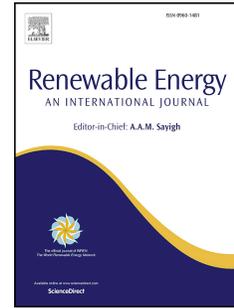


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Modelling tidal stream turbines in a three-dimensional wave-current fully coupled oceanographic model

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Abstract

A tidal turbine simulation system is developed based on a three-dimensional oceanographic numerical model. Both the current and turbulent controlling equations are modified to account for impact of tidal turbines on water velocity and turbulence generation and dissipation. High resolution mesh size at the turbine location is assigned in order to capture the details of hydrodynamics due to the turbine operation. The system is tested against comprehensive measurements in a water flume experiment and results of Computational Fluid Dynamics (CFD) simulations. The validation results suggest that the new modelling system is proven to be able to accurately simulate hydrodynamics with the presence of turbines. The developed turbine simulation system is then applied to a series of test cases in which a standalone turbine is deployed. Here, complete velocity profiles and mixing are

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realized that could not have been produced in a standard two-dimensional treatment. Of particular interest in these cases is an observed accelerated flow near the bed in the wake of the turbine, leading to enhanced bottom shear stress ($\sim 2N/m^2$ corresponding to the critical stress of a range of fine gravel and finer sediment particles).

Keywords: Tidal stream energy, Three-dimensional, Oceanographic model

1 Nomenclature

2 $\%_{RMSE}$ % Root Mean Square Error

3 κ The von Karman constant

4 ρ_0 The water density

5 τ_{bx} The bottom stress in the x direction

6 τ_{by} The bottom stress in the y direction

7 τ_{sx} The surface wind stress in the x direction

8 τ_{sy} The surface wind stress in the y direction

9 \tilde{W} The wall proximity function

10 ε The turbulent kinetic energy dissipation rate

11 \vec{V} The flow velocity vector

12 ζ The height of the free surface

13 B_1 A model coefficient $B_1 = 16.60$

14	C_d	The drag coefficient
15	C_{ext}	The energy extraction coefficient
16	C_l	The coefficient of term P_l
17	C_{td}	The coefficient of term P_{td}
18	C_{tp}	The coefficient of term P_{tp}
19	D	The diameter of the turbine
20	d	The total water column depth
21	E_1	A model coefficient $E_1 = 1.80$
22	E_2	A model coefficient $E_2 = 1.33$
23	f	The Coriolis parameter
24	F_l	The horizontal diffusion of the macroscale
25	F_q	The horizontal diffusion of the turbulent kinetic energy
26	F_u	The horizontal momentum term in the x direction
27	F_v	The horizontal momentum term in the y direction
28	H	The bottom depth
29	K_m	The vertical eddy viscosity coefficient
30	K_q	The vertical eddy diffusion coefficient of the turbulent kinetic energy
31	l	The macroscale

32	n	The number of records in the validation data
33	P_a	The air pressure at sea surface
34	P_b	The buoyancy production terms of turbulent kinetic energy
35	P_H	The hydrostatic pressure
36	P_s	The shear production terms of turbulent kinetic energy
37	P_l	The turbine-induced interference for the turbulence length-scale (l)
38	P_{td}	The turbine-induced turbulence dissipation term
39	P_{tp}	The turbine-induced turbulence generation term
40	q	The non-hydrostatic pressure
41	q^2	The turbulent kinetic energy
42	q_i	One record in the validation data
43	q_{iest}	One record in the calculated result
44	q_{max}	The maximum record in the calculated result
45	q_{min}	The minimum record in the calculated result
46	S_h	A stability function
47	S_m	A stability function
48	t	Time
49	u	The velocity component in the x direction

50	$u_{\tau b}$	The water friction velocity associated with the bottom
51	$u_{\tau s}$	The water friction velocity associated with the surface
52	v	The velocity component in the y direction
53	w	The velocity component in the z direction
54	x	The east axis in the Cartesian coordinate system
55	y	The north axis in the Cartesian coordinate system
56	z	The vertical axis in the Cartesian coordinate system
57	z_0	The bottom roughness parameter
58	z_{ab}	The reference height
59	CFD	Computational Fluid Dynamics
60	EMEC	European Marine Energy Centre
61	FVCOM	The Unstructured Grid Finite Volume Community Ocean Model
62	HATT	Horizontal Axis Tidal Turbine
63	ROMS	Regional Ocean Modelling System
64	TbM	Current-only FVCOM case with turbulence terms activated at the
65		turbine location (for model validation)
66	TbM15	Current-only FVCOM case with turbulence terms activated at the
67		turbine location (for impact identification)

