



Investigation of the interaction of some astrobiological molecules with the surface of a graphite (0001) substrate. Application to the CO, HCN, H₂O and H₂CO molecules

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ABSTRACT

Detailed interaction potential energy calculations are performed to determine the potential energy surface experienced by the molecules CO, HCN, H₂O and H₂CO, when adsorbed on the basal plane (0001) of graphite at low temperatures. The potential energy surface is used to find the equilibrium site and configuration of a molecule on the surface and its corresponding adsorption energy. The diffusion constant associated with molecular surface diffusion is calculated for each molecule.

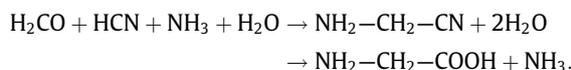
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1. Introduction

Observations in the cold regions of the interstellar medium (ISM) with typical temperatures of about 10–20 K have revealed the presence of clouds which contain high densities (more than 10³ particle per cm³) of atoms, radicals and simple molecules such as H₂, CO, CO₂, HCN, H₂O (the most abundant molecule), NH₃, H₂CO, CH₄, CH₃OH, as well as small solids typically composed of amorphous H₂O, silicates and carbon grains in the form of graphite, amorphous structures and polycyclic aromatic hydrocarbon (PAH) molecules [1,2].

It is nowadays thought that the dominant mechanism for the formation of molecules is provided by surface-catalysed chemical reactions on low temperatures interstellar dust grains. For instance, Watanabe and Kouchi [3] have experimentally produced the formaldehyde H₂CO and methanol CH₃OH molecules by successive hydrogenation of CO on the surface of icy grains at 10 K, as was theoretically proposed by Tielens et al. [4]. Recent laboratory experiments reported that more complex molecules such as glycine and other amino acids (which play an important role in the origin and evolution of life), as well as other organic species, were formed from ultraviolet (UV) irradiation of the analogues of icy interstellar grains held at low temperatures ($T \sim 15$ K) and containing small amounts of HCN, NH₃, H₂CO, and CH₃OH species [5,6].

Stanley Miller [7] in his experiments reported that the production of glycine proceeds *via* the Strecker's chemical reaction



Theoretical quantum-chemical calculations on the synthesis of amino acids were reported by Woon [8] for UV-irradiated astrophysical ices and by Mendoza et al. [9] for ice analogues on the surface of a coronene (PAH) molecule.

Investigations of the chemical processes leading to the production of amino acids on the surface of grains require a knowledge of the interactions between the molecules participating in these processes on the surface, and then of their adsorption characteristics (such as the equilibrium configurations and diffusion constants) when they are isolated on the grain surface.

The interaction of a single water molecule with a graphite surface and with PAH molecules such as the fused-benzene molecules (fbz)_{*n*} (C₆H₆, C₂₄H₁₂, C₅₄H₁₈, C₉₆H₂₄,... for *n* = 1, 7, 19, 37, ..., respectively) has been theoretically studied using *ab-initio* computational methods to determine the binding energies and equilibrium configurations [10–26].

For the water–benzene complex, various authors have reported binding energies: –169 [13], –120 [17,21,25], and –99 meV [22]. The available experimental values are –98 [27], and –106 meV [28].

For the water–C₉₆H₂₄ complex Feller and Jordan [16] have reported a binding energy of –251 meV, which is twice as large as the recently reported value –126 meV by Lin et al. [22]. Nevertheless, in order to determine the influence of the C–H bonds on the interaction for the water–(fbz)_{*n*} complexes up to *n* = 19, Sudiarta and Geldart [23] have reported calculations on both hydrogen and fluorine terminated (fbz)_{*n*}, and after extrapolating the results

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to a graphite sheet (graphene) they obtained a binding energy of -104 meV.

Moreover, various other studies on H_2O adsorbed on graphene have given binding energies of -187 [10], -72 [12], -109 [29], and -138 meV [26].

For the single water molecule adsorbed on the graphite substrate (multi-sheets), several authors reported theoretical binding energy values of -161 [11], -149 [14], -100 [15], -171 [19], -73 [18], -70 [20], -91 [24], -174 [30], and -155 meV [26]. However, the only available experimental value is -156 meV which was measured by Avgul and Kieslev [31].

In the case of the carbon monoxide molecule adsorbed on the graphite surface, experimental data were reported by Beebe et al. [32], Kieslev et al. [33], and Piper et al. [34]. They measured the isosteric heat of adsorption at the zero coverage limit. The obtained values are: 125 meV in the temperature range 192 – 221 K [32], 110 meV in the temperature range 118 – 148 K [33], and ~ 113 meV in the temperature range 79 – 119 K [34]. The latter authors have also estimated, using Monte Carlo simulations, an isosteric heat of adsorption of 113 meV at 79 K.

Finally, it must be noticed that in several of the computational works mentioned above some contributions to the interaction were ignored. For instance, for the water–graphite system the binding energies are $\gtrsim -100$ meV when the hydrogen quantum contributions (see Section 2 below) are neglected and $\lesssim -100$ meV, otherwise [18].

There are apparently no reported studies for HCN and H_2CO single molecules interacting with a graphite surface or with PAH molecules.

In the present work, we study the adsorption properties of several of the molecules which are associated with the synthesis of amino acids. We use the graphite (0001) basal plane as a model substrate to represent the surface of an interstellar dust grain and we consider the surface adsorption of the various molecules on the model surface. We use an approach which we have already developed to determine the adsorption characteristics and infrared spectra of various single molecules adsorbed on a variety of surfaces [35–39].

This paper is organized as follows. In Section 2, we briefly present the contributions to the interaction potential energy of the adsorbed molecule on the adsorbing surface. In Section 3 we describe the minimization process needed to find the possible equilibrium positions of the adsorbed molecule on the surface and give details of the observables which are to be calculated. Section 4 gives the results obtained for the several molecules studied; typical potential surfaces are shown in the figures, to augment the sometimes complicated verbal description of the equilibrium positions of the molecule.

2. Theoretical background

An adsorbed species can be either physically or chemically bonded to the surface of the substrate crystal. In physisorption the interaction is due to the comparatively weak van der Waals–London and electric field–multipole forces, and the interaction potential energy is fairly low (≤ 0.5 eV), with no charge exchange between the adsorbed species and the substrate.

2.1. The physisorbed molecule on a graphite substrate

In this work, we consider a single molecule such as CO, HCN, H_2O or H_2CO physisorbed on a graphite basal plane (0001) at low temperatures.

The graphite crystal is extensively used as a model to simulate the behaviour of interstellar grains in studies of the physical and

chemical behaviour of adsorbed molecular species. Experimentally detected absorption features due to carbon grains have been attributed to the presence of small spherical graphite crystals of size ~ 200 Å in interstellar dust clouds [1,2].

In order to reduce the required numerical calculation times, the graphite crystal is modelled by using ten planes with radii ~ 35 Å (~ 1500 carbon atom per plane). This does not significantly influence the interaction potential energy between the molecule and the substrate (giving an error $< 1\%$).

Fig. 1 shows the geometrical characteristics of a molecule (H_2CO for instance) adsorbed on the graphite surface. This figure also indicates three particular position sites (A, the hexagon centre; B, the middle of the C–C bond; and C, the carbon atom) above which binding energy values will be given for some configurations of the adsorbed molecule.

