

# Nanometer site analysis of electron tracks and dose localization in bio-cells exposed to X-ray irradiation

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## ABSTRACT

This paper reports on a Monte Carlo simulation analysis of the ionization and excitation clusters in electron tracks, which may contribute to radiation damage of biological cells with high probabilities. The study is aimed at investigating the energy transfer to the cell nucleus exposed to X-rays from low doses in the environment to high doses in radiation therapy. As an example, we adopt a water phantom exposed to X-rays from a 6 MV linac to calculate the expected energy transfer to electrons in liquid water. A track simulation of the electrons produced by the photon interactions was performed. The behavior of low energy electrons below 1 keV is of particular importance in forming clusters of ionization and excitation events within a nanometer scale (<100 nm). We describe the clustering pattern in terms of aggregation index, the distribution of point-to-point distance below several nanometers between the events. By comparing the distribution with that of the Poisson configuration, the clustering effects of the events including successive radical processes are evaluated.

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## 1. Introduction

Ionization and excitation of atoms and molecules in bio-tissues take place abundantly following irradiation due to inelastic collisions of the electrons produced by primary incident particles. This is true if the primary particles are low LET (linear energy transfer) radiation such as X-rays,  $\gamma$ -rays and protons with energies above several tens of MeV. From the microscopic point of view, therefore, the electron track process is essential in low LET irradiations for transferring energy to the material rather than due to the primary radiation interaction itself. A review of recent progress in the investigation of the electron track structure has been provided by Nikjoo et al. [1] to show the importance of such processes. The ionization and excitation events are inclined to occur densely by low energy (<1 keV) electron collisions along various local traces of the electron forming spurs or blobs. These are called ionization and excitation “clusters” that may lead to damage of DNA and other elements of bio-materials with high probabilities [1–4].

In this study, we have performed Monte Carlo simulations for photons, electrons and radicals to investigate the spatial concentration of the energy transfer processes through electron collisions in liquid water on the assumption that an equivalent condition for electron track holds when inside bio-cells. In order to evaluate the concentration degree of events with clusters, we have introduced

an “aggregation index (AI)”, that is, the distribution of distances between two arbitrary event locations below several nm. AI enables us to evaluate the probability of causing damage due to adjacent plural reactions such as double strand breaks (DSBs). Diffusion processes of radicals starting at the ionization and excitation positions are also discussed along the lines of AI.

## 2. Simulation model and method

For the present simulation, we adopted a model condition with a water phantom for calibrating dosimeters, commonly used in radiation therapy. First, a Monte Carlo simulation of X-ray photons from a 6 MV linac incident on a water phantom (rectangular solid,  $30 \times 30 \times 30 \text{ cm}^3$ ) was performed to calculate energy transfer to electrons through photon interaction. The radiation intensity was set to yield the absorbed dose from 0.1 Gy to 6.0 Gy. The energy and ejection angle of electrons were sampled in a cube 1 cm on a side located at a depth of 10 cm from the surface center of the phantom, where the field size is  $10 \times 10 \text{ cm}$  for parallel X-ray irradiation. Second, we made a Monte Carlo track simulation of the electrons produced in the photon interactions. The electron track was followed with an event-by-event algorithm using a set of electron collision cross sections for liquid water [5,6] and the scattering angle distribution for elastic and ionization collisions [7–9]. To reduce the computation time for the vast amount of data of ionization and excitation positions, a cyclic boundary condition for a cube voxel  $100 \mu\text{m}$  on a side was applied. We then evaluated the concentration degree of

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the events (clustering) by counting the point-to-point distance distribution within a sphere 10  $\mu\text{m}$  in diameter imitating a cell-nucleus inside the voxel.