68 TbO Current-only FVCOM case without turbulence terms (for model vali-
69 dation)

70 TbO15 Current-only FVCOM case without turbulence terms (for impact
71 identification)

72 TEC Tidal Energy Converter

73 TKE Turbulent Kinetic Energy

74 TSR Tip Speed Ratio

75 1. Introduction

76 As a response to the natural energy resource shortage and worldwide cli-
77 mate change, due in part to burning of fossil fuels to fulfil ever growing energy
78 requirements, clean and renewable alternatives have been gaining significant
79 attention. For example, the UK is aiming for 15% of the country's total en-
80 ergy production to be produced from renewable resources by 2020 [1]. In this
81 regard, tidal stream energy is considered to be a very promising avenue of
82 investigation due to its consistent predictability and availability. At the time
83 of writing, 119 Tidal Energy Converter (TEC) concepts, developed by differ-
84 ent companies, are listed on the European Marine Energy Centre (EMEC)'s
85 website¹; with full-scale tests of such devices currently underway in coastal
86 waters around the world.

87 However, despite the growing interest in tidal stream energy exploita-
88 tion, the analysis of the turbine-induced environmental impact has yet to be

¹<http://www.emec.org.uk/marine-energy/tidal-developers/>

89 a primary focus of any major on-site TEC project, leaving large gaps in our
90 understanding of the impacts of tidal stream energy devices. Alternatively,
91 prototype experiments and numerical models are widely used to investigate
92 such impacts. Prototype experiments often involve small scale laboratory
93 studies, for example, [2, 3, 4] used porous discs to simulate turbines in basic
94 experiments, and more recently, in an effort to reproduce turbulent effects in-
95 duced by real turbines, down-scaled dynamic turbine prototype models have
96 been considered [5, 6]. As a complement to practical laboratory prototype
97 experiments, Computational Fluid Dynamics (CFD) modelling is another
98 common way to study turbine behaviours. Similar to practical experiments,
99 earlier studies conducted using CFD software packages approximated tur-
100 bines as porous discs [7, 8, 9]. Works with realistic turbine geometry resolved
101 in the calculating mesh have been published very recently [10, 11, 12]. These
102 studies focus on how flow patterns are changed both upstream and down-
103 stream of the turbine in near-field scale, and in turn how these changes in
104 flow affect the behaviours of the turbine itself.

105 Numerical oceanographic models (e.g., Regional Ocean Modelling System
106 (ROMS) [13] and The Unstructured Grid Finite Volume Community Ocean
107 Model (FVCOM) [14]) have also been used to study the far-field hydrody-
108 namic changes caused by the operation of turbines and turbine arrays [15, 16].
109 (Here, the far-field refers to the area in which the pressure distribution may
110 be reasonably assumed linear). Such models must be modified in order to
111 simulate the effect of tidal stream turbines. Such modifications found in
112 the literature, overall, can be grouped into two different approaches: im-
113 plementing an additional bottom friction on the seabed and modifying the

114 flow motion with added turbine-induced forces. The first approach is of-
115 ten applied in two-dimensional studies [17, 18, 19]. However, it means the
116 drag of the devices is exerted on the seabed, rather than in the water col-
117 umn, leading to unrealistic predicted effects. The second approach, known
118 as ‘retarding force method’, as noted by [20], is generally more scientifically
119 rigorous in comparison with the ‘additional bottom friction’ method. Also,
120 the extension of this concept to three dimensions is more logically feasible.
121 Hence, the retarding force method is more widely applied in site-specific large
122 scale impact assessment studies [21, 22, 23, 24, 25, 26, 27]. Unfortunately,
123 these works largely relied on two-dimensional models, which is inconsistent
124 with the physical meanings of the turbine representation methods. The two-
125 dimensional models could also result in incomplete prediction of the vertical
126 flow structure downstream of the turbine and hence the mixing in the wake
127 [28, 29]. In contrast, the vertical flow structure and the mixing in the wake
128 of a turbine can be resolved in a three-dimensional model [26].

129 Another outstanding issue is that turbulent mixing downstream of the
130 turbine has yet to become a major focus in large scale modelling. However,
131 water flow within the near wake features a high turbulence level. Apart
132 from the background turbulence, turbines introduce additional turbulence:
133 flow accelerates and decelerates around blades, turbulent mixing occurs in
134 the wake and interacts with the free stream [3], and mechanical turbulence
135 results from the rotating motion of the turbine [30]. It is reported in CFD
136 simulation work that the original two-equation turbulence closure models
137 are not sufficient to account for the extra Turbulent Kinetic Energy (TKE)
138 production caused by turbines [30, 31]. In an effort to account for this within

139 ROMS, [15] modified the $k-\epsilon$ closure to simulate turbine-induced turbulence
140 generation, dissipation and interference for the turbulence length-scale.

