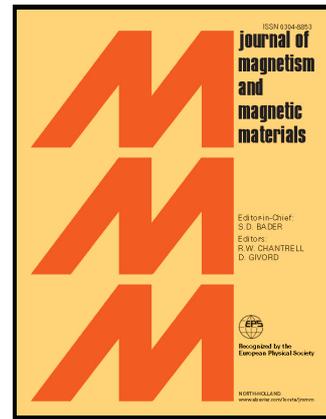


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# Uniaxial anisotropy and low-temperature antiferromagnetism of $\text{Mn}_2\text{BO}_4$ single crystal

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The  $\text{Mn}_2\text{BO}_4$  single crystals have been grown by the flux technique. The careful study of the crystal structure and magnetic properties have been carried out. The antiferromagnetic transition at  $T_N = 26$  K has been traced through the *dc* magnetization and specific heat temperature dependences. The magnetic uniaxial anisotropy has been found with easy axis magnetization lying in the *ab*-plane. A reduction of the effective magnetic moment value is assigned to the non-quenched orbital moment of Jahn-Teller  $\text{Mn}^{3+}$  ions. The discussion of magnetic properties is based on the superexchange interaction calculations.

**Keywords:** antiferromagnets, oxides, magnetic anisotropy, exchange interactions

**PACS:** 75.50.Ee, 75.30.Gw, 78.70.Dm, 75.30.Et

## 1. Introduction

It is well known that low dimensionality in crystal and magnetic structure plays an important role in the physics of magnetic crystals. The experimental and theoretical investigations have revealed properties of the materials with low dimensionality to be quite different from their bulk analogues. This difference results in the rich variety of phases and phase transitions caused by high degree of degeneracy and extraordinary sensitivity to external influences. From this point of view the borates of transition and rare-earth metals with quasi-low dimension crystal structure and unique magnetic and optic properties are the perspective objects for the fundamental and practical investigations. These materials form a wide class of narrow-band oxide semiconductors intensely studied recently [1-5].

The oxyborates  $\text{M}^{2+}\text{M}^{3+}\text{BO}_4$  with the warwickite structure attract attention due to a large number of isomorphous substitutions. There is a large variety of natural and synthetic warwickites containing rare-earth, alkaline earth and transition metal ions ( $\text{M}^{2+} = \text{Mg}, \text{Co}, \text{Mn}, \text{Fe}, \text{Ni}$ , and  $\text{M}^{3+} = \text{Ti}, \text{V}, \text{Cr}, \text{Fe}, \text{Mn}, \text{In}, \text{Lu}, \text{Yb}, \text{Tm}$ ) [6-8]. The metal ions occupy two structurally distinct octahedral sites usually labeled as

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1 and 2. Four octahedra linked by sharing edges to form the *row* of 2-1-1-2. The *rows* are connected by sharing edges forming quasi low-dimensional *ribbons* extending along crystalline *c*-axis. The heterometallic warwickites ( $\text{M}^{2+} \neq \text{M}^{3+}$ ) are naturally disordered materials since each cation site may be occupied by any one of the two metals. Most hetero-metallic warwickites show typical spin-glass transition [6, 9].

Recently, we have performed the crystal structure, magnetic and electronic studies of  $\text{Mg}_{1-x}\text{Co}_x\text{BO}_4$  ( $x=0.0, 0.5, 1.0$ ) single crystals [10-13]. Mössbauer and magnetization studies have shown spin-glass behavior and quantum entanglement behavior  $\chi(T) \propto T^{-\alpha(T)}$  above  $T_{SG}$ . The Co induced magnetocrystalline anisotropy increases the magnetic viscosity of the magnetic lattice, by freezing magnetic fluctuations below  $T_{SG}$ . On the contrary, the introduction of Cobalt does not alter transport properties radically.

Only two homometallic warwickites ( $\text{M}^{2+} = \text{M}^{3+}$ ) are available now:  $\text{Fe}_2\text{BO}_4$  and  $\text{Mn}_2\text{BO}_4$  [14, 15]. Both compounds display the charge ordering (CO). The nature of CO in the warwickites is the subject of hot discussions. The temperature dependence of CO in  $\text{Fe}_2\text{BO}_4$  was extensively investigated by resistivity and differential scanning calorimetry measurements, Mössbauer spectroscopy, synchrotron x-ray scattering, transmission electron

microscopy, and electronic-structure calculations [16-19]. It is supposed that the low-temperature phase ( $T_{CCO} < 280$  K) is a commensurately charge ordered with integer iron valence separation  $Fe^{2+}$  and  $Fe^{3+}$  alternating in the  $a$ -axis direction. The intermediate temperature range ( $T_{CCO} < T < T_{CO}$ , where  $T_{CO} = 340$  K) is characterized by the onset of the temperature-dependent lattice incommensurate CO accompanying by coexisting mobile and immobile carriers. There is a valence fluctuating state ( $Fe^{2+} - Fe^{3+}$  electron hopping) in the high-temperature interval ( $T > T_{CO}$ ) where the structural transformation from monoclinic  $\rightarrow$  orthorhombic symmetry takes place. In  $Mn_2BO_4$  the CO appears to be related to the strong Jahn-Teller distortion of the  $MnO_6$  octahedra. The CO of the kind  $Mn^{2+}(2)-Mn^{3+}(1)-Mn^{3+}(1)-Mn^{2+}(2)$  and relevant orbital ordering ( $d_z^2$ ) occurs. From the magnetic point of view the  $Fe_2BO_4$  was found to be a  $L$ -type ferrimagnet with the transition temperature  $T_N = 155$  K [20]. As for the  $Mn_2BO_4$ , the situation is more intriguing. Nowadays this compound is known in three forms: single crystals [15], powder polycrystals [21-23], and necklace-like nanofibres [24]. The magnetic characterization has been carried out for two first forms  $Mn_2BO_4$  and the results obtained are dramatically controversial. On one hand, the magnetization, the specific heat, and ESR studies of polycrystalline samples have revealed the antiferromagnetic transition at  $T_N = 104$  K and weak ferromagnetism below 70 K. Recent neutron diffraction data have shown the occurring the long-range antiferromagnetic order only below 26 K, while the ferrimagnetic transition at 42 K was found from the magnetization measurements. From the other hand, the weak anomaly at  $\sim 25$  K was observed from the magnetic susceptibility measurements performed on the single crystals. The reason of this dramatic disagreement probably lies in the samples quality. The authors of [21-23] marked the presence of magnetic impurities in the form of  $Mn_2O_3$  and  $Mn_3O_4$  oxides.

Thus, there is no clear understanding of either type of magnetic order or the temperature of magnetic phase transition in  $Mn_2BO_4$ . This paper reports first magnetization and specific heat measurements carried out on the  $Mn_2BO_4$  single crystals. The experimental observation of magnetic phase transition at  $T_N = 26$  K strongly supports the neutron diffraction results. The long-range antiferromagnetic order occurs below  $T_N$ . The magnetic measurements performed for two directions of the applied field relative the crystalline  $c$ -axis allowed to reveal the uniaxial anisotropy. Based on the superexchange interactions analysis the magnetic behavior is explained and possible spin configuration for the ordered state of  $Mn_2BO_4$  is offered.

## 2. Experimental procedure

The solid state reaction method was found to give rise the difficulties in the preparing of pure samples [21-23]. The main synthesis problem relates to the existence of concurring phases with different crystal structures. This problem have been discussed in detail in the well known systematic work by Capponi [7], where it has shown that attempts to grow oxyborates  $Co^{2+}Ga^{3+}BO_4$ ,  $Co^{2+}Cr^{3+}BO_4$ ,  $Co^{2+}Sc^{3+}BO_4$  with the warwickite structure have led to concomitant ludwigite phases  $Co^{2+}_2Ga^{3+}BO_5$ ,  $Co^{2+}_2Cr^{3+}BO_5$ ,  $Co^{2+}_2Sc^{3+}BO_5$ . Due to this reason the exact parameters of growing process are of great importance for the successful preparation of single-phase material. At present work these parameters were defined after some probe reactions and X-ray diffraction control.

