in Figure 2.

736 Figure 9 shows that on heating the total δ -hydride signal increases with temperature until 230 °C,
737 which suggests that the increase for δ' -hydride is larger than the decrease for δ'' -hydride over this
738 initial heating range. Simultaneously, the hydrogen concentration in solution increases with
739 heating, as shown by the rise in the d-spacings of the α -zirconium lines in Figure 14. Because
740 the total amount of hydrogen in solution and as hydride is constant, the implication is that the
741 γ -hydride phase must be suppressed when the total δ -hydride phase reaches a maximum value.
742 When the total δ -hydride signal decreases above ≈ 240 °C, the suppression of the γ -hydride
743 should cease, and the amount of γ -hydride increase, which can be seen in the rise of γ -hydride
744 signal in Figure 10 above 250 °C. These concerted changes in γ -hydride and δ -hydride suggest
745 that these phases are physically close.

746 The amount of γ^t -hydride decreased to a small value as the solvus was approached. γ^t -hydrides
747 formed below the solvus temperature reached maximum values below the solvus, not above it,
748 even though the flux is still negative above the solvus. Because the hydride lattice strain is
749 relieved by hydrogen in solution at the periphery of a hydride, hydrides once formed do not
750 dissolve when heated, until a temperature is reached where $J > 0$, (*i.e.*, when the C_+ line is
751 crossed) at which point the hydride will dissolve. The γ^t -hydrides that formed during cooling
752 from 245 °C to 220 °C will reach C_+ and begin to dissolve on heating at 250 °C, and should be
753 completely dissolved by 280 °C. On heating, once the temperature passes 245 °C, γ^t -hydrides
754 form, but most of these hydrides reach C_+ and dissolve by 280 °C, with just a few lasting to
755 286 °C. Thus, the γ^t -hydride areas are predicted to increase at 245 °C, reach a maximum around
756 255 °C, and fall to low values at the solvus temperature, 280 °C, which is what is observed in
757 Figure 13b.

758 Even though the areas of γ -hydride diffraction lines during heating become small for
759 temperatures above the solvus, they do persist. The γ -phase is stable above the solvus on heating
760 when $J < 0$. The process is self-stressing stabilizing where the sharp edges of hydrides put the
761 local zirconium lattice into tension, which invokes the drift current, and hydrogen in solution is
762 driven to the hydride, even though the solvus temperature has been exceeded. The drift current
763 counteracts the dissolution current and stabilizes the precipitates to higher temperatures. For
764 temperatures above T_+ , J changes sign, and the hydrostatic stress imposed on the lattice by the
765 sharp end of the hydrides is not enough to overcome the propensity of these hydrides to dissolve,
766 and so they do.

767 The γ^a -hydrides do not follow the temperature dependence seen for γ^t -hydrides when heated.
768 Figure 10 shows peak widths of γ^a -hydrides broaden for temperatures above T_{TSS} , while the areas
769 of the peaks remain relatively constant, although the background in Figure 10 weakens definitive
770 inferences. The γ^a -hydrides are possibly more stable at high temperatures because their
771 stabilizing Cottrell atmospheres were also formed at high temperatures on cooling. Above the

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772 solvus temperature, the γ^a -hydrides may experience a broadening range of stress from the
773 underlying dislocation as the hydrides become smaller.

774 The zirconium lattice spacings shown in Figure 14 vary smoothly with increase in temperature.
775 Eventually, on heating, the concentrations of hydrogen in solution associated with hydrides will
776 intersect with, and follow, the C_- boundary, which varies smoothly with temperature. For initial
777 heating, the increase with temperature of lattice parameters for the prism $\{10\bar{1}0\}$ diffraction lines
778 is less than for the basal (0002) line, which agrees with earlier work that suggests hydrogen in
779 solution more easily expands the crystal lattice along the c axis [47]. The relative changes in the
780 lattice parameters with temperature suggests that the anisotropy in the presence of hydrides is
781 temperature dependent. At high temperatures, when all of the hydrides have dissolved, the
782 contribution of hydrogen in solution to the ratio of lattice spacings, c/a , levels off to a constant
783 value [47].

784 Implications of the Phase Rule: a composite hydride with variable stoichiometry
785 For regions in the bulk metal where the chemical potential can be described in terms of two
786 intensive variables, concentration and temperature, there is one degree of freedom, as described
787 in the Introduction. The metal is ideal and defect-free. In these regions, there are no stress
788 gradients and the C_- and C_+ lines collapse about the central $J=0$ solution to Equation 3 shown in
789 Figure 8, which defines the solvus. The Phase Rule in these regions requires that for every
790 temperature there is a unique concentration of hydrogen in equilibrium with a unique hydride
791 phase, as in Equation 2. The solvus concentration is the total hydrogen concentration in the
792 metal in the limit as the temperature approaches the onset precipitation temperature on cooling –
793 the concentration of hydrogen in solution in the bulk does not change appreciably when
794 infinitesimally small amounts of hydride precipitate. At equilibrium, hydrogen in solution at the
795 hydride-metal interface is at the solvus concentration. In the volume where the solvus
796 concentration is defined adjacent to the hydride-metal interface, there are no net concentration
797 gradients, and, by Equation 3, there are no net stress gradients at equilibrium. In this gradient-
798 free volume, the Phase Rule dictates one degree of freedom.

799 Multiple hydride phases are not allowed at equilibrium if hydrogen also exists in solution. If
800 multiple hydride phases existed, then each hydride phase would have a similar region adjacent to
801 its hydride-metal interface where there would be no concentration gradients, and thus no stress
802 gradients. In each of these regions, an equilibrium concentration would exist that would be
803 different from the other equilibrium concentrations for the other hydride phases. But, these
804 different concentrations would cause hydrogen to flow to the hydride phase with the lowest
805 equilibrium hydride-metal interface concentration, by analogy with Ostwald ripening where
806 precipitates with high local solute concentrations dissolve while precipitates with low local
807 solute concentrations grow [65]. If equilibrium concentrations can be defined in regions adjacent
808 to hydrides, then only one hydride phase can exist at equilibrium if hydrogen is in solution.

809 It follows that if there are two hydride phases, then at equilibrium there can be no hydrogen in
810 solution if there is a single degree of freedom. Simultaneous observation of two hydride phases
811 and hydrogen in solution suggests one hydride phase surrounded by another at equilibrium. The
812 sudden formation of δ -hydrides shown in Figure 15 and Figure 16 is therefore a non-equilibrium
813 process: δ -hydrides can never be in equilibrium with hydrogen in solution if γ -hydrides exist
814 simultaneously or are formed first. A single degree of freedom requires a composite hydride

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815 forms with a single outer hydride phase, which can be either γ -hydride or δ -hydride. Which
816 phase forms the outer layer between the hydride and hydrogen in solution may depend on rates
817 of cooling and heating, and amounts of hydrogen.

818 When the δ -hydrides form, γ -hydride areas are observed to decrease, but γ -hydrides still exist in
819 detectable amounts to the end of the observation period (Figure 15). If δ -hydrides form the outer
820 hydride phase of the composite hydride, then the γ -hydrides must be completely surrounded and
821 cut-off from hydrogen in solution to comply with the single degree of freedom. Figure 10 and
822 Figure 13b show the signals from γ -hydrides change at the solvus temperature when heating: the
823 areas of the γ^t -hydrides decrease appreciably, and the diffraction-line widths increase for the
824 γ^a -hydrides. The γ -hydrides will only be sensitive to the solvus if they are in contact with
825 hydrogen in solution, hence, δ -hydrides do not form the outer hydride phase of the composite
826 hydride in this study.

827 When the δ -hydrides form, equilibrium can only be attained if the δ -hydrides are surrounded by a
828 layer of γ -hydride, which would form when there is insufficient hydrogen available to form the
829 higher stoichiometric δ -hydrides. Because γ -hydrides were the first to precipitate, probably
830 because of stoichiometry and lower strain energy, this interpretation would require δ -hydrides to
831 be surrounded by γ -hydrides. The TEM picture in Figure 1 showing δ -hydrides surrounded by
832 γ -hydrides [35] in another zirconium alloy, Zr-2.5Nb, demonstrates that this interpretation has
833 merit. Results of nano-beam electron diffraction experiments on Zircaloy-2 containing 1 at.% H
834 have similarly been interpreted as δ -phase encased in γ -phase [28].

835 Neutron diffraction results also support the proposed composite hydride [33]. Areas of neutron
836 diffraction peaks associated with γ -hydrides and δ -hydrides do not decrease monotonically with
837 heating, but their sum does, following Equation 5 for C_+ . This behaviour is expected if the
838 γ -hydrides and δ -hydrides are not separate and independent, but are connected in a composite
839 where their combined dissolution is constrained by an equilibrium relation. The neutron
840 diffraction results suggest that the energetics of dissolution and precipitation of γ -hydrides and
841 δ -hydrides are similar, otherwise the concentration of hydrogen in solution would change when,
842 for example, γ -hydrides diminish and δ -hydrides increase in Zr-2.5Nb as they do on heating at
843 180 °C in Fig 8 of [33], but such a change in concentration of hydrogen in solution was not
844 observed (see Fig. 4 of [33])¹. The implication is that the heat required to dissolve the γ -hydrides
845 is similar to the heat given off when the δ -hydride precipitates, on a per hydrogen atom basis.
846 Density Functional Theory (DFT) that includes the effects of enthalpy as well as entropy and
847 disorder concurs that γ -hydride and δ -hydride are very close in energy [4]. In the current study,
848 no indication was observed in the DSC exothermic heat flow at 230 °C (Figure 3) where the
849 γ -hydrides decline and δ -hydrides form in Figure 15. The extra exothermic heat flow that might
850 be expected from the δ -hydride that forms after the γ -hydrides stop dissolving (Figure 16) would
851 be small if the δ -hydride formed by condensation of hydrogen trapped in the surrounding
852 hydrogen cloud containing the stoichiometric distribution of hydrogen.

