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Long distance cavity entanglement by entanglement swapping using atomic momenta

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ABSTRACT

We propose a simple technique to generate entanglement between distant cavities by using entanglement swapping involving atomic momenta. For the proposed scheme, we have two identical atoms, both initially in their ground state, each incident on far apart cavities with particular initial momenta. The two cavities are prepared initially in superposition of zero and one photon state. First, we interact each atom with a cavity in a dispersive way. The interaction results into atom–field entangled states. Then we perform EPR state measurement on both atomic momentum states which is an analog of Bell measurement. The EPR state measurement is designed by passing the atoms through cavity beam splitters which transfers the atomic momentum state into the superposition state. Finally, these atoms are detected by the detector. After the detection of the atoms, we can distinguish that cavities in one of the Bell states. This process leads to two distant cavity fields entanglement.

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1. Introduction

Entanglement, a non-local trait of quantum theory, has many applications in quantum informatics [1]. The cavity quantum electrodynamics (QED) techniques are used to generate atom–field, atom–atom and field–field entanglement [2]. Entanglement in the atomic external degrees of freedom using Bragg diffraction is also proposed [3,4]. Bragg diffraction of atomic de-Broglie waves from optical cavity also covers some aspects of quantum information [5,6].

Entanglement swapping, an important technique of entanglement, entangles two parties that have never interacted before. Entanglement swapping between two photons that have never coexisted is demonstrated [7]. Bell measurements are much useful in quantum communication protocols such as teleportation [8] and entanglement swapping [9]. Entanglement swapping is used in quantum repeaters [8], in order to overcome the limiting effect of photon loss in long-range quantum communication.

In this paper, we use a simple technique i.e. atomic interferometry for swapping entanglement between atoms and cavities. This way we are able to entangle distant cavities without direct interaction. For

the proposed scheme, we have two cavities which are in superposition state of zero and one photon. The cavity superposition state is experimentally demonstrated by Rauschenbeutel et al. [10]. First, we interact two atoms, initially in their ground state having momentum $|P_0^i\rangle$, $i \in \{1, 2\}$ each with a cavity in the Bragg diffraction regime. Bragg scattering allows only one of the two directions of propagation for each atom along the cavity field which are the incident and exactly opposite one. The detuning is large as compared to single photon Rabi frequency and hence atom practically stays in the ground state and the state of the field does not change. Here we take first-order Bragg diffraction for simplicity, however higher order Bragg scattering can be taken into account in the same fashion in order to allow larger separation between the atoms after the interaction. The non-resonant interaction entangles the atoms in their external degrees of freedom i.e. in their momentum states with the cavities. Then these entangled atoms are passed through beam splitter. For this purpose we use two beam splitters, one for non-deflected atomic momentum state and the other for deflected atomic momentum state. The beam splitter brings the atomic momentum state of these indistinguishable atoms in the superposition state. A cavity in the superposition state of zero and one photon can be used as a beam splitter [11]. At last, after passing through the beam splitter, these identical atoms are detected. Here, we use four detectors for four possible momentum splits. The detection process

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gives us the information that the two cavities are in the Bell state. Thus entanglement between atoms is swapped to that between two far away cavities.

Our paper proceeds as follow: in Section 2, we explain the Bragg diffraction of atom from the cavity field and the formation of atom–field entanglement. In Section 3, we analyze the action of beam splitter which transfers the atomic momentum component into the superposition state. We then briefly explain the detection process and the final result. Finally we conclude in Section 4 and give experimental parameters to perform our proposed scheme in the laboratory.

2. Bragg atom–field interaction

For the proposed scheme, we first entangle two atoms with their respective cavity fields by atom–field interaction in the Bragg regime. For the purpose, we consider two atoms, A_1 and A_2 , both initially in their ground state, g_1 and g_2 , having transverse momentum state, $|P_{l_0}^i\rangle$, where $i=1, 2$ stands for atoms A_1 and A_2 and $P_{l_0} = (l_0/2)\hbar k$ with l_0 being a positive even integer. We have two cavities, C_1 and C_2 , which are in the superposition state of zero and one photon i.e. $(|0\rangle + |1\rangle)/\sqrt{2}$ [3] as shown in Fig. 1. This superposition can be generated by first passing a two level atom in its excited state for half a Rabi cycle through the field. We dispersively interact atom, A_1 , with cavity, C_1 , and atom, A_2 , with cavity, C_2 . The off-resonant interaction is followed to avoid decoherence that stems from spontaneous emission. Large detuning and large interaction time ensure conservation of energy which leads to only two possible directions of scattering for atoms, first the incident one, P_{l_0} , and second exactly opposite to the incident transverse momentum direction, P_{-l_0} . The off-resonant Bragg diffraction invokes only the virtual transition among different atomic levels [11]. The initial state vector for the system before interaction is

