



Contents lists available at ScienceDirect

Nuclear Instruments and Methods in Physics Research B

journal homepage: www.elsevier.com/locate/nimb

Rare earth substitutional impurities in germanium: A hybrid density functional theory study

E. Igumbor^{a,b,*}, E. Omotoso^a, S.M. Tunhuma^a, H.T. Danga^a, W.E. Meyer^{a,*}

^a Department of Physics, University of Pretoria, Pretoria 0002, South Africa

^b Department of Mathematics and Physical Sciences, Samuel Adegboye University, Km 1 Ogwa/Ehor Rd, Ogwa Edo State Nigeria

ARTICLE INFO

Article history:

Received 29 November 2016
Received in revised form 20 May 2017
Accepted 20 May 2017
Available online xxx

Keywords:

Defects
Formation energy
Charge state
Rare earth

ABSTRACT

The Heyd, Scuseria, and Ernzerhof (HSE06) hybrid functional by means of density functional theory has been used to model the electronic and structural properties of rare earth (RE) substitutional impurities in germanium (RE_{Ge}). The formation and charge state transition energies for the RE_{Ge} (RE = Ce, Pr, Er and Eu) were calculated. The energy of formation for the neutral charge state of the RE_{Ge} lies between -0.14 and 3.13 eV. The formation energy result shows that the Pr dopant in Ge (Pr_{Ge}) has the lowest formation energy of -0.14 eV, and is most energetically favourable under equilibrium conditions. The RE_{Ge} induced charge state transition levels within the band gap of Ge. Shallow acceptor levels were induced by both the Eu (Eu_{Ge}) and Pr (Pr_{Ge}) dopants in Ge. The Ce_{Ge} and Er_{Ge} exhibited properties of *negative-U* ordering with *effective-U* values of -0.85 and -1.07 eV, respectively.

© 2017 Elsevier B.V. All rights reserved.

1. Introduction

Germanium (Ge) is being considered as a material for new generation of microelectronic devices, as a result of its unique properties (carrier mobilities, low dopant activation temperatures and smaller band-gap of 0.78 eV at 0 Kelvin) [1–3]. Several studies of point defects in Ge using experimental [4–7] or theoretical [8–12] techniques have been reported. It has been reported that defect processes of dopants in Ge semiconductors can be influenced by doping and double-donor doping, which may be an effective way to engineer the active donor concentrations of Ge [9]. Rare earth (RE) impurities in semiconductor material have attracted interest due to their unique predictable optical properties [13]. Another interesting property of the RE is its ability to participate in photoluminescence process. For instance, the Er³⁺ ions have been discovered to participate in an energy transfer process during optical or electrical pumping of Er-doped SiO₂ [14]. In another development, according to report by Kanjilal et al. [15], the Er-doped amorphized Ge nanoclusters can recrystallized in absence of Ge out-diffusion during flash-lamp annealing. Channelling experiments by Jones *et al* [16] have given support for a Er tetrahedral interstitial location in Si. Visible emission as well

as an infrared 1.53 μm signal from the Er doped Ge nanowires at room temperature have been observed [17]. Recently, Tm [10] substitutional impurity in Ge was predicted to induce in the band gap of Ge an acceptor level ($-1/-2$) at $E_C - 0.05$ eV (E_C and E_V are the energies of the conduction band minimum and the valence band maximum respectively), and double donor levels at $E_V + 0.10$ and $E_V + 0.19$ for the $(+2/+1)$ and $(+1/0)$ charge state transitions, respectively. The interaction energy between two electrons in a two-level defect is referred to as Hubbard-*U* [18,19]. Hubbard-*U* is regarded as a *negative-U* when the neutral charge state is excited, and it becomes energetically less favourable. A good number of defects in Ge and Si have been observed to exhibit charge state *negative-U* ordering [2,10,20]. The Tm³⁺ and Ce³⁺ interstitials in Ge are found to exhibit charge state *negative-U* ordering [20,10].

It has been reported that materials in the future (due to miniaturization) will have shallow junctions with high conductivity [21,22]. For Ge based device processing damage occurs during ion implantation. As a result, the role of defects that enhance diffusion of the implanted dopant will have to be well understood. Bracht et al. [7] in a review reported the mechanism of self- and dopant diffusion in Ge under thermal equilibrium and non-equilibrium conditions. In this case, the non-equilibrium conditions can be realized by irradiation or implantation. While RE ion defects in Si and other materials have been studied either by theoretical modelling or by experimental techniques [23–25]. Except for the Tm [10], the structural and electronic properties of RE substitutional defects in Ge have not been theoretically studied. In

* Corresponding authors at: Department of Physics, University of Pretoria, Pretoria 0002, South Africa.