¹ The temperature where γ -hydrides diminish and δ -hydrides increase on heating in [33] is similar to the temperatures where the ratio of C_+ to C_{TSS} for Zr-2.5Nb equals the stoichiometry ratios for Zr_4H_7 (1.75) and Zr_3H_5 (1.67): 180 °C and 210 °C, respectively.

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853 Figure 18 shows the phase diagram consistent with the interpretation of the current observations
854 in which a boundary has been added at 0.5 mole fraction for ZrH γ -hydrides. Similar boundaries
855 have been proposed previously [67, 69, 70]. If ZrH is a compound, then it is represented as a
856 vertical line in the phase diagram. Figure 18 also shows a prediction of the boundary delineating
857 the ($\gamma+\delta$) phase field calculated from ratios of C_+ to C_{TSS} determined with Equation 6.

858 The diffraction line profile for δ -hydrides was not the same for formation and dissolution. When
859 δ -hydrides formed the line grew symmetrically with time at 230 °C (Figure 15), but as the
860 temperature was increased, successive isothermal measurements showed the line diminishing
861 from left to right in Figure 10. The δ -hydride line profile includes contributions from δ -hydrides
862 with reported stoichiometry from ZrH_{1.5} to ZrH_{1.67}. The d-spacings increase with stoichiometry
863 as the lattice expands because of the extra hydrogen. The symmetric growth of the δ -hydride
864 diffraction profile shown in Figure 15 suggests that the distribution of stoichiometry does not
865 change when δ -hydrides condense from hydrogen trapped in hydrogen clouds formed when
866 cooling. The range of stoichiometry depends on the range of C_+ values that exist when the δ -
867 hydrides condense, which from the horizontal lines in Figure 8 should correspond to the
868 temperature range of ≈ 35 °C, or from 230 °C to 230 °C + 35 °C for 1 at.% hydrogen. The
869 corresponding ratios of C_+ to C_{TSS} are 1.6 to 1.7, which is the predicted range of stoichiometry
870 for the condensing δ -hydrides. The width of the δ -hydride diffraction peak in Figure 15 includes
871 this range of stoichiometry.

872 In contrast, when heated, the δ -hydride diffraction profile decays asymmetrically with the lowest
873 stoichiometric hydrides systematically disappearing. Stable γ -hydride form with surrounding
874 layers of hydrogen in solution trapped at concentrations C_+ , C_{TSS} and C_- . When these layers
875 condense to form δ -hydride, the concentration profile is recorded in the stoichiometry profile of
876 the δ -hydride. When heated, the composite hydride dissolves systematically from the outermost
877 layers.

878 *Ab initio* calculations suggest that the H-Zr stoichiometric ratio of γ -hydride could vary from 1.1
879 (0.52 mole fraction of H) at temperatures of 850 °C to 1.4 (0.58 mole fraction of H) at
880 temperatures of 300 °C [70], in which case the vertical boundary line at 0.50 mole fraction
881 (50 at.%) would be curved in Figure 18. The stoichiometry of the γ -hydride cannot be
882 determined from the diffraction spectrum, it is assumed to be 1:1 as described in the
883 Introduction. In the temperature range of this study, the position of the γ -hydride diffraction
884 peak does not vary significantly suggesting any variation because of changes in stoichiometry is
885 within the resolution of the measurement.

886 Comparison with previous interpretations

887 The temperatures in Figure 3 where exothermic and endothermic heat flows are most evident
888 have been used to define two independent solvi: one for precipitation, and one for dissolution.
889 On heating, the temperature at which the differential heat flow reaches a minimum value is
890 sometimes called TSSD, which stands for terminal solid solubility at dissolution (315 °C in
891 Figure 3). When the sample is cooled from the state where all of the hydrogen is in solution, the
892 temperatures where exothermic changes can be observed start at 280 °C: this temperature is
893 called the onset TSSP, where P stands for precipitation. The difference between the TSSD and
894 TSSP solvi temperatures is now commonly called the 'hysteresis' [40]. A feature of the previous
895 interpretation of the hysteresis is the hiatus inferred when switching between cooling and heating

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896 where the concentration of hydrogen in solution does not change until TSSD is reached, as
897 indicated by the horizontal line between Points C and D in Figure 2. This previous interpretation
898 is not supported by the X-ray diffraction results because as soon as the temperature is increased,
899 the lattice parameters of zirconium shown in Figure 14 rise monotonically indicating hydrogen
900 going into solution.

901 The interpretation of the current results provides the underlying reasons for the apparent
902 hysteresis. What has been called TSSP, is now labelled simply TSS, which is defined as the
903 single solvus. The TSSD dissolution solvus of yore is C_* , which is determined directly from a
904 $J = 0$ solution of the Einstein flux equation, and written in terms of the TSS concentration
905 (Equation 5), which means TSSD is not an independent entity, and is not a solvus – it is the line
906 about which the flux of hydrogen changes sign above the solvus temperature.

907 In the standard interpretation of TSS depicted in Figure 2, TSSP and TSSD concentrations exist
908 at the same location, but at different times (when cooling and when heating, respectively, the
909 concentrations are everywhere the same). In the current interpretation, the concentrations at
910 equilibrium of hydrogen in solution associated with TSSP (TSS), and TSSD (C_*) exist at
911 different locations at the same time.

912 Theoretical formulations have been developed, for example using accommodation energies
913 required to form hydrides, to account for the apparent hysteresis, and to reconcile multiple solvi
914 [39]; these formulations are unnecessary when invoking the Einstein flux equation.

915 Curiously, in Figure 9 hydrides were seen to form on cooling around 320 °C and might be
916 inferred to dissolve finally on heating around 280 °C. These temperatures are reversed from the
917 precipitation and dissolution temperatures determined from the DSC heat flow curves in
918 Figure 3. If only δ -hydride peaks were observed, then it would appear that precipitation
919 occurred at 230 °C and dissolution finally around 280 °C, which again is not in accord with the
920 DSC heat flow curves in Figure 3. Diffraction data alone can be misleading without
921 complementary information from DSC, which was used in this study to characterize the solvus
922 by the onset precipitation temperature, or from other methods indicating hydride precipitation,
923 for example dilatometry [40].

924 The apparent violation of the Phase Rule by simultaneous observation of hydrogen in solution
925 and two hydride phases was resolved by containing the δ -phase within γ -phase at equilibrium.
926 Previously, it was argued that the δ -phase and γ -phase could exist independently at the same
927 time, but that the γ -phase is metastable and would not be present at equilibrium. Thus, the
928 observation of γ -phase and δ -phase was interpreted to indicate these systems were not at
929 equilibrium, which supported the ‘restricted and dynamic’ definitions of equilibrium during
930 cooling and heating used to interpret TSSD and TSSP curves. The metastable argument requires
931 that the γ -phase should eventually disappear, but it still persists after hours in our experiments
932 and hours in neutron diffraction experiments with 0.783 at.% hydrogen in Zr-2.5Nb up to
933 complete dissolution at 323 °C [33], and after three years at room temperature [11]. If γ -hydrides
934 were consistently metastable, then heating should lead to their disappearance not just lead to
935 reduced amounts [33]. The metastable argument is confounded by DSC experiments that show
936 sharp reproducible indications of precipitation when cooling at rates of 5 °C to 30 °C per minute.

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937 The results of the current study suggest that γ -hydride is the equilibrium phase in contact with
938 hydrogen in solution.

939 The formation of δ -phase requires some previous dissolution of γ -hydrides (e.g. see Figure 14
940 below T_c on cooling) to raise concentrations of hydrogen in solution to the values needed to form
941 new hydrogen clouds when the δ -phase condenses (e.g. see Figures 13a and 14 at 230 °C).
942 When the hydrogen trapped in clouds condenses to form δ -phase, the stabilizing hydrogen cloud
943 is lost and a new cloud needs to form by taking hydrogen from the surrounding matrix to
944 stabilize the newly condensed δ -phase. Thus, the prerequisite step for δ -hydride formation is for
945 some γ -hydrides to dissolve partially, and then nucleate the δ -phase in the hydrogen cloud.

946 Nucleation of appropriate hydrides is the critical step to produce hydrides with their platelet
947 normals parallel with a tensile stress leading to radial hydrides in tubes [71]. The athermal (γ^a)
948 hydrides seen between 0° and 20° are forming close to the $\{10\bar{1}7\}$ hydride habit planes [72, 73],
949 which are 14.7° from the basal plane. If stabilized by applied tensile stress, these hydrides could
950 act as the nucleation sites for damaging radial hydrides in pressure tubes with a strong transverse
951 texture, similar to the current experimental material. The thermal (γ^t) hydrides are associated
952 with the $\{10\bar{1}0\}$ habit planes [73] and are less likely to contribute to radial hydrides.

953 In the current study, hydrogen clouds were postulated to form in regions of tension to relieve the
954 stress. Hydrogen clouds surrounding hydrides stunt their growth during cooling and stabilize
955 them against dissolution during heating. During cooling, the stress-gradient regions, and not the
956 hydrides, become sinks for hydrogen, and when satiated no more hydrogen flows. At
957 equilibrium, the concentration at the unstressed hydride surface, which is C_{TSS} , and the
958 concentration at the end of all the stress gradients must be the same, otherwise hydrogen would
959 flow. Thus, at the point where the stress gradients go to zero, the conditions will be right for
960 another hydride to nucleate, and a series of stable stunted hydrides are expected to form.

