



## Research articles

# Understanding high ordering temperature in Gd<sub>6</sub>FeBi<sub>2</sub> magnet: Critical behavior, electronic structure and crystal-field analysis

Guoming Cui<sup>a</sup>, Huan Ma<sup>b</sup>, Kam Wa Wong<sup>c</sup>, Chan Hung Shek<sup>b</sup>, Guangcun Shan<sup>d,\*</sup>, Jiliang Zhang<sup>e,\*</sup>

<sup>a</sup> Department of Materials Science and Engineering, Henan Institute of Technology, Xinxiang 453003, China

<sup>b</sup> Department of Materials Science and Engineering, City University of Hong Kong, Kowloon, Hong Kong, China

<sup>c</sup> Department of Physics, City University of Hong Kong, Kowloon, Hong Kong, China

<sup>d</sup> School of Instrument Science and Opto-electronics Engineering & Institute of Quantum Sensing, Beihang University, Beijing 100083, China

<sup>e</sup> Department of Energy & Materials Engineering, Dongguk University-Seoul, Seoul 04620, South Korea



## ARTICLE INFO

## Keywords:

Rare earth alloys and compounds  
Crystal and ligand fields  
Electronic band structure  
Magnetisation

## ABSTRACT

Gd<sub>6</sub>FeBi<sub>2</sub> is reported as the only one room-temperature magnet among more than hundreds of compounds with its structural type, which makes it more attractive in potential applications. To reveal the origin of such high ordering temperature, critical behaviors, electronic structure and crystal-field effects of Gd<sub>6</sub>FeBi<sub>2</sub> are investigated in this work. The short-range Gd-Fe ferrimagnetic interaction is supported by the crystal and electronic structure analyses. Unlike the strong Fe-Fe exchange interactions, the Gd-Fe exchange interaction shows limited influence on the critical exponents determined by long-range exchange interactions, which seems a common feature in rare earth – transition metal based alloys without exchange interactions between transition-metal atoms. However, the strong Gd-Fe hybridization reduces the influence of vibronic couplings on the short-range exchange interaction and thus allows a high  $T_c$ . The broadening or splitting mechanism of Gd 4*f*-electron bands is addressed based on crystal-field analysis and likely another factor for elevated  $T_c$  in Gd<sub>6</sub>FeBi<sub>2</sub> and Gd-based compounds with non-magnetic elements. Different magnetic behaviors among isostructural compounds, and the relationship between the band splitting and crystal-field effects is also discussed.

## 1. Introduction

Most heavy rare-earth (RE) metals possess very large magnetic moment ideal for many magnetic applications, but the low magnetic ordering temperature inhibits their application in practice. To overcome this drawback, many efforts are made to develop RE-based RE-TM (TM, transition metal) intermetallic compounds, because the strong RE-TM or TM-TM magnetic interactions can effectively elevate the ordering temperature compared with the indirect 4*f*-4*f* interactions between RE atoms, while the small magnetic moment of TM will not change the net magnetic moment of these compounds significantly. Another chemical element, generally from the p-block of main groups, is usually added into these RE-TM systems to produce even greater diversity of new compounds and structures, as well as to improve properties.

A new family of Fe<sub>2</sub>P type with the general formula RE<sub>6</sub>TMX<sub>2</sub> (RE = Gd-Tm, and Lu; TM = Mn, Fe, Co, Ni and Ru; and X = Al, Ga, Sn, As, Sb, Bi, S, Se and Te) firstly discovered in 2003 by different research groups independently is a typical example of such strategy [1–5]. These compounds show fruitful magnetic behaviours as

characterized by multiple magnetic transitions and the absence of magnetic moment from TM in many members [6–8]. Some members also show large magnetocaloric effects around their Curie temperatures ( $T_c$ ) [9–12]. However, the reported magnetic ordering temperature of all members are lower than room temperature except Gd<sub>6</sub>FeBi<sub>2</sub> [11], which has an ordering temperature up to 350 K, higher than that of most Gd-based intermetallic compounds [13].

Due to the great potential for practical applications, many efforts are made to understand the origin of high ordering temperature or strong magnetic interactions in these Gd-based compounds with high  $T_c$ , e.g. Gd<sub>5</sub>Si<sub>4</sub> (336 K) and Gd<sub>4</sub>Bi<sub>3</sub> (340 K) [14,15]. A typical explanation for the compounds with non-magnetic elements (NMEs) is the Ruderman-Kittle-Kasuya-Yosida (RKKY) interaction, where the *f*-shell electron spins couple with those of a neighbouring Gd atom through the conduction electrons. Such indirect exchange interaction can induce the fluctuation of  $T_c$  depending on the conduction electrons and distance between neighbouring magnetic atoms, but it is difficult to elevate  $T_c$  significantly because of the nature of indirect interactions. Later it is realized that the high  $T_c$  can be induced by extra magnetic moment

\* Corresponding authors.

E-mail addresses: [gcschan@buaa.edu.cn](mailto:gcschan@buaa.edu.cn) (G. Shan), [jiliangz@dongguk.edu](mailto:jiliangz@dongguk.edu) (J. Zhang).

<https://doi.org/10.1016/j.jmmm.2019.166301>

Received 3 October 2019; Accepted 13 December 2019

Available online 14 December 2019

0304-8853/ © 2019 Elsevier B.V. All rights reserved.

from the localized/polarized 5d electrons in Gd [16], or extra magnetic moment from NMEs (e.g. Bi in Gd<sub>4</sub>Bi<sub>3</sub>) due to strong interactions or polarizations [17]. Very recently, the low-temperature structure of Gd<sub>6</sub>FeBi<sub>2</sub> was determined from single crystals, and the DFT calculations based on the structural model did show the magnetic moment from 5d electrons of Gd and a ferrimagnetic interaction between Gd and Fe, accounting for the high ordering temperature in Gd<sub>6</sub>FeBi<sub>2</sub> [18]. However, multiple magnetic transitions (and very likely structural transitions) exist in this family and some may induce a significant change of interactions between atoms. Thus, to understand the origin for the high  $T_c$ , it is more proper to use the data from the high-temperature magnetic phase for analysis.

In this work, we attempt to reveal the magnetic exchange interactions from the critical behaviours of the high-temperature magnetic phase and understand the chemical and magnetic interactions in the compound from its electronic structure and crystal-field analysis, so that the structural landscape for the enhanced magnetic exchange interactions can be constructed.

## 2. Experimental

Gd<sub>6</sub>FeBi<sub>2</sub> ingots were fabricated by arc melting the mixtures of pure constituent elements Gd (99.9 wt%), Fe (99.95 wt%), and Bi (99.9 wt%) under a Ti-getterred argon atmosphere. A small extra amount of Bi (0.4%, 0.6%, 0.8%, 1.0% and 1.2%, respectively) were added into samples to compensate for the loss of Bi due to vaporization during arc melting. All ingots were remelted for four times to improve compositional homogeneity. After melting, all ingots were sealed into high vacuum quartz tube and then annealed at 1073 K for 10 days. Finally, the sealed quartz tube was quenched into ice water. Phase identification was conducted on a Philips X'pert X-rays diffractometer (Cu K $\alpha$ ,  $\lambda = 0.15406$  nm). Isothermal magnetisation were measured using a LakeShore VSM with a maximum field of up to 50 kOe. The applied magnetic fields ( $H_E$ ) were corrected for the demagnetization to get the internal field  $H = H_E - NM(T, H_E)$ , where N is the demagnetization factor and M is the measured magnetization. Demagnetization factors were calculated from low-field magnetization following the method in given in reference [19]. To further reduce the effects of demagnetization, only data obtained from the field above 0.5 T were used for analysis. Experimental electronic structures were measured by X-ray photoelectron spectroscopy (XPS) using an ULVAC-PHI 5802 spectrometer equipped with a monochromatized Al K $\alpha$  radiation ( $h\nu = 1486.6$  eV) in vacuum of about  $10^{-9}$  mbar. All samples were sputtered by Ar ion to remove the O<sub>2</sub>-contaminated surface before the measurement.