$$|\Psi(0)\rangle = \frac{1}{\sqrt{2}} \sum_{i=1,2} (|0_i\rangle + |1_i\rangle) \otimes |g_i, P_{l_0}^i\rangle. \quad (1)$$

Total Hamiltonian governing this atom–field interaction under the dipole and rotating wave approximation with atom of mass, M , and centre of mass momentum, P , is [3]

$$\hat{H} = \frac{\hat{P}^2}{2M} + \frac{1}{2}\hbar\omega_0\hat{\sigma}_z + \hbar\nu\hat{a}^\dagger\hat{a} + \hbar g \cos(k\hat{x})[\hat{\sigma}_+ \hat{a} + \hat{\sigma}_- \hat{a}^\dagger]. \quad (2)$$

Here, $\hat{\sigma}_\pm$ and $\hat{\sigma}_z$ are the Pauli operators, \hat{x} is the position operator of atom, \hat{a} (\hat{a}^\dagger) is the field annihilation (creation) operator, g is the vacuum Rabi frequency and Δ is the detuning between the atomic

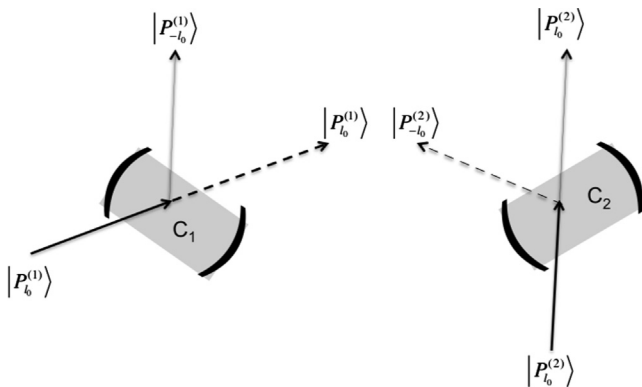


Fig. 1. We show dispersive interaction of atoms with cavity fields. The atoms with initial momentum, $|P_{l_0}^i\rangle$, interact with the cavities which are in superposition of zero and one photon state. The interaction time is set such that when the cavities are in zero photon state, the atoms do not get deflected and have same momentum $|P_{l_0}^i\rangle$ as initial one. For one photon state of the cavities, the atoms are deflected and have momentum $|P_{-l_0}^i\rangle$.

transition frequency, ω_0 , and the field frequency, ν . We follow the large detuning case where we have no direct atomic transition and it is rare to find the atom in their excited state. Hence, the system may be governed by following effective Hamiltonian, under the adiabatic approximation as

$$\hat{H}_{\text{eff}} = \frac{\hat{P}^2}{2M} - \frac{\hbar|g|^2}{2\Delta}\hat{n}\hat{\sigma}_- \hat{\sigma}_+ + (\cos 2k\hat{x} + 1). \quad (3)$$

The state of each i th atom–field pair at any time t is given as

$$|\Psi(t)\rangle = \frac{1}{\sqrt{2}} \sum_{l=-m}^m (C_{0,\tilde{P}_l} |0, g_i, \tilde{P}_l^i\rangle + C_{1,\tilde{P}_l} |1, g_i, \tilde{P}_l^i\rangle), \quad (4)$$

where m is the total number of the orders of deflections and $\tilde{P}_l = P_{l_0} + \hbar k$, l being an even integer. Time evolution of the state vector is given by the Schrodinger equation

$$i\hbar \frac{\partial |\Psi(t)\rangle}{\partial t} = H_{\text{eff}} |\Psi(t)\rangle \quad (5)$$

