

# Anomalous dispersion and band gap reduction in $\text{UO}_{2+x}$ and its possible coupling to the coherent polaronic quantum state



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## ABSTRACT

Hypervalent  $\text{UO}_2$ ,  $\text{UO}_{2(+x)}$  formed by both addition of excess O and photoexcitation, exhibits a number of unusual or often unique properties that point to it hosting a polaronic Bose–Einstein(-Mott) condensate. A more thorough analysis of the O X-ray absorption spectra of  $\text{UO}_2$ ,  $\text{U}_4\text{O}_9$ , and  $\text{U}_3\text{O}_7$  shows that the anomalous increase in the width of the spectral features assigned to predominantly U 5*f* and 6*d* final states that points to increased dispersion of these bands occurs on the low energy side corresponding to the upper edge of the gap bordered by the conduction or upper Hubbard band. The closing of the gap by 1.5 eV is more than twice as much as predicted by calculations, consistent with the dynamical polaron found by structural measurements. In addition to fostering the excitation that is the proposed mechanism for the coherence, the likely mirroring of this effect on the occupied, valence side of the gap below the Fermi level points to increased complexity of the band electronic structure that could be associated with the Fermi topology of BEC–BCS crossover and two band superconductivity.

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## 1. Introduction

As the origin of many of the interesting properties of matter, covalency is as important as it is awkward to define [1]. In classic real space physics, if the role of quantum mechanics is to define the distribution of electrons but the forces are electrostatic, then covalency is the accumulation of electron density between the nuclei that renders the overall force between the atom pair attractive. An important factor is therefore the spatial extent of the original atomic orbitals since their overlap determines the shared volume available for building up the charge. The concept of covalency is more easily depicted in momentum space as the shifts in the energy levels of the molecular orbitals from their parent atomic states in molecules and the dispersion of the bands in condensed systems. The structures of transition metals possessing localized electrons in flat bands tend to be defined by the longer range magnetic interactions of the isolated spins. In contrast, delocalized,

itinerant electrons can interact directly to give bands with large dispersions, with bulk properties that result from these bonds. Elements in the crossover region are the ones that display polymorphism, complicated magnetism, chemically reactive electronic states, and other manifestations of correlated electrons.

The rare earth elements, whose frontier 4*f* orbitals are confined to the core of the atom, and the heavier actinides whose 5*f* orbitals are similarly constrained therefore for the most part behave in predictable and relatively unexciting ways. The lighter actinides are, however, the opposite, with one example being the radical change in atomic radius at plutonium [2,3]. Residing at the crossover between spatially extended and localized 5*f* orbitals, it is the most complex element in the periodic table with six solid phases encompassing monoclinic to fcc symmetries, two of which exhibit negative thermal expansion coefficients, that span a 22% range of densities before it melts from the bcc  $\epsilon$  phase into a higher density liquid at a relatively modest 912.5 K. In addition to this evidence for the ambiguity in the ability of the 5*f* states to overlap, it has also recently been shown that the absence of the predicted magnetism

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in Pu is because the temporal fluctuations that create hybridized or mixed electronic states in dynamical mean field theory appear to have physical significance, scrambling the spins faster than they can collectively orient [4]. It would not be surprising if these two phenomena, one in time and one in space, are coupled. This pattern of diversity is also displayed in their chemistry. Pm-Am exhibit an usually large number of valences in their chemical compounds that are correlated with a radical change in bonding and symmetry from spherical and highly ionic in their (III) and (IV) states to the highly oblate (trans di-) oxo moiety with the ultra short, triply bonded oxo ion for (V)–(VII), or a tetraoxo configuration under certain conditions [1,5].