141 The primary objective of the work documented in this paper was to de-
142 velop a Horizontal Axis Tidal Turbine (HATT) simulation system, that could
143 simulate, on a realistic spatial scale, the impact of tidal stream turbines on
144 flow speed and TKE in the far-field. This paper details the development
145 of such a simulation system within the aforementioned three-dimensional
146 oceanographic model —FVCOM. To represent the presence of the turbine
147 and its operation, the current module within FVCOM is modified based on
148 the ‘retarding force method’ and the turbulence module is modified based
149 on simulation terms proposed by [15] for turbine-induced turbulence genera-
150 tion, dissipation and interference for the turbulence length-scale. A thorough
151 validation study is also presented in which the developed model is tested,
152 utilizing a combination of real experimental data collected from a prototype
153 experiment conducted in the laboratory flume of [6], and CFD simulated
154 results.

155 The structure of the paper is provided as follows for clarity. Firstly in
156 Section 2 the FVCOM model is introduced and the integration of turbine
157 simulation within this framework is discussed. Next, Section 3 details the
158 validation study for the turbine which considers current and turbulence. Note
159 that as the experimental data available was considered insufficient for com-
160 prehensive validation, this section also details generation of further validation
161 data via CFD modelling (which itself was validated with the experimental
162 data). In Section 4, the new model system is then applied to test cases in
163 order to reveal impacts of a single turbine on the surroundings. Important

164 results from Sections 3 and 4 are highlighted in Section 5 in terms of impact
165 and potential future developments followed finally by concluding remarks in
166 Section 6.

167 **2. Modelling system**

168 *2.1. Three-dimensional FVCOM*

169 FVCOM was selected to model the impacts of tidal stream energy devices
170 on coastal regions. It is a three-dimensional, free surface, terrain-following
171 oceanographic model for solving shallow water equations numerically using
172 the finite-volume method [14]. There were three main considerations for
173 choosing FVCOM as the basic modelling tool in the present work:

- 174 1. The model system includes fully coupled three-dimensional wave-current-
175 sediment modules, which is critical for any realistic far-field modelling
176 at a coastal regional scale.
- 177 2. It enables the use of an unstructured triangular mesh for discretisation
178 of the computational domain, allowing for varied mesh resolution. Such
179 a treatment of spatial discretisation is particularly important in this
180 study as the mesh can be refined to particular high resolution around an
181 individual turbine site and maintain a smooth transition to a relatively
182 large mesh size far from the turbine so that the total computational
183 cost can be restricted.
- 184 3. It provides a three-dimensional turbulence model ‘MY-2.5’ which is
185 suitable for implementing the turbine effects at oceanographic scale
186 simulations.

187 For completeness, the basic theory surrounding FVCOM is given in the fol-
 188 lowing. More details of the model can be found in [32].

189 In Cartesian coordinates, the governing equations of FVCOM are:

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} - f v = -\frac{1}{\rho_0} \frac{\partial(P_H + P_a)}{\partial x} - \frac{1}{\rho_0} \frac{\partial q}{\partial x} + \frac{\partial}{\partial z} \left(K_m \frac{\partial u}{\partial z} \right) + F_u \quad (1)$$

$$\frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} + f u = -\frac{1}{\rho_0} \frac{\partial(P_H + P_a)}{\partial x} - \frac{1}{\rho_0} \frac{\partial q}{\partial y} + \frac{\partial}{\partial z} \left(K_m \frac{\partial v}{\partial z} \right) + F_v \quad (2)$$

$$\frac{\partial w}{\partial t} + u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} = -\frac{1}{\rho_0} \frac{\partial q}{\partial z} + \frac{\partial}{\partial z} \left(K_m \frac{\partial w}{\partial z} \right) \quad (3)$$

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \quad (4)$$

193 where t is the time, x , y , and z are the east, north, and vertical axes in the
 194 Cartesian coordinate system; u , v , and w are the three velocity components
 195 in the x , y , and z directions respectively; ρ_0 is water density; P_a is the
 196 air pressure at sea surface; P_H is the hydrostatic pressure; q is the non-
 197 hydrostatic pressure; f is the Coriolis parameter and K_m is the vertical eddy
 198 viscosity coefficient. F_u , F_v represent the additional horizontal momentum
 199 terms. In the present study, the turbine effects are represented through
 200 these two terms as specified in later section. The total water column depth
 201 is $d = H + \zeta$, where H is the bottom depth and ζ is the height of the free
 202 surface.