The solution has been made by the step by step melting of  $B_2O_3$  oxide (6.9 g),  $Bi_2Mo_3O_{12}$  (51 g),  $Mn_2O_3$  (17.7 g) and  $Na_2CO_3$  (4.1 g) at  $T_1 = 1100^0$  C during 3 hours. Then the temperature was rapidly lowered to  $T_2 = 970^0$  C followed by a slow cooling at a rate of  $4^0$  C a day. In two days the crucible was pulled out from the furnace and the solution was removed. Single crystals spontaneously formed on the walls of the crucible were rinsed with the aqueous nitric acid at room temperature. The crystals were in the form of black needles up to 12 mm long, and the cross sectional area was smaller than  $1.0 \times 0.5$  mm.

The room temperature X-ray diffraction measurements were carried out using X-ray diffractometer SMART APEX II (MoK $\alpha$  radiation, CCD detector).

The field magnetization was measured using the handmade vibrating samples magnetometer (VSM) at the International Laboratory of High Magnetic Fields and Low Temperatures (Wroclaw, Poland). The  $dc$  magnetization has been measured as function of the temperature and applied magnetic field up to 140 kOe. The temperature interval was 1.8 - 300 K. The measurements were carried out for two directions of the external magnetic field relative to the crystallographic  $c$ -axis, which coincides with the needle's axis. The holder contribution was subtracted from the integral signal and the corrections associated with form anisotropy were taken into account.

The specific heat measurements have been done by the relaxation method on commercial PPMS Quantum Design platform in the entire temperature interval ( $T = 2-300$  K). The experimental error didn't exceed 1% for all temperatures.

## 3. Experimental results

### 3.1. X-ray diffraction and normal coordinates calculation

In this section, we present some crystallographic data, which are relevant for theoretical discussion below. The  $Mn_2BO_4$  has a monoclinic unit cell ( $P2_1/n$  space group), with the angle  $\beta \approx 90.751^0$  slightly different from  $90^0$  (Table 1). No impurity phases have been detected by means of X-ray diffraction. All parameters are in good agreement with those reported earlier [15, 23]. The metal ions have two distinct positions labeled as 1 and 2, which are at general  $4e$  Wyckoff positions, oxygen atom has four distinct positions and boron have only one position. The

atomic coordinates, isotropic displacement parameters, selected bond lengths and angles are listed in the Supplemental Materials (SM) Tables SM1 - SM3 [25].

The Mn1O<sub>6</sub> octahedron is considerably smaller than the Mn2O<sub>6</sub> one as deduced from the average <M-O> bond length (2.065 instead 2.210 Å). The smaller <M - O> distances lead to increasing oxidation state and can indicate that the Mn<sup>3+</sup> ions prefer the M1O<sub>6</sub> octahedra, while Mn<sup>2+</sup> occupies the M2O<sub>6</sub> ones. As it was expected the shortest distances (less than 1.5 Å) are

**Table 1.** Crystal data and structure refinement of Mn<sub>2</sub>BO<sub>4</sub>.

Empirical formula	Mn <sub>2</sub> BO <sub>4</sub>
Formula weight (g mol <sup>-1</sup> )	184.69
Crystal system	monoclinic
Space group	<i>P2<sub>1</sub>/n</i>
Unit cell parameters (Å, deg)	
<i>a</i>	9.2934(5)
<i>b</i>	9.5413(5)
<i>c</i>	3.2475(2)
$\beta$	90.7510(10)
Unit cell volume (Å <sup>3</sup> )	287.93(3)
Z	4
Calculated density (g cm <sup>3</sup> )	4.26023
Radiation	MoK $\alpha$
Wavelength, $\lambda$ (Å)	0.71073
Temperature (K)	296
Crystal shape	Needle (along <i>c</i> )
Abs. coefficient (mm <sup>-1</sup> )	8.581
F(000)	348
$\Theta$ range (deg)	3.06 - 34.00
Limiting indices	-14 $\leq h \leq$ 14 -14 $\leq k \leq$ 14 -5 $\leq l \leq$ 4
Reflections collected	4701
Reflections independent	1157
Data / restraints / parameters	1157 / 0 / 65
Extinction coefficient	0.200(4)
GooF	1.173
Final <i>R</i> indices	
<i>R</i> 1	0.0184
<i>wR</i> 2	0.0422
<i>R</i> indices (all data)	
<i>R</i> 1	0.0199
<i>wR</i> 2	0.0428

B - O inside the BO<sub>3</sub> triangle, which is the most tightly bound group in oxyborate structures.

The Mn<sup>2+</sup> and Mn<sup>3+</sup> distribution over the metallic sites can be studied by means of bond valences sums (BVS) calculation [26]. These empirical estimations predict atomic charges of 3.20/2.95 for Mn1 and 2.01/1.85 for Mn2, when bond valence parameters are related to Mn<sup>2+</sup>/Mn<sup>3+</sup>. So, there is a clear propensity of Mn<sup>3+</sup> to occupy the site 1 with atomic charge 2.95, while for Mn<sup>2+</sup> it is the site 2 (atomic charge 2.01). The obtained values are in agreement with the BVS calculation results reported by Norrestam [15] confirming that Mn<sub>2</sub>BO<sub>4</sub> is a transition metal oxyborate with the explicit charge ordering. The BVS value for the boron atom was found to be 2.96 close to the formal valence 3+.

Both Mn1O<sub>6</sub> and Mn2O<sub>6</sub> octahedra are distorted. The distortions of the coordination octahedra can be described by the normal coordinates  $Q_\alpha$  ( $\alpha = 1, 2, \dots, 3N-3$ ;  $N$  – number of ligands), which are linear combinations of the Cartesian coordinates of oxygen, and classified according to the irreducible representations of the coordination complex symmetry (Tables 2), in terms of the  $O_h$  symmetry group (Table SM4 [25]). The  $Q_1$  coordinate describes high-symmetry distortions like the breathing-mode. The other normal coordinates correspond to the low – symmetry distortions like the Jahn-Teller (JT) ( $Q_2$  and  $Q_3$ ) and trigonal ( $Q_4$ ,  $Q_5$ ,  $Q_6$ ) ones. The  $Q_3$  coordinate presents tetragonal octahedral distortion along the  $z$  – axis, whereas the  $Q_2$  ones corresponds to the distortions with rhombic symmetry. The observed JT distortion is a combination of the normal modes  $Q_1$ ,  $Q_2$ ,  $Q_3$ . There are a larger axial elongation of the Mn1O<sub>6</sub> octahedron along the O1-Mn1-O3 axis with the average axial radii 2.325 Å and the compression of the other four Mn1-O bonds (the average planar radii is 1.935 Å), which suggests a  $d_z^2$  orbital

ordering at the Mn1 site as will be discussed below. Contrary, the bonds distribution in Mn<sub>2</sub>O<sub>6</sub> is so that two long bonds (O1, O4) and two medium bonds (O2, O3) are roughly coplanar with an average radius of 2.238 Å, while two remain short bonds (O2, O4) are axial with the average radii 2.155 Å (see Fig. SM1 and Table SM3 [25]). It can be noted that both normal coordinates  $Q_2, Q_3$  are considerably prevailing for M1 site, testifying the pronounced JT distortion of Mn1O<sub>6</sub> octahedron. The trigonal distortions are comparable for both types of the octahedra.

The electrical field gradient (EFG) generated by the oxygen octahedron on the metal sites M1 and M2 is a tensor value  $G_{\alpha\beta}$ . The main component  $V_{zz}$  of the  $G_{\alpha\beta}$  has been calculated and the obtained values are 0.42 and 0.11 e·Å<sup>-3</sup> for Mn1 and Mn2 sites, respectively. Thereby, the Mn1O<sub>6</sub> octahedron was found to be ~4 times more distorted than Mn<sub>2</sub>O<sub>6</sub> one. The EFG principal axis lies along the M1 – O1 (2.379 Å) and M2 – O2 (2.088 Å) bonds. The EFG principal axes of Mn2 - Mn1 pair are parallel and antiparallel to that of neighbor Mn1-Mn2 pair (Fig. SM1 [25]). This indicates the inversion of the principal axis in the ribbon substructure.

The main results of the structural study on Mn<sub>2</sub>BO<sub>4</sub> may be written as follows: i) the trivalent and divalent Mn ions occupy the M1 and M2 sites, respectively, that leads to the charge ordering in the row Mn<sup>2+</sup>(2)-Mn<sup>3+</sup>(1)-Mn<sup>3+</sup>(1)-Mn<sup>2+</sup>(2); ii) the  $Q_2$  and  $Q_3$  dominated modes corresponding to the JT distortions are significantly pronounced for Mn1O<sub>6</sub> octahedra; iii) strong JT distortion of Mn1O<sub>6</sub> octahedra suggests a  $d_z^2$  orbital at the Mn1 site; and iv) there is an inversion center of the principal axis of octahedra at the center of the row.