Analogous to Pu metal, the most complicated binary metal oxide phase diagram may be that for U [6,7] where there is not even consensus whether the number of distinct compounds between  $\text{UO}_{1.5}$  and  $\text{UO}_3$  is greater than 20 [8] or not [9]. It divides into two regions. Below  $\text{UO}_{2.33-2.5}$  the structures are strictly or approximately cubic. At temperatures below those where rapid O diffusion eliminates crystallographic disorder there are two mixed valence compounds that are single phase in diffraction,  $\text{U}_4\text{O}_9$  and  $\text{U}_3\text{O}_7$ , although the multiplicity of their extended superlattices has prevented their structures from being completely solved [10–14]. Even in this ionic region, however, there are indications of more complexity, such as superionic conductivity of  $\text{UO}_{2+x}$  and the aggregation of the adventitious O in  $\text{UO}_{2+x}$  so that it is better described as  $\text{UO}_2:\text{U}_4\text{O}_9$  and  $\text{U}_4\text{O}_9:\text{U}_3\text{O}_7$  mixtures [10,15,16]. At higher O:U ratios the structures are layered because of the propensity of U(V) and (VI) to form the trans dioxo species. Another unusual or even unique anomaly is the loss of the normal correlation between valence and geometry/bond length in the higher oxides. In molecular or coordination compounds the U–O bonding patterns are quite rigid with the distances falling into ranges of only a few hundredths of an Å, [5] with the only suggestion of flexibility being a small expansion of the U-oxo bond that is coupled to greatly increased lability in hydroxide complexes [17]. However, in the solid state the  $\alpha$  phase of  $\text{UO}_3$  is highly oblate with an extremely short reported 1.64 Å U-oxo distance, [18] whereas the  $\delta$  phase prepared by a slightly different procedure places the U ions in fully octahedral sites with U–O equals 2.08 Å, [19] with the intermediate phases giving intermediate distances in less distorted sites [20,21]. If the ternary uranates are included, [22–25] U(VI) exhibits essentially a continuous range of U–O bond lengths from 1.64 to 2.45 Å and longer. U(V) displays a continuous range of U–O distances from 1.9 to 2.7 Å in a single compound,  $\text{U}_2\text{O}_5$ . This behavior implies an exceptionally flat U–O potential for the higher valences that is highly susceptible to small changes in other factors influencing the structure and that can shift quite easily in response to such factors. It also implies a large degree of what would most likely be termed covalency; hard spherical ions do not change their conformations because of interactions with their neighbors. The shortness of the U-oxo bond points to a predilection for covalency that could potentially be distributed to other bonds if it is diminished in that one.

These properties of U(V) and (VI) that stabilize them in layered structures and the way they combine with the much less covalent U(IV) ions [26] with their cubic or spherical geometries underlie the special flexibility of the (111) planes in  $\text{UO}_2$  [27]. Not only do dislocation loops form along them, [28] but their easy [111] expansion also causes substitutional cations that prefer octahedral environments, e.g.,  $\text{Cr}^{3+}$ , to cluster along them as well. This behavior establishes the environment that promotes the dynamical polaron in fluorite structured, chemically or photodoped  $\text{UO}_{2(+x)}$  [29,30]. The  $2\text{U(V)} \leftrightarrow \text{U(IV)} + \text{U(VI)}$  disproportionation excitation of these polarons would occur easily via the transfer of O ions between their buckled-apical positions for fluorite and planar-apical positions for layered, triggered by a [111] type

acoustic phonon that causes the separation of the (111) U planes to oscillate. The synchronization of this internal reaction throughout the  $\text{U}_4\text{O}_9$ -type domain formed by the aggregation of the adventitious O or photoinduced charges then gives the coherence that defines the polaronic Bose–Einstein(-Mott) condensate. We have previously reported the O XAS of  $\text{UO}_{2+x}$  that demonstrated a significant enhancement of the widths of the U 5f states in the upper Hubbard band (UHB, the conduction band) that is opposed to the trend of narrower spectral features with increasing charge [29] that we attributed to the mixing of the electronic states and increased dispersion that occurs with a dynamical polaron [31]. We now examine these results in greater detail to show that this increased dispersion specifically reduces the lower boundary of the UHB. This substantial reduction of the gap energy and the increased DOS within the  $\text{UO}_2$  gap would then facilitate the excitation that results in the condensate formation [30]. In addition, it is likely that the cause of this effect acts on additional U 5f states so that it is mirrored in the lower Hubbard band (LHB, valence band). This would be of significant interest because much recent work on BEC–Barden–Cooper–Schrieffer (BCS) superconducting condensate crossover in mixed valence metal oxide and chalcogenide exotic superconductors is focused on the character of these bands closest to the Fermi level [32] and its implications for two band superconductivity [33–39].