## 3. Scaling analysis

A variety of physical systems exhibited critical phenomena, in which the physical behaviors can be well described using a set of parameters. And the second order magnetic transition is a well-known critical point. For such magnetic systems, the low-temperature magnetization and high-temperature susceptibility can be well described using a scaling rule constructed by critical exponents. According to the scaling hypothesis, the mathematical definitions of these critical exponents for magnetic systems can be described as follows [20]:

$$M_S(T) = M_0(-\varepsilon)^\beta, \varepsilon < 0 \quad (1)$$

$$\chi_0^{-1}(T) = \Gamma\varepsilon^\gamma, \varepsilon > 0 \quad (2)$$

$$M = DH^{1/\delta}, \varepsilon = 0 \quad (3)$$

where:

$\varepsilon = (T - T_c)/T_c$ , the reduced temperature;  $M_0$ ,  $\Gamma$ ,  $D$ , the critical amplitudes;

$\beta$ , a critical exponent associated with the spontaneous

magnetization  $M_S$ ;

$\gamma$ , a critical exponent associated with the initial magnetic susceptibility  $\chi_0$ ;

$\delta$ , a critical exponent associated with the critical isothermal magnetization at  $T_c$ .

These exponents are not independent of each other, but correlated by some relationships. And finally a scaling hypothesis, describing the magnetic equation of state, is achieved. Using the scaling hypothesis the magnetization can be expressed as:

$$M(H, \varepsilon) = |\varepsilon|^\beta f_\pm \left( \frac{H}{|\varepsilon|^\beta + \gamma} \right) \quad (4)$$

where  $f_\pm$  are regular analytical functions with  $f_+$  for  $\varepsilon > 0$ , and  $f_-$  for  $\varepsilon < 0$ . In terms of scaled magnetization  $m \equiv |\varepsilon|^{-\beta} M(H, \varepsilon)$  and scaled field  $h \equiv |\varepsilon|^{-(\beta+\gamma)} H$ , the Eq. (4) can be written into the more familiar form:

$$m = f_\pm(h) \quad (5)$$

It is clear that the above equation above implies that the scaled  $m$  plotted as a function of the scaled  $h$  will fall onto two different universal curves described by  $f_+$  and  $f_-$  respectively, for true scaling relations and right choice of these critical exponents.

Although the exponents generally show universal properties in the asymptotic region ( $\varepsilon \rightarrow 0$ ), various systemic trends or crossover phenomenon are often observed, mostly due to the presence of various competing couplings and/or disorder. In the present case, Gd<sub>6</sub>FeBi<sub>2</sub> shows non-Curie-Weise paramagnetic behaviors, in contrast to the HCP Gd with clearly Curie-Weise paramagnetic behaviors above magnetic transition [21]. Therefore it is useful to introduce the temperature-dependent effective exponents for  $\varepsilon \neq 0$ , which are defined as [20]:

$$\beta_{eff}(\varepsilon) = \frac{d[\ln M_S(\varepsilon)]}{d(\ln \varepsilon)} \quad (6)$$

$$\gamma_{eff}(\varepsilon) = \frac{d[\ln \chi_0^{-1}(\varepsilon)]}{d(\ln \varepsilon)} \quad (7)$$

These effective exponents are general non-universal, but approach universal exponents in the asymptotic limit.

## 4. Results and discussion

Among the synthesized samples, the one with an extra 0.8% Bi has the best phase purity. The XRD pattern of Gd<sub>6</sub>FeBi<sub>2</sub> at room temperature is similar to the simulated XRD pattern generated from structure parameters obtained by single crystals despite the slight shift due to different temperatures (see Fig. 1) [18]. All reflections in XRD pattern of Gd<sub>6</sub>FeBi<sub>2</sub> can be well indexed according to the Fe<sub>2</sub>P-type structure, and gives the unit cell of  $a = 8.366(5)$  Å and  $c = 4.243(4)$  Å, in good agreement with previous reports [5,11]. RKKY indirect exchange interaction, which is common in RE-based compounds without other NMEs, can induce the fluctuation of  $T_c$  depending on the concentration of conduction electrons and distance between neighbouring magnetic atoms. Our recent work shows that exchange interaction in Gd<sub>6</sub>CoTe<sub>2</sub> is dominated by the RKKY mechanism, while extra short-range exchange interactions exist in Gd<sub>6</sub>FeBi<sub>2</sub> accounting for the high  $T_c$  [18]. To understand these exchange interactions, critical behaviors around the  $T_c$  are to be first investigated.

### 4.1. Critical behaviors

Near the transition, the Landau theory of second-order phase transition suggests that the free energy  $G$  of a magnetic system can be expanded in the powers of its order parameter  $M$  in the following form [22]:

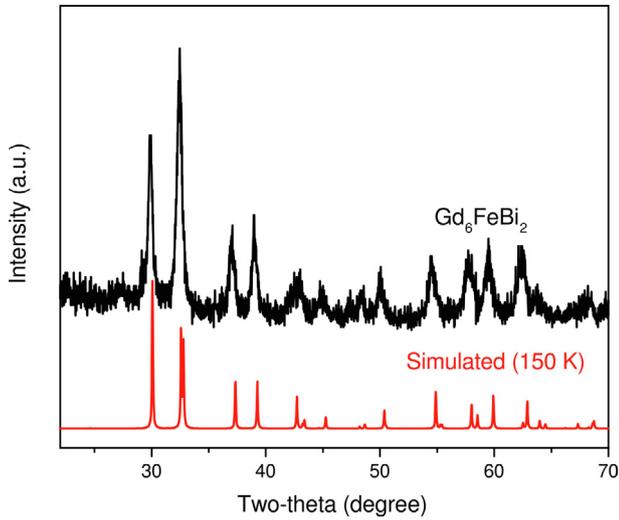


Fig. 1. Experimental XRD patterns (black) of  $Gd_6FeBi_2$  and the simulated pattern (red) from the crystal structure determined at 150 K. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

$$G(T, M) = G_0 + \frac{1}{2}A(T)M^2 + \frac{1}{4}B(T)M^4 + \dots - MH \quad (8)$$

where coefficients A and B are temperature-dependent parameters, and the last term describes the energy of spins in an external field H. Generally the higher order items can be neglected in practice due to their small values. In the case of equilibrium, the energy is minimized ( $\frac{\partial G}{\partial M} = 0$ ), which leads to the magnetic equation of states in the form of Arrott formula [23]:

$$\frac{M}{H} = A + BM^2 \quad (9)$$

Therefore the  $M^2$  versus  $H/M$  curves should be straight lines, of which the intercept on the  $H/M$  axis determines the ordering transition. As shown in Fig. 2a, the Arrott plots of  $Gd_6FeBi_2$  exhibit positive slope, which indicates that the magnetic transition is second-order according to the criterion suggested by Banerjee [24]. It is also noted in Fig. 2a that the plots of  $Gd_6FeBi_2$  show slightly downward from the linearity, because the Arrott plot is actually based on the mean-field approach without considering microscopic exchange interactions and fluctuations in magnetic systems.