E-mail addresses: elgumuk@gmail.com (E. Igumbor), wmeyer@up.ac.za (W.E. Meyer).

order for us to provide a frontier insight for the experimental study of the electronic properties of defects resulting from the implantation of the RE in Ge, we have used the hybrid functional of Heyd, Scuseria, and Ernzerhof (HSE06) [26] by means of density functional theory (DFT) to calculate the structural and electronic properties of rare earth substitutions in Ge (RE_{Ge} for RE: Ce, Pr, Eu and Er). The energies of formation for the Ce_{Ge} , Pr_{Ge} , Eu_{Ge} and Er_{Ge} are calculated for charge states $(-2, -1, 0, +1, +2)$. The charge state transition levels with the accessible thermodynamic region are examined and presented as well.

2. Computational details

Results of this report are based on DFT. We used the projector-augmented wave (PAW) [27,28] to separate the core electrons from the valence electrons. Vienna *Ab initio* Simulation Package (VASP) [27] code was used. All calculations were carried out using Heyd, Scuseria, and Ernzerhof (HSE06) [26] hybrid functional. According to the HSE06 approach, the short-range exchange potential is calculated by mixing 25% fraction of nonlocal Hartree–Fock exchange with the Perdew, Burke, and Ernzerhof (PBE) [29] functional. In the past, defects in Ge were difficult to study theoretically, since the local density approximation (LDA) and the generalized gradient approximation (GGA) functionals incorrectly predict Ge to be a metal [2,30]. However, the HSE06 functional has been used to predict accurately the electronic band gap and improve charge state transition properties for group–IV semiconductors [2,12,30]. According to our previous reports [10,20], the modelling and prediction of the electronic properties of material with the f orbital valence shell was difficult, because the f orbital is highly localized. Recently, the hybrid functional has been successfully used to predict the electronic and band gap properties of several materials with the f orbital in the valence shell [10,31,32]. Following this success of the hybrid functional, the f orbital in the valence shell of RE can be handle.

To calculate the properties of the RE substitutional impurities in Ge, a periodic supercell containing 64 atoms of Ge was used. A regularly spaced mesh of $2 \times 2 \times 2$ Monkhorst–Pack [33] scheme k -point was used to integrate the Brillouin zone. We set the plane wave cutoff of the wave function expansion to 400 eV. To obtain an equilibrium geometry of a perfect supercell, we refined the geometry until the final change in the total energy and the forces were less than 10^{-5} eV and 0.001 eV/Å, respectively. The formation energy of a strongly correlated system is strongly dependent on the spin–orbit coupling (SOC) due to the presence of relativistic effects in heavy atomic systems. The scalar relativistic effect was taken into consideration by including in the PAW potential the mass–velocity and Darwin correction terms. In addition, spin orbit coupling was taken into account for all calculations. The formation energy (E^f) of defects is derived directly from total energies, allowing the calculation of equilibrium defect concentrations [34]. To determine the defect formation energy and transition energy ($\epsilon(q/q')$) levels, we calculated the total energy $E(\text{RE}_{\text{Ge}}, q)$ for a supercell containing an optimized defect RE_{Ge} in its charge state q . The RE substitutional impurity in Ge formation energy $E^f(\text{RE}_{\text{Ge}}, q)$ as a function of electron Fermi energy (ϵ_F) is given as [35]

$$E^f(\text{RE}_{\text{Ge}}, q) = E(\text{RE}_{\text{Ge}}, q) - E(\text{pristine}) + \sum_i (\Delta n)_i \mu_i + q[E_V + \epsilon_F] + E_{\text{cor}}^q, \quad (1)$$

where $E(\text{pristine})$ is the total energy of a supercell containing 64 atoms of Ge, $(\Delta n)_i$ ($\Delta n < 0$, when a RE atom is included to a supercell containing 64 atoms of Ge and $\Delta n > 0$ when a Ge atom is removed from a supercell containing 64 atoms of Ge) is the difference in the number of constituent atoms of type i between the