The simulation codes were developed by the authors. In the photon code, the cross sections for the photon interactions (i.e. coherent scattering, photoelectric effect, Compton scattering and pair production) are taken from Storm and Israel [10], and algorithms and related data by several papers [11–14] are used. Particular attention was paid to the electron track code because the behavior of electrons with low energies below several 100 eV has some uncertainty among the codes reported depending on the electron collision cross sections built in [1,4,15–18]. Comparisons of the CSDA range and stopping power deduced by our code with those in ICRU Report 37 [19] were made as benchmark tests, and we confirmed good agreements between those for the both quantities, respectively, in the electron energy range from 10 eV to 10 MeV. In the radical simulation, radical diffusion length in a random direction was estimated from the diffusion equation as [20]

$$\lambda = \sqrt{6Dt}, \quad (1)$$

where  $D$  is the diffusion coefficient and  $\lambda$  is the diffusion length at an elapsed time  $t$ . For a trial example to estimate the distance distribution between two radicals, the OH radical was adopted and its diffusion coefficient was assumed to be  $2.8 \times 10^{-5} \text{ cm}^2/\text{s}$  [21]. The time step for chasing the diffusion process  $\Delta t = 10^{-12} \text{ s}$  was set in the present study.

### 3. Results and discussion

The energy distribution of electrons generated by 6 MV X-ray interactions in the water phantom is shown in Fig. 1. A typical spectrum of 6 MV X-rays used here is plotted in Fig. 1, obtained from calculation by Schiff's formula [22] for photon production at a Tungsten target and a consideration of beam attenuation by a flattening filter (Tungsten, 12.5 mm thickness) [23]. In Fig. 1 the energy of electrons arising from the photon interactions is distributed abundantly below 1 MeV (average 0.568 MeV), and most of the electrons are from Compton scattering. This implies that the average number of photon interactions to yield 2 Gy (typical absorbed dose in radiation therapy per fraction) in the phantom is roughly  $2.2 \times 10^{10} \text{ cm}^{-3}$ , and the average number per cell nucleus is 11.5 for the nuclear diameter of 10  $\mu\text{m}$ . The number of electron tracks arising from the photon interactions per cell nucleus is well described by the Poisson distribution for this average value.

Fig. 2 shows the distribution of distances between inelastic collision processes (i.e. ionization and excitation). The distribution curve for a Poisson configuration is also plotted for comparison. Here, the Poisson configuration stands for the random point formation in a bounded area. When we assume a spherical volume of ra-

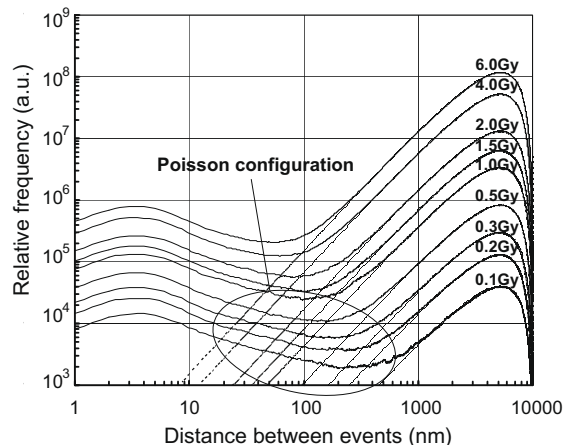


Fig. 2. Distribution of distances between ionization and excitation events in comparison with that of a Poisson configuration.

dius  $R$ , the probability distribution of distance  $x$ , between two arbitrary points in the sphere is described by

$$F(x) = \frac{3}{16R^6}x^5 - \frac{9}{4R^4}x^3 + \frac{3}{R^2}x^2, \quad (0 \leq x \leq 2R) \quad (2)$$