Compared with the mean-field theory, both Ising and Heisenberg models include the exchange interaction between spins (short-range/direct interactions). And both models can also give critical exponents for the well-known modified Arrott (MA) relation which can be expressed as [25]:

$$\left(\frac{M}{H}\right)^{1/\gamma} = A\varepsilon + BM^{1/\beta} \quad (10)$$

Based on the critical exponents  $\beta$  and  $\gamma$  predicted by 3D-Ising and 3D-Heisenberg models (see Table 1) [26], MA plots of  $Gd_6FeBi_2$  are drawn in Fig. 2b and 2c respectively, and all plots seem curved upward from the linearity.

According to Eq. (10), linear extrapolation of the high field portions of the isotherms will give an intercept on both  $M^{1/\beta}$  and  $\left(\frac{M}{H}\right)^{1/\gamma}$  axis, from which the spontaneous magnetization  $M_S$  and the inverse initial susceptibility  $\chi_0^{-1}$  can be calculated. Using these calculated data, new critical exponents can also be obtained based on Eqs. (1) and (2). The best values of  $\beta$  and  $\gamma$  obtained by fitting Eq. (10) should be self-consistent with the values yielded by fitting Eqs. (1) and (2) to the extrapolated data. To get the best values, we programmed according to the idea which was also introduced in literature [27], and then got the best

values fitting our data. Previous work shows that effective exponents converge approaching to the universal exponents only when  $\varepsilon < 0.1$  [26]. Thus our estimations on critical exponents were performed using data in the range. After several cycles, the exponents converged into stable values. The values obtained after 30 cycles are  $\beta = 0.441(8)$ ,  $\gamma = 1.098(12)$  for  $Gd_6FeBi_2$ . Evidently, the MA plot of  $Gd_6FeBi_2$  exhibit good linearity around  $T_c$  as shown in Fig. 2d. The spontaneous magnetization  $M_S$  and the inverse initial susceptibility  $\chi_0^{-1}$  obtained using these exponents are then plotted as a function of temperature in Fig. 3a. The fitting of these values to Eq. (1) gives  $\beta = 0.439(6)$ ,  $T_c = 347.9(1)$  K, and to Eq. (2) gives  $\gamma = 1.107(10)$ ,  $T_c = 348.1(1)$  K. These values are also listed in Table 1. It is distinct that these values are closer to those given by mean-field model rather than 3D-Ising or 3D-Heisenberg model.

Using determined  $M_S$  and  $\chi_0^{-1}$  by the above method (see Fig. 3a), the critical exponents and  $T_c$  of high precision can be obtained by following the Kouvel-Fisher (KF) method [28], which is described by an alternative form of Eqs. (1) and (2):

$$M_S \left(\frac{dM_S}{dT}\right)^{-1} = (T - T_c)/\beta \quad (11)$$

$$\chi_0^{-1} \left(\frac{d\chi_0^{-1}}{dT}\right)^{-1} = (T - T_c)/\gamma \quad (12)$$

According to the method, in critical regions, the plots of  $M_S \left(\frac{dM_S}{dT}\right)^{-1}$  vs.  $T$  and  $\chi_0^{-1} \left(\frac{d\chi_0^{-1}}{dT}\right)^{-1}$  vs.  $T$  yield straight lines with slopes  $1/\beta$  and  $1/\gamma$  respectively, and intercepts of such fitted straight lines on their  $T$  axis equal to  $T_c$ . The most important advantages of the KF method is: no previous knowledge of  $T_c$  is required, and it provides a consistency condition for  $T_c$ , namely, the fitting of both plots should give the same value of  $T_c$ . The KF plots of  $Gd_6FeBi_2$  is shown in Fig. 3b, and estimated critical exponents and  $T_c$  by fitting these straight lines are:  $\beta = 0.446(6)$ ,  $T_c = 348.2(1)$  K and  $\gamma = 1.092(10)$ ,  $T_c = 348.0(1)$  K.

All these critical exponents estimated from above methods, together with predicted theoretically values from different models, are listed in Table 1. It is evident that values of critical exponents and  $T_c$  calculated using both methods match reasonably well, which indicates that these estimated values are self-consistent. However, it is also clear that these values do not match the conventional universality classes. Thus it is necessary to verify whether these critical exponents can produce the scaling equation of state. Taking the values of critical exponents and  $T_c$  listed in Table 1, the plots of scaled  $m$  against scaled  $h$  are drawn in Fig. 4a. These plots depict the two different universal curves distinctly as predicted by the scaling equation Eq. (5), which indicates the reliability of the calculated critical exponents and  $T_c$ . The inset of Fig. 4a shows the same plot on log-log scale, which suggests the converging of two curves towards to  $T_c$ .

A more rigorous way to confirm whether the estimated values of critical exponents and  $T_c$  are reliable and whether the isotherms taken in the critical region obey the scaling equation of state, is to analyze the experimental data in terms of the well-established asymptotic form of the scaling equation given by [29]

$$\frac{h}{m} = \pm a_{\pm} + b_{\pm} m^2 \quad (13)$$

where plus and minus signs have the same meaning as that in Eq. (4),  $a$  and  $b$  are two scaling parameters for Gibbs potential concerning both thermal and magnetic field effects. Then the coefficients in the equation can be related to the critical amplitudes in Eqs. (1) and (2) as

$$(a_-/b_-)^{1/2} = M = m_0 \quad (14)$$

$$a_+ = \Gamma = h_0/m_0 \quad (15)$$

It is significant that these critical amplitudes  $m_0$  and  $h_0/m_0$  can be obtained by intercepting the universal curves with  $m^2$  and  $\frac{h}{m}$  axis in the

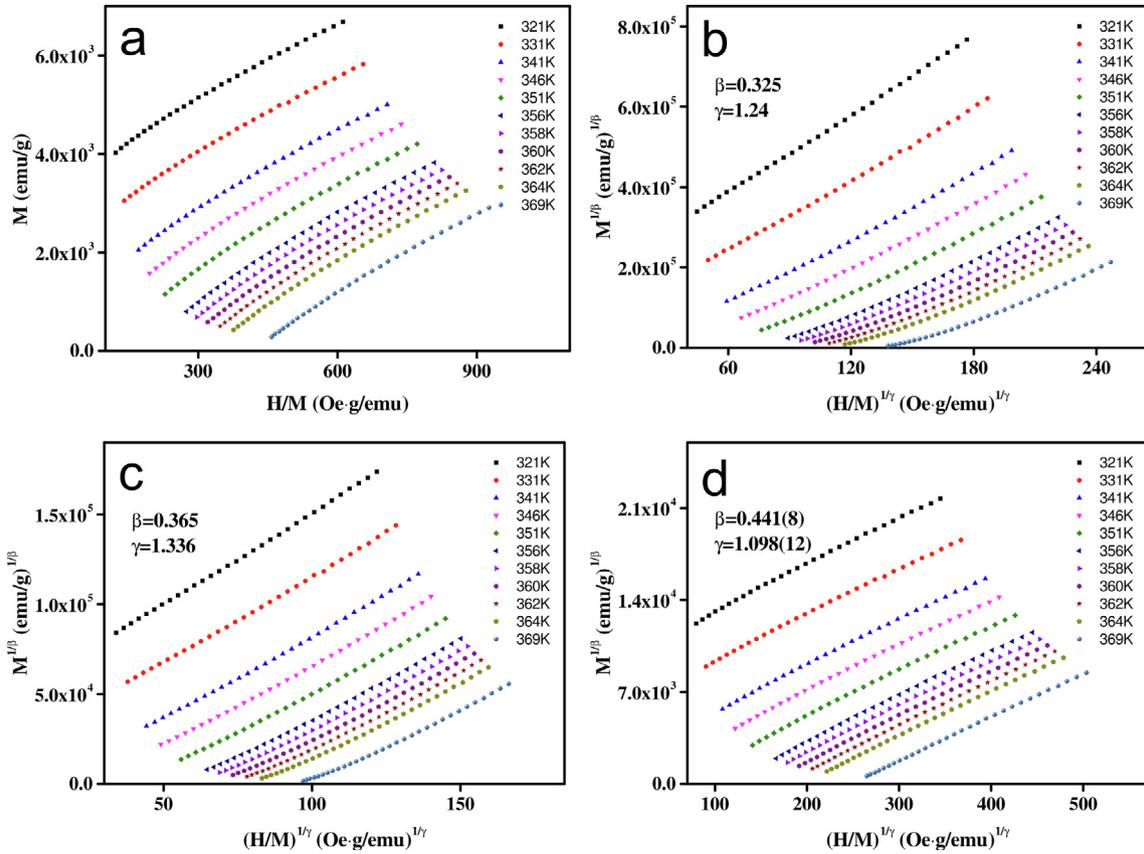


Fig. 2. Arrott plots (a) and modified arrott plots using different exponents: (b) 3D Ising model, (c) 3D Heisenberg model and (d)  $\beta = 0.441(8)$ ,  $\gamma = 1.098(12)$ .