supercell containing 64 atoms of Ge and the supercell containing the defect, μ_i represents the chemical potential of different constituent atoms and as mentioned earlier, E_V is energy of the valence band maximum (VBM). The E_{cor}^q is the Freysoldt, Neugebauer, and Van de Walle (FNV) correction term. The E_{cor}^q accounts for the potential alignment between the charged defect and bulk at a point far from the defect. In addition, the E_{cor}^q accounts for the charge corrections in a supercell of finite size [36,35]. The FNV scheme explicitly uses the electrostatic potential obtained from DFT calculations to obtain an electrostatics model. The defect transition energy level $\epsilon(q/q')$ which is the Fermi energy at which two different charge states of the same defect have the same energy of formation, is given as [35]

$$\epsilon(q/q') = \frac{E^f(\text{RE}_{\text{Ge}}, q; \epsilon_F = 0) - E^f(\text{RE}_{\text{Ge}}, q'; \epsilon_F = 0)}{q' - q} \quad (2)$$

As reported in ref [2], we took the modelled band gap of the pristine Ge to be 0.78 eV.

3. Results and discussion

3.1. Structural properties

Fig. 1 shows the relaxed geometric structures of RE substitutional impurities in Ge. Fig. 1a and b display relaxed geometric structures of the Ce_{Ge} and Pr_{Ge} , respectively, and Fig. 1c and d display the relaxed geometric structures of the Eu_{Ge} and Er_{Ge} , respectively. Table 1 lists the predicted shortest bond distance (β_d) in (Å) between a RE and its nearest neighbour Ge atom, and the difference Δ_d between the β_d and the relaxed Ge–Ge bond length. After structural relaxation, we obtained the bond angle between three Ge atoms to be 109.4° and Ge–Ge bond length to be 2.46 Å. This bond length is in close agreement with both experimental (2.45 Å) [37] and GGA theoretical (2.48 Å) [38] results. The shortest bond length between Ce, Pr, Eu, Er and its nearest neighbour Ge atom is 2.80, 2.78, 2.74 and 3.18 Å, respectively. The difference

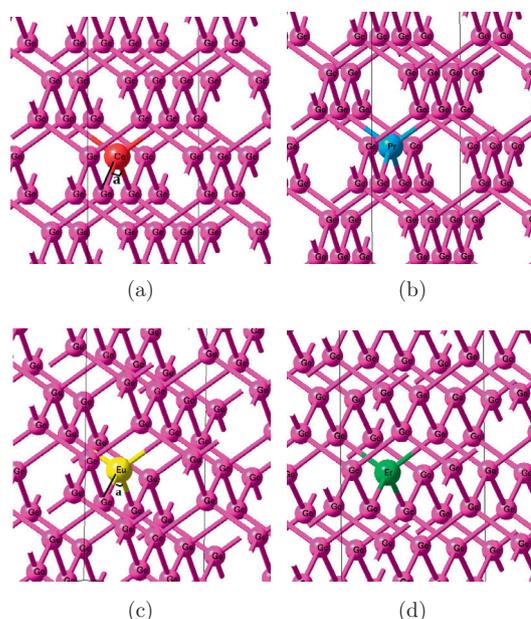


Fig. 1. Relaxed geometric structures of RE substitutions in Ge. (a) Ce_{Ge} , (b) Pr_{Ge} , (c) Eu_{Ge} and (d) Er_{Ge} . According to a and c, the black line and the text “a” represent the shortest bond length and the angle formed between a RE and two nearest neighbour Ge atoms. This same pattern applies to all other RE_{Ge} systems.

Table 1

Predicted bond length (β_d) between a RE and Ge atoms after geometric relaxation and the difference (Δ_d) between β_d and Ge–Ge relaxed bond length (2.46 Å) for RE substitutional impurities in Ge. The RE–Ge bond length is calculated with respect to the nearest neighbour Ge atoms around the RE.

| | β_d (Å) | Δ_d (Å) |
|-------|---------------|----------------|
| Ce–Ge | 2.80 | 0.34 |
| Pr–Ge | 2.78 | 0.32 |
| Eu–Ge | 2.73 | 0.27 |
| Er–Ge | 3.18 | 0.72 |

between the pristine nearest neighbour Ge bond length and the RE–Ge bond lengths for the Ce, Pr, Eu and Er is 0.34 0.32 0.27 and 0.72 Å, respectively. The amount of strain in the bond length experienced by atoms plays a vital role in predicting the stability (using the formation energy) of any doped system. We observed that the order of increase of difference in the bond length of RE–Ge and that of Ge–Ge after structural relaxation is $\text{Eu} < \text{Ce} < \text{Pr} < \text{Er}$ (see Table 1). Based on this ordering, we expect the bond length of the Er–Ge to experience more strain than that of other dopants. This suggests that the energy required for Er–Ge to form due to the high strain experienced, will be higher compare to that of other RE–Ge. The bond angles formed by a RE atom and its nearest neighbour two Ge atoms for all the rare earth dopants in Ge being investigated are all approximately 109.5° . This suggests that there is no much difference between the bond angle of pristine Ge and that of the RE substitution in Ge.