961 High-resolution micrographs of hydrides in zirconium alloys show that they are composed of
962 linear arrays of small platelets [74], Figure 19. These ideas are reminiscent of θ' phase
963 precipitation in Al-3 wt.% Cu. Precipitates of θ' phase originate at dislocations, but stop
964 growing and then reinitiate via an autocatalytic nucleation process to form a linear array of plate-
965 shaped precipitates. The resulting elastically-locked arrays are stabilized against growth or
966 coarsening, or both [76].

967 DFT calculations of free energies for hydrides showed positive values for 1 at.% hydrogen in
968 zirconium, which means that hydrides could not form; similar results were seen for hydrogen
969 concentrations up to 2.7 at.% (300 ppm) [4], contrary to observations. This DFT free-energy
970 calculation did not include the additional term to account for the work done to expand the solvent
971 by the solute, which is the product of the hydrostatic pressure and the partial molar volume of the
972 solute. This additional work term led to the drift term in Equation 3 and makes the free energies
973 negative for hydride formation. Hydrides stabilized by a hydrogen cloud that forms in response
974 to the misfit between the hydride and the matrix is consistent with suggestions from DFT that an
975 additional hydrogen concentrating mechanism, such as “precipitate interface lattice strain”, is
976 required to overcome the positive free energy calculated for hydride precipitation in zirconium
977 with 1 at.% hydrogen [4].

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978 The equations for C_+ and C_- should be generally applicable to any stress gradient within metals
979 where a solute can move to relieve that stress gradient. The source of the stress gradient is
980 decorated by a Cottrell atmosphere or a cloud of solute atoms until the limiting C_+ and C_-
981 conditions are met, where the flux changes sign and the solute moves away from the stress
982 source. The C_+ and C_- lines can be crossed by varying temperature and stress. Thus, an applied
983 stress can be used to release the Cottrell atmosphere that prevents dislocations from moving, and
984 maxima, called yield points, are seen in stress-strain curves [60]. Similarly, varying temperature
985 was used in this work to unlock the Cottrell atmosphere or hydrogen cloud stabilizing hydrides
986 against dissolution, and maxima were seen for the amounts of hydride formed with temperature.

987 We are aware that results presented in this paper run counter to common perceptions of what
988 hydrides, and precipitates in general, are supposed to do when heated and cooled. But, think for
989 a moment about the common perception that for hydrogen in zirconium there are two TSS solvus
990 lines: one line applies when we cool, TSSP, and another line applies when we heat, TSSD (see
991 Figure 2). The solvus defines an equilibrium condition, so it should not depend on direction of
992 approach, yet the common perception is that it does for hydrogen in hydride forming metals,
993 with zirconium being a clear example. What is counter to thermodynamics is equilibrium
994 defined differently depending whether the system is heated or cooled. Over-all, we report that
995 hydrides precipitate with cooling, and dissolve with heating, as expected. But, close to the
996 solubility limit, because of the stress imposed by the hydrides on the lattice, we see these little
997 perturbations. The flux of hydrogen to the hydrides depends on competing concentration
998 gradients and stress gradients that orchestrate a marvelous dance about a central single
999 solvus. The governing equation for this dance is of the form Einstein used to explain Brownian
1000 motion.

1001 Concluding remarks

1002 The behaviour of hydrides in zirconium have been observed using differential scanning
1003 calorimetry and X-ray diffraction on specimens of Zircaloy-2 containing up to 1 at.% hydrogen:
1004 hydrides both precipitate and dissolve on cooling and dissolve and precipitate on heating. These
1005 unexpected phenomena can be understood quantitatively with the Einstein flux equation, which
1006 is the sum of a concentration-gradient diffusion current (Fick's Law) and a drift current
1007 emanating from tensile stress gradients. Three zero-flux solutions to the equation exist. The
1008 solution where there are no gradients in concentration and stress defines the terminal solid
1009 solubility - the solvus. There are two solutions where the diffusion and drift currents are non-
1010 zero and cancel: these solutions define a region above and below the solvus where the flux of
1011 hydrogen is negative, and hydrides grow. Outside this region, the flux is positive and hydrides
1012 dissolve. The tensile stress can come from dislocations in the lattice, which can stabilize hydride
1013 formation above the solvus. The stress also comes from the edges around hydrides that put the
1014 local metal lattice into tension. Other sources of stress include differential thermal expansion
1015 leading to intergranular stresses. Hydrogen in solution moves into these tensile regions forming
1016 Cottrell atmospheres and hydrogen clouds to relieve the stress, which stabilizes the hydride
1017 against the effects of heating and cooling. One consequence of this interpretation is that hydrides
1018 should form linear arrays of small platelets. The lattice spacing of the zirconium matrix expands
1019 and contracts in response to the hydrogen going in and out of solution.

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1020 It has not escaped our attention that this description of precipitation and particle dissolution
1021 should have general application to other hydride forming metals, for example Hf, Ti, Ta, Nb and
1022 V, and may be even more general for other precipitates.

1023 Hydrides are inferred to form composite structures when δ -hydrides are observed. These
1024 composites will include a surrounding layer of γ -hydrides to satisfy the Phase Rule. There is no
1025 solvus for δ -hydrides; they are never at equilibrium with hydrogen in solid solution because there
1026 is always a γ -hydride intermediary.

1027 Technological significances of these results are:

- 1028 • Contrary to the usual interpretation, only a single terminal solid solubility limit
1029 (solvus) exists, based on precipitation of the γ -phase;
- 1030 • The large differences inferred from DSC measurements (and other methods) between
1031 the temperatures at which hydrides start to precipitate and completely dissolve is not
1032 observed in these X-ray diffraction experiments. Hydrides have been observed to
1033 form on cooling at temperatures above the precipitation temperature inferred from
1034 DSC. The current results are useful for understanding phenomena such as delayed
1035 hydride cracking, blister formation, and hydride orientation;
- 1036 • The δ -phase is not the equilibrium phase in contact with hydrogen in solution in the
1037 zirconium even when it is the most abundant phase. The implication of this
1038 conclusion is that the equilibrium phase diagram should include a boundary at
1039 50 at.% (0.5 mole fraction) hydrogen. The observed stoichiometry of the δ -phase
1040 captured by the curvature of the $\gamma+\delta/\delta$ line in the phase diagram can be calculated
1041 from the concentration of hydrogen in solution in hydrogen clouds that condense to
1042 form δ -hydrides;
- 1043 • The temperature dependence of the precipitation process is complicated when
1044 compared with that of dissolution and contributes to the variation of hydride phases
1045 reported in the literature.

1046

Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium1047 **Acknowledgements:**

We would like to thank Argonne National Laboratory and J. Almer for setting up the X-ray source and diffraction equipment at the Advanced Photon Source, A. Buyers, C. Dixon, S. Hanlon, Z. He, B.W. Leitch, H. Nordin, S. Read, P. Wilson (all of CNL), C. Cochrane (Queen's U) and K. Colas (CEA) for help with the experiments, B. He (Carleton U.) for assistance with the analysis of the diffraction patterns. Useful discussions with J. Goldak and A. Artemev at Carleton University are much appreciated. CEC was supported as a Researcher Emeritus by CNL (né Atomic Energy of Canada Limited).