**Table 2.** The normal coordinates and ligand's displacement (Å) for metal ions in the M1O<sub>6</sub> and M2O<sub>6</sub> octahedral complexes. The  $R_0$  is the M - O distance in the undistorted octahedron, that are accepted such in order to provide a zero value of  $Q_1$ .  $R_0$  is 2.054 and 2.092 Å, for Mn1 and Mn2 respectively.

Normal coordinates	Mn1		Mn2	
	normal coordinate	displacement	normal coordinate	displacement
$Q_2$	-0.3937	-0.1968	0.0330	0.0165
$Q_3$	-0.2122	-0.0919	0.0828	0.0358
$Q_4$	-0.3347	-0.1674	-0.2095	-0.1048
$Q_5$	-0.2045	-0.1023	-0.4691	-0.2345
$Q_6$	-0.2612	-0.1306	-0.2403	-0.1201
$Q_7$	0.0828	0.0414	-0.0703	-0.0351
$Q_8$	0.1464	0.0732	-0.4739	-0.2369
$Q_9$	-0.0688	-0.0344	-0.2562	-0.1281
$Q_{10}$	-0.0485	-0.0343	-0.0556	-0.0393
$Q_{11}$	0.0835	0.0590	-0.2871	-0.2030
$Q_{12}$	-0.0225	-0.0159	-0.0565	-0.0399
$Q_{13}$	0	0	0	0
$Q_{14}$	-0.0284	-0.0142	0.0679	0.0339
$Q_{15}$	-0.0371	-0.0185	-0.1763	-0.0881

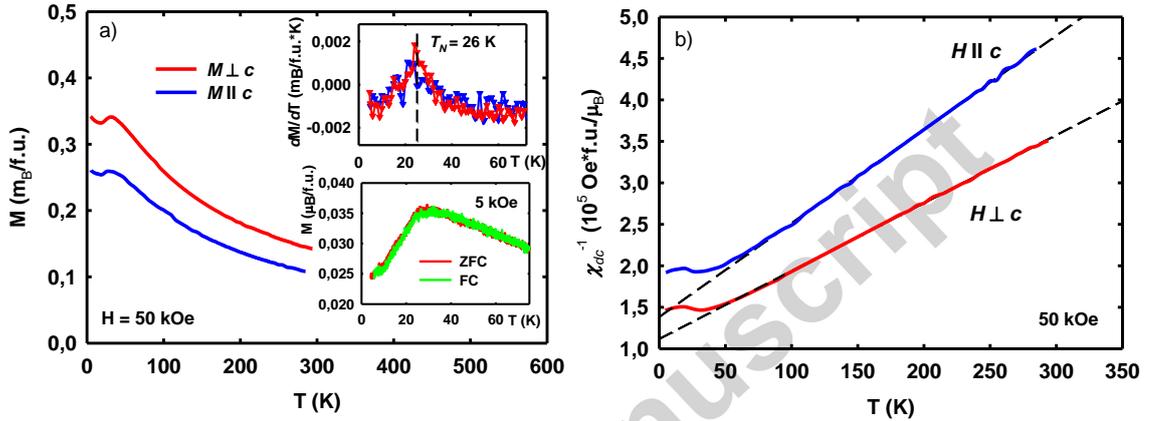
### 3.2 *dc* Magnetization

Figure 1(a) shows the magnetization curves as functions of temperature, measured with the applied field perpendicular and parallel to the *c*-axis. It can be seen that the homometallic manganese warwickite is an antiferromagnet with its easy axis of the magnetization perpendicular to the crystalline *c*-axis. Broad maxima near 30 K are pronounced. In the top inset the dependences of the derivative  $dM/dT$  as function of the temperature appear for both directions of the applied field. From these curves we have obtained  $T_N = 26$  K in agreement with the data [15, 23]. In the bottom inset a zoom of the field-cooled (FC) and zero-field-cooled (ZFC) *dc* magnetization curves as a function of temperature for the applied field perpendicular to the *c*-axis are shown. We note that no thermo-irreversibility between the FC and ZFC curves occurs below a critical temperature, that allows suggesting the antiferromagnetic spin arrangement in Mn<sub>2</sub>BO<sub>4</sub>.

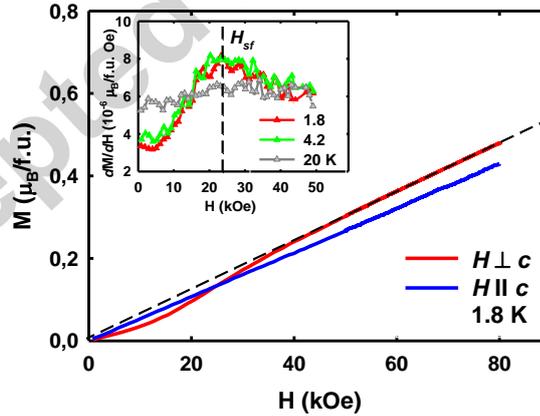
Figure 1(b) shows the linearization of the inverse *dc* susceptibility ( $1/\chi_{dc}$ ). The Curie-Weiss law is obeyed within an extensive temperature range. The Curie-Weiss temperatures were found to be  $\theta = -118$  K and  $-134$  K for the applied field parallel and perpendicular to *c*-axis, respectively. The temperatures are negative strongly supporting the antiferromagnetic interactions as dominant. We note that this result is contrary to the reported data [22], where the positive value of Curie-Weiss temperature has been found. The ratio  $\frac{\theta}{T_N} \approx 5$  indicates the presence of disordering components in the magnetic coupling network. The effective magnetic moments per formula unite obtained from Curie-Weiss constants were found to be 6.25 and 6.95  $\mu_B$  for the parallel and perpendicular directions of the applied field, respectively. Assuming that both Mn ions are in the high-spin state we calculated the spin component of the effective moment neglecting the orbital component. Accounting for the contribution of each type of Mn ions, the spin component is given by  $\mu_s^2 = \sum_i g_i^2 S_i(S_i + 1)$ . The effective moment per formula unit with one divalent ( $S = 5/2$ ) and one trivalent ( $S = 2$ ) Mn ions and  $g = 2$  is  $\mu_s = 7.68 \mu_B$ . This value is larger than that

experimentally finding. The effective magnetic moment per formula unit taking into account the orbital contribution is expressed by  $\mu_J^2 = \sum_i g_i^2 J_i(J_i + 1)$ . We have estimated the value of  $\mu_J$  using the results of work [27], where the orbital magnetism has to be taken into account in the description of electron level energies in the  $3d$ -ion compounds. For  $\text{Mn}^{3+}$  ion ( $d^4$ )  $J = 1$  and  $g = 1.1$ , and for  $\text{Mn}^{2+}$  ion ( $d^5$ ) it is  $J = 5/2$  and  $g = 2$ . The obtained value is  $\mu_J = 6.12 \mu_B$ . The result supposes that the orbital moments of  $\text{Mn}^{3+}$  ions are not quenched and contribute to the observed magnetic moment. This result also supports the data of neutron diffraction [23], showing the considerably reduced  $\text{Mn}^{3+}$  magnetic moments  $\mu = 1.0 \mu_B$  relative spin values.

Magnetization as a function of applied magnetic field was measured in the temperature range 1.8 – 75 K for both directions of external field. We note that the curves do not display the saturation up to 140 kOe. The isotherms of magnetization at 1.8 K vs applied field are plotted in Fig.2. The magnetization isotherm measured with applied field perpendicular to  $c$ -axis shows the inflection point at the field  $H_{sf} = 24$  kOe, which can be determined as the maxima in the derivative function plotted in the coordinates of  $dM/dH$  vs  $H$  (top inset). The derivatives of the isotherms measured at 4.2 and 20 K are displayed also. As the temperature increases the curve becomes smooth, nevertheless, the transition can be observed right up to 20 K. We identified the critical field corresponding to the maxima as a spin-flop field.



**Fig. 1.** a) The temperature dependencies of  $dc$  magnetization of  $\text{Mn}_2\text{BO}_4$  single crystal measured in applied field of 50 kOe directed along two orthogonal directions: parallel ( $H \parallel$ ) and perpendicular ( $H \perp$ )  $c$ -axis. The top inset shows the peak of the derivative  $dM/dT$  corresponding to the critical temperature  $T_N$ . The bottom inset is the field-cooled and zero-field-cooled magnetization curves measured for the applied field perpendicular to the  $c$ -axis. b) The inverse susceptibility as a function of the temperature at  $H = 50$  kOe.