We have

$$\cos 2k\hat{x} |\tilde{P}_l\rangle \sim |\tilde{P}_{(l+2)}\rangle + |\tilde{P}_{(l-2)}\rangle \quad (6)$$

and we drop the unchanged atomic ground state vector $|g_i\rangle$. Under condition of Bragg scattering with only two possible directions of deflection $l=0$ with $\tilde{P}_0 = P_{l_0}$ and $l=-l_0$ with $\tilde{P}_{-l_0} = P_{-l_0}$. Thus we obtain the state of each i th atom–field pair after interaction as [3,12]

$$|\Psi(t)\rangle = \frac{1}{\sqrt{2}} (|0_i, P_{l_0}^i\rangle + C_{1,l_0}(t) |1_i, P_{l_0}^i\rangle + C_{1,-l_0}(t) |1_i, P_{-l_0}^i\rangle) \quad (7)$$

where $C_{n,\pm l_0}$ is the probability amplitude of the atom exiting with momentum P_{+l_0} or P_{-l_0} when there are n photons in the field and is given as

$$C_{n,\pm l_0}(t) = e^{-iA_n t} \left[C_{n,\pm l_0}(0) \cos\left(\frac{1}{2}B_n t\right) + iC_{n,\mp l_0}(0) \sin\left(\frac{1}{2}B_n t\right) \right] \quad (8)$$

where

$$A_n \equiv \begin{cases} -\frac{(|g|^2 n / 4\Delta)^2}{\omega_{\text{rec}}(l_0 - 2)(2)} & \text{for } l_0 \neq 2 \\ 0 & \text{for } l_0 = 2 \end{cases}$$

and

$$B_n \equiv \begin{cases} \frac{(|g|^2 n / 2\Delta)^{l_0/2}}{(2\omega_{\text{rec}})^{l_0/2-1} [(l_0-2)(l_0-4)\dots 4.2]} & \text{for } l_0 \neq 2 \\ |g|^2 n / 2\Delta & \text{for } l_0 = 2 \end{cases}$$

Initially both atoms are sent with momentum P_{l_0} , so probability of finding the exiting atom in either directions flips as a cosine function of interaction time. We adjust the interaction time of atoms with fields to ensure that if there is one photon in the fields, the atoms definitely get deflected. The adjusted time is thus $t = r\pi/|B_n|$, where r is an odd integer. For first-order Bragg scattering, this time simplifies to $t = 2r\pi\Delta/|g|^2$. The wave function of the two atom–field pairs is

$$|\Psi(t)\rangle = \left[\frac{1}{\sqrt{2}} (|0_1, P_{l_0}^1\rangle + ie^{-i\phi} |1_1, P_{-l_0}^1\rangle) \right] \otimes \left[\frac{1}{\sqrt{2}} (|0_2, P_{l_0}^2\rangle + ie^{-i\phi} |1_2, P_{-l_0}^2\rangle) \right], \quad (9)$$

where $\phi = r\pi A_1/B_1$. The atoms in their external degrees of freedom become entangled with their respective cavity fields. The combined state of the system can be written as

$$|\Psi(t)\rangle = \frac{1}{2} (|0_1, 0_2, P_{l_0}^1, P_{l_0}^2\rangle + ie^{-i\phi} |0_1, 1_2, P_{l_0}^1, P_{-l_0}^2\rangle + ie^{-i\phi} |1_1, 0_2, P_{-l_0}^1, P_{l_0}^2\rangle - e^{-i2\phi} |1_1, 1_2, P_{-l_0}^1, P_{-l_0}^2\rangle). \quad (10)$$

After adding and subtracting some terms and rearranging, we have

$$\begin{aligned} |\Psi(t)\rangle = & \frac{1}{4} \left(|P_{l_0}^{(1)}, P_{l_0}^{(2)}\rangle + e^{-i2\phi} |P_{-l_0}^{(1)}, P_{-l_0}^{(2)}\rangle \right) (|00\rangle - |11\rangle) \\ & + \frac{1}{4} \left(|P_{l_0}^{(1)}, P_{l_0}^{(2)}\rangle - e^{-i2\phi} |P_{-l_0}^{(1)}, P_{-l_0}^{(2)}\rangle \right) (|00\rangle + |11\rangle) \\ & + \frac{1}{4} i e^{-i\phi} \left(|P_{l_0}^{(1)}, P_{l_0}^{(2)}\rangle + |P_{-l_0}^{(1)}, P_{l_0}^{(2)}\rangle \right) (|10\rangle + |01\rangle) \\ & + \frac{1}{4} i e^{-i\phi} \left(|P_{l_0}^{(1)}, P_{l_0}^{(2)}\rangle - |P_{-l_0}^{(1)}, P_{l_0}^{(2)}\rangle \right) (|10\rangle - |01\rangle). \end{aligned} \quad (11)$$