## 2. Experimental and calculation methods

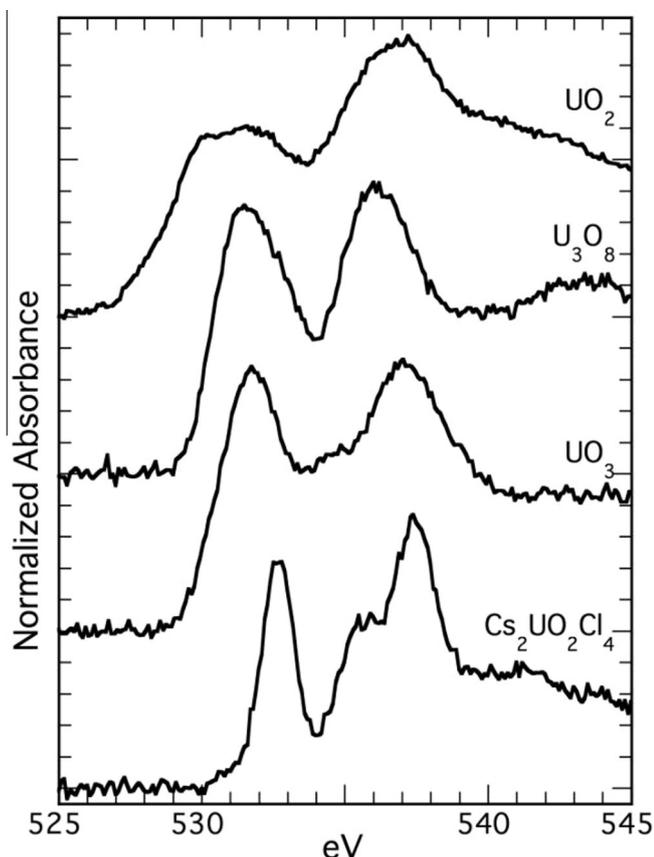
Samples were prepared and NIXS and XAS experiments were performed as previously described, [29,40–42] as were the calculations [43].

## 3. Results and discussion

### 3.1. O XAS of standards and $\text{UO}_2$

The O XAS of U-oxides [44–49] and even the oxo group of uranyl-containing molecules that are coordination complexes of U(VI) [50] consist of two principal features (Fig. 1). There is consensus not only for  $\text{UO}_2$  but for all of them that, in agreement with theory, the lower energy feature around 530–535 eV originates in transitions to unoccupied states of the upper Hubbard band (UHB) that are predominantly U 5f in character and the higher energy feature around 537–543 eV in transitions to unoccupied states that are predominantly U 6f. This is true not only for  $\text{UO}_2$  where the U is in a cubic site and the O surrounded by a tetrahedron of U, but also for layered compounds such as  $\text{U}_3\text{O}_8$  with relatively long U– $\text{O}_{\text{oxo}}$  bonds and  $\alpha$   $\text{UO}_3$  with its extremely short one and even the oxo O ion in  $\text{Cs}_2\text{UO}_2\text{Cl}_4$ . The pattern is the result of the symmetry relationship between cubic and octahedral geometries where the latter results from locating a neighbor atom in the center of each of the six square that constitute the cube's sides whose corners are the eight vertices. It is also because the shift in energy between the different types of O, terminal oxo, symmetrically bridging oxo, asymmetrically bridging oxo, and planar O with varying coordination numbers and bond lengths is less than 1 eV. The increase in the width of the peaks in the layered oxides with their multiple O species relative to that of the single type of O in the uranyl tetrachloride is therefore not excessive. The spectral pattern is therefore preserved across all of these species because the differences in energies for the different O and U species are much smaller than their U 5f-5d separations that are relatively insensitive to the speciation and geometry [48].