To perform the calculations, we need to define:

- (i) an absolute frame ($O, \mathbf{X}, \mathbf{Y}, \mathbf{Z}$) connected to the surface of the substrate, with respect to which all of the vectors and the tensors associated with the molecule and the graphite carbon atoms must be described;
- (ii) a frame ($G, \mathbf{x}, \mathbf{y}, \mathbf{z}$) tied to the molecule with centre of mass G , and with respect to which the molecular vibrational motions are still described. The transformation from the absolute frame to the molecular frame is obtained by using the Rose's rotational matrix [40], in terms of the molecular orientational degrees of freedom $\Omega = (\varphi, \theta, \chi)$ (precession, nutation, and proper rotation Euler angles).

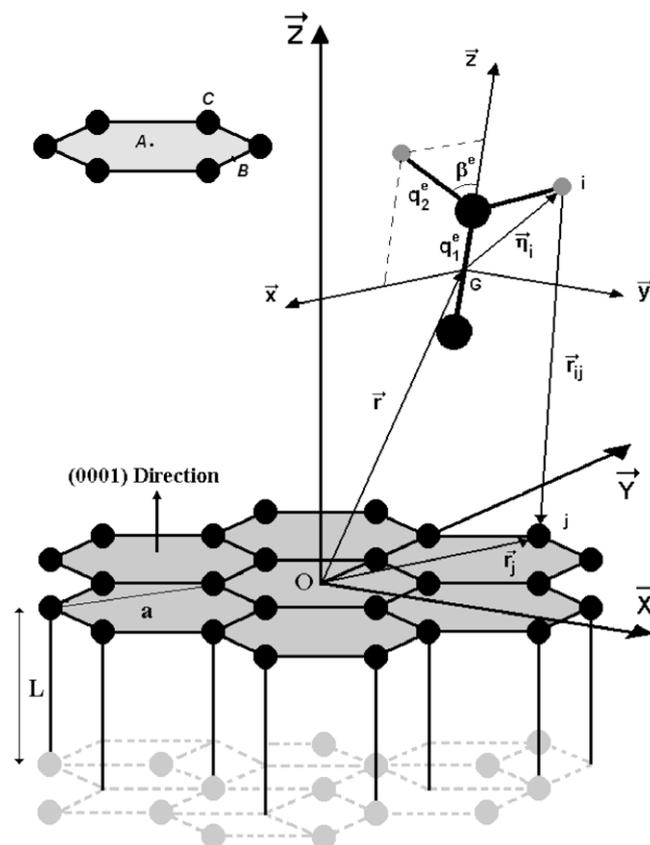


Fig. 1. Geometrical characteristics of an H_2CO molecule adsorbed on the graphite (0001) substrate. ($O, \mathbf{X}, \mathbf{Y}, \mathbf{Z}$) and ($G, \mathbf{x}, \mathbf{y}, \mathbf{z}$) represent the surface absolute frame and the molecular frame, respectively. L and a are the interlayer spacing and the distance between two next-nearest neighbour carbon atoms of the graphite and q_1^e , q_2^e and β^e define the equilibrium internal coordinates of the adsorbed molecule. The A, B, and C sites are, respectively, the hexagon centre, the middle of the carbon–carbon bond, and the graphite carbon atom.

2.2. Interaction potential energy

The interaction potential energy V_{MG} between an adsorbed molecule and the graphite substrate can be written as the sum of three parts

$$V_{MG} = V_{LJ} + V_E + V_I, \quad (1)$$

which are detailed below.

2.2.1. Quantum contributions

The first term V_{LJ} in Eq. (1) is generally treated by using semi-empirical 12-6 Lennard-Jones (LJ) pairwise atom-atom potentials to describe the short-range atomic repulsion energy arising from the overlap of the electronic clouds of the adsorbate and the substrate at very short distances and also the long-range many-body dispersion energy arising from the lowering of the quantum zero-point energy of the system by the correlated fluctuations of the adsorbate and substrate atomic dipoles.

However, it is widely known that carbon atoms in the graphite basal plane (0001) exhibit anisotropic polarizability effects which modify the spherical shape of these atoms. To account for these anisotropies, Carlos and Cole [41] proposed a modified expression for V_{LJ} , of the form

$$V_{LJ} = \sum_j \sum_i 4\epsilon_{ij} \left\{ \left(\frac{\sigma_{ij}}{|\mathbf{r}_{ij}|} \right)^{12} \left[1 + \gamma_R \left(1 - \frac{6}{5} \cos^2 \theta_{ij} \right) \right] - \left(\frac{\sigma_{ij}}{|\mathbf{r}_{ij}|} \right)^6 \left[1 + \gamma_A \left(1 - \frac{3}{2} \cos^2 \theta_{ij} \right) \right] \right\}. \quad (2)$$

In this equation, \mathbf{r}_{ij} is the distance vector between the i th atom of the molecule and the j th carbon atom of the graphite substrate (Fig. 1), while ϵ_{ij} and σ_{ij} are the mixed LJ potential parameters, obtained from the usual Lorentz-Berthelot combination rules $\epsilon_{ij} = \sqrt{\epsilon_{ii}\epsilon_{jj}}$ and $2\sigma_{ij} = \sigma_{ii} + \sigma_{jj}$. The two coefficients γ_R and γ_A specify the modifications to the repulsion and dispersion parts of the energy, respectively, and θ_{ij} is the angle between the surface normal axis and the \mathbf{r}_{ij} vector. The various molecule-graphite mixed parameters are given in Table 1. Note that the LJ parameters used in this work have been improved several times in our other works.

2.2.2. Electrostatic and induction contributions

It is well known that the bonds in the graphite crystal give rise to aspherical atomic charge distributions which produce multipole electrostatic fields with rapid spatial variations external to the graphite [12]. This phenomenon is modelled by introducing axially symmetric quadrupole moment tensors Θ^c at each carbon atom site [12].

The quadrupole moment tensor Θ^c of the j th carbon atom produces the electrical potential

$$\Phi^j(\mathbf{r}) = \frac{1}{3} L_p \nabla \nabla \left(\frac{1}{|\mathbf{r}_j - \mathbf{r}|} \right) : \Theta^c, \quad (3)$$

on the molecule at its centre of mass position \mathbf{r} . In turn, the multipole moments ($\boldsymbol{\mu}$, Θ , ...) of the molecule produce the electrical potential

Table 1
Lennard-Jones parameters for atom-graphite combinations.

Gr-atom	ϵ (meV)	σ (Å)	γ_A^a	γ_R^a
Gr-H	2.265	2.965	0.4	-0.54
Gr-O	3.450	3.141	0.4	-1.05
Gr-C	2.981	3.305	0.4	-1.05
Gr-N	2.811	3.390	0.4	-1.05

^a From Refs. [41–45].

$$\Phi^M(\mathbf{r}_j) = L_p \nabla \left(\frac{1}{|\mathbf{r}_j - \mathbf{r}|} \right) \cdot \boldsymbol{\mu} + \frac{1}{3} L_p \nabla \nabla \left(\frac{1}{|\mathbf{r}_j - \mathbf{r}|} \right) : \Theta + \dots, \quad (4)$$

on the j th carbon atom at position \mathbf{r}_j .

In Eqs. (3) and (4), L_p is a screening factor, equal to 1 for the surface plane and to $2/(\epsilon + 1)$ for the internal planes ($p \geq 2$), where ϵ is the static dielectric constant of the graphite crystal, which we take to be 2.8 [45].