Here, we entangle the cavities and atoms in four EPR states, separately, and all the four states are also entangled with each other. Measurement of atoms in one of the EPR states projects the two cavities into a corresponding Bell state. We discuss this process in next section.

3. EPR state measurement on atomic momenta EPR states

The scheme proposed in this paper is to develop entanglement between two far away cavities. EPR state measurement on atomic momentum states collapses the field states into one of the four EPR states. For EPR measurement on atomic momenta we pass these entangled atoms through beam splitters. We have two beam splitters, BS₁ and BS₂. The beam splitters are cavities prepared in superposition of zero and one photon. The atomic momentum components, $|P_{l_0}^{(1)}\rangle$ and $|P_{l_0}^{(2)}\rangle$, pass through beam splitter, BS₂, and momentum components, $|P_{-l_0}^{(1)}\rangle$ and $|P_{-l_0}^{(2)}\rangle$, pass through beam splitter BS₁ as shown in Fig. 2. Mirror can be used to deflect atoms to desired cavities. Here, the two atoms are indistinguishable. The dispersive interaction of atoms with cavity beam splitter for an interaction time, $t = 2\pi\Delta'/|g'|^2$ [13], transfers the atomic momentum states into the superposition state. Here, Δ' is the atom–beam splitter field detuning and g' is the vacuum Rabi frequency. The atoms or beam splitting cavities can be oriented such that atoms undergo first-order Bragg scattering. The beam splitter action is performed as follows:

$$\begin{aligned} |P_{l_0}^{(1)}\rangle & \longrightarrow |P_{l_0}^{(1)}\rangle + i|P_{l_0}^{(2)}\rangle, \\ |P_{l_0}^{(2)}\rangle & \longrightarrow i|P_{l_0}^{(1)}\rangle + |P_{l_0}^{(2)}\rangle, \\ |P_{-l_0}^{(1)}\rangle & \longrightarrow |P_{-l_0}^{(1)}\rangle + i|P_{-l_0}^{(2)}\rangle, \\ |P_{-l_0}^{(2)}\rangle & \longrightarrow i|P_{-l_0}^{(1)}\rangle + |P_{-l_0}^{(2)}\rangle. \end{aligned} \quad (12)$$

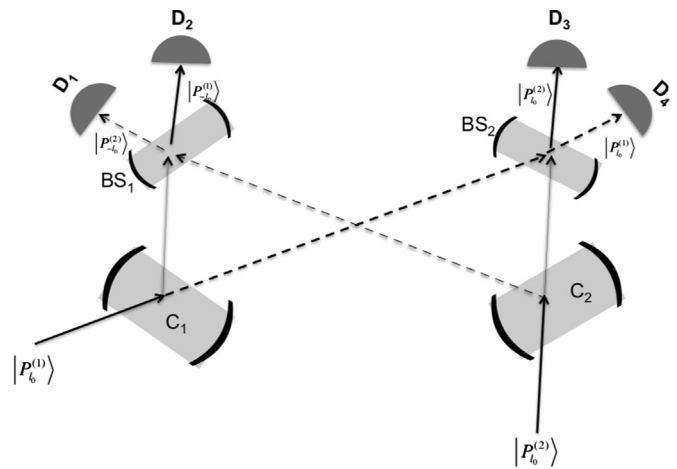


Fig. 2. For EPR state measurement on atomic momenta, the atoms are passed through the beam splitter BS₁ and BS₂ and are finally detected by the detector D₁, D₂, D₃ and D₄. The undeflected components pass through beam splitter BS₁ and deflected components interact with BS₂. The beam splitters are cavities prepared in superposition of zero and one photon. The two cavities C₁ and C₂ get entangled after detection of the atomic momenta states.