The exception to this assignment is the small shoulder on the leading edge of the first peak. This was not assigned for  $\text{Cs}_2\text{UO}_2\text{Cl}_4$  despite a very thorough set of experiments that utilized

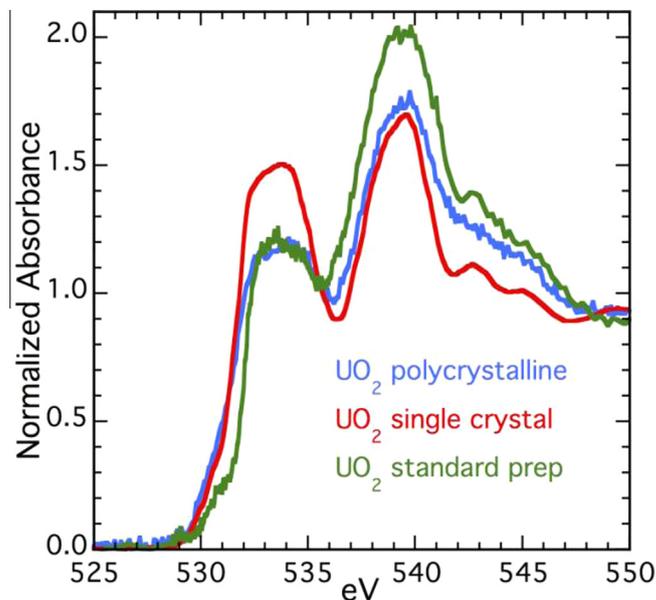


**Fig. 1.** O K-edge XAS fluorescence yield spectra of indicated compounds ( $\text{UO}_3$  is in the uranyl containing  $\alpha$  phase) with edge jumps normalized to unity. These are not calibrated.

polarization dependence of single crystals and emission spectra [50]. Curve-fits show that it is necessary for all of these spectra even when the change in slope is not apparent. Because the analysis of the tetrachloride utilized the transitions to the lowest energy unoccupied states it is difficult to explain. One possibility is a multi-electron transition.

For  $\text{UO}_2$ , the peaks or shoulders signifying peaks at around 530–531, 532, 534, 537, 539, 540, 542, and 545 eV are relatively consistent in their energies and sufficiently consistent in their relative amplitudes so that the overall shapes are similar [26,44–47,49]. The precise intensities and shapes of these two features, however, vary between samples (Fig. 2) even when their impurity levels are at or below the 100 ppm range. The changes in relative amplitudes result in motions of some of the features, including the leading edge of the first peak around 531 eV and the valley at 535–536 eV. The spectral features are therefore affected by even the small amounts of disorder that vary between different preparations, which in an XAS measurement will be exacerbated by the surface quality. This comparison, then, provides a measure of the level of reproducibility to expect in evaluating the spectra from different compounds.

Within this level of uncertainty, it is apparent that these two spectral features for  $\text{UO}_2$  are significantly and consistently wider than those from the other non-fluorite compounds. Both of them consist of multiple peaks, causing their flatness across the tops. Calculations indicate that this is an effect of spin-orbit coupling [49,51–53] that causes multiplet splitting in the spectra. The reduction in such splitting as the valence increases and the number of electrons residing in these states decreases therefore explains the observed narrowing of the spectral features.



**Fig. 2.** O K-edge XAS fluorescence yield measurements of  $\text{UO}_2$  from a single crystal, which will have the highest surface quality and impurity level, polycrystalline material prepared from recrystallized  $\text{UO}_2\text{O}_2$  that will have the lowest impurity concentrations, and from commercially available high purity  $\text{UO}_2$  that is reduced to  $\text{UO}_{2.00}$  by standard procedures.