3.2. Total and projected density of states

Fig. 2 displays the plot of both the total density of states (DOS) and projected density of states (PDOS) of Ge and the RE_{Ge} . For the pristine Ge, as shown in Figs. 2a and 2b, the majority (spin up) and minority (spin down) density of states are symmetrical, suggesting non-spin polarisation of the system. For the Ce_{Ge} (Figs. 2c and 2d), Pr_{Ge} (Figs. 2e and 2f) and Eu_{Ge} (Figs. 2g and 2h), the majority and minority spins are not symmetrical, which suggests that the ground state of these systems are spin polarised. But on the other hand, the ground state of the Er_{Ge} (Figs. 2i and 2j) is not spin polarised since the spin up and spin down are symmetrically the same. For all RE_{Ge} , significant orbital states are located above the Fermi level at the VBM. For the Ce_{Ge} , the orbital states mainly contributed by the strong p -orbitals of both Ce and Ge atoms and d -orbital of Ce atoms, are 0.35 and 0.04 eV above the Fermi level for the minority and majority spins, respectively. This suggests that the Ce_{Ge} has a p -type semiconductor behaviour and can be considered for application in spintronics. For the Pr_{Ge} , the orbital states contributed by p and d -orbitals of Pr atom are 0.34 and 0.02 eV above the Fermi level for the spin down and up, respectively. For the Eu_{Ge} , the contributions of the p and d -orbital states are 0.28 and 0.01 eV above the Fermi level for the minority and majority spins, respectively. We also observed that for the Er_{Ge} , the contribution of both the p and d -orbital states are located above the Fermi level at the valence band maximum with energy of 0.36 eV, suggesting a p -type semiconductor material. Apart from the contributions by the orbital states above the Fermi level at the VBM, we observed a strong orbital hybridization between the p and s -orbitals of Ge. For the RE_{Ge} , (depending of the participating RE atom) we noticed orbital hybridization between p -orbital and s -orbital of Ge and RE atoms, respectively. In addition, a noticeable significant hybridization occurs between p -orbitals of both participating RE and Ge atoms. Generally speaking, for all the RE_{Ge} there is strong presence of each RE d -orbital in the band gap of Ge.