**Fig. 2.** The field dependences of  $\text{Mn}_2\text{BO}_4$  magnetization for two orthogonal directions of the

The magnetization isotherms measured for the applied field parallel to  $c$ -axis do not show any peculiarities pointing out the easy axis of magnetization lies in the  $ab$  plane, which confirms the results of the magnetization measurements as temperature function.

### 3.3. Specific heat

Further evidence for AF transition is obtained from the specific heat data. The specific heat measurement data at  $H = 0$  are shown in Fig. 3(a), where the specific-heat curve is plotted in the coordinates  $C/T$  versus  $T$ . One can clearly see a feature at the magnetic ordering temperature  $T_N^* = 23$  K. We note that the specific heat magnitude of  $\text{Mn}_2\text{BO}_4$  is higher than those of  $\text{MgScBO}_4$  in wide temperature range [22], which has not the magnetic contribution to the specific heat. Our attempts to fit the low-temperature data range by the power law  $C/T = \gamma + \beta T^2$  result in

the following fitting parameters:  $\gamma = 2.52 \text{ mJ/mol}\cdot\text{K}^2$  and  $\beta = 9.54 \text{ mJ/mol}\cdot\text{K}^4$ . The linear term turns out to be of the same order of magnitude as for the related ludwigites  $\text{Co}_3\text{BO}_5$  and  $\text{Co}_2\text{FeBO}_5$  (3.30 and  $3.28 \text{ mJ/mol}\cdot\text{K}^2$ , respectively) [28]. Note that our attempts to measure the transport properties of  $\text{Mn}_2\text{BO}_4$  single crystal have not been successful due to extremely large resistance of the sample ( $>10^8 \text{ Ohm}$  at room temperature). Taking into account the insulating nature of all mention materials the question about the origin of this term remains open. The  $\beta T^3$  is the contribution due to three-dimensional phonons in the Debye model. The application of this simplified model for the description of the low-temperature data of the specific heat gets too low value of effective Debye temperature than that is expected for an oxyborate rigite structure. So, for correct description critical behavior of the specific heat and for an anomalous part separation, it is necessary to consider other contributions to the specific heat.

The specific heat of a crystalline solid can be expressed by the sum of three main contributions:

$$C_V = C_V^{latt} + C_V^{mag} + C_V^{Sch}, \quad (1)$$

where  $C_V^{latt}$  is the lattice vibration contribution,  $C_V^{mag}$  is the magnetic contribution, and  $C_V^{Sch}$  is the Schottky contribution. The crystal defects, anharmonicity effect, and free electrons contributions are small and can be neglected. The difference between  $C_V$  and  $C_p$  can be evaluated by the thermodynamic relationship, which requires knowledge of thermal expansion coefficient, material's volume, and isothermal compressibility. However, the difference between  $C_V$  and  $C_p$  was shown to be important only at high temperatures [29]. In order to quantitatively estimate the critical behavior near  $T_N$  the anomalous contribution of the specific heat  $\Delta C_V = C_V^{mag} + C_V^{Sch}$  was separated from the measured dependence of the specific heat by subtracting of the regular lattice contribution  $C_V^{latt}$ . The latter can be expressed using simple model including Debye and Einstein approaches. The lattice contribution to the specific heat given by the equation:

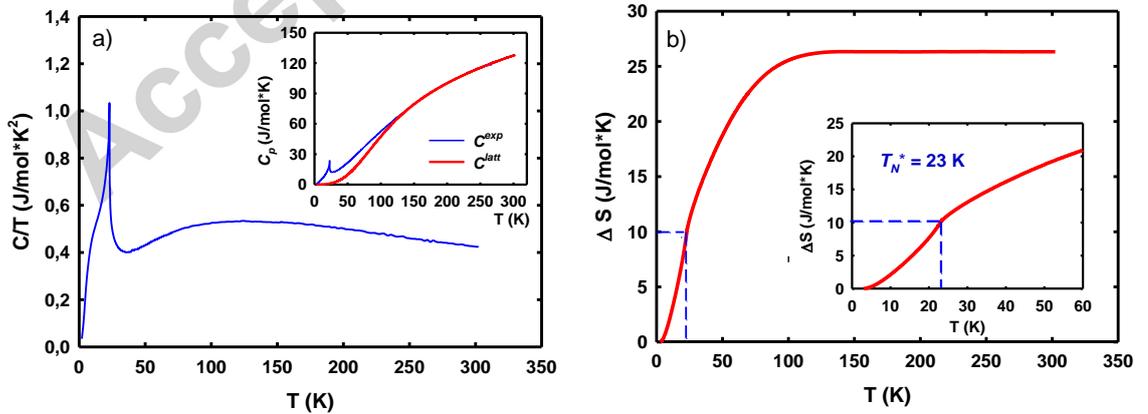
$$C_V^{latt}/R = K_D D (\Theta_D/T) + K_E E (\Theta_E/T), \quad (2)$$

$$D (\Theta_D/T) = 9 \frac{1}{(\Theta_D/T)^3} \int_0^{\Theta_D/T} \frac{(\Theta_D/T)^4 \exp(\Theta_D/T)}{[\exp(\Theta_D/T) - 1]^2} d(\Theta_D/T),$$

$$E (\Theta_E/T) = 3 (\Theta_E/T)^2 \frac{\exp(\Theta_E/T)}{[\exp(\Theta_E/T) - 1]^2}$$

is shown in the inset fig.3a. Here,  $R$  is the gas constant,  $\Theta_D$ ,  $\Theta_E$  is characteristic Debye and Einstein temperatures, the  $K_D$ ,  $K_E$  are numerical coefficients. The fit in the temperature range  $T > 130 \text{ K}$  gives follow estimations of parameters  $\Theta_E = 695 \text{ K}$ ,  $\Theta_D = 299 \text{ K}$ . The obtained value of  $\Theta_D$  is well agreed with that for  $\text{MgScBO}_4$  ( $\Theta_D = 306 \text{ K}$ ).

The non-lattice contribution to the entropy ( $\Delta S$ ) including the magnetic ( $\Delta S_{mag}$ ) and Schottky ( $\Delta S_{Sch}$ ) entropies is presented in fig.3b. The full magnetic ordering could accompanied by the entropy released of  $\Delta S_{mag} = R[\ln(2S1 + 1) + \ln(2S2 + 1)] = 28.278 \text{ J/mol}\cdot\text{K}$  expected for one  $\text{Mn}^{3+}$  ( $S1 = 2$ ) and one  $\text{Mn}^{2+}$  ( $S2 = 5/2$ ) ions per formula unite. The entropy at the critical temperature is being  $\Delta S(T_N) = 10.06 \text{ J/mol}\cdot\text{K}$ , that is less than half of the theoretical limit of magnetic entropy  $\Delta S_{mag}$ . Thus, at the temperatures well above  $T_N$  the magnetic entropy is



**Fig. 3.** a) Specific heat of  $\text{Mn}_2\text{BO}_4$  plotted as  $C/T$  versus  $T$ . The inset: experimental specific heat (blue circle) and the lattice contribution to the specific heat obtained by fitting to eq. (2) (red solid line). b) Entropy as a function of temperature. The inset: the zoom of the magnetic transition range,  $S(T_N) = 10.06 \text{ J/mol}\cdot\text{K}$ .

associated with the retention of short-range magnetic order in the magnetic spin system. As the temperature increase the magnetic correlations vanish. This fact is consistent with the magnetization data and theoretical calculation of the superexchange interactions.