see [24,25]. In Fig. 2 the curve for the electron track has a local maximum at around 3–4 nm, while it coincides with that of the Poisson configuration greater than about 100 nm. We call this distribution within a short distance (below several tens of nm) the aggregation index of the inelastic collision events. The local maximum is largely attributable to the clustering of ionization and excitation events. Ionization and excitation occur significantly with low energy electrons slowed down from 1 keV to 10 eV forming the clusters, independent of the initial energy [4,5]. Two neighboring events (of ionization and/or excitation) and succeeding radical formations in a few nanometers must be fundamental for causing double strand breaks of DNA since this distance scale is equivalent to the double helix local site. The curve in the short distance region seems to be linearly shifted to upper values with dose. In Fig. 3(a), the integrated value over 0–10 nm is plotted as a function of dose for three cases, ionization and excitation events, ionization events only and excitation events only, respectively. Here, 10 nm was assumed in the integration as the upper limit for a possible length causing DSBs. This value may be rather large, but the subsequent discussion remains unchanged granting that the limit is set to 3.4 nm (equivalent to the length of 10 base pairs for DNA [26]). In our calculation range up to 6 Gy, the integrated value is simply proportional to dose. This suggests that the inter-track damage, associated with two adjacent tracks shown in Fig. 3(b), for directly inducing DSBs hardly occurs. In other words, it can be interpreted that the two arbitrary tracks are found in space independently. If the inter-track processes have occurred in a local site within 10 nm, the curve in Fig. 3(a) should have been not linear (e.g. exponential) with dose.

Apart from the possibility of molecules attacked directly by electrons, the indirect reactions by radicals were examined by the radical simulation. Radical species such as OH,  $e_{aq}^-$  (aqueous electron),  $\text{H}_3\text{O}^+$  and H were taken into account. The thermal diffusion coefficients for each radical have been given in pure water [20,21]. As a typical radical having a minimum value of diffusion coefficient among the above species, we adopted the OH radical to observe the diffusion behavior. Fig. 4 shows the AI for OH radical formation originating from the electron tracks for initial electron energies, 10 keV and 1 keV, as a function of time. The radical production rate was assumed to be one OH radical per event (ionization or excitation) at each event location. The results for both cases show that two arbitrary OH radicals produced along

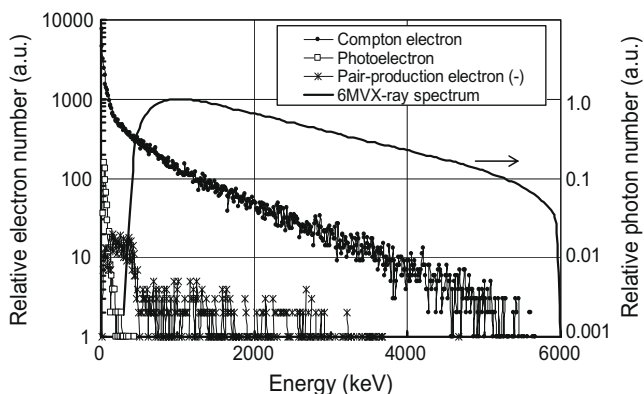
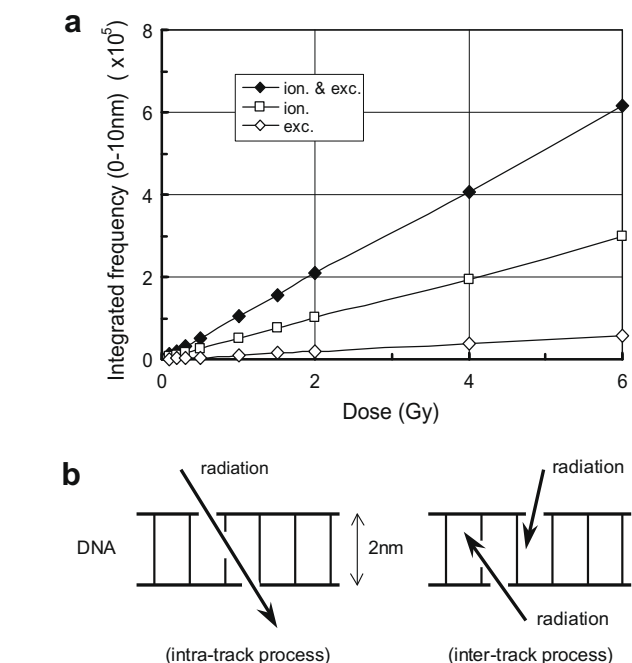
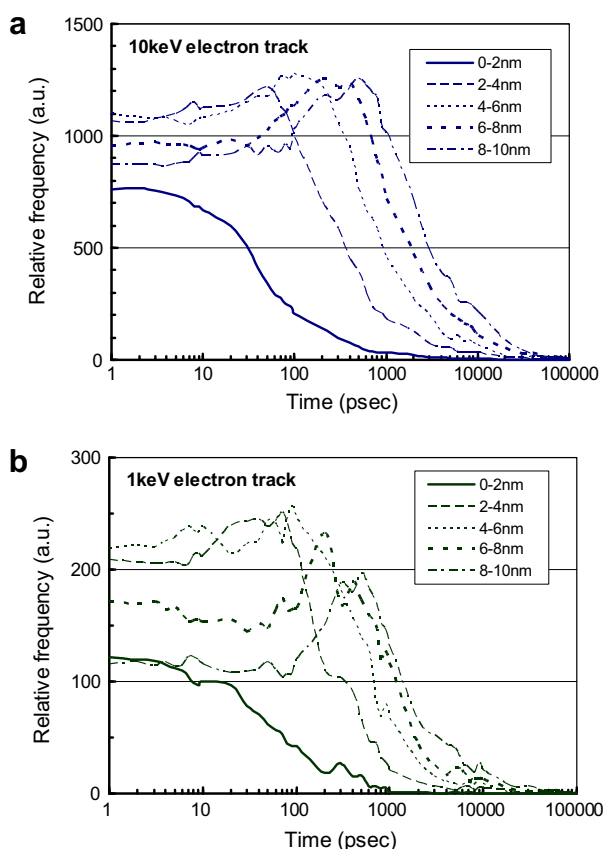