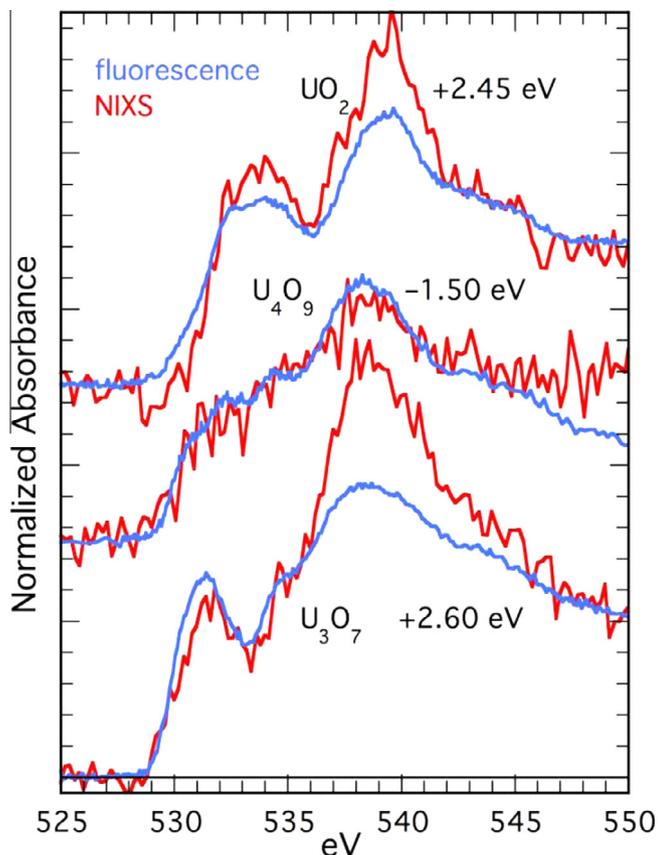
### 3.2. O K-edge XAS and NIXS of $\text{UO}_{2+x}$

In addition to variations because of surface quality, XAS spectra at these energies are affected by self-absorption because the samples are fully opaque to the X-rays. Self-absorption causes a flattening of the spectra around the average absorption, increasing the amplitudes of features below this average proportionate to the amount by which they are less than this average, and reducing the amplitudes of features above the average absorption in the same way. Both of these problems that distort the spectra are solved by using Non-resonant Inelastic X-ray Scattering (NIXS) with a high energy ( $\sim 10$  keV) beam that penetrates deeply into the sample [40,41]. The NIXS spectra can therefore confirm the features constituting the more conventionally measured but surface sensitive XAS and also give the correct amplitudes, albeit with much greater noise levels because of the weakness of the NIXS signal. The comparison (Fig. 3) of the NIXS and XAS using this information validates the measured spectra.

This verification is crucial because the spectra of these mixed valence compounds do not adhere to the pattern exhibited by the other U compounds (Figs. 1 and 3). For  $\text{U}_3\text{O}_7$  the U 5f manifold is greatly reduced. For  $\text{U}_4\text{O}_9$  there is no distinct feature separated by an equally distinct valley from the principal one at higher energy, all features are suppressed so that after the initial abrupt rise the spectrum is almost featureless – or contains a number of very small features – until it rises somewhat more steeply to a low peak in the U 6d region.

Because of the self-absorption issues the positions and widths of the features are best obtained via the NIXS spectra. The differences in amplitude, energy, and the presence or absence of features are apparent when the spectra are overlaid (Fig. 4). Also obvious is that the  $\text{U}_4\text{O}_9$  spectrum is not an average of the  $\text{UO}_2$  and  $\text{U}_3\text{O}_7$  endpoints [29] despite the supposition that it contains the same defects and therefore O environments whose larger number in  $\text{U}_3\text{O}_7$  are simply organized differently.