#### 4. Uniaxial anisotropy and exchange interactions

The experimental data have shown that  $\text{Mn}_2\text{BO}_4$  can be considered as standard uniaxial antiferromagnet with easy axis of magnetization lied at the crystallographic  $ab$  plane. We have estimated the anisotropy constant  $K$  and anisotropy field  $H_a$  values in  $\text{Mn}_2\text{BO}_4$ :

$$\begin{aligned} K(T) &= \frac{1}{2} H_{sf}^2 (\chi_{\perp} - \chi_{\parallel}), \\ H_a &= \frac{K}{M_s} \end{aligned} \quad (3)$$

where  $\chi_{\perp}$  and  $\chi_{\parallel}$  are the experimental values of magnetic susceptibilities above and below critical field  $H_{sf}$ ,  $M_s$  is the sublattice magnetization. Assuming that the average spin per formula unite is  $\langle S \rangle = \frac{1}{n} \sum_{i=1}^n S_i = 2.25$ , where  $n$  denotes the number of magnetic ions per formula unit, the obtained value is  $K(1.8 \text{ K}) = 48.03 \text{ erg/cm}^3$ , which corresponds to  $H_a = 165 \text{ Oe}$ . These values are in a good agreement with that reported earlier for  $\text{Mn}_2\text{B}_2\text{O}_5$  pyroborate, where only one type of manganese ions presents [30]. The exchange field acting along crystalline  $c$ -axis was found to be  $H_{ex\parallel} = 834 \text{ kOe}$ , while the exchange field inside  $ab$ -plane is  $H_{ex\perp} = 766 \text{ kOe}$ .

In a molecular field approximation for a two-sublattice model with one exchange interaction  $J$ , the exchange parameter and the Neel temperature are related by simple expression

$$z|J| = \frac{3k_B}{2S(S+1)} T_N, \quad (4)$$

where  $z$  is the number of nearest neighbors with the exchange interaction  $J$ ,  $k_B$  is the Boltzmann constant. Putting the values of  $T_N = 26 \text{ K}$  and average spin, we get  $z|J| = 5.33 \text{ K}$ .

The consistent approach to analysis of the magnetic behavior of  $\text{Mn}_2\text{BO}_4$  requires calculating the superexchange interaction. We note that the estimations of the superexchange interactions have been made earlier in the work [23], but the interaction through  $t_{2g}$ -orbitals wasn't taken into account, along with the interribbon interactions. We present the deep analysis of superexchange interaction in  $\text{Mn}_2\text{BO}_4$ , considering all nonequivalent superexchange pathways of ferromagnetic and antiferromagnetic nature. That allowed to explain observed magnetic behavior and to offer a scenario of the magnetic ordering in  $\text{Mn}_2\text{BO}_4$ .

The inter-ion distances inside the ribbon are the order of  $3 \text{ \AA}$  as can be seen from the crystallographic data. Namely, the shortest is  $\text{Mn}^{3+}\text{-Mn}^{3+}$  ( $2.84 \text{ \AA}$ ), and the longest is  $\text{Mn}^{2+}\text{-Mn}^{3+}$  ( $3.36 \text{ \AA}$ ). That is too long for a direct orbital overlapping. The anisotropy energy is much smaller than the exchange one ( $\sim 0.25 \text{ K}$  versus  $\sim 5 \text{ K}$ ). We have used the simple model of superexchange interactions [31] applied earlier to the analysis of the complex magnetic structure in  $\text{Co}_3\text{O}_2\text{BO}_3$ ,  $\text{Co}_2\text{FeO}_2\text{BO}_3$  ludwigites [1, 5], and  $\text{Co}_3\text{B}_2\text{O}_6$  kotoites [32], with a satisfactory agreement with the experimental results. Manganese warwickite  $\text{Mn}_2\text{BO}_4$  belongs to the related family of oxyborate that justifies the analogous consideration. The calculation is restricted by the nearest-neighbor approximation; i.e. only the interactions along the short M-O-M bonds are considered, while the long bonds M-O-M-O-M and M-O-B-O-M are neglected. The ferromagnetic (F) and antiferromagnetic (AF) contributions to Mn-O-Mn couplings exist. Orbitally non-generate  $\text{Mn}^{2+}$  states ( $d^5$ ) have singly occupied  $e_g$  orbitals, that supposes the antiferromagnetic exchange interaction to be dominant. The  $\text{Mn}^{3+}$  states ( $d^4$ ) have one  $e_g$  hole at  $d_{x^2-y^2}$  orbital, that leads to ferromagnetic (F) contributions to the exchange integrals.

The  $\text{Mn}_2\text{BO}_4$  warwickite structure has several types of indirect couplings:  $92^\circ$ ,  $95^\circ$ - $99^\circ$ ,  $102^\circ$ , and  $105^\circ$ , which can be assigned to  $90^\circ$  exchange interactions, as well as  $115^\circ$ ,  $119^\circ$  and  $125^\circ$  exchange interactions. In the 2-1-1-2 row the neighboring cations with common octahedral edges take part in the exchange couplings with bond angles of  $99^\circ$ - $105^\circ$  ( $J1$ ) and  $97^\circ$  ( $J2$ ). The octahedra belonging to the adjacent rows, which are connected by a common edge, allow indirect couplings  $92^\circ$ - $105^\circ$  ( $J3$ ),  $96^\circ$ - $102^\circ$  ( $J4$ ),  $95^\circ$  ( $J5$ ), and  $89^\circ$ - $102^\circ$  ( $J6$ ). The octahedra connected by a common oxygen ion and belonging to the adjacent ribbons allow indirect couplings of  $115^\circ$ ,  $119^\circ$ , and  $125^\circ$ , corresponding to  $J7$ ,  $J8$ , and  $J9$  exchange interactions respectively. So, the magnetic structure of  $\text{Mn}_2\text{BO}_4$  can be described by nine exchange integrals  $J1$ - $J9$ , where  $J1$ - $J6$  are intra-ribbon interactions, while  $J7$ - $J9$  are inter-ribbon ones. The full set of the orbitals pairs participating in the coupling is presented in Table SM5 [25]. The total integral of cation-cation exchange interaction  $J$  can be calculated as a sum of individual orbitals exchange integrals

$$J = \frac{1}{4} \sum_{i,j=1}^{5(d)} \sum_{p=1}^3 \frac{1}{S_i S_j} I_{ij}^p, \quad (5)$$

where  $S_{ij}$  - the interacting cations spins; the sum accounts for the five magnetic ion  $d$ -orbitals and three  $p$ -orbitals of the ligand;  $I_{ij}^p$  - the superexchange interaction integral between the individual orbitals  $i, j$  of two cations via oxygen  $p$  orbital. Interactions between two filled or two empty orbitals are neglected.

Taking into account superexchange bonds selected by lattice symmetry and cation distribution we have been wrote the expressions for the exchange integrals as following:

$$\begin{aligned}
J1 &= -\frac{1}{20}c \left[ \left( \frac{10}{3}b + 2c \right) (U_1 + U_2) - 2bJ_{in} \right] = -4.03 \text{ K}; \\
J2 &= -\frac{1}{16}c \left[ \left( \frac{4}{3}b + 2c \right) (U_1 + U_2) - 4bJ_{in} \right] = -1.44 \text{ K}; \\
J3 &= -\frac{1}{16}c \left[ \left( \frac{13}{3}b + 2c \right) (U_1 + U_2) - bJ_{in} \right] = -6.83 \text{ K}; \\
J4 &= -\frac{1}{16}c \left[ \left( \frac{10}{3}b + 2c \right) (U_1 + U_2) - 2bJ_{in} \right] = -5.03 \text{ K}; \\
J5 &= J4; \\
J6 &= -\frac{1}{25}c \left( \frac{16}{3}b + 4c \right) (U_1 + U_2) = -5.21 \text{ K}; \\
J7 &= -\frac{1}{20} \left( \frac{16}{9}b^2 + 2c^2 \right) (U_1 + U_2) |\cos 119^\circ| = -2.41 \text{ K}; \\
J8 &= -\frac{1}{20} \left[ \left( \frac{4}{9}b^2 + 2c^2 \right) (U_1 + U_2) - \frac{4b^2}{3}J_{in} \right] |\cos 115^\circ| = -0.47 \text{ K}; \\
J9 &= -\frac{1}{20} \left[ \left( \frac{4}{9}b^2 + 2c^2 \right) (U_1 + U_2) - \frac{4b^2}{3}J_{in} \right] |\cos 125^\circ| = -0.65 \text{ K};
\end{aligned}
\tag{6}$$

The factor  $|\cos \theta|$  accounts the angle dependence of the transfer parameters. The basic parameters of the model are the ligand-cation excitation energies  $U$  ( $U_1 = U(\text{Mn}^{3+}-\text{O}) = 5.0$  eV,  $U_2 = U(\text{Mn}^{2+}-\text{O}) = 4.4$  eV), intra-atomic exchange energy  $J_{in}$  ( $J_{\text{Mn}^{3+}} = 3.0$  eV) and electron transfer parameters  $b = 0.02$  ( $\sigma$ -coupling),  $c = 0.01$  ( $\pi$ -coupling) defined in the work [33]. The calculated values are presented also. The integrals  $J5 = J4$  are equivalent because the similar magnetic ions interact through the same electron orbitals. One can note that the exchange integral values are comparable with those  $z|J|$  estimated from the  $T_N$ , assuming  $z = 1$ . The intraribbon interactions ( $J1$ - $J6$ ) are comparative in magnitude and considerably exceed the interribbon ones. The AF intra-row interaction  $J2$  is quenched by ferromagnetic pathway from the  $e_g$  hole on  $d_{x^2-y^2}$  orbitals of  $\text{Mn}^{3+}$  ions. The  $J6$  interaction includes antiferromagnetic superexchange pathways only due to singly occupied five  $d$ -orbitals of  $\text{Mn}^{2+}$ .