When the beam splitter action is performed, the first factor of the first term of Eq. (11) becomes

$$\begin{aligned} |P_{l_0}^{(1)}, P_{l_0}^{(2)}\rangle + e^{-i2\phi} |P_{-l_0}^{(1)}, P_{-l_0}^{(2)}\rangle & \longrightarrow \left(|P_{l_0}^{(1)}\rangle + i|P_{l_0}^{(2)}\rangle, i|P_{l_0}^{(1)}\rangle + |P_{l_0}^{(2)}\rangle \right) \\ & + e^{-i2\phi} \left(|P_{-l_0}^{(1)}\rangle + i|P_{-l_0}^{(2)}\rangle, i|P_{-l_0}^{(1)}\rangle + |P_{-l_0}^{(2)}\rangle \right) \\ & = i \left(|P_{l_0}^{(1)}, P_{l_0}^{(1)}\rangle + |P_{l_0}^{(2)}, P_{l_0}^{(2)}\rangle \right) \\ & + e^{-i2\phi} \left(|P_{-l_0}^{(1)}, P_{-l_0}^{(1)}\rangle + e^{-i2\phi} |P_{-l_0}^{(2)}, P_{-l_0}^{(2)}\rangle \right). \end{aligned} \quad (13)$$

Similarly, the first factor of the second term in Eq. (11) after the action of beam splitter is

$$\begin{aligned} |P_{l_0}^{(1)}, P_{l_0}^{(2)}\rangle - e^{-i2\phi} |P_{-l_0}^{(1)}, P_{-l_0}^{(2)}\rangle & \longrightarrow \left(|P_{l_0}^{(1)}\rangle + i|P_{l_0}^{(2)}\rangle, i|P_{l_0}^{(1)}\rangle + |P_{l_0}^{(2)}\rangle \right) \\ & - e^{-i2\phi} \left(|P_{-l_0}^{(1)}\rangle + i|P_{-l_0}^{(2)}\rangle, i|P_{-l_0}^{(1)}\rangle + |P_{-l_0}^{(2)}\rangle \right) \\ & = i \left(|P_{l_0}^{(1)}, P_{l_0}^{(1)}\rangle + |P_{l_0}^{(2)}, P_{l_0}^{(2)}\rangle \right) \\ & - e^{-i2\phi} \left(|P_{-l_0}^{(1)}, P_{-l_0}^{(1)}\rangle - e^{-i2\phi} |P_{-l_0}^{(2)}, P_{-l_0}^{(2)}\rangle \right), \end{aligned} \quad (14)$$

and that of the third term of Eq. (11) is

$$\begin{aligned} |P_{l_0}^{(1)}, P_{-l_0}^{(2)}\rangle - |P_{-l_0}^{(1)}, P_{l_0}^{(2)}\rangle & \longrightarrow \left(|P_{l_0}^{(1)}\rangle + i|P_{l_0}^{(2)}\rangle, i|P_{-l_0}^{(1)}\rangle + |P_{-l_0}^{(2)}\rangle \right) \\ & - \left(|P_{-l_0}^{(1)}\rangle + i|P_{-l_0}^{(2)}\rangle, i|P_{l_0}^{(1)}\rangle + |P_{l_0}^{(2)}\rangle \right) \\ & = 2 \left(|P_{l_0}^{(1)}, P_{-l_0}^{(2)}\rangle - |P_{-l_0}^{(1)}, P_{l_0}^{(2)}\rangle \right), \end{aligned} \quad (15)$$

and the same for the fourth term of Eq. (11) transforms as

$$\begin{aligned} |P_{l_0}^{(1)}, P_{-l_0}^{(2)}\rangle + |P_{-l_0}^{(1)}, P_{l_0}^{(2)}\rangle & \longrightarrow \left(|P_{l_0}^{(1)}\rangle + i|P_{l_0}^{(2)}\rangle, i|P_{-l_0}^{(1)}\rangle + |P_{-l_0}^{(2)}\rangle \right) \\ & + \left(|P_{-l_0}^{(1)}\rangle + i|P_{-l_0}^{(2)}\rangle, i|P_{l_0}^{(1)}\rangle + |P_{l_0}^{(2)}\rangle \right) \\ & = 2i \left(|P_{l_0}^{(1)}, P_{-l_0}^{(1)}\rangle - |P_{l_0}^{(2)}, P_{-l_0}^{(2)}\rangle \right). \end{aligned} \quad (16)$$

The interaction time of atoms with cavity fields, acting as beam splitter, can be controlled by using velocity selector.