The noise level of the NIXS causes difficulties in determining the energies of the features, a problem that is ameliorated by taking

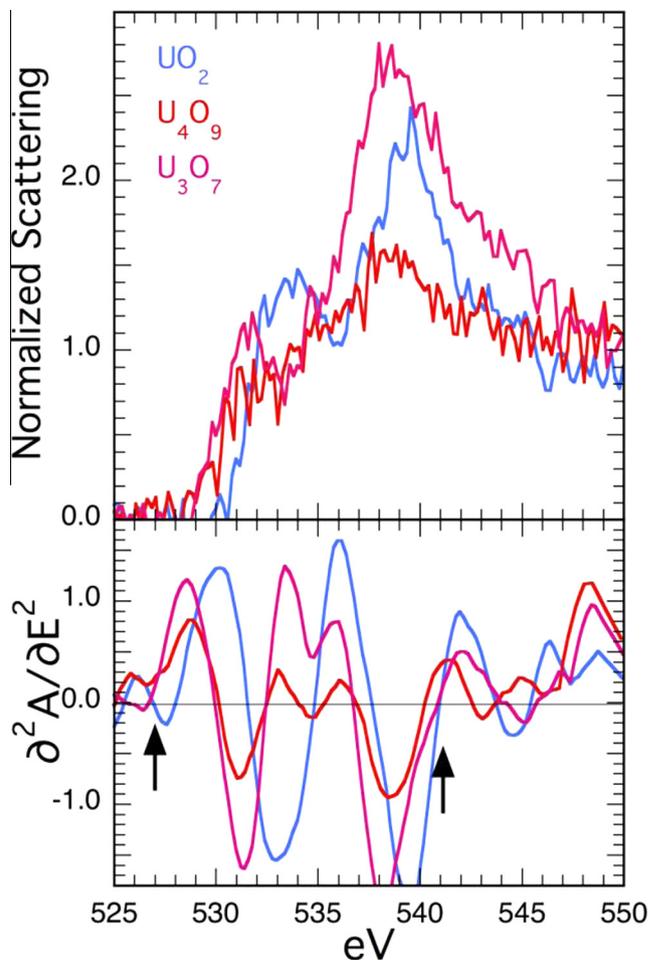


**Fig. 3.** Fluorescence yield and NIXS spectra of  $\text{UO}_{2+x}$  compounds. Numbers are the shift of the FY data to match the NIXS whose energies are set by the difference from the excitation line.

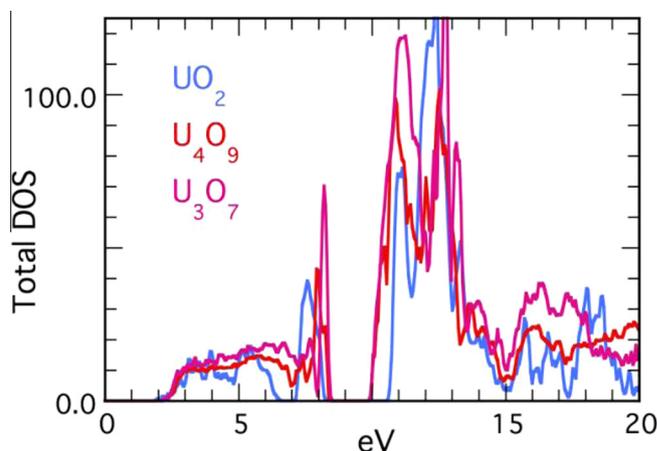
the derivatives that also finds the energies of the features of interest more accurately. In this case the issue is not the increase in the dispersion and total width of the DOS with doping that has been described previously [29] but more specifically the effects on the gap. The energies of the inflection points of the initial absorption increase are 531.5 for  $\text{UO}_2$ , 530.1 for  $\text{U}_4\text{O}_9$ , and 529.9 for  $\text{U}_3\text{O}_7$ , giving shifts of  $-1.4$  and  $-1.6$  eV for the O-doped compounds. In contrast, the values for the inflection point on the far side of the 538–539 eV peak are, respectively, 541.0, 540.3, and 540.9 eV. The shift for  $\text{U}_3\text{O}_7$  is only  $-0.1$  eV, which is in the uncertainty level. For  $\text{U}_4\text{O}_9$  it is  $-0.7$  eV. This would reduce the overall increase in the dispersion of the U DOS for this compound, but given the flatness of the spectrum because of the low amplitude of this peak and the high noise level the uncertainty is higher. We point out that the peaks of this feature for both doped compounds coincide, making it likely that the U 6d bands of  $\text{U}_4\text{O}_9$  and  $\text{U}_3\text{O}_7$  have similar overall energies. It is therefore notable that the increased dispersion of overall U DOS occurs as shifts to lower energy. To the extent that the principal peak reflects the U 6d states its increased width relative to that for  $\text{UO}_2$  indicates that both these and 5f states are affected.