To gain insight into the magnetic properties of  $\text{Mn}_2\text{BO}_4$  the division into magnetic sublattices is needed. The number of magnetic sublattices is determined by the different cations number, nonequivalent local cation positions number relative to the principal crystal axes, and interaction sign between the nearest neighbors at last. In  $\text{Mn}_2\text{BO}_4$  the octahedra principal axes have four different directions relative to the cell axes (Fig. SM1). Let warwickite be considered as a magnetic system consisting of eight magnetic sublattices in which crystallographic positions M1 and M2 are divided into four magnetic sublattices:  $1a$ ,  $1b$ ,  $1c$ ,  $1d$  and  $2a$ ,  $2b$ ,  $2c$ ,  $2d$ , that leads to two types of the rows  $2a - 1a - 1b - 2b$  and  $2c - 1c - 1d - 2d$  (Fig. 4).

The exchange interactions parameters calculated with taking into account the nearest neighbors numbers ( $z_{ij}$ ) are collected in Table 3. The mutual orientation of the sublattices magnetic moments is shown by arrows. The exchange integrals of minimum energy correspond to the strongest coupling. As can be seen the strongest interactions are  $2 \cdot J4$  and  $2 \cdot J6$  (via two equivalent pathways,  $z_{ij} = 2$ ) between the manganese ions belonging to the chains  $1a-1c-1a$ ,  $1b-1d-1b$ ,  $2a-2c-2a$ ,  $2b-2d-2b$  extending along  $c$ -axis.

**Table 3.** The exchange interactions integrals (K) in  $\text{Mn}_2\text{BO}_4$  warwickite. The strongest ordering interactions are shown in bold. The disordering interactions are shown in italic.

	<b>1a</b> ↑	<b>1b</b> ↑	<b>1c</b> ↓	<b>1d</b> ↓	<b>2a</b> ↑	<b>2b</b> ↑	<b>2c</b> ↓	<b>2d</b> ↓
<b>1a</b> ↑	0	<i>-1.44</i>	<b>-10.06</b>	<b>-5.03</b>	<i>-4.68</i>	<i>-0.47</i>	<b>-6.83</b>	<b>-2.41</b>
<b>1b</b> ↑	<i>-1.44</i>	0	<b>-5.03</b>	<b>-10.06</b>	<i>-0.47</i>	<i>-4.68</i>	<b>-2.41</b>	<b>-6.83</b>
<b>1c</b> ↓	<b>-10.06</b>	<b>-5.03</b>	0	<i>-1.44</i>	<b>-6.83</b>	<b>-2.41</b>	<i>-4.68</i>	<i>-0.47</i>
<b>1d</b> ↓	<b>-5.03</b>	<b>-10.06</b>	<i>-1.44</i>	0	<b>-2.41</b>	<b>-6.83</b>	<i>-0.47</i>	<i>-4.68</i>
<b>2a</b> ↑	<i>-4.68</i>	<i>-0.47</i>	<b>-6.83</b>	<b>-2.41</b>	0		<b>-10.42</b>	
<b>2b</b> ↑	<i>-0.47</i>	<i>-4.68</i>	<b>-2.41</b>	<b>-6.83</b>		0		<b>-10.42</b>
<b>2c</b> ↓	<b>-6.83</b>	<b>-2.41</b>	<i>-4.68</i>	<i>-0.47</i>	<b>-10.42</b>		0	
<b>2d</b> ↓	<b>-2.41</b>	<b>-6.83</b>	<i>-0.47</i>	<i>-4.68</i>		<b>-10.42</b>		0

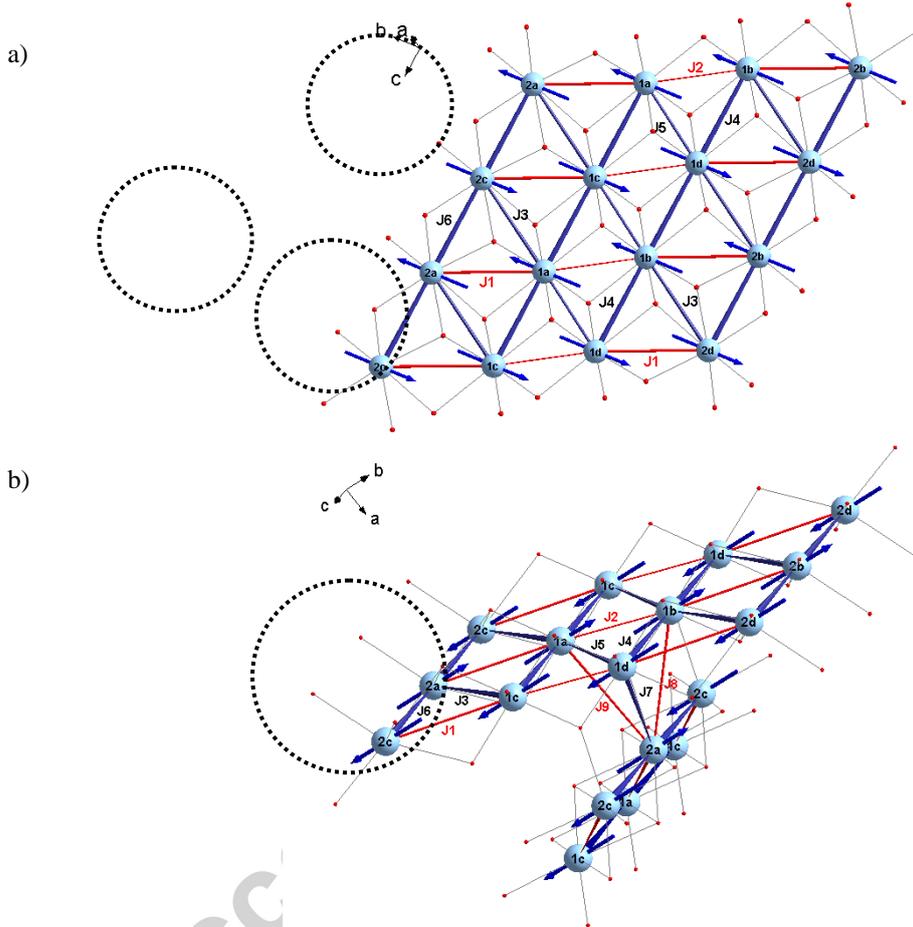
The strong inter-chain interaction  $|J3| = 6.83$  K favors antiferromagnetic alignment of  $\text{Mn}^{2+}$  and  $\text{Mn}^{3+}$  moments. These three interactions reinforce each other and impose the antiferromagnetic alignment between the magnetic moments of  $1a$  sublattice and those of  $1c$ ,  $2c$  sublattices. The same interactions lead to the magnetic moments of the  $1b$  sublattice to be ordered antiferromagnetically with respect to those of  $1d$  and  $2d$ . This type of the coupling is marked as “ordering interaction” and denoted in bold in Table 3, and with bold lines in Fig. 4, where the calculated local magnetic structure, depicting the short range order, is presented. According to these ordering interactions the arrows directions ( $\uparrow$  or  $\downarrow$ ) have been established. The relative weak  $J1$ ,  $J2$ ,  $J8$  and  $J9$  interactions tend to disturb the AF order imposed by dominant ordering interactions. Such couplings have frustrating character and are named as “disordering interactions”. They are denoted in italic in Table 3 and with red lines in Fig. 4.