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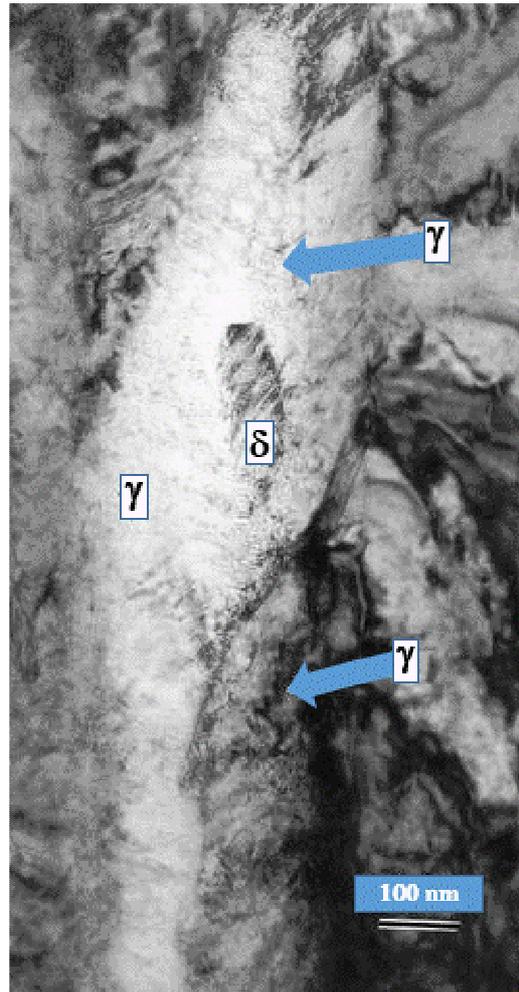
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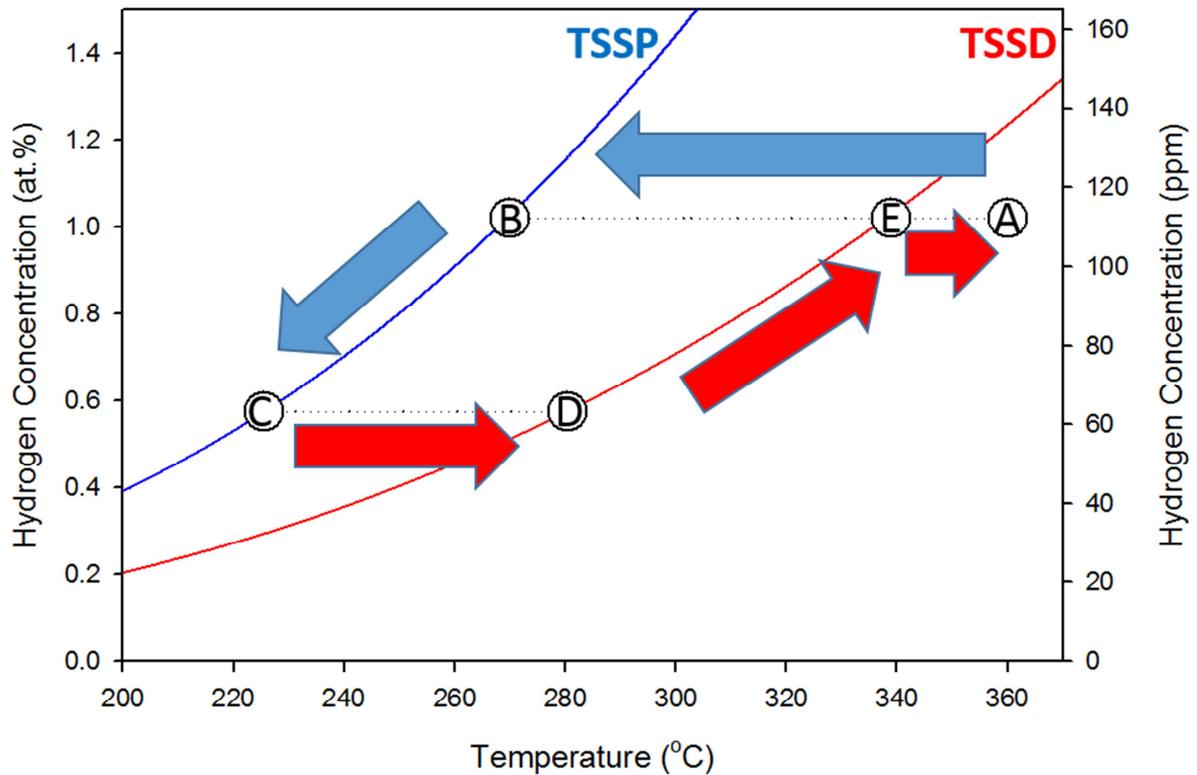
Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium



1228

1229 Figure 1: TEM micrograph showing δ -hydride surrounded by γ -hydride in Zr-2.5Nb, based on
1230 [35].

Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium



1231

1232 Figure 2: TSS lines for 1 at.% hydrogen in Zircaloy-2 and some points that are used in the text to
 1233 illustrate the standard interpretation of a cooling-heating cycle starting at Point A and
 1234 proceeding to Points B-C-D-E and back to A.

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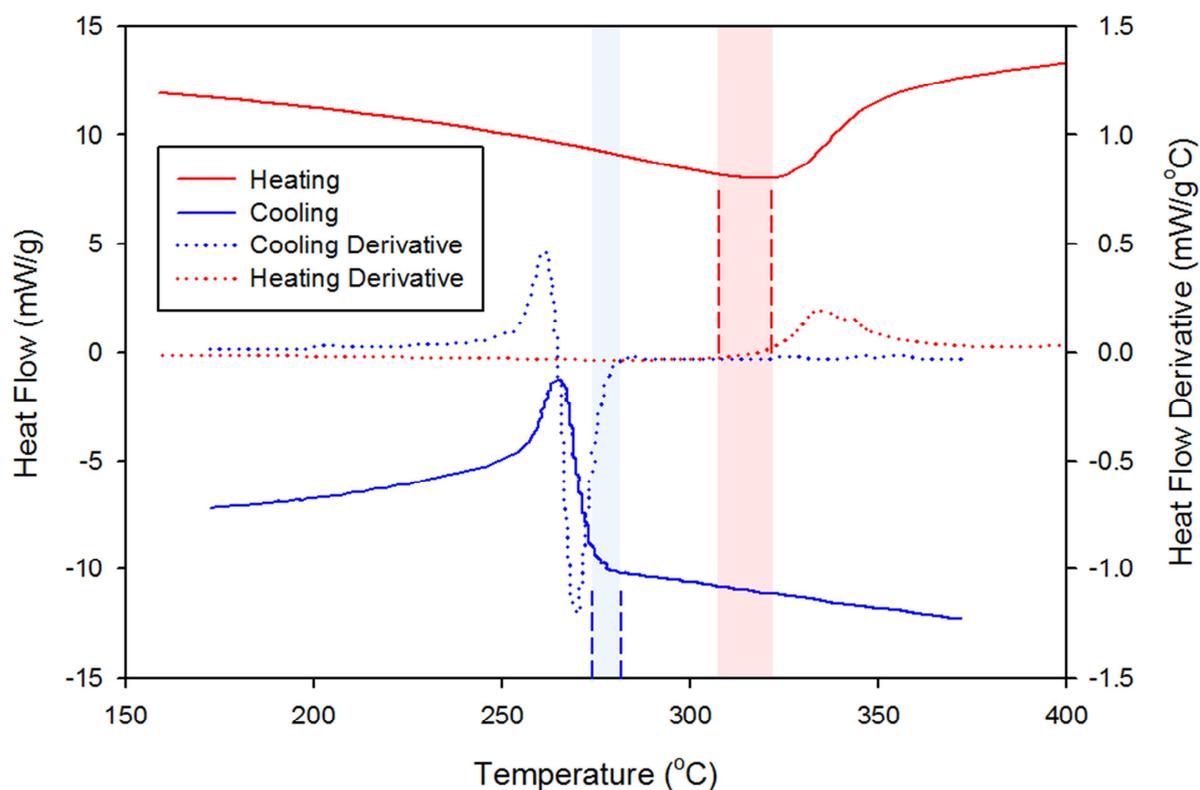


Figure 3: DSC heating and cooling curves for 1 at.%, (113±4) ppm, hydrogen in zirconium. The vertical coloured bands show one standard deviation about the mean of measurements of the onset temperature for precipitation on cooling, the TSS or solvus ($278\text{ °C} \pm 4\text{ °C}$; left band; blue), and the minimum heat-flow temperature on heating ($T_+ = 315\text{ °C} \pm 7\text{ °C}$; right band; pink).

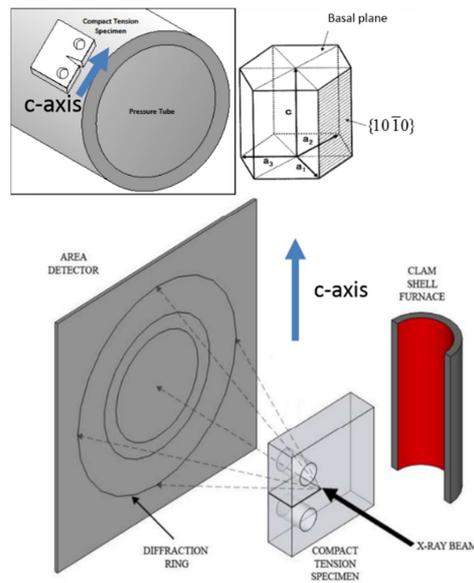
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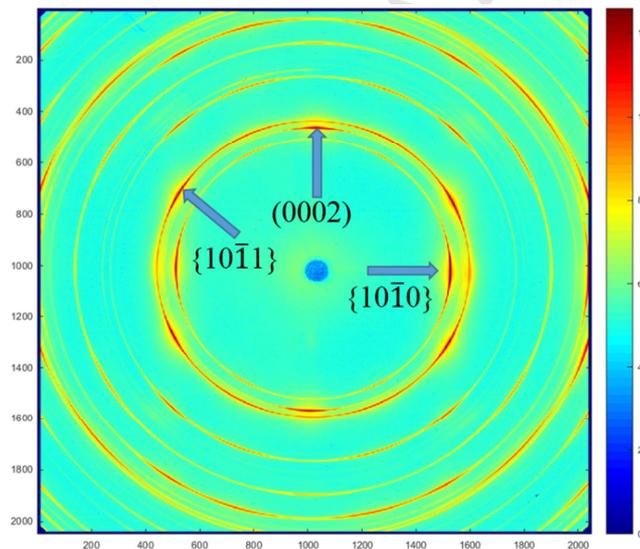
Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium



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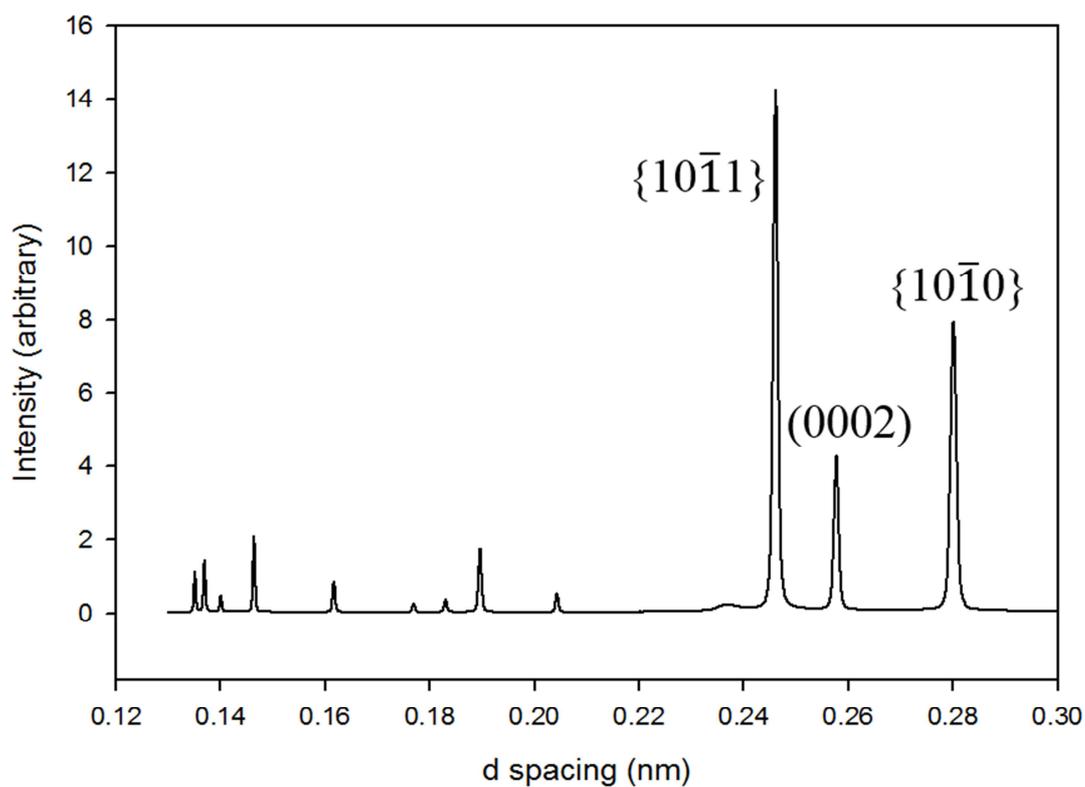
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Figure 4: Experimental arrangement (not to scale).



1241

1242 Figure 5: Diffraction rings from the Zircaloy-2 specimen with hydrogen concentration 0.1 at.%,
 1243 (12 ± 3) ppm. The intensity scale is arbitrary. The innermost most ring is $\{10\bar{1}0\}$, the next ring is
 1244 (0002) . The variable intensity around the circumference of each ring is because of the texture in
 1245 the zirconium: the basal plane normals tend to point 'north', or towards 12 o'clock, because of
 1246 the predominant transverse texture of the pressure tube from which the specimens were cut. The
 1247 zirconium specimens were cut in the form of compact toughness specimens, but the notch was
 1248 not examined in this experiment: all reported observations were made at distances of millimeters
 1249 from the notch, which was loaded with 10 N to hold the specimens in place.

Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium

1250

1251 Figure 6: Diffraction spectrum of the Zircaloy-2 specimen with hydrogen concentration
1252 0.1 at.%, (12±3) ppm. The basal (0002) plane, prism plane {10 $\bar{1}$ 0}, and pyramidal {10 $\bar{1}$ 1}
1253 diffraction lines are labeled. This spectrum is the sum of spectra from 14 different locations in
1254 the specimen.

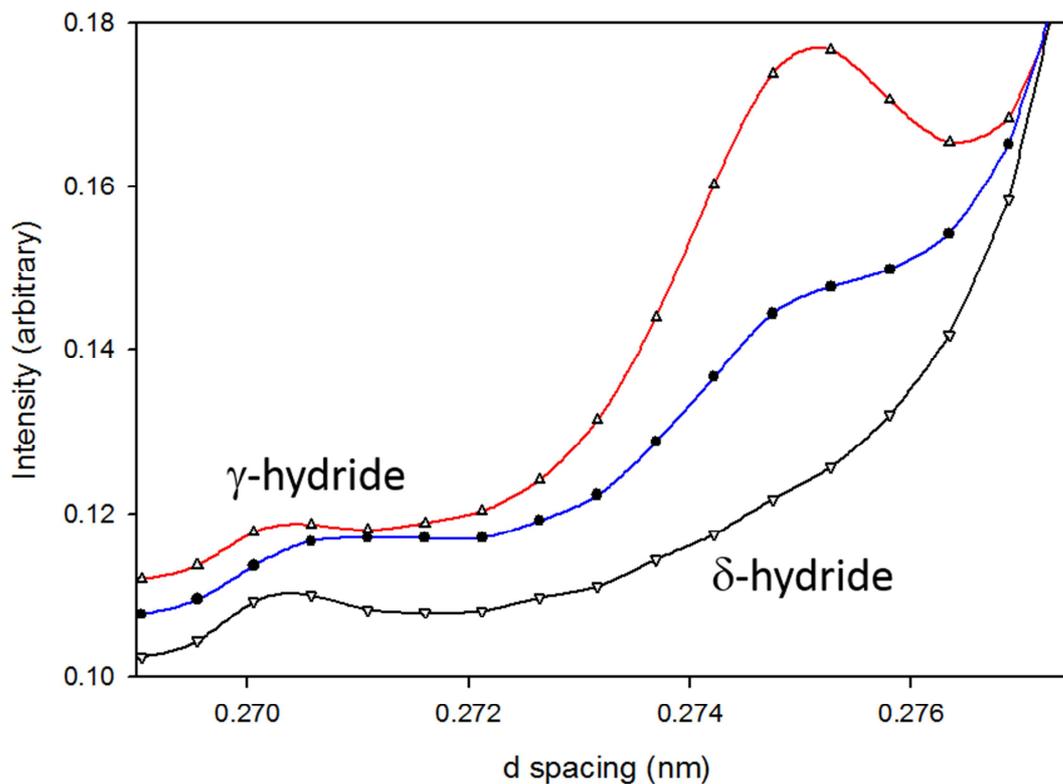
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Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium

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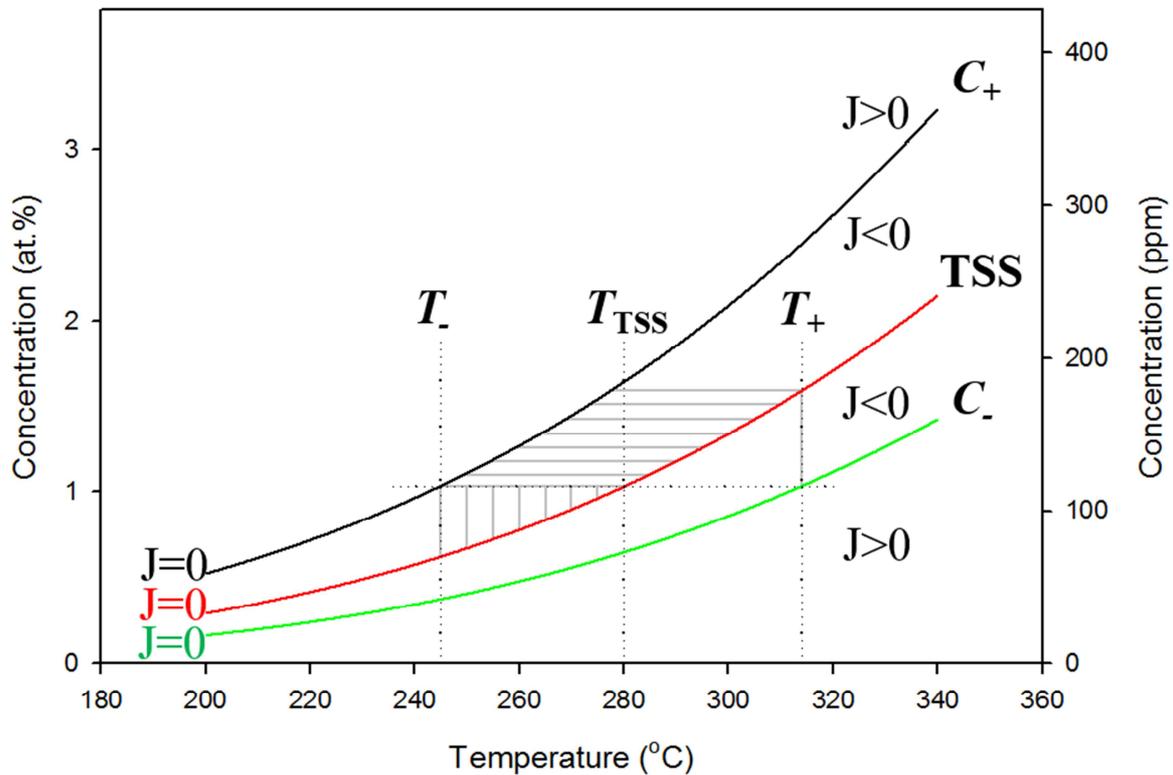


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1260 Figure 7: Diffraction lines in the region where peaks associated with diffraction from {111}
 1261 planes of γ - and δ -hydrides can be found for three hydrogen concentrations (1, 0.6 and 0.1 at.%,
 1262 (113 \pm 4, 63 \pm 4, and 12 \pm 3) ppm, top to bottom) at room temperature after cooling (summed from
 1263 14 separate locations in each specimen). The spectra are successively offset by 0.005 intensity
 1264 units from the low concentration spectrum. The γ -hydride signal is relatively constant compared
 1265 with the δ -hydride signals, which are larger for larger hydrogen concentrations. Only γ -hydrides
 1266 are seen for the specimen containing a low concentration of hydrogen.