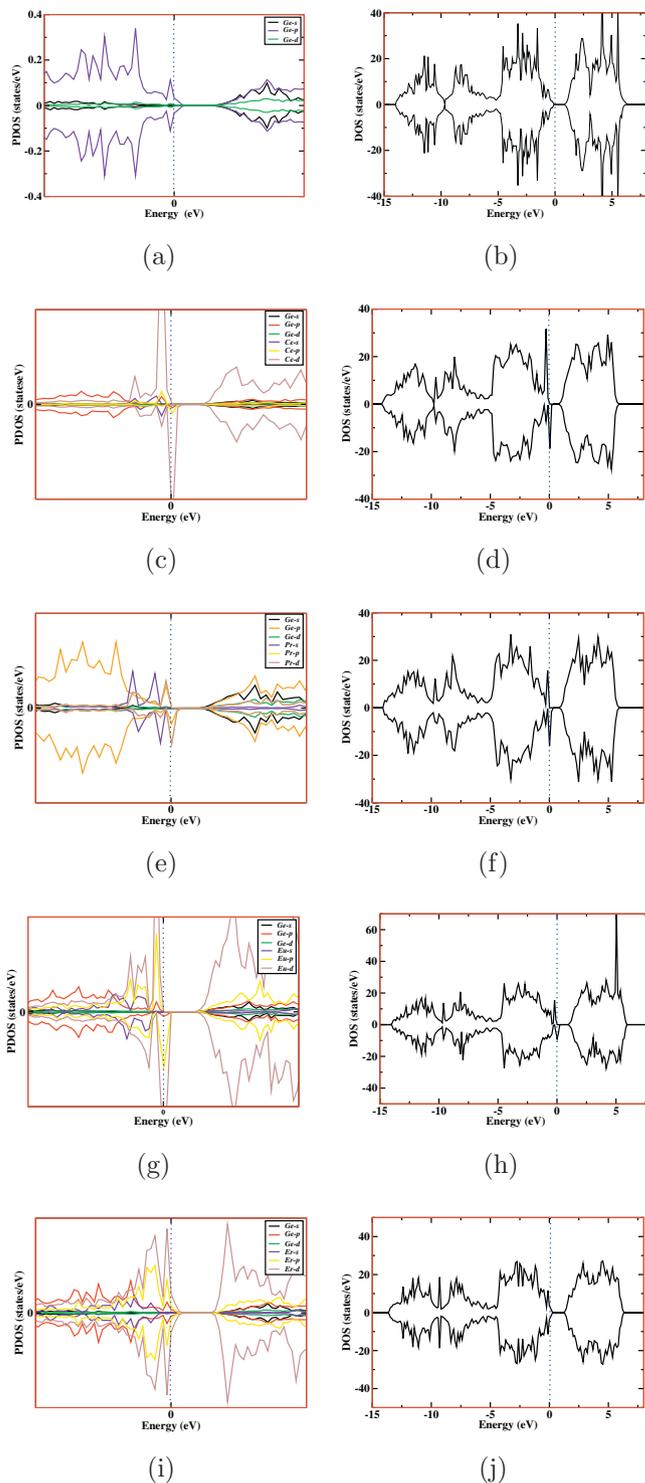


Fig. 2. Plots showing the spin polarised partial density of states (PDOS) left and total density of states (DOS) right of the RE_{Ge} . The Fermi level (at $\epsilon_f = 0$ eV) is shown by the dashed vertical blue line. (a) PDOS of pristine Ge, (b) Total DOS of pristine Ge, (c) PDOS of Ce_{Ge} , (d) Total DOS of Ce_{Ge} , (e) PDOS of Pr_{Ge} , (f) Total DOS of Pr_{Ge} , (g) PDOS of Eu_{Ge} , (h) Total DOS of Eu_{Ge} , (i) PDOS of Er_{Ge} and (j) Total DOS of Er_{Ge} .

3.3. Formation energies and charge state transition levels

Table 2 lists the results of formation energies at $\epsilon_f = 0$ for the neutral charge state of the Ce_{Ge} , Pr_{Ge} , Eu_{Ge} and Er_{Ge} . As listed in Table 2, the formation energies of the RE_{Ge} varied from -0.14 to 3.13 eV. For all RE_{Ge} , the energy of formation (-0.14 eV) of the

Table 2

Calculated formation energies ($E^f(RE_{Ge}, 0)$) in eV at $\epsilon_f = 0$ for the neutral charge state of the Ce_{Ge} , Eu_{Ge} , Er_{Ge} and Pr_{Ge} . The difference in formation energy ($dE^f(RE_{Ge}, 0)$) was calculated with respect to the lowest formation energy.

| Defect | $E^f(RE_{Ge}, 0)$ | $dE^f(RE_{Ge}, 0)$ |
|--------|-------------------|--------------------|
| Ce | 0.07 | 0.21 |
| Er | 3.13 | 3.27 |
| Eu | 0.01 | 0.15 |
| Pr | -0.14 | 0.00 |

Pr_{Ge} is the lowest and the Er_{Ge} has the highest formation energy of 3.13 eV. For the neutral charge state, the energy of formation of the Er_{Ge} is at least 3.00 eV higher than the other dopants. This suggests that the Er as a dopant in Ge, under equilibrium conditions requires a higher formation energy to form compare to other RE (Ce, Eu and Pr) dopants in Ge. In addition, as already mentioned in the structural part, the high strain experienced by the atoms of Er_{Ge} could also possibly be the reason while it has the highest formation energy. Considering that the strain experienced by the

atoms of Pr_{Ge} are less than that of Er_{Ge} and Ce_{Ge} , and that the formation energy of the Pr_{Ge} is lower than Ce_{Ge} with 0.21 eV, hence: we expect the Pr_{Ge} under equilibrium condition to be energetically the most favourable.