The electrostatic and induction contributions to the interaction potential energy V_{MG} are

$$V_E = \sum_j \boldsymbol{\mu} \cdot \nabla \Phi^j(\mathbf{r}) + \frac{1}{3} \sum_j \Theta : \nabla \nabla \Phi^j(\mathbf{r}) + \dots \quad (5)$$

$$V_I = -\frac{1}{2} \sum_j [\nabla \Phi^M(\mathbf{r}_j) : \boldsymbol{\alpha}^c : \nabla \Phi^M(\mathbf{r}_j)] - \frac{1}{2} \sum_{jj'} [\nabla \Phi^j(\mathbf{r}) : \boldsymbol{\alpha}^c : \nabla \Phi^{j'}(\mathbf{r})], \quad (6)$$

where $\boldsymbol{\alpha}$ and $\boldsymbol{\alpha}^c$ are the polarizability tensors of the molecule and of the graphite carbon atoms, respectively.

The elements of the polarizability $\boldsymbol{\alpha}^c$ and quadrupole moment Θ^c tensors (Eqs. (3)–(6)) of the carbon atoms are given in the absolute frame (O, X, Y, Z) by

$$\alpha_{XX}^c = \alpha_{YY}^c = \alpha_{\perp}^c \text{ and } \alpha_{ZZ}^c = \alpha_{\parallel}^c, \quad (7)$$

$$\Theta_{XX}^c = \Theta_{YY}^c = -\frac{1}{2} \Theta_{ZZ}^c = -\frac{1}{2} \Theta^c, \quad (8)$$

with all other elements being zero. Note that graphite is about 3.5 times more polarizable in-plane than perpendicular to the plane [46].

Moreover, it must be noticed that the molecular frame corresponds, for each of the studied molecules, to its principal frame of inertia, in which only the z -component of the dipole moment $\boldsymbol{\mu}$ vector and the three diagonal elements of the polarizability $\boldsymbol{\alpha}$ and quadrupole moment Θ tensors are non-vanishing elements. In the potential energy calculations these quantities must be expressed in the absolute frame by using the Rose's rotational matrix transformation [40].

The various geometrical and electrical parameters of the graphite substrate and of the studied molecules are given in Table 2.

2.2.3. Separation of V_{MG}

The distance vector \mathbf{r}_{ij} in Eq. (2) can be expressed as

$$\mathbf{r}_{ij} = \mathbf{r}_j - \mathbf{r} - \boldsymbol{\eta}_i, \quad (9)$$

where \mathbf{r} and \mathbf{r}_j are the position vectors of the molecular centre of mass and the j th graphite carbon atom, respectively.

Table 2
Molecular and graphite parameters: internal bonds and angles, dipole moments, polarizabilities, quadrupole moments, and rotational constants for the molecules studied.

Molecule	CO	HCN	H ₂ O	H ₂ CO	Graphite ^a	
$\langle q^e \rangle$ (Å)	1.144	1.150	0.958	1.198	L (Å)	3.36
	–	1.079	–	1.121	a (Å)	2.46
β^e (°)	–	–	54.7	58.1		
μ (D)	0.112	2.986	1.855	2.330		
α_{xx} (Å ³)	1.63	2.05	1.53	2.51	α_{\perp}^c (Å ³)	1.44
α_{yy} (Å ³)	1.63	2.05	1.42	1.94	α_{\parallel}^c (Å ³)	0.41
α_{zz} (Å ³)	2.60	3.66	1.47	2.90		
Θ_{xx} (DÅ)	1.02	-2.20	2.63	1.91	Θ^c (DÅ)	1.0
Θ_{yy} (DÅ)	1.02	-2.20	-2.50	-5.01		
Θ_{zz} (DÅ)	-2.05	4.40	-0.13	3.09		
A (cm ⁻¹)	1.93	1.48	27.33	1.22		
B (cm ⁻¹)	1.93	1.48	14.57	1.13		
C (cm ⁻¹)	–	–	9.49	9.40		

^a From Refs. [41–45].

The vectors η_i characterize the positions of the atoms in the molecule. They, as well as the molecular electrical parameters μ , Θ , α , depend on the molecular internal vibrational motions. They could be written, with respect to the (G, \mathbf{x} , \mathbf{y} , \mathbf{z}) frame, as

$$\begin{aligned}\eta_i &= \eta_i^e + \sum_v \mathbf{a}_i^v Q_v + \dots, \\ \mu &= \mu^e + \sum_v \mathbf{b}^v Q_v + \dots, \\ \Theta &= \Theta^e + \sum_v \mathbf{c}^v Q_v + \dots, \\ \alpha &= \alpha^e + \sum_v \mathbf{d}^v Q_v + \dots.\end{aligned}\quad (10)$$

In these expressions the superscript e refers to the equilibrium internal configuration of the molecule (rigid molecule) and \mathbf{a}_i^v , \mathbf{b}^v , \mathbf{c}^v , and \mathbf{d}^v are the first derivatives of η_i , μ , Θ , and α with respect to the normal coordinate Q_v , associated with the v th molecular vibrational mode with frequency ω_v .

However, the present work is devoted to finding the adsorption energies and diffusion constants of single molecules adsorbed on the graphite substrate. Therefore, we can assume: (i) the substrate to be rigid ($\{\mathbf{r}_j\} = \{\mathbf{r}_j^e\}$), (ii) the adiabatic approximation to be valid, permitting us to separate the high frequency vibrational modes of the molecule from its low frequency external translational and orientational modes, and (iii) the dynamical coupling between all of the molecular and the graphite degrees of freedom to be negligible.

The interaction potential energy V_{MG} can then be written as

$$V_{MG} = V_{MG}(\mathbf{r}, \Omega, \{Q_v^e\}) + V_{MG}(\{Q_v\}, \mathbf{r}^e, \Omega^e), \quad (11)$$

where $V_{MG}(\mathbf{r}, \Omega, \{Q_v^e\})$ represents the external motion-dependent part of the potential energy experienced by the non-vibrating molecule. $V_{MG}(\{Q_v\}, \mathbf{r}^e, \Omega^e)$ characterizes the vibrational dependent part, for the molecule at its equilibrium position and orientation; in a perturbative approach it contributes to the molecular gas phase vibrational Hamiltonian and leads to small vibrational frequency shifts.

3. Adsorption observables

At sufficiently low temperatures and within the rigid molecule and substrate approximation, the potential energy surface $V_{MG}(X, Y)$, which is experienced by the adsorbed molecule as it moves laterally above the surface can be calculated by minimizing V_{MG} with respect to both the perpendicular distance Z between the molecular centre of mass and the surface and the molecular angular coordinates (φ , θ , χ).

The resulting energy map gives information about the equilibrium site (\mathbf{r}^e , Ω^e), and the lateral diffusion valley leading from one equilibrium site to an adjacent one. This makes it possible to determine the isosteric heat of adsorption or adsorption energy and also the surface diffusion constant.