203 The surface and bottom boundary conditions for u , v , and w are:

$$K_m \left(\frac{\partial u}{\partial z}, \frac{\partial v}{\partial z} \right) = \frac{1}{\rho_0} (\tau_{sx}, \tau_{sy}), w = \frac{\partial \zeta}{\partial t} + u \frac{\partial \zeta}{\partial x} + v \frac{\partial \zeta}{\partial y} + \frac{E - P}{\rho}, \quad z = \zeta(x, y, t) \quad (5)$$

$$K_m \left(\frac{\partial u}{\partial z}, \frac{\partial v}{\partial z} \right) = \frac{1}{\rho_0} (\tau_{bx}, \tau_{by}), w = -u \frac{\partial H}{\partial x} - v \frac{\partial H}{\partial y}, \quad z = -H(x, y) \quad (6)$$

205 where (τ_{sx}, τ_{sy}) and $(\tau_{bx}, \tau_{by}) = C_d \sqrt{u^2 + v^2}(u, v)$ are the x and y components
 206 of surface wind and bottom stresses. The drag coefficient C_d is determined
 207 by matching a logarithmic bottom layer to the model at a height z_{ab} above
 208 the bottom:

$$C_d = \max \left(\frac{\kappa^2}{\ln^2 \left(\frac{z_{ab}}{z_0} \right)}, 0.0025 \right) \quad (7)$$

209 where $\kappa = 0.4$ is the von Karman constant and z_0 is the bottom roughness
 210 parameter.

211 The three-dimensional MY-2.5 turbulence module is based on the follow-
 212 ing controlling equations:

$$\frac{\partial q^2}{\partial t} + u \frac{\partial q^2}{\partial x} + v \frac{\partial q^2}{\partial y} + w \frac{\partial q^2}{\partial z} = 2(P_s + P_b - \varepsilon) + \frac{\partial}{\partial z} \left(K_q \frac{\partial q^2}{\partial z} \right) + F_q \quad (8)$$

$$\frac{\partial q^2 l}{\partial t} + u \frac{\partial q^2 l}{\partial x} + v \frac{\partial q^2 l}{\partial y} + w \frac{\partial q^2 l}{\partial z} = l E_1 (P_s + P_b - \frac{\tilde{W}}{E_1} \varepsilon) + \frac{\partial}{\partial z} \left(K_q \frac{\partial q^2 l}{\partial z} \right) + F_l \quad (9)$$

213
 214 where $q^2 = (u'^2 + v'^2)/2$ is the turbulent kinetic energy; l is the macroscale;
 215 K_q is the vertical eddy diffusion coefficient of the turbulent kinetic energy;
 216 F_q and F_l represent the horizontal diffusion of the turbulent kinetic energy
 217 and macroscale; $P_s = K_m(u_z^2 + v_z^2)$ and $P_b = (gK_h \rho_z)/\rho_0$ are the shear and
 218 buoyancy production terms of turbulent kinetic energy; $\varepsilon = q^3/B_1 l$ is the
 219 turbulent kinetic energy dissipation rate; $B_1 = 16.60$ is a model coefficient;
 220 $\tilde{W} = 1 + E_2 l^2 / (\kappa L)^2$ is a wall proximity function where $L^{-1} = (\zeta - z)^{-1} +$
 221 $(H + z)^{-1}$; $E_1 = 1.80$ and $E_2 = 1.33$ are model coefficients. F_q and F_l are
 222 parameterized using the Smagorinsky eddy parameterization method [33]. A
 223 constant value can also be assigned to the horizontal diffusion coefficient in
 224 FVCOM, which means the turbulence closure model can be run with both
 225 F_q and F_l set to zero.

226 The turbulent kinetic energy and macroscale equations are closed by
 227 defining:

$$K_m = lqS_m, \quad K_h = lqS_h, \quad K_q = 0.2lq \quad (10)$$

228 where S_m and S_h are stability functions, calculation of which can be found
 229 in [32].