Fig. 1. Energy distribution of electrons produced by X-rays from a 6 MV linac.



**Fig. 3.** (a) Distance frequency integrated from 0 to 10 nm as a function of dose:  $\bullet$  both events for ionization and excitation,  $\square$  ionization events only,  $\diamond$  excitation events only. (b) Basic concept of intra-track and inter-track processes in the DNA scale.



**Fig. 4.** Aggregation index for OH radical diffusing as a function of time: (a) for 10 keV electron track and (b) for 1 keV electron track.

the electron track spread out from each other more than 10 nm by diffusion at least in 0.1  $\mu$ s, leading to the Poisson configuration in the lifetime of the radical ( $\sim 1 \mu$ s). The results in Fig. 4 have statis-

tical variations because these computations are subject to one track history. However, the trials for some histories showed the same tendency in regard to the time dependence. The result of this radical spatial formation may imply that the possibility of the inter-track damage of DNA is negligible even though the radical processes are taken into account. A problematic issue of this simulation is the validity of the diffusion coefficient because the value used here is for pure water while the real situation of radicals is in bound (by hydrogen bonding) water with a variety of proteins and other materials. It is well known that the mobility of radicals is much impaired in bound water by some orders of magnitude [27]. Therefore, further consideration is necessary for the radical diffusion in the real cell condition filled with bound water.

The present study is based upon the assumption of X-ray irradiation using a 6 MV linac with a rather high dose. However, it should be noted that the AI approach and the radical behavior from one electron track are applicable to a wide range of dose.

#### 4. Conclusion

We have carried out Monte Carlo simulations for photon, electron and radicals assuming a water phantom model exposed to 6 MV X-ray irradiation. The ionization and excitation clusters were evaluated by the distance distribution between the events, and the distribution was compared with that of a Poisson configuration. The difference is significant in a short distance below a few tens of nm, showing a major possibility of causing double strand breaks of DNA. The integrated value over 0–10 nm of this distribution is almost linear as a function of dose up to 6 Gy. This linearity suggests that the inter-track damage in DNA scale sites hardly occurs through the electron direct collisions even with the therapeutic dose. The radical simulation (typically with OH radical) was made starting at the ionization and excitation locations of the electron track. The distance distribution between two arbitrary OH radicals spreads out ( $>10$  nm) from each other in a short period of time (0.1  $\mu$ s) converging to the Poisson configuration.

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