3.1. Adsorption energy

The isosteric heat of adsorption E_a of a single adsorbed molecule on the graphite substrate can be defined as the energy required to keep the molecule with thermal energy $(\frac{n}{2} + 1)kT$ at its equilibrium configuration on the surface of the substrate. It is approximately expressed as

$$E_a \simeq \left(\frac{n}{2} + 1\right)kT - V_{MG}^m(\mathbf{r}^e, \Omega^e) - \sum_{s=1}^n \frac{\hbar\omega_s}{2} \coth\left(\frac{\hbar\omega_s}{2kT}\right), \quad (12)$$

where n is the number of external degrees of freedom for the molecule (5 for linear molecules and 6 for non-linear molecules) and k is the Boltzmann constant. The ω_s ($s = 1$ to n) are the frequencies

associated with the translational and orientational motions of the molecule around their equilibrium positions.

3.2. Surface diffusion constant

Let $V_{MG}(\tau, \xi_\gamma(\tau))$ be the instantaneous potential energy surface experienced by the adsorbed molecule with mass m as it moves along the diffusion valley described by the coordinate path τ . $\xi_\gamma(\tau)$ describe the instantaneous distance from the surface ($\gamma = Z$) and the instantaneous orientation ($\gamma = \varphi, \theta, \chi$) of the molecule for the given τ value.

If we disregard the dynamics of the ξ degrees of freedom around their τ -dependent equilibrium values ξ along the diffusion motion of the molecule and use the classical transition state theory [47], then the jumping rate for the diffusion from one equilibrium site S_1 to an equivalent adjacent one S_2 can be written at a T temperature as [36]

$$K(T) \simeq \left(\frac{kT}{2\pi m^*}\right)^{\frac{1}{2}} \frac{\exp[-\Delta V_{MG}(\tau_0)/kT]}{\int_{\tau_1}^{\tau_2} d\tau \exp[-\Delta V_{MG}(\tau)/kT]}, \quad (13)$$

where $\Delta V_{MG}(\tau) = V_{MG}(\tau) - V_{MG}(\tau_1)$ is the instantaneous potential energy function associated with the coordinate path value τ along the diffusion valley, and $\Delta V_{MG}(\tau_0)$ is the energy barrier height associated with the saddle point (maximum) position τ_0 . The diffusion constant is then

$$D(T) = \lambda^2 K(T), \quad (14)$$

where $\lambda = \tau_2 - \tau_1$ is the jump length, i.e., the distance (in the diffusion direction) between the two adjacent equilibrium sites S_1 and S_2 .

In Eq. (13) m^* is an effective molecular mass which is due to an inertial effect resulting from the changes in the distance of the molecule from the surface and in the molecular orientation as the diffusion process proceeds. It is expressed as

$$m^* = m \left(1 + \sum_\gamma \frac{A_\gamma}{m} \hat{\alpha}_\gamma^2\right), \quad (15)$$

where A_γ represents the molecular mass m for $\gamma = Z$ and the molecular moments of inertia I_a , I_b , and I_c for $\gamma = \varphi$, θ , and χ , respectively. The $\hat{\alpha}_\gamma = \frac{\partial \xi_\gamma}{\partial \tau}$ represent deformation parameters as the molecule migrates from an equilibrium site to the saddle point position along the diffusion valley.

4. Numerical results

4.1. Potential energy surfaces and equilibrium configurations

The potential energy surfaces $V_{MG}(X, Y)$ for the H_2O , CO , HCN , H_2CO single molecules adsorbed on the graphite substrate are presented in Figs. 2–5 using a square surface area of $(a \times \frac{2a}{\sqrt{3}})$, where the lattice parameter a is shown in Fig. 1.

In Table 4 we give, for each adsorbed species, some characteristics of the adsorption, such as the most favourable positions and orientations and their associated energy minima V_{MG}^m , as well as the energy maxima V_{MG}^M .

4.1.1. H_2O admolecule

Before presenting the potential energy surface $V_{MG}(X, Y)$ of the non-linear H_2O molecule adsorbed on the graphite substrate, we give in Table 3 the calculated local potential energy minimum values (binding energies) for some selected configurations of the molecule above the surface sites A, B, and C defined in Fig. 1. The configurations are described as: (a) and (b), the C_2 (twofold) molecular symmetry axis (z -axis) is perpendicular to the surface with the

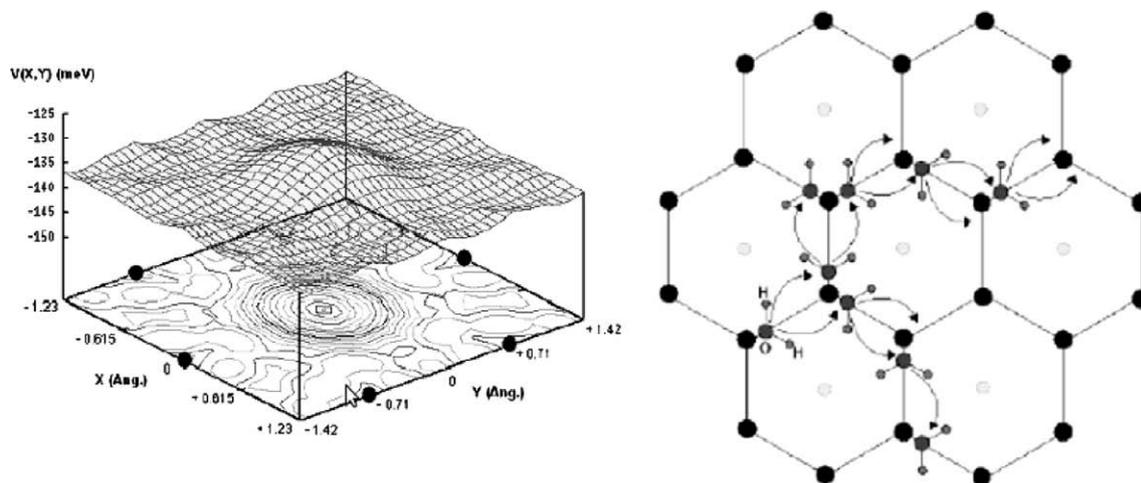


Fig. 2. (Left) The calculated potential energy surface for the H_2O molecule as it moves on the surface of the graphite substrate. Solid circles represent the carbon atoms of the substrate. (Right) The energetically favoured paths for diffusion between the equilibrium positions.

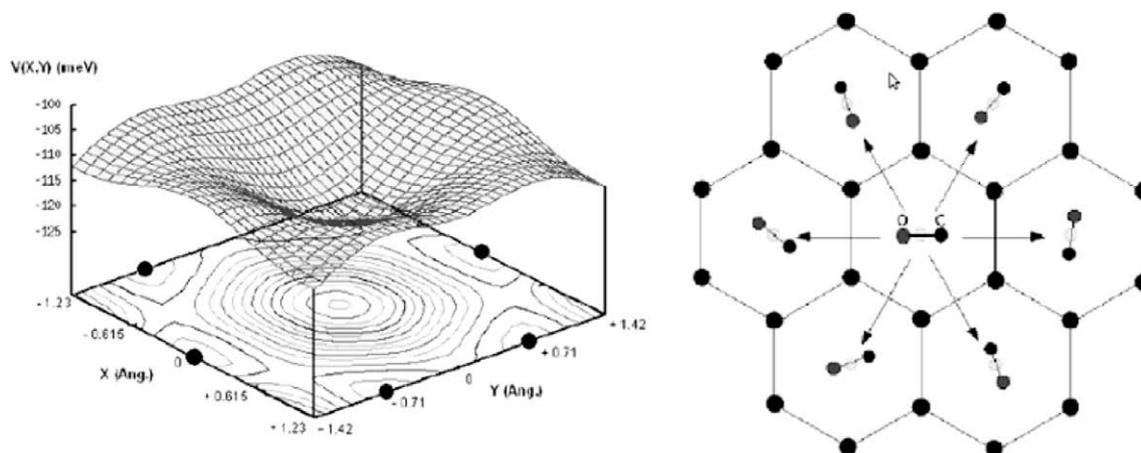


Fig. 3. (Left) The calculated potential energy surface for the CO molecule as it moves on the surface of the graphite substrate. Solid circles represent the carbon atoms of the substrate. (Right) The energetically favoured paths for diffusion between the equilibrium positions.