In a molecular field approximation for the multisublattice model the exchange field operating on magnetic ions with spin  $S_i$ , belonging to  $i$ -th sublattice on the part of other sublattices is given by the expression

$$H_{exi} = \sum_{j=1}^p \frac{2J_{ij}}{g_i g_j \mu_B^2} \mu_j, \quad (7)$$

$$\mu_j = g_j \mu_B S_j.$$

Here  $i, j = 1, 2, \dots, p$  denote sublattice numbers ( $p = 8$  at present case),  $J_{ij}$  is the exchange interaction parameter between the sublattices,  $g_i, g_j$  are spectroscopic factors,  $\mu_B$ - Bohr magneton, and  $S_j$  is spin of the magnetic ion belonging to  $j$ -th sublattice. In  $Mn_2BO_4$  the exchange fields acting on the magnetic ions are defined by the competition between ordering and disordering interactions. We have estimated the exchange fields  $H_{exi}$  acting on the manganese ions belonging to the  $1a-1d$  and  $2a-2d$  sublattices and obtained the values of  $H_{ex}^{1a-1d} = 558$  and  $H_{ex}^{2a-2d} = 509$  kOe, respectively. These values are well agreed with those obtained from  $dc$  magnetization measurements.



**Fig. 4.** (a) the intra-ribbon indirect exchange interactions ( $J1-J6$ ) and b) inter-ribbon ones ( $J7-J9$ ) in the  $Mn_2BO_4$  warwickite. Numerals indicate the belonging of a crystallographic position to a magnetic sublattice. The frustrated bonds are highlighted red. The interactions strength is shown by the lines thickness. The magnetic moments direction is randomly chosen at the crystallographic  $ab$ -plane and demonstrates the ordering and disordering bonds. The non-equilateral triangles are highlighted by the circles.

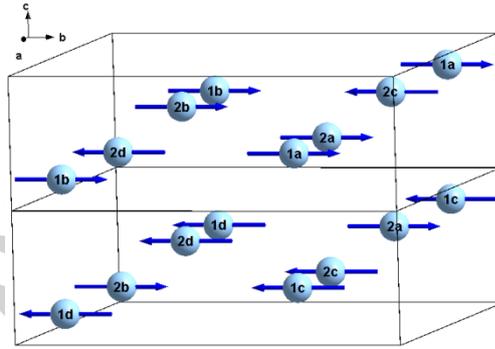
## 5. Discussion

This work presents a careful study of the magnetic properties of homometallic manganese warwickite through  $dc$  magnetization and specific heat measurements. Magnetic characterization is supported with XRD analysis and superexchange interactions calculations. The X-ray data analysis and normal coordinates calculation have shown that  $Mn_2BO_4$  demonstrates the charge ordering of  $Mn^{2+}(2)-Mn^{3+}(1)-Mn^{3+}(1)-Mn^{2+}(2)$ . The JT distortions result in the compression of the  $Mn2O_6$  and the considerable elongation of  $Mn1O_6$  octahedra along one of the nominal 4-fold axis. The latter suggests a  $d_z^2$  orbital at the Mn1 site.

The magnetization measurements have been carried out for two directions of the applied magnetic field: parallel and perpendicular to the crystalline  $c$ -axis. A small anisotropy is observed between two directions of the magnetic field. Our magnetic studies has clear revealed the anomaly in the behavior of  $dc$  magnetization at  $T_N = 26$

K which can be unequivocally identified as long-range antiferromagnetic transition. The results of the specific heat strongly support the above-mentioned suggestion, where the  $\lambda$ -type anomaly was found at  $T_N^* = 23$  K, indicating a second-order phase transition. At temperatures  $T_N^* < T < 125$  K the short-range magnetic correlations develop, leading to the decrease in the entropy  $\Delta S$  and high values of Curie-Weiss temperatures. The easy axis of the magnetization lies in  $ab$ -plane and spin-flop transition takes place at  $H_{sf} = 24$  kOe. The low uniaxial anisotropy  $H_a$  is probably associated with orbitally non-degenerate  $Mn^{2+}$  state ( $S$  state). According to the neutron diffraction data the  $Mn^{2+}(2)$  moments are being parallel to  $b$ -axis [23]. One can suppose that the spin-flop transition at  $H_{sf}$  is due to the flopping of the magnetic moments of  $Mn^{2+}$  -  $Mn^{2+}$  inside the antiferromagnetic chain. The depressed values of effective magnetic moments 6.25 and 6.95  $\mu_B/f.u.$  obtained for two orthogonal directions of the external magnetic field may be result of the non-quenched orbital moment of  $Mn^{3+}$  ions, as well as the intraribbon frustrating superexchange interactions.

The geometric frustrations are underlying by the warwickite structure. There is almost hexagonal arrangement of Mn ions inside the ribbon. The several types of triangular motifs both inside the ribbon and between the adjacent ribbons exist (see Fig. 4 and Table SM3 [25]). Three triangles are resolved inside of the ribbon involving different exchange couplings  $J1$ - $J3$ - $J6$ ,  $J1$ - $J3$ - $J4$  and  $J2$ - $J4$ - $J5$ . The disordering coupling  $|J2| = 1.44$  K is weak in compare with  $|J4| = |J5| = 5.03$  K and does not break the FM alignment of moments within the row 2-1-1-2. While the rather strong AF coupling  $|J1| = 4.03$  K favors an AF alignment of moments  $Mn^{2+}$  -  $Mn^{3+}$  within the row and leads to considerable frustration of the intra-chains interactions along  $c$ -axis. The geometry of interribbon bonds such that three types of triangles can be singled out also:  $J4$ - $J7$ - $J8$ ,  $J2$ - $J8$ - $J9$ , and  $J5$ - $J7$ - $J9$ . The rather weak interribbon couplings  $|J8| = 0.47$  K and  $|J9| = 0.65$  K are outweighed by strong  $|J7| = 2.41$  K one. So, interribbon interaction  $J7$  favors the AF alignment of magnetic moments  $Mn^{2+}(2)$  and  $Mn^{3+}(1)$  belonging to adjacent ribbons and can be responsible for long-range order in  $Mn_2BO_4$ . The magnetic frustration experimentally manifests itself in the large ratio of  $|\theta|/T_{C,N}$ , which is considered as the frustration criteria [34]. For instance, for ferromagnetic materials  $|\theta|/T_C \sim 1$ , for antiferromagnetic systems,  $|\theta|/T_N \sim 2-5$ . For the majority of the warwickites of interest the value  $|\theta|/T_{SG}$  is ranged from 8 to 37, which is consistent with a high level of frustration [6, 8, 10]. The value of  $|\theta|/T_{SG}$  was found to be  $\sim 5$  in  $Mn_2BO_4$ . We conclude, in spite of the magnetic frustration in  $Mn_2BO_4$  no dramatic frustration level occurs, allowing the on-set of long magnetic order at  $T_N = 26$  K. In spite of the simplicity of the theoretical method, the calculations have been shown to provide correct description of the magnetic behavior of  $Mn_2BO_4$ . Therefore, it could be thought of as an available tool for basic and qualitative understanding of magnetic properties of warwickites and related oxyborates.



**Fig. 5.** The spin configuration for the ordered state of  $Mn_2BO_4$  warwickite resulting from the simple model of superexchange interactions. The double magnetic unit cell along  $c$ -axis is shown.

In summary, homometallic warwickite  $Mn_2BO_4$  can be considered as conventional antiferromagnet showing uniaxial anisotropy. The long-range order occurs below  $T_N = 26$  K. The dominant exchange interaction is antiferromagnetic as was found from the superexchange interactions calculations. The strongest interactions are the intra-ribbon ones between the cations along  $c$ -axis ( $J4$  and  $J6$ ). As result, the antiferromagnetic chains  $2a$ - $2c$ - $2a$ ,  $1a$ - $1c$ - $1a$ ,  $1b$ - $1d$ - $1b$ , and  $2b$ - $2d$ - $2b$  extending along  $c$ -axis occur. ii) It leads to the doubling of the magnetic cell along the  $c$ -axis (Fig. 5). We note that a magnetic supercell with twice the volume of the structural cell was found in  $Mn_2BO_4$  by neutron diffraction measurements [23], but the doubling direction was not defined. iii) The magnetic coupling between two adjacent ribbons is depressed due to frustrating interactions  $J8$ ,  $J9$ . The three-dimensional AF ordering is supported by the inter-ribbon interaction  $J7$  via the coupling  $Mn^{3+}$  - O -  $Mn^{2+}$  with the coupling angle  $115^\circ$ , where  $Mn^{3+}$  and  $Mn^{2+}$  ions belong to the adjacent ribbons.

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**Supporting Information available:** structure parameters, refined bond lengths and angles according to Reitveld refinements of the XRD data, the normal coordinates expressed in Cartesian shifts, the tabulated parameters for superexchange interactions calculation in  $\text{Mn}_2\text{BO}_4$ .