Table 1

Comparison of critical exponents of  $Gd_6FeBi_2$  and different theoretical models.

Composition	Technique	$\beta$	$\gamma$	Ref.
$Gd_6FeBi_2$	Modified Arrott Plot	0.441(8)	1.098(12)	Present
	Kouvel-Fisher method	0.446(6)	1.092(10)	Present
3D Ising		0.325	1.241	[26]
3D Heisenberg		0.365	1.386	[26]
Mean Field		0.5	1	[23]

plots of  $m^2$  vs.  $\frac{h}{m}$  respectively, as shown in Fig. 4b. These values are determined as:  $m_0 = 169(6)$  emu/g, and the effective exchange interaction field  $h_0 = 11.6(2)$  kOe.

#### 4.2. Magnetic exchange interaction and electronic structure

In RE-based compounds with NMEs, the RKKY interaction is generally the dominant long-range interaction, but other long-range forces like dipolar interaction can also influence the critical fluctuations of magnetization. According to the criterion given by Tadaoff et al [30], such long-range forces can be neglected in case

$$|\epsilon| \gg [\mu M_S(0)/k_B T_C]^{1/\beta(\delta-1)} \equiv t \quad (16)$$

where  $\mu = g\mu_B S$  is the moment of per spin,  $k_B$  is Boltzmann constant, and the saturation magnetization  $M_S(0)$  can be calculated from Eq. (1) as 1600 Oe. Then using Eq. (16)  $t$  is estimated as  $2.5 \times 10^{-3}$ , much smaller than the range of  $|\epsilon|$ . Thus the dipolar interactions, if present, have a negligible effect on the critical fluctuation of magnetization.

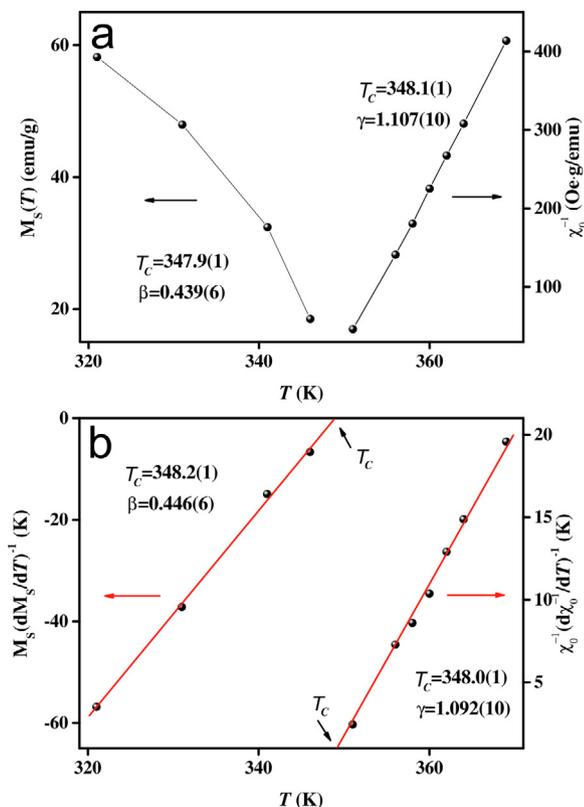
Above analyses on critical behaviors indicate the dominant long-range exchange interactions, while both the deviation from Curie-Weiss paramagnetic behavior above  $T_C$  in a linear compound and previous DFT calculation suggest the important role of short-range exchange interaction in  $Gd_6FeBi_2$  for high  $T_C$ . Actually the  $T_C$  of  $Gd_6FeBi_2$  is much

higher than that of its analogue  $Gd_6CoTe_2$  (350 K against 220 K) [31], which is not expected by RKKY interactions.

It is also known that the ferromagnetism/ferrimagnetism-paramagnetism transition is actually the destabilization of magnetic orders by thermal coupling. The scaling equation of state actually involves the role of thermal energy. Since  $h_0$  is the effective exchange interaction field, the product of  $h_0$  and an average effective elementary moment ( $\mu_{eff}$ ) involved in the FM-PM transition, namely the effective exchange energy  $\mu_{eff} h_0$ , is expected to equal the thermal energy at  $T = T_C$ . In mean-field model,  $\mu_{eff} h_0/k_B T_C$  equal 1.73. Using the value,  $\mu_{eff}$  is estimated as  $4.55\mu_B$  ( $\sim 6.8\mu_B$  per Gd atom) for the  $Gd_6FeBi_2$  compound, smaller than the theoretical value ( $7\mu_B$  per Gd atom) and suggestive of the Gd-Fe ferrimagnetic exchange interaction.

To address the inconsistency between critical exponents and short-range exchange interaction, it is necessary to analyse the structural origin of the Gd-Fe exchange interaction first. Like other  $RE_6FeBi_2$ ,  $Gd_6FeBi_2$  also presents multiple magnetic transitions, and no evident structural change is observed at low temperature (see Fig. 1). Neutron diffraction experiments show that these transitions are related to non-linear magnetic structures. Unlike other RE, Gd is a linear alloy and does not show orbital-spin couplings for conical or helical magnetic structures, and thus the multiple magnetic transitions in are very likely to be related with the crystal-field effects. The typical energy between the ground state and the first excited crystal field state in REs varies from 1 to 10 meV (10 K to 100 K) with the overall spread of all levels up to 20 meV, a value compared to the exchange energy for Gd (25 meV) [32].