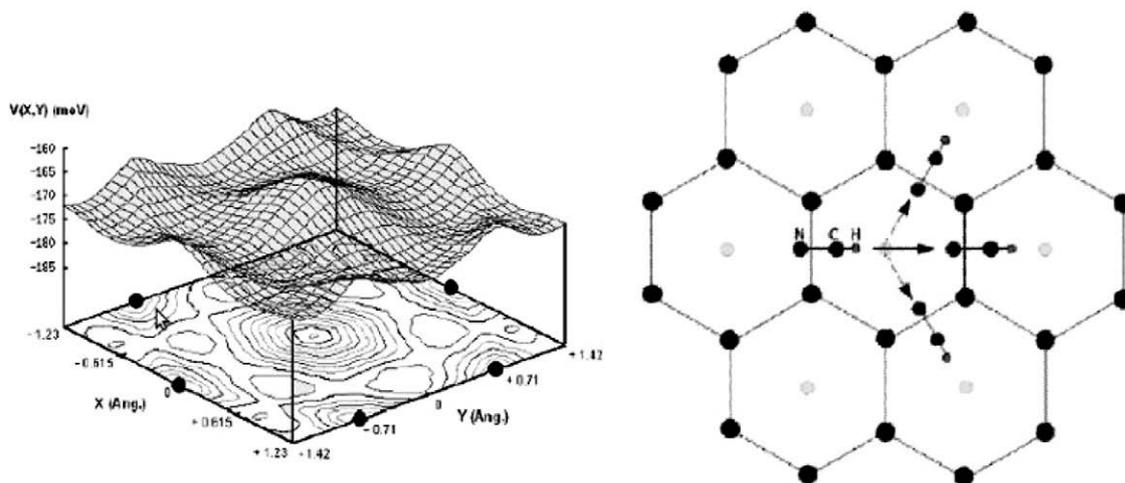


Fig. 4. (Left) The calculated potential energy surface for the HCN molecule as it moves on the surface of the graphite substrate. Solid circles represent the carbon atoms of the substrate. (Right) The energetically favoured paths for diffusion between the equilibrium positions.

H atoms pointing away from and toward the surface, respectively; (c) and (c'), the water plane is parallel to the surface with the C_2

axis perpendicular and parallel to the carbon–carbon bonds, respectively; and (d), the O–H bond pointing toward the surface.

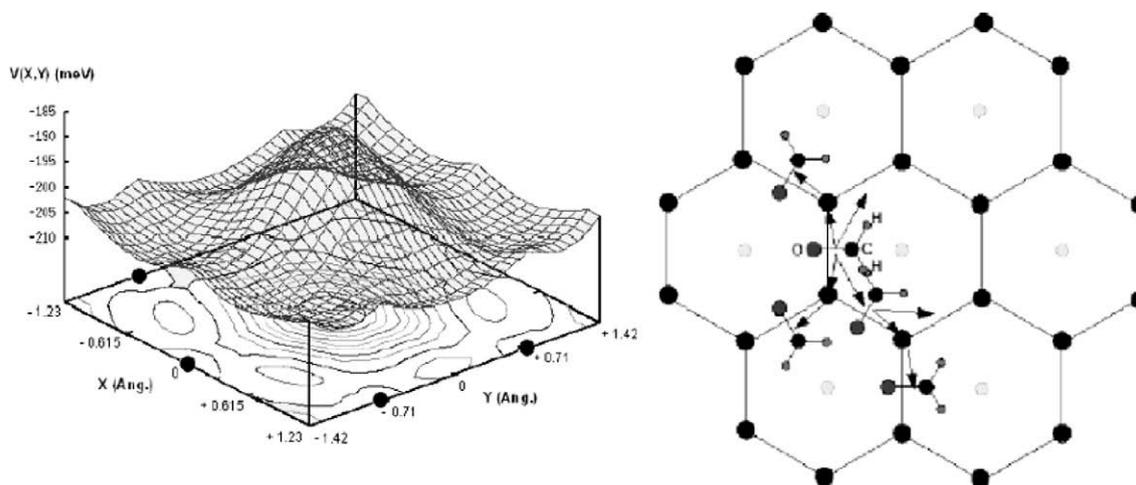


Fig. 5. (Left) The calculated potential energy surface for the H₂O molecule as it moves on the surface of the graphite substrate. Solid circles represent the carbon atoms of the substrate. (Right) The energetically favoured paths for diffusion between the equilibrium positions.

Their corresponding angular coordinates (φ , θ , χ) and the distances Z from the surface are also presented.

For comparison, the available binding energy values which have been obtained elsewhere using *ab-initio* calculation methods [24,26,30] are given in the right column. It is obvious that the configuration (d) of the water molecule with the O–H bond pointing toward the surface clearly appears to be an unstable position due to the repulsive force on the hydrogen atom near the graphite surface. The calculated binding energies do not agree with the values reported by Ruběš *et al.* [26]. Moreover, we note that the binding energies reported by González *et al.* [24] were calculated without taking in account for the hydrogen quantum and electrostatic contribution parts.

Furthermore, it can be seen from Table 3 that the molecule can exhibit a nearly free rotation motion about its x -axis above the hexagon site centre (site A); and that the more stable positions

Table 3

Calculated potential energy minimum values for a water molecule when adsorbed above the A, B, and C sites (see Fig. 1) of the graphite surface in some particular configurations (see the text) at distance Z . Right column displays the literature available values obtained from previous *ab-initio* calculations.

Site	Configuration	φ (°)	θ (°)	χ (°)	Z (Å)	V_{MG} (meV)	V_{MG} literature (meV)
A	(a)	0	0	0	2.92	-129	-91 [26] -174 [30]
	(b)	0	180	0	3.30	-128	-90 [24] -143 [30] -155 [26]
	(c)	0	90	90	3.00	-128	-112 [26]
	(c')	90	90	90	3.00	-128	
	(d)	0	125	0	3.50	-103	-91 [24] -127 [30] -131 [26]
B	(a)	0	0	0	3.00	-125	
	(b)	0	180	0	3.24	-131	-142 [26]
	(c)	0	90	90	3.02	-130	
	(c')	90	90	90	3.00	-136	
	(d)	0	125	0	3.70	-88	-137 [26]
C	(a)	0	0	0	3.04	-119	
	(b)	0	180	0	3.34	-122	-146 [26]
	(c)	0	90	90	3.00	-134	
	(c')	90	90	90	3.00	-136	
	(d)	0	125	0	3.72	-85	-139 [26]

are obtained for the flat configurations (c') above the middle of the carbon–carbon bond (site B), and (c) and (c') above the carbon atom (site C).