For the detection of direction of atomic momentum component we use four detectors, D₁, D₂, D₃ and D₄ [14]. The detectors are placed in the spatial paths of the atoms in different directions of propagation of atoms, which correspond to different momenta. A click in the detector corresponds to the presence of atom in that direction and hence with that particular momentum. Recently, detectors have been built which can efficiently detect fast moving Rydberg atoms [15]. A click in detector D₁ corresponds to the momentum direction $|p_{-l_0}^{(2)}\rangle$, a click in detector D₂ corresponds to the momentum direction $|p_{-l_0}^{(1)}\rangle$, a click in detector D₃ corresponds to the momentum direction $|p_{l_0}^{(2)}\rangle$, and a click in detector D₄ corresponds to momentum direction $|p_{l_0}^{(1)}\rangle$ as shown in Fig. 2. Combining Eqs. (13)–(16) with Eq. (11), the state of the cavities for different detector clicks is as given in Table 1. Here, from various combinations of clicks on detectors, we can distinguish between $|\psi^+\rangle$, $|\psi^-\rangle$, and $|\phi^+\rangle$ or $|\phi^-\rangle$. Hence after the detection of atoms we can tell that cavities are in the Bell state. It must be noted as with linear optics Bell state measurement, this process will only be able to distinguish between states $|\psi^+\rangle$, $|\psi^-\rangle$ and $\{|\phi^+\rangle, |\phi^-\rangle\}$. States $|\phi^+\rangle$ and $|\phi^-\rangle$ cannot be distinguished. Deterministic

Table 1

The entangled state of the two cavities corresponding to different clicks in the four detectors.

Cavities' State	Detectors' click
$ \phi^+\rangle = \frac{1}{\sqrt{2}}(00\rangle + 11\rangle)$	Two atoms in either D ₁ , D ₂ , D ₃ , or D ₄
$ \phi^-\rangle = \frac{1}{\sqrt{2}}(00\rangle - 11\rangle)$	Two atoms in either D ₁ , D ₂ , D ₃ , or D ₄
$ \psi^+\rangle = \frac{1}{\sqrt{2}}(10\rangle + 01\rangle)$	Coincidence between D ₁ and D ₄ or D ₂ and D ₃
$ \psi^-\rangle = \frac{1}{\sqrt{2}}(10\rangle - 01\rangle)$	Coincidence between D ₂ and D ₄ or D ₁ and D ₃

optical Bell measurement schemes rely either on non-linear interactions which are highly inefficient in practice [16], or using ancilla entangled photons [17] which require large interferometers to combine the signal and ancilla modes and give near deterministic Bell measurement with asymptotically large ancilla states. Recently single-mode squeezers together with beam splitters have been proposed to give up to 64.3% success probability [18]. The EPR state analogs of these near deterministic Bell measurements require further study.

4. Conclusion

We have proposed a scheme for entangling long distance cavities by entanglement swapping. For this purpose the external degrees of freedom of atomic momenta are first entangled with cavity fields. We then propose a method to perform Bell measurement on atomic momentum states which in turn swaps entanglement to cavity fields. The Bell measurement process involves additional cavity fields which act as a beam splitter for atomic momenta.

The scheme that we have proposed for cavities entanglement in Bell states possesses stronger non-locality. The microwave regime cavity QED have life time up to seconds and high fidelity can be achieved as proposed by Khosa et al. [19]. They consider the passage of 15–20 helium atoms under the first-order Bragg diffraction through a quantized cavity field. We perform quantum measurement on atomic momentum state of neutral atoms which are easy to handle and manipulate than a photonic flying qubit. The external atomic momentum states are more useful states against decoherence [20]. Our scheme is experimentally feasible as Bragg scattering of atoms in the optical regime has already been demonstrated by Rempe and his co-worker at $\lambda = 780$ nm for ^{85}Rb atoms [21].

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