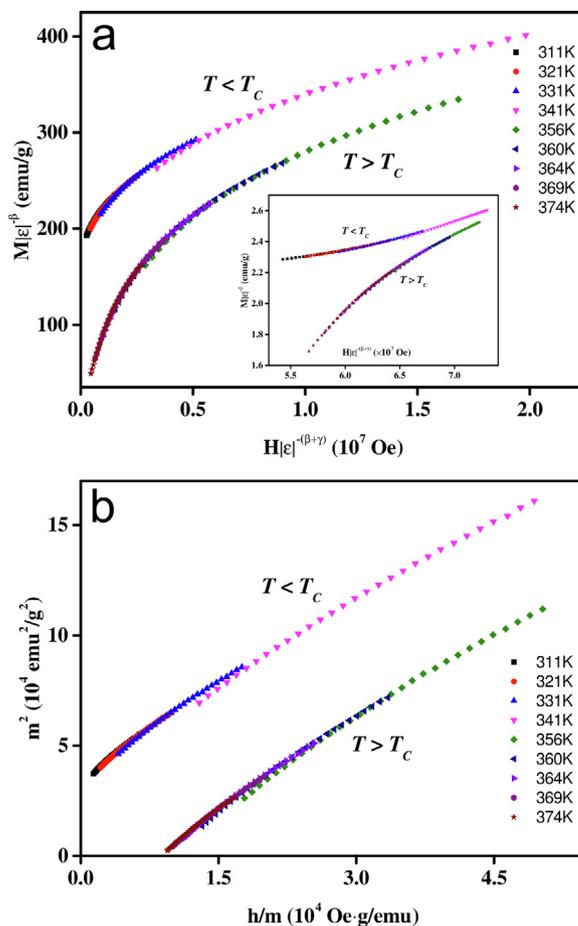
Because the magnetic structures of  $Ho_6FeBi_2$  determined by neutron diffraction show no magnetic contribution from Fe [6], different structural features for the Gd-Fe ferrimagnetic interaction are expected in  $Gd_6FeBi_2$ . The electronic configuration of Fe is  $[Ar]3d^64s^2$ , which allows a minimum-energy state with paired d electrons corresponding to a nonmagnetic state. However, the spatial extent of 3d electron wave



**Fig. 3.** (a) Temperature variation in spontaneous magnetization  $M_S(T)$  (left axis) and inverse initial susceptibility  $\chi_0^{-1}(T)$  (right axis); (b) Kouvel-Fisher plot of spontaneous magnetization  $M_S(T)$  (left axis) and inverse initial susceptibility  $\chi_0^{-1}(T)$  (right axis). Black solid lines in (a) are guides for eyes, and red straight lines in (b) are due to linear fitting of data. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

function is considerably large, and thus 3d electron wave functions of neighbouring atoms show a strong overlap, leading to 3d electron bands, where the relatively strong effective Coulomb repulsion between 3d electrons can favor situations in which the number of spin up and spin down electrons is no longer equal and leads to the formation of a magnetic moment. In the  $RE_6TMX_2$  family,  $TM$  atoms are surrounded only by  $RE$  atoms (Fig. 5a). The absence of  $TM$ - $TM$  contacts and the low electronic density of states of  $s$  electron bands in  $RE$ s account for the nonmagnetic state of  $TM$  in these compounds except Gd analogues. In Gd analogues, the 5d electron band of Gd may have an overlap with 3d electron bands in  $TM$ , depending on the Gd- $TM$  bond strength. In  $Gd_6CoTe_2$ , for instance, the Gd-Co interaction seems similar in strength to other  $RE$ -Co as characterized by the nearly linear relationship between  $a/c$  and atomic radii of  $RE$  elements (Fig. 5b), because lattice constant  $a$  is related to the Fe site and  $a/c$  is an indicator of the  $RE$ -Fe bond strength. In contrast, Gd-Fe interaction is much stronger than other  $RE$ -Fe interactions in  $RE_6FeBi_2$ , which is characterized by the  $a/c$  of  $Gd_6FeBi_2$  much smaller than the extrapolated value from the linear relationship between  $a/c$  and atomic radii of  $RE$  elements in other  $RE_6FeBi_2$ . Thus a stronger overlap of electron wave functions between Gd 5d electron bands and Fe 3d electron bands is expected, accounting for the magnetic moment from Fe in  $Gd_6FeBi_2$ . Such strong Gd-Fe interaction also benefits the spin polarization of Gd 5d electrons for an extra magnetic moment, in consistent with DFT calculations. In  $Gd_6CoTe_2$ , however, the overlap should be very weak or negligible due to the weak Gd-Co interaction, and a net magnetic moment from Co may not be expected.

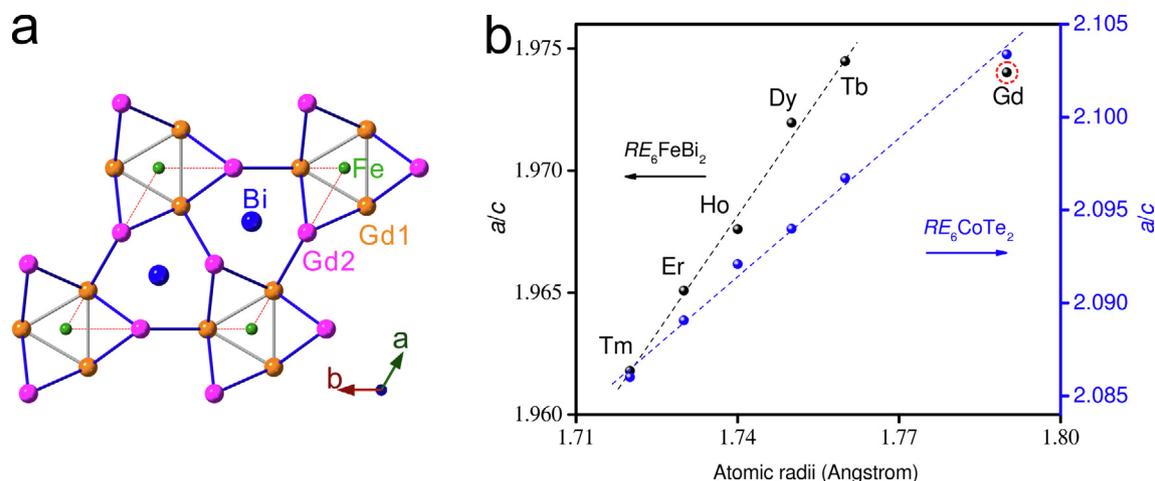
The interactions between Gd and Fe in  $Gd_6FeBi_2$  can be inspected more directly from its electronic structure, as seen in the XPS spectra in



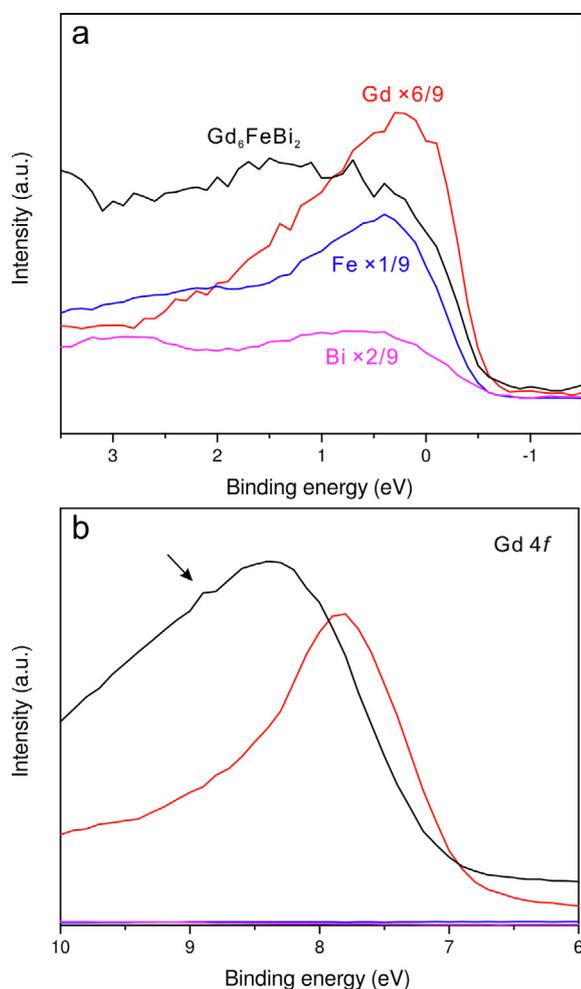
**Fig. 4.** (a) Scaled magnetization of the  $Gd_6FeBi_2$  compound below and above  $T_c$ , using critical exponents given by the Kouvel-Fisher plot. (b) The scaled magnetization and field are plotted in the form of  $m^2$  vs.  $h/m$  for the  $Gd_6FeBi_2$  compound. The inset in (a) shows the same plot on a log-log scale.