Plots of the formation energy as a function of the Fermi energy for the RE_{Ge} are shown in Fig. 3. Table 3 lists the charge state transition levels. The induced charge state transition levels for the Ce_{Ge} are deep within the band gap of Ge (see Fig. 3a). The first noticeable charge state transition level of the Ce_{Ge} is (+2/+1), a deep donor lying at 0.21 eV above the VBM. The Ce_{Ge} also induced a (+1/-1) charge state thermodynamic transition level at $E_C - 0.38$ eV. The (+1/-1) charge state transition level induced by the Ce_{Ge} exhibits properties of *negative-U* ordering. By using the method of Refs [18,19], we calculated the *effective-U* value of the (+1/-1) *negative-U* ordering to be -0.82 eV. This suggests that the Ce_{Ge} experiences large lattice distortion when charges are introduced. Fig. 3b shows that the Pr_{Ge} induced a shallow (-1/-2) acceptor level with an energy of 0.10 eV below the conduction band minimum. For the Pr_{Ge} , we also observed additional two charge state transition levels, the (+1/0) and (+1/-2) which are not thermody-

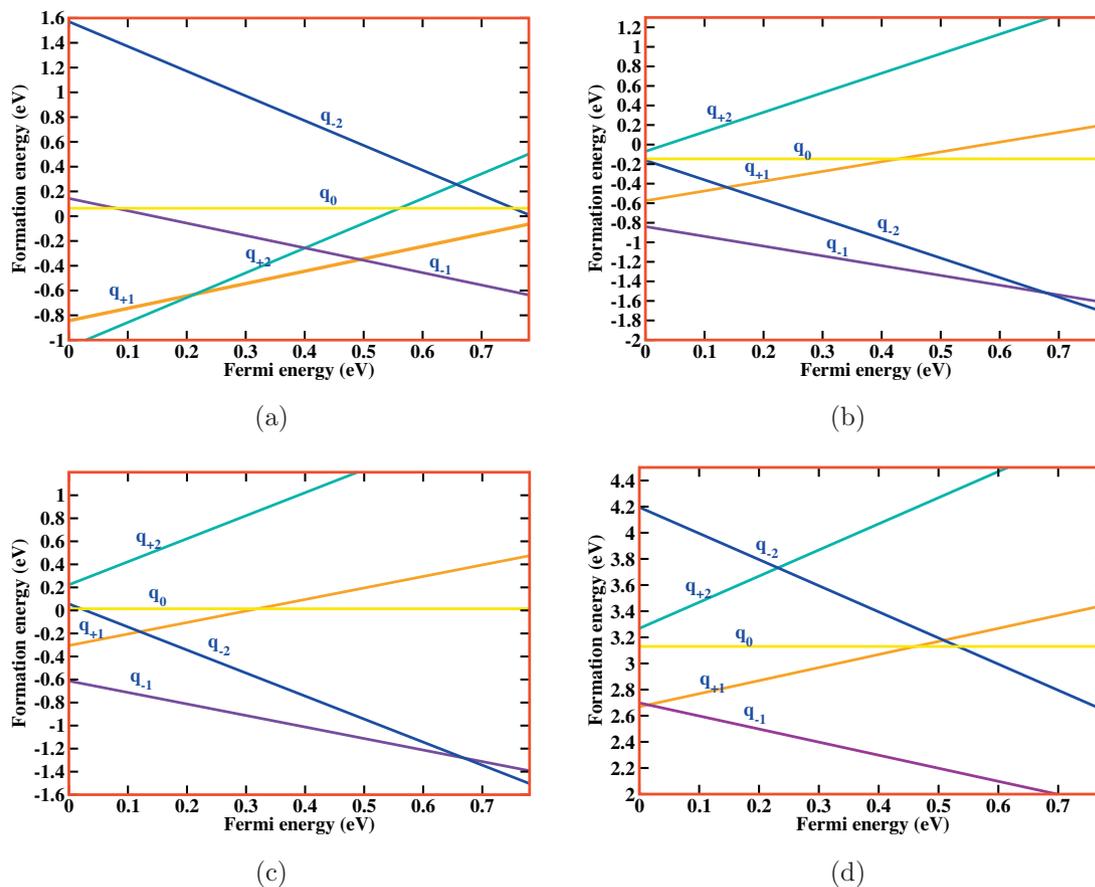


Fig. 3. Plot of formation energy as a function of the Fermi energy for RE substitutional impurities in Ge; (a) The Ce_{Ge} showing evidence of a donor level and *negative-U* properties in the band gap of Ge; (b) The Pr_{Ge} showing evidence of an acceptor level in the band gap of Ge; (c) The Eu_{Ge} showing an acceptor level close to the conduction band. (d) The Er_{Ge} showing a *negative-U* ordering.