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Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium



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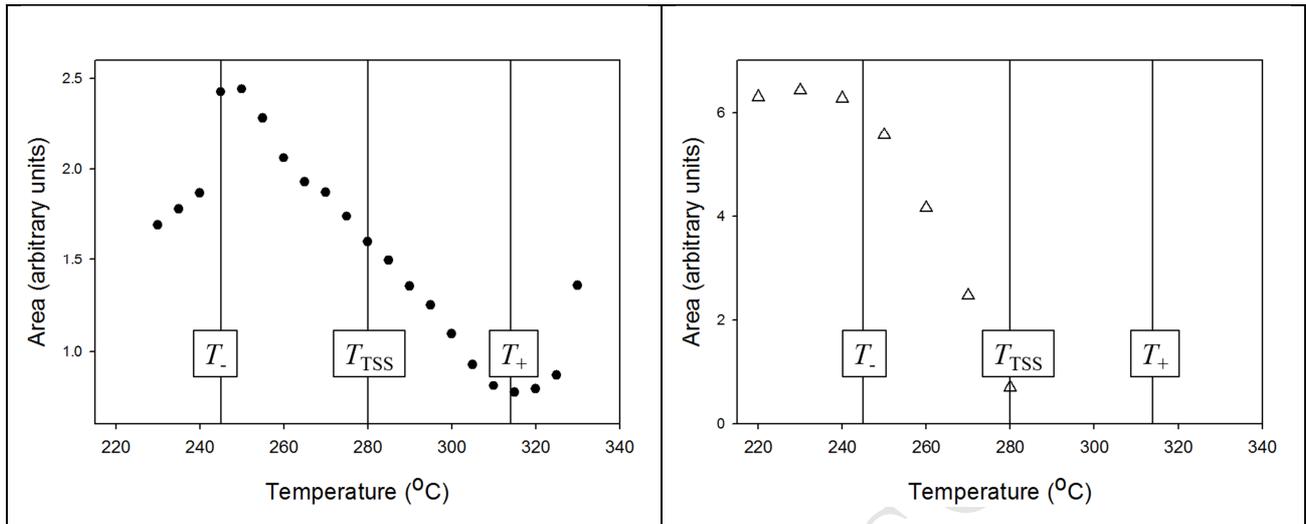
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1270 Figure 8: The no-flux solutions to the Einstein flux equation when hydrides are present (C_+ ,
 1271 TSS, C_-); in the regions between these three solutions the initial flux of hydrogen in solution, J ,
 1272 is negative and hydrogen flows towards regions of tensile stress forming hydrides. Vertical
 1273 dotted lines show the upper and lower 'J < 0' temperature limits calculated with $K = 2$. The
 1274 solvus is at 280 °C for 1 at.% hydrogen, which is shown by the horizontal dotted line. The solid
 1275 vertical and horizontal lines are used to describe γ^a -hydride precipitation and dissolution above
 1276 and below the solvus temperature, as detailed in the text.

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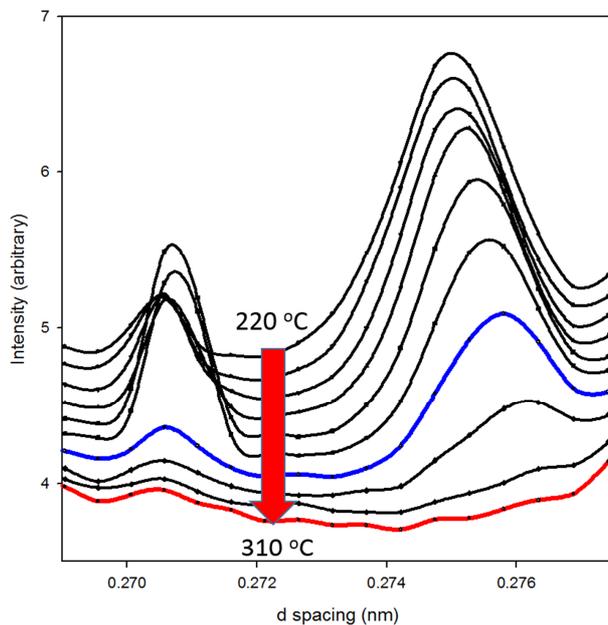
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Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium

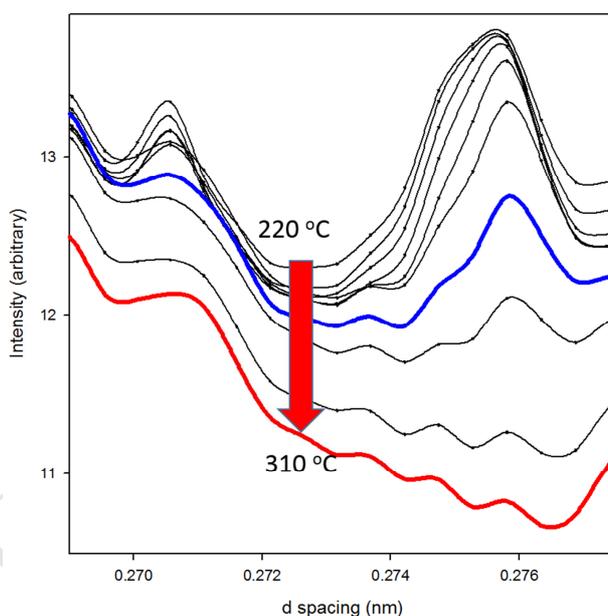


1279 Figure 9: Areas of {111} hydride diffraction peaks integrated around the diffraction rings for the
 1280 specimen with 1 at.%, (113±4) ppm, hydrogen: γ -hydrides on cooling (left) and δ -hydrides on
 1281 heating (right). The vertical lines show T_- , the solvus temperature, and T_+ for $K = 2$, as discussed
 1282 in the text.

Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium



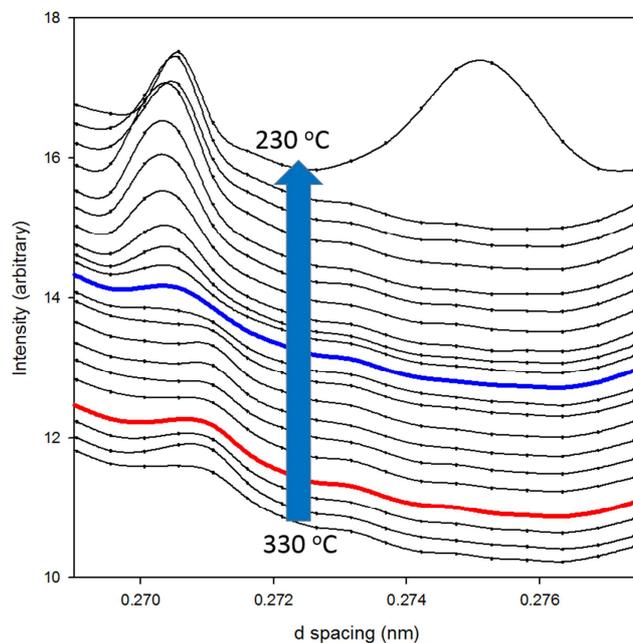
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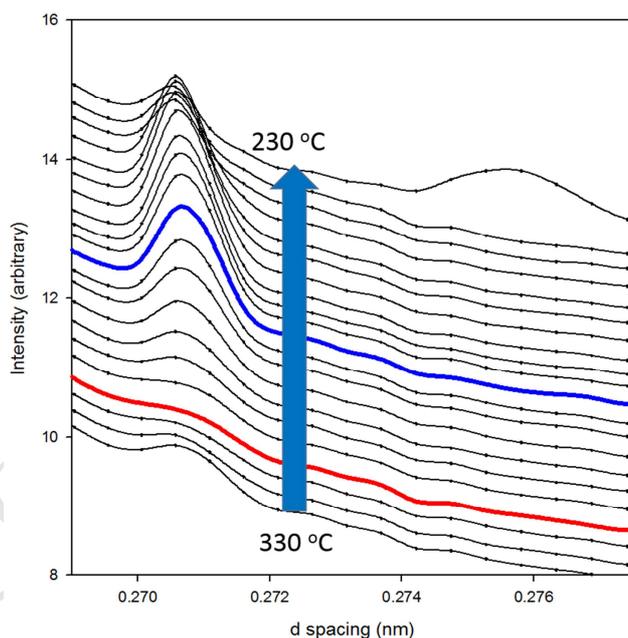
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1285 Figure 10: Spectra obtained with 1 at.%, (113±4) ppm, H in Zircaloy-2 for a series of isothermal
 1286 measurements obtained by integrating intensity around the diffraction ring from 55° to 75° (top)
 1287 and 0° to 20° (bottom). The temperature of the spectrum drawn in blue is the same as the onset
 1288 precipitation temperature determined from DSC (278 °C ± 4 °C); the temperature of the red-
 1289 coloured spectrum is similar to the minimum heat-flow temperature during heating (315 °C
 1290 ± 7 °C).

Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium



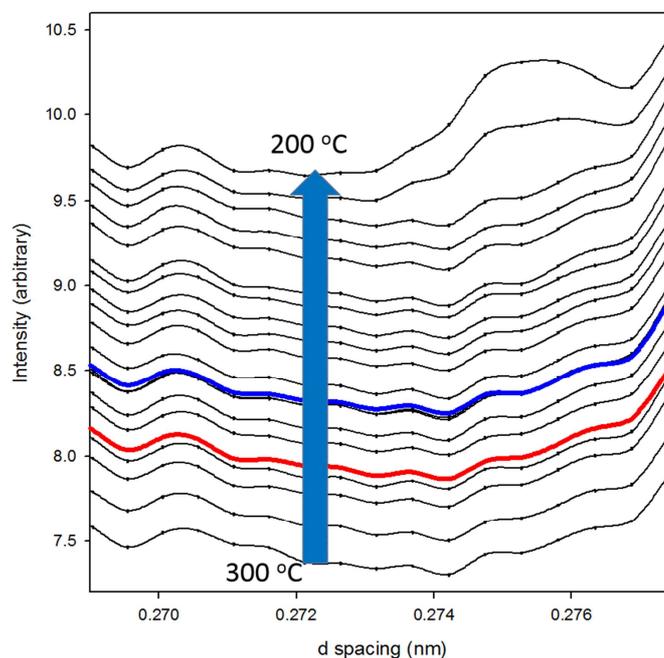
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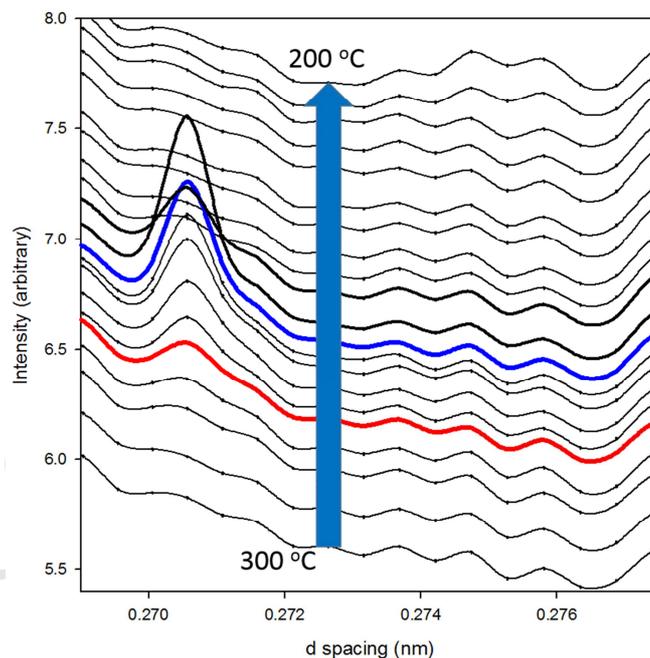
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1293 Figure 11: Spectra obtained with 1 at.%, (113±4) ppm, H in Zircaloy-2 for a series of isothermal
 1294 measurements obtained by integrating intensity around the diffraction ring from 55° to 75° (top)
 1295 and 0° to 20° (bottom). The temperature of the spectrum drawn in blue is the same as the onset
 1296 precipitation temperature determined from DSC (278 °C ± 4 °C); the temperature of the red-
 1297 coloured spectrum is similar to the minimum heat-flow temperature during heating (315 °C ±
 1298 7 °C).

Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium



1299



1300

1301 Figure 12: Spectra obtained with 0.6 at.%, (63 ± 4) ppm, H in Zircaloy-2 for a series of isothermal
 1302 measurements obtained by integrating intensity around the diffraction ring from 55° to 75° (top)
 1303 and 0° to 20° (bottom). The temperature of the spectrum drawn in blue is the same as the onset
 1304 precipitation temperature determined from DSC ($255.3^\circ\text{C} \pm 2^\circ\text{C}$); the temperature of the red-

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1305 coloured spectrum is similar to the minimum heat-flow temperature during heating ($282.4\text{ }^{\circ}\text{C} \pm$
1306 $2\text{ }^{\circ}\text{C}$).

1307

ACCEPTED MANUSCRIPT

Precipitates in metals that dissolve on cooling and form on heating: an example with hydrogen in alpha-zirconium

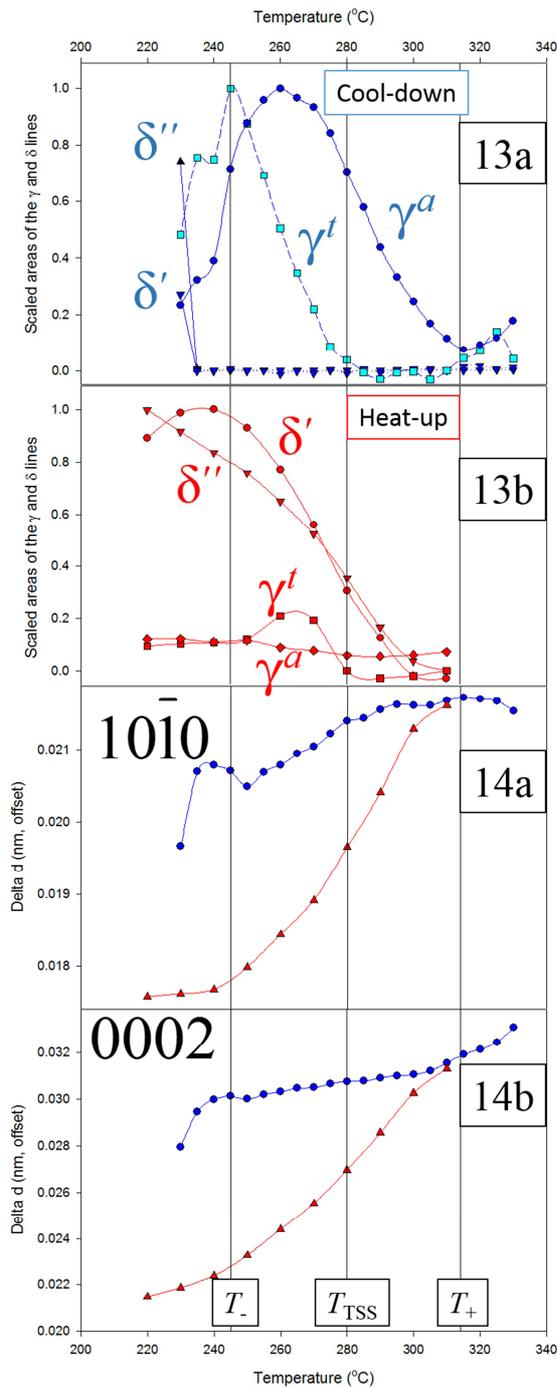


Figure 13: Normalized areas of hydride diffraction peaks obtained during cooling (a) and heating (b): δ'' -hydrides and γ^t -hydrides are seen between 55° and 75° around the ring; δ' -hydrides and γ^a -hydrides are seen between 0° and 20° . The vertical lines show, left to right, T_- , the solvus temperature, and T_+ for $K=2$, as discussed in the text. (1 at.%, (113±4) ppm, H in Zircaloy-2)

Figure 14: d-spacings for the $\{10\bar{1}0\}$ (a) and (0002) (b) α -zirconium lines, determined by integrating around the diffraction ring, and corrected for thermal expansion. Values of 'Delta d' are proportional to the concentration of hydrogen in solid solution. Circles denote cool-down and triangles heat-up. (1 at.%, (113±4) ppm, H in Zircaloy-2)

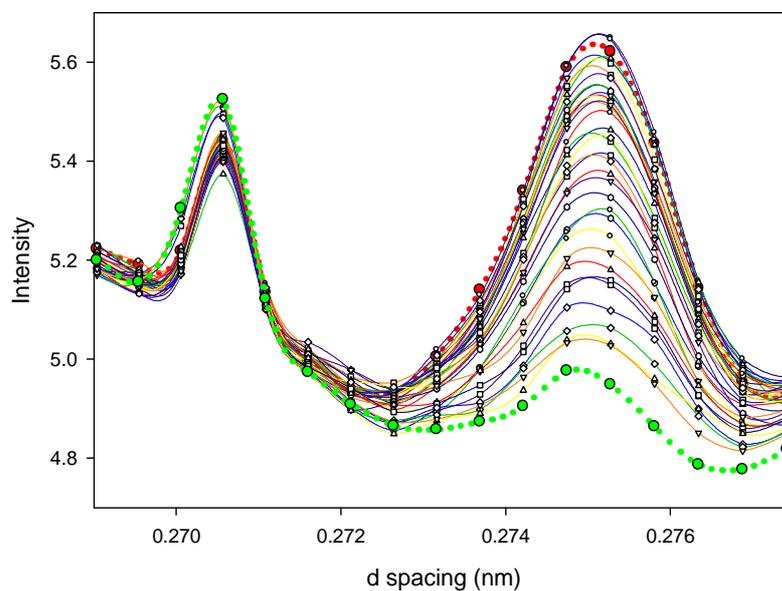


Figure 15: Diffraction peaks from $\{111\}$ planes of the γ' -hydrides (left) and δ'' -hydrides (right) at 0.5 s intervals after cooling from 235 °C to 230 °C, at 10 °C/min, and a 3 min isothermal hold. The first spectrum in the time sequence is shown by green-filled circles connected with green dots; the last spectrum is red-filled circles connected by red dots. The areas of the peaks as a function of time are shown in Figure 16. The intensities of the peaks were measured around the diffraction ring from 55° to 75°. (1 at.%, (113±4) ppm, H in Zircaloy-2)

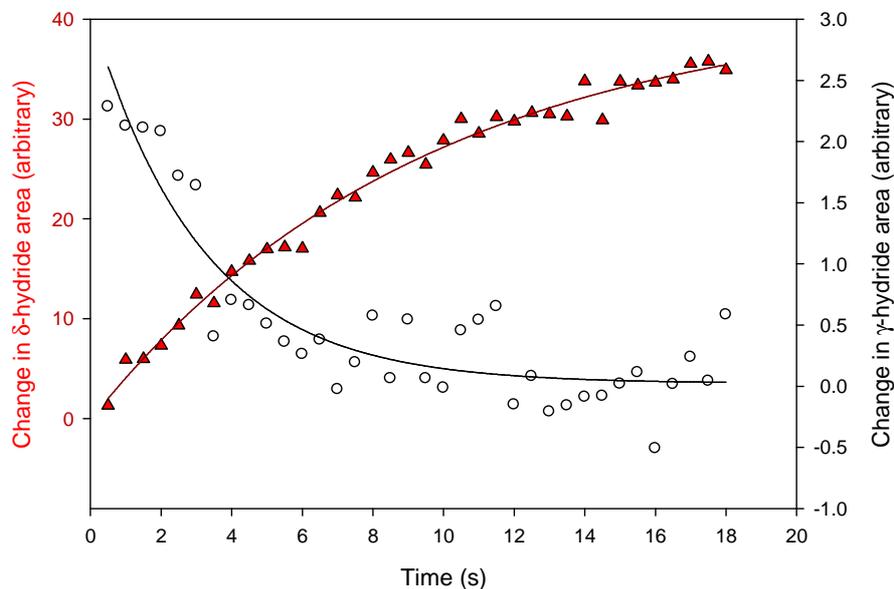


Figure 16: Time dependence of the areas of the diffraction peaks shown in Figure 15 from $\{111\}$ planes of the γ -hydrides and δ -hydrides starting 3 min after cooling from 235 °C to 230 °C at 10 °C/min. The γ -hydride peak areas decrease in the first few seconds, then stop. The δ -hydride peaks continually increase over the observation time of 18 s. The zirconium diffraction peaks did not move over this time. The hydride areas are relative to the initial and final areas of the δ - and γ -hydride peaks, respectively.