**Fig. 6.** Compared with sharp peaks in their electronic density of states (DOS) around the fermi level  $E_F$  in Gd and Fe metals,  $Gd_6FeBi_2$  has a more flat DOS up to several eV below  $E_F$  (Fig. 6a), suggestive of Gd-Fe hybridization and in agreement with previous DFT calculations. The low and flat DOS at  $E_F$  supports the high stability of  $Gd_6FeBi_2$ , because the orbital splitting due to the hybridization allows more low-energy bands. However, the DOS of  $Gd_6FeBi_2$  at  $E_F$  is still much larger than that of  $Gd_4Bi_3$  [14], a compound with a high  $T_c$  (340 K) due to an extra Bi magnetic moment induced by the strong Gd-Bi hybridization [17]. Thus the magnetic contributions from Gd 5d and Fe 3d are expected in  $Gd_6FeBi_2$ , despite the reduced magnetic moment from  $d$  electrons due to some unpaired  $d$  electrons in these elements moved into lower energy orbitals to pair other electrons after the hybridization.

Compared with the strong overlap of  $d$  electron wave functions between neighbouring atoms in Gd and Fe metals, the overlap is effectively reduced in  $Gd_6FeBi_2$  due to the hybridization and low DOS around  $E_F$ . Therefore the exchange interaction between Gd 5d and Fe 3d  $Gd_6FeBi_2$  in should be weaker than those of Gd 5d - Gd 5d in Gd and  $TM$  3d -  $TM$  3d in Fe, which accounting for critical exponents more close to the values predicted by the long range interactions. In other words, the critical exponents corresponding to the Ising or Heisenberg model in  $Gd$ - $TM$  alloys should result from the  $TM$ - $TM$  exchange interaction, because the Gd- $TM$  exchange interaction is not strong enough. Thus the critical behavior of  $Gd$ - $TM$  alloys can be tuned from the Ising/Heisenberg model to the mean-field model by hybridizing  $TM$  with a third element (e.g. metalloid elements). This is exactly the case of  $Gd_4Co_3$  alloys doped by Si: from  $\beta = 0.389$  and  $\gamma = 1.229$  in  $Gd_4Co_3$  to



**Fig. 5.** (a) The representative crystal structure of  $Gd_6FeBi_2$  viewed along  $c$  axis, and (b) plots of  $a/c$  against atomic radii of  $RE$  elements in  $RE_6FeBi_2$  (black) and  $RE_6CoTe_2$  (blue). The dashed circle in (b) emphasizes the contraction in the basal plane of  $Gd_6FeBi_2$ . (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)



**Fig. 6.** XPS spectra of  $Gd_6FeBi_2$  and the constitute elements in the valence band (a) and Gd  $4f$  region (b). The intensity in XPS spectra of constitute elements is multiplied by their fraction in the formula. In the  $4f$  band of  $Gd_6FeBi_2$ , a shoulder peak is arrowed and the much high intensity is due to the strong inelastic electronic scattering.

$\beta = 0.465$  and  $\gamma = 1.134$  in  $(Gd_4Co_3)_{0.9}Si_{0.1}$  [33].

The ordering temperature in these compounds should be related to not only the magnetic moment, but also the vibronic coupling effects.

Due to the strong Gd-Fe hybridization, the influence of such coupling on  $d$  electrons in  $Gd_6FeBi_2$  should be much smaller than those of the Gd metal, and thus the short-range exchange interaction in  $Gd_6FeBi_2$  diminishes more slowly with increased temperatures, accounting for the elevated  $T_c$  and the deviation from the Curie-Weiss paramagnetic behavior above  $T_c$ . Similar phenomena are also observed in Si-doped  $Gd_4Co_3$  with an increased  $T_c$  (213 K against 208 K in  $Gd_4Co_3$ ) [33].

Compared with Gd, the  $4f$  band of  $Gd_6FeBi_2$  has a lower energy state (more below the  $E_F$ ) and shows a clear splitting feature as a results of the hybridization and crystal-field effect (Fig. 6b), suggestive of the higher structural stability. Although it does not produce extra moment, the split peak shifting towards low energy and spin-spin interactions should make it stronger against the vibronic coupling and thus also contribute to an elevated  $T_c$ . Such splitting of majority bands seems to be a common feature of electronic structures in the Gd-NME alloys with a high  $T_c$ , such as  $Gd_5Si_4$ ,  $Gd_4Bi_3$  and the present compound [11,17,34]. It is also suggested by the observation that the temperature shift of the vibronic peak was proportional to the splitting of ground level in La-CaMnO perovskite manganites [35]. However, the splitting also implies a wider temperature region of the magnetic transition or a small slope of moment against temperature, leading to small magnetic entropy change as confirmed by experiments on these alloys [34,36–38].

#### 4.3. Crystal-field effects

According to above discussion, the crystal-field effect related to the Gd-Fe hybridization also plays an important role for the high  $T_c$ , and thus a brief analysis is needed. The local atomic environments (AEs) around two kinds of Gd atoms in  $Gd_6FeBi_2$  can be representatively depicted as Gd-centered polyhedra, as shown in Fig. 7a and 7b. It is clear that Gd1 at  $3g$  site has an octahedral symmetry marked as  $O_h$ , while Gd2 at  $3f$  site shows a  $C_{4v}$  symmetry in the form of square pyramid. For the  $O_h$  symmetry, the sevenfold orbitally degenerate F item of the free Gd atom with one  $f$  electron in each orbital is split by the octahedral crystal field into three terms as depicted in Fig. 7c: one is nondegenerate ( $A_{2u}$ ) and two are threefold degenerate ( $T_{1u}$  and  $T_{2u}$  respectively) [39,40]. The splitting suggests DOS spectra of two main peaks of high energy levels plus a narrow peak of low energy levels. For the  $C_{4v}$  symmetry, the F item is split into five terms (three non-degenerate items  $A_1$ ,  $B_1$ ,  $B_2$  and two twofold degenerate items  $E_1$  and  $E_2$ ) by the ligand field of square prism, as shown in Fig. 7d [38]. Generally, the energy gap of the splitting  $F \rightarrow A_1 + B_1 + B_2 + E_1 + E_2$  is small, thus one or two broadening  $4f$  peak instead of five peaks was expected. In the splitting  $F \rightarrow A_{2u} + T_{1u} + T_{2u}$ , the energy gaps

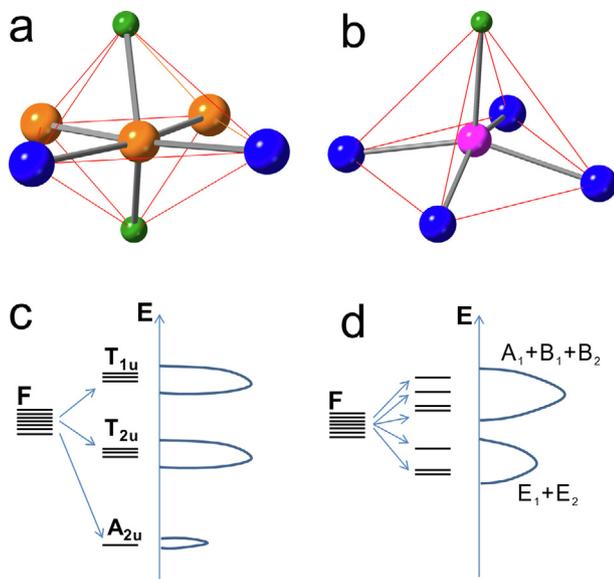


Fig. 7. Atomic environments of Gd atoms in  $Gd_6FeBi_2$ : (a) Gd1 atom and (b) Gd2 atom, and schematic illustration on corresponding crystal-field splitting of energy bands for Gd1 (c) and Gd2 (d).