Table 3

The energy of the charge state transition levels $\epsilon(q/q')$ in eV within the band gap of Ge for the Ce_{Ge} , Eu_{Ge} , Er_{Ge} and Pr_{Ge} .

| Transition level | Ce_{Ge} | Eu_{Ge} | Er_{Ge} | Pr_{Ge} |
|------------------|--------------|--------------|--------------|--------------|
| (+2/+1) | $E_V + 0.21$ | - | - | - |
| (-1/-2) | - | $E_C - 0.11$ | - | $E_C - 0.10$ |
| (+2/-1) | $E_C - 0.38$ | - | - | - |
| (+1/-1) | - | - | $E_V + 0.02$ | - |

namic stability. The Pr_{Ge} did not exhibit any *negative-U* ordering and donor level for all Fermi energies in the band gap of Ge as observed for the case of the Ce_{Ge}. The same charge state transition level observed for the Pr_{Ge} is also observed for the Eu_{Ge}. The only difference is that for the Eu_{Ge}, the (−1/−2) acceptor level is 0.11 eV below the conduction band as shown in Fig. 3d. For the Er_{Ge}, we found a shallow level at (+1/−1) in the band gap of Ge as displayed by Fig. 3c. The Er_{Ge} exhibits a *negative-U* ordering with *effective-U* value of −0.89 eV.

4. Summary

Results of the formation energies and charge state transition levels of the Ce, Pr, Eu and Er substitutions in Ge were described in detail. The energy of formation of the Ce_{Ge}, Pr_{Ge}, Er_{Ge} and Eu_{Ge} for the neutral charge state lies between −0.14 and 3.13 eV. Amongst the RE, the formation energy of the Pr_{Ge} for the neutral charge state is the lowest and energetically the most favourable. We have shown that the RE substitutional impurities induced charged state transition levels in the band gap of Ge. The Ce_{Ge} induced a deep donor level at E_V + 0.38 eV for the (+2/+1) charge states transition level. The Pr_{Ge} and Eu_{Ge} induced only acceptor levels within the band gap of Ge. For the Eu_{Ge} and Pr_{Ge}, the induced levels are at E_C − 0.11 and E_C − 0.10 eV, respectively. The Ce_{Ge} and Er_{Ge} exhibit properties of *negative-U* ordering with *effective-U* values of −0.82 and −0.89 eV, respectively.

Acknowledgement

This work is based on the research supported partly by National Research foundation (NRF) of South Africa (Grant specific unique reference number (UID) 98961). The opinions, findings and conclusion expressed are those of the authors and the NRF accepts no liability whatsoever in this regard.