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Figure 17: Thin-film transmission electron micrograph of Zircaloy-2 specimen showing dislocation lines decorated with hydride particles.

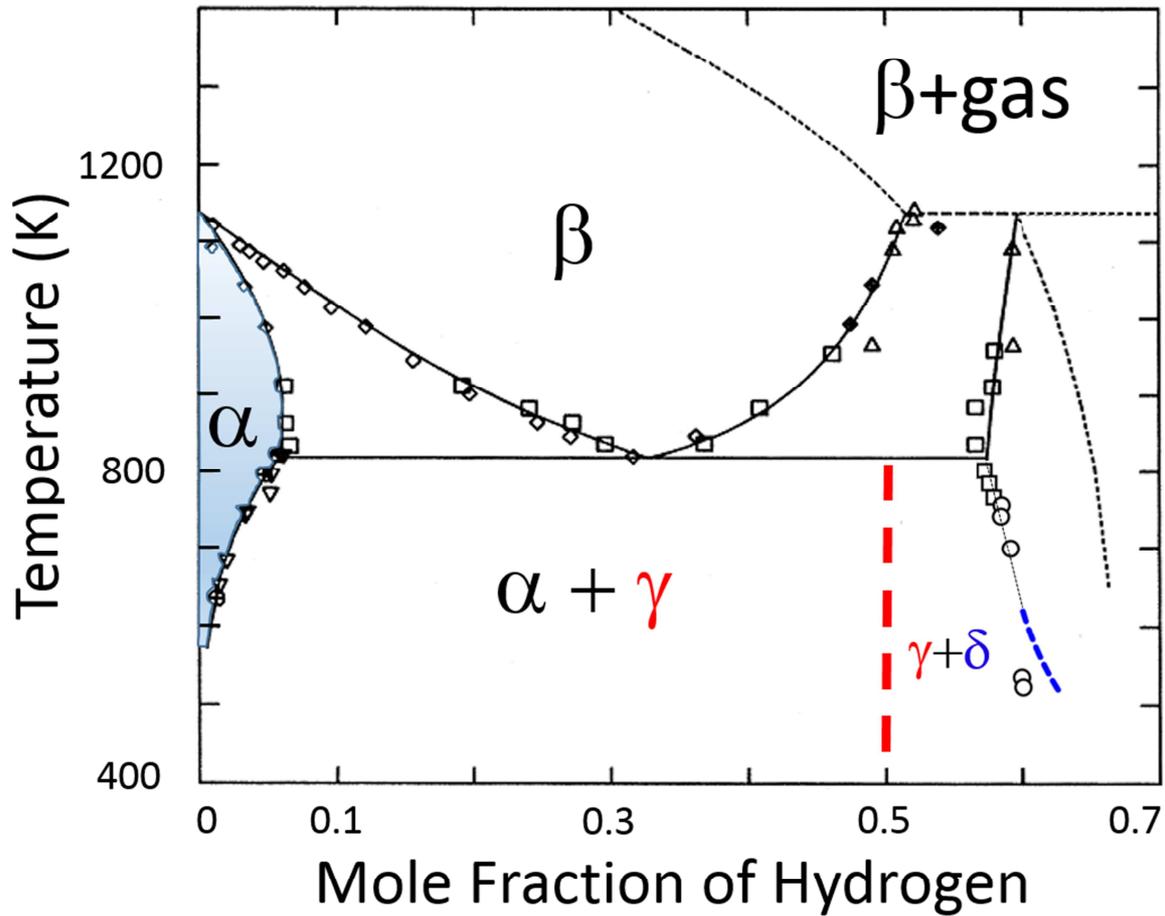


Figure 18: Zirconium-Hydrogen phase diagram based on [66]. The dashed vertical line for 0.5 mole fraction is proposed for γ -hydride (ZrH). The solvus is the equilibrium boundary that separates the shaded region (α), where hydrogen is in solid solution in the α -zirconium matrix, and the region ($\alpha + \gamma$ -hydride), where ZrH hydrides have precipitated in the matrix. Mole fractions about 0.6 are associated with δ -hydrides. The dashed blue curve is the $\gamma + \delta / \delta$ boundary calculated from concentrations of hydrogen in solution in hydrogen clouds that condense to form δ -hydrides (Equation 6). For mole fractions between 0.5 and 0.6, γ -hydride is in equilibrium with δ -hydride. The simultaneous observation of γ -hydrides and δ -hydrides apparently in equilibrium with hydrogen in solution suggests that to satisfy Gibbs' Phase Rule δ -hydrides are surrounded by a layer of γ -hydride.

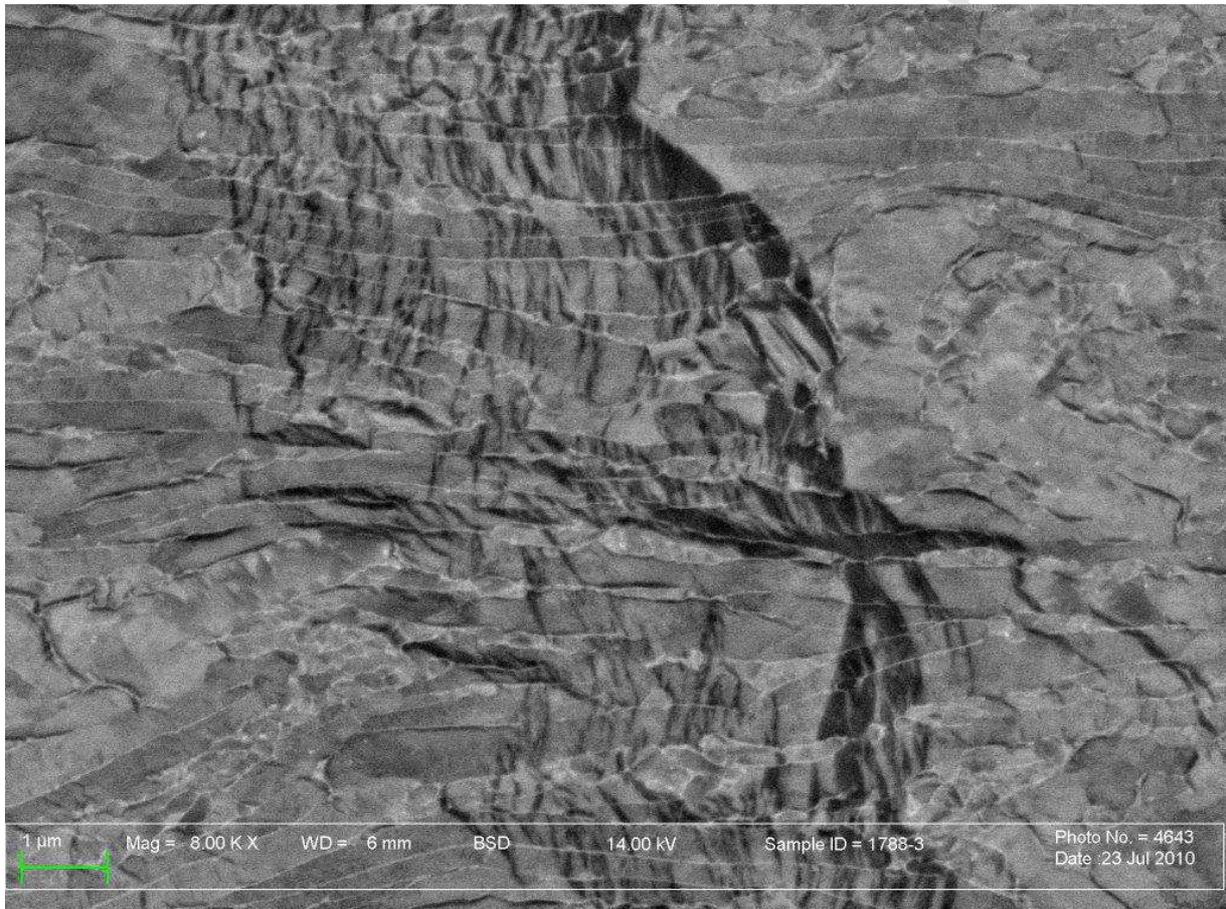


Figure 19: Electron-backscatter SEM micrograph showing ‘black’ hydride platelets forming linear arrays in Zr-2.5Nb [75]. At lower magnification in light microscopy, these platelets appear as single particles.