between T items and F is small compared with that between A and F, and seems similar to that in the splitting of  $C_{4v}$  symmetry. Thus a broadening 4f peak including T, B, E and  $A_1$  items is expected, while the  $A_{2u}$  can be also enclosed or form a split peak. If  $A_{2u}$  formed a split peak, the ratio of the small peak to the main peak should be around 1:13 in intensity. The inference is well supported by the observation of a shoulder in the broad Gd 4f XPS peak (Fig. 6b). It should be noted that the energy gap of band splitting is highly dependent on the strength of crystal fields and shortly expressed as [38]

$$\Delta = 5/3eqFR \quad (17)$$

where  $e$  is electronic charge,  $q$  atomic effective charge,  $R$  is interatomic distance and  $F$  is a function of  $R$ . Thus the isostructural compounds can show different electronic structure, e.g. larger splitting energy which can even induce the filling of minor bands, or no observed splitting peak which corresponds for a relatively lower Curie temperature. In the viewpoint here, the low  $T_c$  in the isostructural  $Gd_6CoTe_2$  can be well understood [31]. In turn, the energy gap of the splitting also is an indicator characterizing the stability of the crystal structure.

## 5. Conclusions

In conclusion, the critical behaviors of  $Gd_6FeBi_2$  at  $T_c$  are investigated comprehensively by isothermal magnetization, and estimated critical exponents are more close to the values predicted by the mean-field model. The analyses based on its crystal and electronic structure show that the Gd-Fe exchange interaction is much weaker than Fe-Fe exchange interaction and thus its influence on the critical behavior is limited, which is likely a typical feature for  $RE-TM$  alloys without  $TM-TM$  exchange interactions. Due to the strong Gd-Fe hybridization, the influence of vibronic couplings on the Gd-Fe short-range exchange interaction is diminished, accounting for the high  $T_c$ . On the other hand, the crystal-field effect results in the broadening or splitting of  $f$ -electron bands, which provides another important insight for the elevated  $T_c$  in Gd-NME compounds, and remarkably different magnetic behaviors among isostructural compounds.

## Acknowledgements

We thank Dr. Z.G. Zheng in South China University of Technology for kind discussions on critical behaviors. The work was supported by

National Key R&D Program of China [Grant No. 2016YFE0204200] and also partially supported by a grant from the Research Grants Council of Hong Kong SAR [(RGC Project No.) CityU 11253716].

## References

- [1] F. Meng, C. Magliocchi, T. Hughbanks, Synthesis, structure and bonding of  $Gd_6MTe_2$  ( $M = Co, Ni$ ),  $Er_6RuTe_2$ , J. Alloys Compd. 358 (2003) 98–103, [https://doi.org/10.1016/S0925-8388\(03\)00456-0](https://doi.org/10.1016/S0925-8388(03)00456-0).
- [2] A.V. Morozkin, New  $Zr_6CoAs_2$ -type  $R_6FeSb_2$  ( $R = Sc, Y, Lu, Dy, Ho, Tm$ ) and  $Ho_6FeBi_2$  compounds, J. Alloys Compd. 353 (2003) L16–L18, [https://doi.org/10.1016/S0925-8388\(02\)01322-1](https://doi.org/10.1016/S0925-8388(02)01322-1).
- [3] L. Zeng, H. Zhao, The 773 K isothermal section of the Ho–Fe–Sb ternary system, J. Alloys Compd. 366 (2004) 201–204, <https://doi.org/10.1016/j.jallcom.2003.07.003>.
- [4] A.V. Morozkin, R. Nirmala, S.K. Malik, Structural and magnetic properties of Fe2P-type  $R_6TX_2$  compounds ( $R = Zr, Dy, Ho, Er, T = Mn, Fe, Co, Cu, Ru, Rh, X = Sb, Bi, Te$ ), Intermetallics 19 (2011) 1250–1264, <https://doi.org/10.1016/j.intermet.2011.04.002>.
- [5] A.V. Morozkin, New  $Zr_6CoAs_2$ -type  $R_6FeBi_2$  ( $R = Y, Lu, Gd-Dy, Er, Tm$ ) compounds, J. Alloys Compd. 358 (2003) L9–L10, [https://doi.org/10.1016/S0925-8388\(03\)00134-8](https://doi.org/10.1016/S0925-8388(03)00134-8).
- [6] A.V. Morozkin, Magnetic structures of  $Zr_6CoAs_2$ -type  $Ho_6FeSb_2$ ,  $Ho_6CoBi_2$ ,  $Ho_6FeBi_2$  and  $Ho_6MnBi_2$  compounds, J. Alloys Compd. 395 (2005) 7–16, <https://doi.org/10.1016/j.jallcom.2004.11.022>.
- [7] A.V. Morozkin, V.N. Nikiforov, B. Malaman, Magnetic structure of the  $Zr_6CoAs_2$ -type  $Tb_6FeBi_2$  compound, J. Alloys Compd. 393 (2005) L6–L9, <https://doi.org/10.1016/j.jallcom.2004.08.103>.
- [8] G. Cai, J. Zhang, W. He, P. Qin, L. Zeng, Crystal structure and magnetic properties of  $Tb_6FeSb_2$ , J. Alloys Compd. 421 (2006) 42–44, <https://doi.org/10.1016/j.jallcom.2005.11.020>.
- [9] W. He, J. Zhang, L. Zeng, P. Qin, G. Cai, Thermomagnetic properties near transitions of  $Tb_6FeX_2$  ( $X = Sb, Bi$ ), J. Alloys Compd. 443 (2007) 15–19, <https://doi.org/10.1016/j.jallcom.2006.10.005>.
- [10] F. Wang, J. Zhang, F. Yuan, Y. Cao, C. Gao, Y. Hao, J. Shen, J. Sun, B. Shen, Magnetic properties and magnetocaloric effect in  $Ho_{6-x}Er_xMnBi_2$  compounds, J. Appl. Phys. 107 (2010) 09A918, <https://doi.org/10.1063/1.3359812>.
- [11] J. Zhang, G. Shan, Z. Zheng, C.H. Shek, Structure and magnetic behaviors of  $Gd_6FeBi_2$  compound, Intermetallics 68 (2016) 51–56, <https://doi.org/10.1016/j.intermet.2015.07.013>.
- [12] A.V. Morozkin, V.K. Genchel, A.V. Knotko, V.O. Yapaskurt, J. Yao, S. Quezado, S.K. Malik, Structural and magnetic properties of Fe2P-type  $R_6TTe_2$  compounds ( $R = Tb, Dy, Ho, Er, T = Fe, Co, Ru$ ): Magnetic properties and specific features of magnetic entropy change, J. Solid State Chem. 258 (2018) 201–211, <https://doi.org/10.1016/j.jssc.2017.10.023>.
- [13] J. Szade, M. Neumann, Electronic structure investigation of Gd intermetallics, J. Phys.: Condens. Matter 11 (1999) 3887–3896, <https://doi.org/10.1088/0953-8984/11/19/308>.
- [14] J. Szade, M. Drzyzga, Magnetism and electronic structure of  $Gd_6Bi_3$  and  $Gd_4Bi_3$ , J. Alloys Compd. 299 (2000) 72–78, [https://doi.org/10.1016/S0925-8388\(99\)00799-9](https://doi.org/10.1016/S0925-8388(99)00799-9).
- [15] T. Nilges, Understanding of magnetic ordering in Gd-rich compounds, Acta Cryst. C 75 (2019) 609, <https://doi.org/10.1107/S2053229619007149>.
- [16] J.O. Dimmock, A.J. Freeman, Band structure and magnetism of gadolinium metal, Phys. Rev. Lett. 13 (1964) 750–752, <https://doi.org/10.1103/PhysRevLett.13.750>.
- [17] X.B. Liu, Z. Altounian, Exchange interaction in  $Gd_4Bi_3$  and Gd from First-Principles calculations, IEEE Trans. Mag. 45 (2009) 3989–3992, <https://doi.org/10.1109/TMAG.2009.2023063>.
- [18] J. Zhang, Y.M. Kang, G. Shan, S. Bobev, Structural analysis of  $Gd_6FeBi_2$  from single-crystal X-ray diffraction methods and electronic structure calculations, Acta Cryst. C 75 (2019) 562–567, <https://doi.org/10.1107/S2053229619004868>.
- [19] S.N. Kaul, S. Srinath, Gadolinium: A helical antiferromagnet or a collinear ferromagnet, Phys. Rev. B 62 (2000) 1114–1117, <https://doi.org/10.1103/PhysRevB.62.1114>.
- [20] H.E. Stanley, Introduction to Phase Transitions and Critical Phenomena, Oxford University Press, London, 1971.
- [21] B.J. Beaudry, A.H. Daane, The Sc-Gd system, J. Less-Common Met. 6 (1964) 322–325, [https://doi.org/10.1016/0022-5088\(64\)90129-8](https://doi.org/10.1016/0022-5088(64)90129-8).
- [22] L.P. Levy, Magnetism and Superconductivity, Springer-Verlag, Berlin Heidelberg, 2000.
- [23] A. Arrott, Criterion for ferromagnetism from observations of magnetic isotherms, Phys. Rev. 108 (1957) 1394–1396, <https://doi.org/10.1103/PhysRev.108.1394>.
- [24] B.K. Banerjee, On a generalised approach to first and second order magnetic transitions, Phys. Lett. 12 (1964) 16–17, [https://doi.org/10.1016/0031-9163\(64\)91158-8](https://doi.org/10.1016/0031-9163(64)91158-8).
- [25] A. Arrott, J.E. Noakes, Approximate equation of state for nickel near its critical temperature, Phys. Rev. Lett. 19 (1967) 786–789, <https://doi.org/10.1103/PhysRevLett.19.786>.
- [26] S.N. Kaul, Static critical phenomena in ferromagnets with quenched disorder, J. Magn. Magn. Mater. 53 (1985) 5–53, [https://doi.org/10.1016/0304-8853\(85\)90128-3](https://doi.org/10.1016/0304-8853(85)90128-3).
- [27] A.K. Pramanik, A. Banerjee, Critical behavior at paramagnetic to ferromagnetic phase transition in  $Pr_0.5S_{0.5}Mn_0.3$ : A bulk magnetization study, Phys. Rev. B 79 (2009) 214426, <https://doi.org/10.1103/PhysRevB.79.214426>.