### 3.3. Comparison with calculations

The question of whether the broadening of the DOS to lower energies is expected or instead indicates an unusual phenomenon such as the condensate is addressed by DFT+U calculations [43] using the neutron-scattering type structure [10,13,54] that retains the fluorite lattice and incorporates the adventitious O into the vacant cubic sites concomitant with the displacement of some number of adjacent original O ions into neighboring sites. These calculations show (Fig. 5) the decrease in energy of the boundary



**Fig. 4.** NIXS spectra of  $\text{UO}_{2+x}$  compounds, absorbance and second derivatives. The arrows indicate the locations of the inflection points for the initial edge jump that would be the initial energy for the UHB and the limit of the large feature assigned to U 6d final states and therefore mark the boundaries of the U DOS.



**Fig. 5.** DFT+U calculations of the total density of states for the normal and doped compounds.

and lowest energy peaks of the UHB as well as the shift of the DOS in the U 6d region to lower energy on doping and the reduced amplitude for  $\text{U}_4\text{O}_9$  relative to  $\text{U}_3\text{O}_7$ . However, the reduction in the energy of the UHB edge is only half or somewhat less than half of the experimental value, and the calculation also fails to find the reduction or loss of the separation between the 5f and 6d states

that is seen in the spectra. Thus, instead of the  $-0.6$  eV shift of the UHB edge with doping, with the overall gap shrinking by  $\sim 0.9$  eV to reduce it from around 2.5 eV (somewhat larger than the experimental number of  $\sim 2.1$  eV) to around 1.6 eV, the measurements show a shift of the initial absorption increase in the doped compounds relative to  $\text{UO}_2$  of around  $-1.5$  eV. Modeling has demonstrated that the energies of the local electronic states associated with dynamic polarons bend, with the deviations from a horizontal line increasing in tandem with the electron–phonon coupling constant. Avoided crossings can therefore actually change the state that occurs at the band edge. The energy differences between the states are also affected, with some increasing but other decreasing to give a small amount of absorption through the IR region down to almost zero energy. The dynamics that has been identified from the structural measurements and is intrinsic to the condensate and related phenomena can thus be a possible contributor or even cause of this large reduction in the UHB edge.

1.5 eV begins to approach the closing of the gap. This will be especially true if the lowering of the UHB is mirrored by a concomitant increase in the upper edge of the LHB that occurs in the calculations, which might be characterized by RIXS [55]. Such a process would be expected if the energy shifts in the levels associated with – using the analogy with molecules – antibonding states move in the opposite direction as those in the LBH that are involved in bonding. This correlation of the states that is the definition of covalency is a process for increasing the dispersion of the bands, as happens when O is added to  $\text{UO}_2$  to give the mixed valence compounds. A reduction in the energy across the gap is consistent with the proposed mechanism involving a flat U–O pair potential and a facile excitation between the cubic U(V) ground state and the layered U(VI) excited state [29,30]. Although U(VI) was not detected in high resolution or RIXS studies, [55,56] insofar as the structural chemistry of U-oxides required this valence for the short distances that have been identified by XAFS [57] it is possible that the improvement in energy resolution increases the time domain via the uncertainty principle, confining the experiment to the ground state. In addition, as previously stated, this region is of interest because this upper edge of the valence band is where not only BEC but also BCS states will occur, stimulated or at enhanced by the same dispersion, avoided crossings, and similar covalency-related correlated phenomena. This multiplicity of bands at the Fermi level is the basis for the complicated Fermi topology that is coupled to BEC–BCS crossover [32] and two-band exchange as the origin of pseudogap states and exotic superconductivity [33–39] and would therefore place  $\text{UO}_{2(+x)}$  within this class of materials, albeit at an extreme position.

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