We have also performed calculations for the same configurations as in Table 3 disregarding the hydrogen quantum contributions, that is, by taking $\epsilon(\text{Gr-H}) = 0$ and $\sigma(\text{Gr-H}) = 0$. The results show that all the binding energies decrease by 25–50% of the values in Table 3 except that for the A(d) configuration (O–H bond pointing toward the surface) which increases by 3% and becomes the more stable configuration.

The potential energy surface experienced by the water molecule as it moves above the graphite surface is presented in Fig. 2. The most favourable sites are obtained for the molecular centre of mass at $Z = 3.00$ Å above the C–C bonds, with a displacement of 0.36 Å from the graphite carbon atom, the oxygen atom of the molecule being always close to this graphite carbon atom (Fig. 2).

The energy minimum $V_{MG}^m = -138$ meV is obtained with the molecule in a nearly flat configuration ($\theta^e \simeq 100^\circ$ and $\chi = \frac{\pi}{2}$) and sitting astride the carbon–carbon bonds (Table 4), and is in agreement with the available experimental value -156 meV obtained by Avgul and Kiselev [31] as well as with the calculated values -149 meV reported by Marković *et al.* [14], and -126 meV reported by Lin *et al.* [22] for H₂O–graphene complex.

It should be noted that in the equilibrium sites the angular motions of the C₂ molecular symmetry axis parallel (φ motion) and perpendicular (θ motion) to the surface around their equilibrium values are moderately hindered motions with energy barrier heights of about 8 and 15 meV, respectively. The angular (spinning) motion about this axis (χ motion) is a completely hindered motion, the energy barrier height being about 400 meV.

The energy maximum $V_{MG}^M = -129$ meV is reached for $Z = 2.92$ Å above the hexagon site centre (site A) with the C₂ molecular symmetry axis perpendicular to the surface of the graphite with the H atoms pointing away from the surface (configuration (a) in Table 3). Note, however, that the H atoms pointing toward the surface (b) and the flat (c) configurations of the molecule are almost energetically equal to that of the (a) configuration. The surface corrugation energy is then 8.5 meV which agrees with the value of about 10 meV reported in Ref. [26].

In Fig. 2 we sketch also the valley of diffusion of the water molecule on the surface. The barrier height at the saddle point is $\Delta V_{MG}(\tau_0) = 1$ meV (Table 7). Note however, that to obtain such a motion it is necessary to combine the translational motion and a reorientational motion parallel to the surface ($\varphi = \pm \frac{\pi}{3}$).

Table 4
Adsorption characteristics for CO, HCN, H₂O and H₂CO molecules. The superscript e refers to the equilibrium position and orientation associated with the energy minimum V_{MG}^m .

Molecule	X^e (Å)	Y^e (Å)	Z^e (Å)	φ^e (°)	θ^e (°)	χ^e (°)	V_{MG}^m (meV)	V_{MG}^M (meV)
CO	0.	0.	3.08	free	95	–	–120	–107
HCN	–0.95	0.	3.20	0	103	–	–175	–162
H ₂ O	–1.23	–0.36	3.00	90	100	90	–138	–129
H ₂ CO	–1.11	0.	3.04	0	90	90	–208	–186

4.1.2. CO admolecule

The potential energy surface experienced by the CO adsorbed molecule is presented in Fig. 3. The molecule exhibits an equilibrium configuration with an associated energy minimum $V_{MG}^m = -120$ meV located above the hexagon site centre at a distance $Z = 3.08$ Å from the surface and for a nearly flat orientation ($\theta^e \simeq 95^\circ$) position (Table 4).

The perpendicular orientational motion around this equilibrium configuration is a librational motion with an energy barrier height of about 40 meV, while that in the plane parallel to the surface (φ) is a free rotational motion.

The energy maximum $V_{MG}^M = -107$ meV is obtained with the molecule in a nearly flat configuration at a distance $Z = 3.24$ Å above the graphite carbon sites. There is a surface corrugation energy $V_{MG}^M - V_{MG}^m = 13$ meV.

The saddle point of the diffusion path is reached when the molecular centre of mass is above the middle of the carbon–carbon bonds at $Z = 3.20$ Å from the surface, with the molecule perpendicular to the carbon–carbon bonds and being always in the nearly flat configuration (Fig. 3). The associated energy barrier height is $\Delta V_{MG}(\tau_0) = 12$ meV (Table 7).

4.1.3. HCN admolecule

The linear HCN adsorbed molecule presents a potential energy surface with six most favourable sites per graphite hexagon (Fig. 4). The energy minimum $V_{MG}^m = -175$ meV is reached with the molecule in a nearly flat configuration ($\theta^e \simeq 100^\circ$) with its centre of mass at $Z = 3.20$ Å on the half of the carbon–carbon bonds, with a displacement of 0.28 Å inside the hexagon surface and with the hydrogen atom of the molecule pointing in the hexagon site centre direction (Table 4).

In these equilibrium sites there is a strongly hindered orientational motion perpendicular to the surface (θ motion) with an energy barrier height of about 75 meV and a moderately hindered parallel one (φ motion) with an energy barrier height of about 16 meV.

However, it is interesting to note that this latter orientational motion, combined with the translation motion of the molecule between the six equilibrium sites along a quasi-circular trajectory of radius $\simeq 0.95$ Å around the hexagon site centre, could be regarded as a quasi-free motion (Fig. 3) with an energy barrier height ≤ 1.5 meV. Thus, an associated effective moment of inertia must be defined with respect to a new HCN y -axis lying at 0.95 Å from its centre of mass (between the C and H atoms).

The energy maximum of $V_{MG}^M = -162$ meV is obtained with the molecular centre of mass at $Z = 3.24$ Å, nearly above the hexagon site centre and also with the nearly flat configuration. This induces a surface corrugation energy of 13 meV.

Moreover, this position also corresponds to the saddle point of the diffusion motion from one equilibrium site of a hexagon to one equivalent equilibrium site of an adjacent hexagon (Fig. 4).

4.1.4. H₂CO admolecule

Like the HCN molecule, the H₂CO molecule adsorbed on the graphite substrate exhibits six equilibrium sites per hexagon (Fig. 5). The energy minimum $V_{MG}^m = -208$ meV is obtained for

the molecule in a flat configuration ($\theta^e = 90^\circ$ and $\chi^e = 90^\circ$) with its centre of mass at $Z = 3.04$ Å on half of the carbon–carbon bonds, with a displacement of 0.12 Å inside of the hexagon surface and with its C₂ (twofold) molecular symmetry axis (z -axis) pointing towards the hexagon site centre (Table 4).

It should be noted that in its equilibrium sites H₂CO behaves nearly like HCN with regard to the perpendicular θ and parallel φ angular motions of its z -axis, in one hand, but like H₂O with regard to its spinning motion about this axis.

The energy maximum is $V_{MG}^M = -186$ meV, with the molecule in the flat configuration at $Z = 3.12$ Å above the hexagon site centre. The surface corrugation energy is then 22 meV.

The saddle point of the diffusion path is obtained for the molecule in the flat configuration at $Z = 3.04$ Å above the C carbon site with a corresponding energy barrier height $\Delta V_{MG}(\tau_0) = 5$ meV (Table 7). Moreover, the rotation of the molecule parallel to the surface plane is a free motion on this site.