- [28] J.S. Kouvel, M.E. Fisher, Detailed magnetic behavior of nickel near its Curie point, *Phys. Rev.* 136 (1964) A1626–A1632, <https://doi.org/10.1103/PhysRev.136.A1626>.
- [29] D. Hohnke, E. Parthé, Rare-earth bismuthides with D88 and Hf<sub>5</sub>Sn<sub>3</sub>Cu-type structures, *J. Less-Common Met.* 17 (1969) 291–296, [https://doi.org/10.1016/0022-5088\(69\)90146-5](https://doi.org/10.1016/0022-5088(69)90146-5).
- [30] L.P. Kadanoff, W. GÖtze, D. Hamblen, R. Hecht, E.A.S. Lewis, V.V. Palciauskas, M. Rayl, J. Swift, D. Aspnes, J. Kane, Static phenomena near critical points: Theory and Experiment, *Rev. Mod. Phys.* 39 (1967) 395–431, <https://doi.org/10.1103/RevModPhys.39.395>.
- [31] A.V. Morozkin, Y. Mozharivskiy, V. Svitlyk, R. Nirmala, O. Isnard, P. Manfrinetti, A. Provino, C. Ritter, Magnetic properties of Fe<sub>2</sub>P-type R<sub>6</sub>CoTe<sub>2</sub> compounds (R = Gd–Er), *J. Solid State Chem.* 183 (2010) 1314–1325, <https://doi.org/10.1016/j.jssc.2010.04.002>.
- [32] S. Legvold, *Rare Earth Metals and Alloys*, in: E.P. Wohlfarth (Ed.), *Handbook of Magnetic Materials*, North-Holland Publishing Company, North Holland, 1980, pp. 183–296.
- [33] Z.G. Zheng, X.C. Zhong, Z.W. Liu, D.C. Zeng, V. Franco, J.L. Zhang, Magnetocaloric effect and critical behavior of amorphous (Gd<sub>4</sub>Co<sub>3</sub>)<sub>1-x</sub>Si<sub>x</sub> alloys, *J. Magn. Mater.* 343 (2013) 184–188, <https://doi.org/10.1016/j.jmmm.2013.04.087>.
- [34] Y.I. Spichkin, V.K. Pecharsky, K.A. Gschneidner, Preparation, crystal structure, magnetic and magnetothermal properties of (Gd<sub>x</sub>R<sub>5-x</sub>)Si<sub>4</sub>, where R=Pr and Tb, alloys, *J. Appl. Phys.* 89 (2001) 1738–1745, <https://doi.org/10.1063/1.1335821>.
- [35] V.A. Voloshin, A.A. Gusev, I.A. Danilenko, L.I. Medvedeva, A.D. Prokhorov, S.I. Khartsev, Interplay of structure, magnetism and resistivity of La<sub>0.5</sub>Ca<sub>0.54</sub>MnO<sub>3+x</sub>, *Phys. Lett. A* 271 (2000) 121–127, [https://doi.org/10.1016/S0375-9601\(00\)00326-1](https://doi.org/10.1016/S0375-9601(00)00326-1).
- [36] S.Y. Dan'kov, A.M. Tishin, V.K. Pecharsky, K.A. Gschneidner, Magnetic phase transitions and the magnetothermal properties of gadolinium, *Phys. Rev. B* 57 (1998) 3478–3490, <https://doi.org/10.1103/PhysRevB.57.3478>.
- [37] X.J. Niu, K.A. Gschneidner, A.O. Pecharsky, V.K. Pecharsky, Crystallography, magnetic properties and magnetocaloric effect in Gd<sub>4</sub>(Bi<sub>x</sub>Sb<sub>1-x</sub>)<sub>3</sub> alloys, *J. Magn. Mater.* 234 (2001) 193–206, [https://doi.org/10.1016/S0304-8853\(01\)00391-2](https://doi.org/10.1016/S0304-8853(01)00391-2).
- [38] J. Zhang, Z. Zheng, G. Shan, S. Bobev, C.H. Shek, Abnormal thermal expansion, multiple transitions, magnetocaloric effect, and electronic structure of Gd<sub>6</sub>Co<sub>4.85</sub>, *J. Appl. Phys.* 118 (2015) 133903, <https://doi.org/10.1063/1.4931982>.
- [39] I.B. Bersuker, *Electronic Structure and Properties of Transition Metal Compounds: Introduction to the Theory*, second ed., John Wiley & Sons Inc, New Jersey, 2010.
- [40] G.C. Shan, H.B. Gao, New topological semimetal candidate of nonsymmorphic PdSb<sub>2</sub> with unique six-fold degenerate point, *Front. Phys.* 14 (2019) 43201, <https://doi.org/10.1007/s11467-019-0909-0>.