## References

- [1] J. Bartolome, A. Arauzo, N.V. Kazak N.V., N.B. Ivanova, S.G. Ovchinnikov, Yu.V. Knyazev, I.S. Lyubutin, *Phys. Rev. B* 83 (2011) 144426(1-12).
- [2] H. Yamane, T. Kawano, *J. Cryst. Soc. Jpn.* 54, (2012) 68-73.
- [3] D.C. Freitas, R.B. Guimaraes, J.C. Fernandes, M.A. Continentino, C.B. Pinheiro, J.A.L.C. Resende, G.G. Eslava, L. Ghivelder, *Phys. Rev. B* 81 (2010) 174403(1-7).
- [4] Yu.V. Knyazev, N.B. Ivanova, N.V. Kazak, M.S. Platonov, L.N. Bezmaternykh, D.A. Velikanov, A.D. Vasiliev, S.G. Ovchinnikov, G.Yu. Yurkin, *J. Magn. Magn. Mater.* 324 (2012) 923-927.
- [5] N.V. Kazak, N.B. Ivanova, O.A. Bayukov, S.G. Ovchinnikov, A.D. Vasiliev, V.V. Rudenko, J. Bartolome, A. Arauzo, Yu.V. Knyazev, *J. Magn. Magn. Mater.* 323 (2011) 521-527.
- [6] A. Apostolov, M. Mikhov, and P. Tcholakov, *Phys. Status Solidi A*, 56 (1979) K33-K36.
- [7] J. J. Capponi, J. Chenavas, and J. C. Joubert, *J. Solid State Chem.* 7 (1973) 49-54.
- [8] M.A. Continentino, B. Boechat, R.B. Guimãraes, J.C. Fernandes, L. Ghivelder, *J. Magn. Magn. Mater.* 226-230 (2001) 427-430.
- [9] R. B. Guimãraes, J. C. Fernandes, M. A. Continentino, H. A. Borges, C. S. Moura, J. B. M. da Cunha, and C. A. dos Santos, *Phys. Rev. B* 56 (1997) 292-299.
- [10] A. Arauzo, N.V. Kazak, N.B. Ivanova, M.S. Platonov, Yu.V. Knyazev, O.A. Bayukov, L.N. Bezmaternykh, I.S. Lyubutin, K.V. Frolov, S.G. Ovchinnikov, and J. Bartolomé, submitted to *J. Magn. Magn. Mater.*, ArXiv: 1504.05912 (2015).
- [11] N. V. Kazak, M.S. Platonov, N.B. Ivanova, Y. V. Zubavichus, A.A. Veligzhanin, A.D. Vasiliev, L.N. Bezmaternykh, O.A. Bayukov, A. Arauzo, K. V. Lamonova, S.G. Ovchinnikov, submitted to *Phys. Status Solidi B* (2015), arXiv:1412.6236.
- [12] I.S. Lyubutin, N.Y. Korotkov, K. V Frolov, N. V Kazak, M.S. Platonov, Y. V Knyazev, L.N. Bezmaternykh, *J. Alloy Comp.* (2015), doi:10.1016/j.jallcom.2015.04.067.
- [13] Yu. V. Knyazev, N. V. Kazak, M. S. Platonov, N. B. Ivanova, L. N. Bezmaternykh, A. Arauzo, J. Bartolomé, and S. G. Ovchinnikov, *J. Alloy Comp.* (2015), doi:10.1016/j.jallcom.2015.04.056.
- [14] J.P. Attfield, A.M.T. Bell, L.M. Rodriguez-Martinez, J.M. Greneche, R.J. Cernik, J.F. Clarke, and D.A. Perkins, *Nature* 396 (1998) 655-658.
- [15] R. Norrestam, M. Kritikos, A. Sjdin, *J. Solid State Chem.* 114 (1995) 311-316.
- [16] A. Akrap, M. Angst, P. Khalifah, D. Mandrus, B. C. Sales, and L. Forró, *Phys. Rev. B* 82 (2010) 165106(1-7).
- [17] G. R. Hearne, W.N. Sibanda, E. Carleschi, V. Pischedda, and J. P. Attfield, *Phys. Rev. B* 86 (2012) 195134(1-5).
- [18] H.X. Yang, H.F. Tian, Y.J. Song, Y.B. Qin, Y.G. Zhao, C. Ma, and J.Q. Li, *Phys. Rev. Lett.* 106 (2011) 016406(1-4).
- [19] Z. Chen, C. Ma, Y.J. Song, H.X. Yang, H.F. Tian, and J.Q. Li, *Phys. Rev. B* 86 (2012) 045111(1-6).
- [20] J.P. Attfield, A.M.T. Bell, L.M. Rodrigues-Martinez, J.M. Greneche, R. Retoux, M. Leblanc, R.J. Cernik, J.F. Clarke and D.A. Perkins, *J. Mater. Chem.* 9 (1999) 205-209.
- [21] B. Rivas-Murias, F. Rivadulla, M. Sanchez-Andujar, A. Castro-Couserio, M.A. Senaris-Rodrigues, J. Rivas, *Chem. Mater* 18 (2006) 4547-4552.
- [22] M.A. Continentino, A.M. Pedreira, R.B. Guimaraes, M. Mir, J.C. Fernandes, R.S. Freitas, L. Ghivelder, *Phys. Rev. B* 64 (2001) 014406(1-6).
- [23] R.J. Goff, A.J. Williams, J.P. Attfield, *Phys. Rev. B* 70 (2004) 014426(1-5).
- [24] Sh. Li, J. Leng, Y. Fan, Ch. Fu, H. Shen, Y. Xue, D. Xu, *Phys. Status Solidi A* 208 (2011) 114-117.
- [25] Supplementary Material for: Uniaxial anisotropy and low-temperature antiferromagnetism of  $\text{Mn}_2\text{BO}_4$  single crystal
- [26] I.D. Brown and D. Altermatt, *Acta Cryst. B* 41 (1985) 244-247.
- [27] R.J. Radwanski, Z.Ropka, *Acta Physica* 1 (2006) 3-11.
- [28] D.C. Freitas, M.A. Continentino, R.B. Guimãraes, J.C. Fernandes, E.P. Oliveira, R.E. Santelli, J. Ellena, G.G. Eslava, L. Ghivelder, *Phys. Rev. B* 79 (2009) 134437(1-8).
- [29] B.F. Woodfield, J. Boerio-Goates, J.L. Shapiro, R.L. Putnam, and A. Navrotsky, *J. Chem. Thermodyn.* 31 (1999) 245-253.

- [30] J.C. Fernandes, F.S. Sarrat, R.B. Guimarães, R.S. Freitas, M.A. Continentino, A.C. Doriguetto, Y.P. Mascarenhas, J. Ellena, E.E. Castellano, J-L. Tholence, J. Dumas L. Ghivelder, Phys. Rev. B 67 (2003) 104413(1-7).
- [31] M. V. Eremin, *The spectroscopy of the crystals* (Nayka, Leningrad, 1985) p.150.
- [32] N. V. Kazak, M. S. Platunov, N. B. Ivanova, Yu. V. Knyazev, L. N. Bezmaternykh, E. V. Eremin, A. D. Vasil'ev, O. A. Bayukov, S. G. Ovchinnikov, D. A. Velikanov, and Ya. V. Zubavichus, J. Exp. Theor. Phys. 117 (2013) 94-107.
- [33] O.A. Bayukov, A.F. Savitskii, Phys. Stat. Sol. B 155 (1989) 249-255.
- [34] J.E. Greedan, J. Mater. Chem. 11 (2001) 37-53.

### Highlights

of the manuscript “Uniaxial anisotropy and low-temperature antiferromagnetism of  $\text{Mn}_2\text{BO}_4$  single crystal”

*N.V. Kazak, M.S. Platunov, Yu.V. Knyazev et al.*

- Single-crystalline samples of  $\text{Mn}_2\text{BO}_4$  of high quality were grown. The charge ordering of type  $\text{Mn}^{2+}(1)\text{-Mn}^{3+}(2)$  was found.
- The intrinsic antiferromagnetic transition at  $T_N = 26$  K was observed through the magnetization and specific heat measurements.
- An uniaxial magnetic anisotropy with easy axis of magnetization lying in  $ab$ -plane was found.
- The superexchange interactions were calculated and the magnetic frustration was found.