4.2. Conclusion and discussion

From the above potential energy calculations we can conclude that:

- (i) the fact that the equilibrium configuration is nearly above the carbon–carbon bonds for HCN, H₂O, and H₂CO molecules results from their strong multipole moments, particularly the dipole moments. Their quantum V_{LJ} , induction V_I and electrostatic V_E contribution parts represent $\sim 80\%$, $\sim 15\%$ and $\sim 5\%$, respectively, of the total potential energy for these molecules;
- (ii) the weakly polar CO molecule behaves as a quadrupolar molecule and adopts an equilibrium configuration above the hexagon site centre. Its quantum contribution part V_{LJ} represents more than $\sim 95\%$ of the total potential energy;
- (iii) the induction contribution part (second term of Eq. (6)) due to the quadrupole moment tensors Θ^c of the graphite atoms on each of the molecules is negligible (≤ 0.5 meV);
- (iv) the contribution due to the internal planes of the graphite substrate represents $\sim 9\text{--}13\%$ of the total potential energy for each of the studied molecules; $\sim 90\%$ of this contribution is due to the quantum part V_{LJ} . This result is in agreement with those obtained from *ab-initio* calculation methods [24,26,30] for the water–graphene complex with respect to the water–graphite complex;
- (v) one cannot neglect the hydrogen quantum contribution to the interaction potential energy as we have mentioned above for a water molecule adsorbed on graphite substrate.

4.3. Adsorption energy calculations

The calculation, using Eq. (12), of the adsorption energy values for single molecules adsorbed on the graphite substrate requires a knowledge of the frequencies ω_s associated with the linear and angular oscillations associated with the translational and orientational motions of the molecules around their equilibrium configurations on the most favourable sites.

A discrete variable representation method [48] was used to solve the Schrödinger equation giving the energy levels of a molecule undergoing linear and angular oscillations at its equilibrium site, with the other degrees of freedom being assumed to remain at their equilibrium values. The various frequencies calculated for the molecules treated in this work are reported in Table 5.

As can be expected from the potential energy surfaces, the frequencies associated with the orientational motions perpendicular to the surface (θ and χ motions) (except the θ motion for H₂O molecule) are large compared to those associated with the orientational motion parallel to the surface (φ motion).

Finally, the calculated frequencies were introduced into Eq. (12) and the adsorption energies were determined for three typical temperatures. The resulting values are reported in Table 6. It must be noticed that for the CO adsorbed molecule, our calculated value $E_a = 115$ meV at temperature $T = 100$ K is in good agreement with the experimental value ~ 113 meV reported by Piper et al. [34] in the 79–119 K temperature range, and also with their calculated one 113 meV at 79 K.

4.4. Diffusion constant calculations

The study of the potential energy surface for each adsorbed species allows us to determine the diffusion path, its length λ and potential energy function $\Delta V_{MC}(\tau)$ as well as the energy barrier height $\Delta V_{MC}(\tau_0)$, and the deformation parameters \hat{a}_γ as the molecular diffusion proceeds on the surface.

It must be mentioned that large values for \hat{a}_γ correspond to important equilibrium changes when the molecular centre of mass migrates from the minimum to the saddle point position along the diffusion valley. For instance, the angular deformation parameter values \hat{a}_φ are 1.03 and 0.74 rad/Å for H₂O and H₂CO admolecules, respectively.

In contrast, the angular deformation parameters \hat{a}_θ and \hat{a}_χ are negligibly small for all the admolecules because of the very weak

changes of their perpendicular orientation with respect to the surface during the diffusion motion.

The linear deformation parameter values \hat{a}_z are 0.10, 0.05, 0.04 and 0.00 for CO, HCN, H₂O and H₂CO admolecules, respectively.

Introducing the calculated deformation parameters in Eq. (15) the mass ratios $\frac{m^*}{m}$ are obtained and presented in Table 7. Note that for the CO and HCN admolecules the mass changes are negligibly small, while for H₂O and H₂CO they are of about 11% and 27%, respectively. The effective masses of the latter molecules are ~ 20 and 38 g mol⁻¹ instead of 18 and 30 g mol⁻¹, respectively.

Finally, the possible diffusion paths are indicated in Figs. 2–5 and the corresponding lengths λ and energy barrier heights $\Delta V_{MC}(\tau_0)$ are given in Table 7.

It is obvious from Table 7 that the diffusion constant is strongly and simultaneously dependent on the energy barrier height and on the temperature. This is due to the $\exp[-\Delta V_{MC}(\tau_0)/kT]$ term as it can be seen in Eq. (13). Thus, at low temperature $T = 10$ K the diffusion constant increases by about five orders of magnitude when the energy barrier height decreases from 13 (for HCN admolecule) to 1 meV (for H₂O admolecule). While, when the temperature increases ($T = 40$ K) the energy barrier height effect is compensated inducing diffusion constant values of almost the same order of magnitude.

5. Discussion

In the present work, we have studied the adsorption of several single molecules on a graphite substrate; the molecules were selected because of their biophysical interest, as explained in the introduction.

The major calculation was that of the potential energy surface for each molecule and the figures show the resulting surfaces. A minimization calculation then gave the possible equilibrium positions for each molecule, while the potential energy surface indicated the favourable pathways between these positions which would facilitate surface diffusion of the adsorbed molecule.

The calculated adsorption energies as shown in Table 6 show only a relatively weak variation with temperature, although the particular values of the molecule–surface interaction parameters for the HCN molecule lead to a temperature dependence which is in the opposite direction to that for the other three molecules studied.

The calculated diffusion constants for the molecules are shown in Table 7 and it is clear that the different saddle point barrier heights lead to a variation of several orders of magnitude between the low temperature diffusion constants of the various molecules. In effect, one can remark that at $T = 10$ K the H₂O molecule could diffuse ~ 1.8 , 4.7, and 5.2 orders of magnitude more easily than H₂CO, CO, and HCN molecules, respectively.

However, as the temperature increases the thermal energy kT becomes sufficiently large to overcome the barriers for all the molecules, with the consequence that the diffusion constants vary much less from molecule to molecule as the temperature rises.

The present calculations have treated the adsorption and diffusion of single molecules on a graphite surface and thus refer to the

Table 5

Calculated frequencies (cm⁻¹) associated with the translational and orientational oscillations of CO, HCN, H₂O and H₂CO molecules.

Molecule	ω_x	ω_y	ω_z	ω_φ	ω_θ	ω_χ
CO	26.6	26.6	62.1	~ 0	76.6	–
HCN	21.0	23.4	79.0	32.3	109.7	–
H ₂ O	~ 0	~ 0	90.3	22.6	35.5	233.9
H ₂ CO	25.0	~ 0	155.7	21.0	91.1	203.3

Table 6

Calculated adsorption energy E_a (meV) of CO, HCN, H₂O and H₂CO molecules for three typical temperatures.

Molecule	$T = 10$ K	$T = 40$ K	$T = 100$ K
CO	111	115	115
HCN	169	164	160
H ₂ O	118	124	130
H ₂ CO	181	187	190

Table 7

Calculated surface diffusion constant $D(T)$ (cm²/s) of CO, HCN, H₂O and H₂CO molecules for three typical temperatures.