References

- [1] F.J. Morin, J.P. Maita, *Phys. Rev.* 94 (1954) 1525.
- [2] E. Igumbor, C. Ouma, G. Webb, W. Meyer, *Physica B: Condensed Matter* 480 (2016) 191.
- [3] E. Igumbor, R.E. Mapasha, W.E. Meyer, *J. Electron. Mater.* 1–8 (2016), <http://dx.doi.org/10.1007/s11664-016-5026-z>.
- [4] C.O. Chui, K. Gopalakrishnan, P.B. Griffin, J.D. Plummer, K.C. Saraswat, *Appl. Phys. Lett.* 83 (16) (2003) 3275.
- [5] C.E. Lindberg, J.L. Hansen, P. Bomholt, A. Mesli, K.B. Nielsen, A.N. Larsen, L. Dobaczewski, *Appl. Phys. Lett.* 87 (17) (2005) 172103.
- [6] M.L.W. Thewalt, D. Labrie, I.J. Booth, B.P. Clayman, E.C. Lightowers, E.E. Haller, *Physica B+ C* 146 (1) (1987) 47.
- [7] H. Bracht, *Physica Status Solidi (a)* 211 (1) (2014) 109.
- [8] E. Igumbor, R. Mapasha, R. Andrew, W. Meyer, *Comput. Condensed Matter* 8 (2016) 31.
- [9] A. Chroneos, *J. Appl. Phys.* 107 (7) (2010).
- [10] E. Igumbor, W. Meyer, *Mater. Sci. Semicond. Process.* 43 (2016) 129.
- [11] P. Spiewak, J. Vanhellefont, K.J. Kurzydłowski, *J. Appl. Phys.* 110 (6) (2011).
- [12] H. Tahini, A. Chroneos, R.W. Grimes, U. Schwingenschlöggl, H. Bracht, *Appl. Phys. Lett.* 99 (7) (2011) 072112.
- [13] A. Colder, P. Marie, T. Wojtowicz, P. Ruterana, S. Eimer, L. Méchin, K. Lorenz, U. Wahl, E. Alves, V. Matias, *Superlattices Microstruct.* 36 (4) (2004) 713.
- [14] B. Garrido, C. Garcia, S.Y. Seo, P. Pellegrino, D. Navarro-Urrios, N. Daldosso, L. Pavesi, F. Gourbilleau, R. Rizk, *Phys. Rev. B* 76 (24) (2007) 245308.
- [15] A. Kanjilal, L. Rebohle, M. Voelskow, M. Helm, W. Skorupa, *J. Appl. Phys.* 107 (2) (2010).
- [16] R. Jones, *Opt. Mater.* 28 (6) (2006) 718.
- [17] S. Manna, N. Prtljaga, S. Das, N. Daldosso, S. Ray, L. Pavesi, *Nanotechnology* 23 (6) (2012) 065702.
- [18] E. Igumbor, K. Obodo, W.E. Meyer, *Solid State Phenomena* 242 (2015) 440.
- [19] Christoph Freysoldt, Blazej Grabowski, Tilmann Hickel, J. Neugebauer, Georg Kresse, Anderson Janotti, V. de Walle, Christoph Freysoldt, Blazej Grabowski, Tilmann Hickel, J. Neugebauer, Georg Kresse, Anderson Janotti, C.G. V. de Walle, *Rev. Mod. Phys.* 86 (2014) 253.
- [20] E. Igumbor, R.C. Andrew, W.E. Meyer, *J. Electron. Mater.* (2016).
- [21] V. Markevich, *Mater. Sci. Semicond. Process.* 9 (4–5) (2006) 589, Proceedings of Symposium T E-MRS 2006 Spring Meeting on Germanium based semiconductors from materials to devices.
- [22] G. Impellizzeri, S. Mirabella, M. Grimaldi, *Appl. Phys. A* 103 (2) (2011) 323.
- [23] G.S. Pomrenke, E. Silkowski, J.E. Colon, D.J. Topp, Y.K. Yeo, R.L. Hengehold, *J. Appl. Phys.* 71 (4) (1992).
- [24] Y. Miyata, Y. Nose, T. Yoshimura, A. Ashida, N. Fujimura, *J. Crystal Growth* 425 (2015) 158.
- [25] H. Przybylinska, W. Jantsch, Y. Suprun-Belavitch, M. Stepikhova, L. Palmethofer, G. Hendorfer, A. Kozanecki, R.J. Wilson, B.J. Sealy, *Phys. Rev. B* 54 (1996) 2532.
- [26] J. Heyd, G.E. Scuseria, M. Ernzerhof, *J. Chem. Phys.* 118 (18) (2003) 8207.
- [27] G. Kresse, J. Furthmüller, *Phys. Rev. B* 54 (1996) 11169.
- [28] P.E. Blochl, *Phys. Rev. B* 50 (1994) 17953.
- [29] J.P. Perdew, K. Burke, M. Ernzerhof, *Phys. Rev. Lett.* 77 (1996) 3865.
- [30] P. Deák, B. Aradi, T. Frauenheim, E. Jánzén, A. Gali, *Phys. Rev. B* 81 (2010) 153203.
- [31] B.G. Janesko, T.M. Henderson, G.E. Scuseria, *Phys. Chem. Chem. Phys.* 11 (3) (2009) 443.
- [32] J.L. Da Silva, M.V. Ganduglia-Pirovano, J. Sauer, V. Bayer, G. Kresse, *Phys. Rev. B* 75 (4) (2007) 045121.
- [33] H.J. Monkhorst, J.D. Pack, *Phys. Rev. B* 13 (1976) 5188.
- [34] S.B. Zhang, J.E. Northrup, *Phys. Rev. Lett.* 67 (1991) 2339.
- [35] C. Freysoldt, J. Neugebauer, C.G. Van de Walle, *Physica Status Solidi (b)* 248 (5) (2011) 1067.
- [36] C. Freysoldt, J. Neugebauer, C.G. Van de Walle, *Phys. Rev. Lett.* 102 (2009) 016402.
- [37] D. Batchelder, R. Simmons, *J. Chem. Phys.* 41 (8) (1964) 2324.
- [38] A. Chroneos, B. Uberuaga, R. Grimes, *J. Appl. Phys.* 102 (8) (2007) 083707.