Molecule	$\frac{m^*}{m}$	λ (Å)	$\Delta V_{MC}(\tau_0)$ (meV)	$D(10$ K)	$D(40$ K)	$D(100$ K)
HCN	1.002	2.46	13	1.1×10^{-10}	1.2×10^{-5}	7.2×10^{-5}
CO	1.01	2.46	12	3.3×10^{-10}	1.0×10^{-5}	7.3×10^{-5}
H ₂ CO	1.27	1.42	5	2.2×10^{-7}	1.8×10^{-5}	5.1×10^{-5}
H ₂ O	1.11	1.02	1	1.5×10^{-5}	4.3×10^{-5}	7.2×10^{-5}

case of low surface density of adsorbed molecules. The obtained results will permit us in a future work to explore the interactions between the HCN, H₂O, H₂CO and NH₃ molecules participating in the glycine production when they are simultaneously adsorbed on the graphite surface which could play a roll in bringing nearer these molecules.

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References

- [1] B.T. Draine, *Astrophys. J.* 333 (1988) 848.
- [2] J.S. Mathis, G. Whiffen, *Astrophys. J.* 341 (1989) 808.
- [3] N. Watanabe, A. Kouchi, *Astrophys. J. Lett.* 571 (2002) 173.
- [4] A.G.G.M. Tielens, D.C.B. Whittet, in: E.F. van Dishoeck (Ed.), *Molecules in Astrophysics*, Kluwer, Dordrecht, 1997, p. 45.
- [5] M.P. Bernstein, J.P. Dworkin, S.A. Sandford, G.W. Cooper, L.J. Allamandola, *Nature* 416 (2002) 401.
- [6] G.M. Muñoz Caro, U.J. Meierhenrich, W.A. Schutte, B. Barbier, A. Arcones Segovia, H. Rosenbauer, W.H.P. Thiemann, A. Brack, J.M. Greenberg, *Nature* 416 (2002) 403.
- [7] S.L. Miller, *Science* 117 (1953) 528.
- [8] D.E. Woon, *Astrophys. J. Lett.* 571 (2002) 177.
- [9] C. Mendoza, F. Ruetter, G. Martorell, L.S. Rodríguez, *Astrophys. J. Lett.* 601 (2004) 59.
- [10] R.L. Gale, R.A.J. Beebe, *Phys. Chem.* 68 (1964) 555.
- [11] G. Vidali, G. Ihm, H.Y. Kim, M.E. Cole, *Surf. Sci. Rep.* 12 (1991) 135.
- [12] A. Vernov, W.A. Steele, *Langmuir* 8 (1992) 155.
- [13] D.J. Feller, *Phys. Chem. A* 103 (1999) 7558.
- [14] N. Marković, P.U. Andersson, M.B. Nagard, J.B.C. Pettersson, *Chem. Phys.* 247 (1999) 413.
- [15] M.C. Gordillo, J. Martí, *Chem. Phys. Lett.* 329 (2000) 341.
- [16] D. Feller, K.D.J. Jordan, *Phys. Chem. A* 104 (2000) 9971.
- [17] S. Tsuzuki, K. Honda, T. Uchimaru, M. Mikami, K.J. Tanabe, *Am. Chem. Soc.* 122 (2000) 11450.
- [18] T. Werder, J.H. Walther, R.L. Jaffe, T. Halicioglu, P.J. Koumoutsakos, *Phys. Chem. B* 107 (2003) 1345. and references therein.
- [19] W.H. Noon, K.D. Ausman, R.E. Smalley, J. Ma, *Chem. Phys. Lett.* 355 (2002) 445.
- [20] S. Picaud, P.N.M. Hoang, S. Hamad, J.A. Mejias, S.J. Lago, *Phys. Chem. B* 108 (2004) 5410.
- [21] U. Zimmerli, M. Parrinello, P.J. Koumoutsakos, *Chem. Phys.* 120 (2004) 2693.
- [22] C.S. Lin, R.Q. Zhang, S.T. Lee, M. Elstner, Th. Frauenheim, L.J.J. Wan, *Phys. Chem. B* 109 (2005) 14183.
- [23] I.W. Sudiarta, D.J.W.J. Geldart, *Phys. Chem. A* 110 (2006) 10501.
- [24] B.S. González, J. Hernández-Rojas, J. Bretón, J.M.J. Gomez-Llorente, *Phys. Chem. C* 111 (2007) 14862.
- [25] S. Li, V.R. Cooper, T. Thonhauser, A. Puzder, D.C.J. Langreth, *Phys. Chem. A* 112 (2008) 9031.
- [26] M. Rubeš, P. Nachtigall, J. Vondrášek, O.J. Bludský, *Phys. Chem. C* 113 (2009) 8412.
- [27] B.-M. Cheng, J.R. Grover, E.A. Walters, *Chem. Phys. Lett.* 232 (1995) 364.
- [28] A. Courty, M. Mons, I. Dimicoli, F. Piuze, M.-P. Gaigeot, V. Brenner, P.D. Pujó, P.J. Millié, *Phys. Chem. A* 102 (1998) 6590.
- [29] K. Karapetian, K.D. Jordan, in: J.P. Devlin, V. Buch (Eds.), *Water in Confined Environments*, Springer, New York, 2003, p. 139.
- [30] D.J.W. Geldart, I.W. Sudiarta, G. Lesins, P. Chylek, 2008. arXiv:0801.2807.
- [31] N.N. Avgul, A.V. Kieslev, in: P.L. Walker (Ed.), *Chem. Phys. Carbon* 6 (1970) 1 (Dekker, New York).
- [32] R.A. Beebe, R.L. Gale, T.C.W.J. Kleinsteuber, *Phys. Chem.* 70 (1966) 4010.
- [33] A.V. Kieslev, V.L. Khudyakov, Y.I. Yashin, *Russ. J. Phys. Chem.* 47 (1973) 1200.
- [34] J. Piper, J.A. Morrison, C. Peters, *Mol. Phys.* 53 (1984) 1463.
- [35] A. Lakhlifi, C. Girardet, *Surf. Sci.* 241 (1991) 400.
- [36] A. Lakhlifi, C.J. Girardet, *Chem. Phys.* 94 (1991) 688.
- [37] A. Lakhlifi, S. Picaud, C. Girardet, A. Allouche, *Chem. Phys.* 201 (1995) 73.
- [38] A. Lakhlifi, *Eur. Phys. J. D* 8 (2000) 211.
- [39] A. Lakhlifi, J.P.J. Killingbeck, *Phys. Chem. B* 109 (2005) 11322.
- [40] M.E. Rose, *Elementary Theory of Angular Momentum*, Wiley, New York, 1967.
- [41] W.E. Carlos, M.W. Cole, *Surf. Sci.* 119 (1982) 21.
- [42] G. Vidali, M.W. Cole, *Phys. Rev. B* 29 (1984) 6736.
- [43] F.Y. Hansen, L.W. Bruch, S.E. Roosevelt, *Phys. Rev. B* 45 (1992) 11238.
- [44] F.Y. Hansen, L.W. Bruch, *Phys. Rev. B* 51 (1995) 2515.
- [45] S.I. Ionov, M.E.J. La Villa, *Chem. Phys.* 97 (1992) 9379.
- [46] J.C. Phillips, *Covalent Bonding in Crystals, Molecules, and Polymers*, University of Chicago Press, 1969.
- [47] A.F. Voter, J.D.J. Doll, *Chem. Phys.* 80 (1984) 5832.
- [48] J.C. Light, I.P. Hamilton, J.V.J. Lill, *Chem. Phys.* 82 (1985) 1400.