230 The surface and bottom boundary conditions for the turbulent kinetic
 231 energy and macroscale equations are:

$$q^2 l = 0, \quad q^2 = B_1^{\frac{2}{3}} u_{\tau s}^2, \quad z = \zeta(x, y, t) \quad (11)$$

$$q^2 l = 0, \quad q^2 = B_1^{\frac{2}{3}} u_{\tau b}^2, \quad z = -H(x, y) \quad (12)$$

233 where $u_{\tau s}$ and $u_{\tau b}$ are the water friction velocities associated with the sur-
 234 face and bottom. Since $q^2 \neq 0$ at the surface and bottom, $l = 0$ at both
 235 boundaries, which means K_m , K_h and K_q are always 0 at the surface and
 236 bottom.

237 2.2. Representation of HATT in FVCOM

238 The original FVCOM is designed for ocean circulation in coupling with
 239 surface wave propagation at a regional scale. There is no direct tool avail-
 240 able within the package to simulate tidal stream turbines. Therefore new
 241 features must be added into the model system to represent the turbine and
 242 its operation; these include changes to the current and turbulence modules.

243 2.2.1. Modelling HATT in current model

244 It is widely recognised that the deceleration of the passing flow, largely
 245 due to energy loss around the turbine as well as the blockage effect of the
 246 device, is the major impact of a turbine on its ambient current. In this work,

247 the energy extraction process is modelled based on the additional sink term
 248 put forward by [21] as:

$$F_u = -C_{ext} \cdot \frac{1}{2} \cdot \rho_0 \cdot u \cdot |\vec{V}| \quad (13)$$

249

$$F_v = -C_{ext} \cdot \frac{1}{2} \cdot \rho_0 \cdot v \cdot |\vec{V}| \quad (14)$$

250 where F_u and F_v are the additional sink term components per unit area; C_{ext}
 251 is the energy extraction coefficient which determines the strength of the sink
 252 term; \vec{V} is the flow velocity vector and $|\vec{V}|$ is the magnitude of the velocity
 253 in a cell.

254 These two terms are added onto the right hand side of the horizontal
 255 momentum equations of FVCOM (Equation 1 & 2) respectively. It should
 256 be noted that the purpose of these modifications are not to simulate detailed
 257 hydrodynamics immediately around each individual turbine blade, but to
 258 represent the modified flow field at 4D to 6D away from the turbine further
 259 downstream. The complex flow-turbine interactions in the immediate wake
 260 of the turbine violate the basic assumption in oceanographic models like
 261 FVCOM, i.e. the pressure distribution across water depth is linear, resulting
 262 in the exclusion of non-hydrostatic pressure terms. This particular difficulty
 263 means that the predictions from FVCOM are invalid in close proximity to the
 264 turbine. Although the distance at which the pressure distribution becomes
 265 linear will be dependent on the background turbulence level and configuration
 266 of the turbine, it has been observed by [3] to generally lie between 4D and
 267 6D from the turbine disk. Therefore, the aim of the proposed modifications
 268 in the above-mentioned equations is to introduce accurate turbine effects to
 269 the passing flow beyond 4D-6D downstream of the device.

270 In addition, the present study identifies each individual turbine structure
271 within a farm, rather than treating the entire turbine farm as a whole as in
272 many previous studies [21, 22, 24, 25]. In this way, the effects from each device
273 can be identified. It is therefore proposed that the unstructured mesh is used
274 with particularly fine resolution at each turbine device site. In the present
275 study, mesh size close to the turbine is strictly assigned as the diameter of the
276 device. To represent a turbine, an element of the model mesh is selected to
277 exert the energy extraction coefficient (C_{ext}) set along the water depth. C_{ext}
278 of each sigma layer is treated individually in this research. Figure 1 illustrates
279 the turbine position in the x-y plane on the mesh, and Figure 2 illustrates the
280 three-dimensional application of the C_{ext} set. Layers between the two dotted
281 lines are intercepted by the turbine. These layers are controlled by assigning
282 C_{ext} values. Layers do not directly interact with the turbine are called ‘free
283 layers’. C_{ext} of these layers are 0. Such an approach is very different from
284 previously mentioned two-dimensional studies [21, 22, 23, 24, 25, 26, 27] and
285 a three-dimensional study [16] in which a single value was assigned to one of
286 the layers, both of which failed to distinguish the velocity difference among
287 various depths due to the turbine presence.

288 It should be noted that FVCOM is a mode-split model which calculates
289 the velocity in both the two-dimensional external and three-dimensional in-
290 ternal modes. To ensure the consistency of the two modes, an adjustment is
291 made in every internal time step to the three-dimensional internal mode, ac-
292 cording to the results of the two-dimensional mode. Therefore, the sink term
293 is also added into the two-dimensional external mode. The corresponding
294 depth averaged C_{ext} is used in the two-dimensional mode. The effective ve-

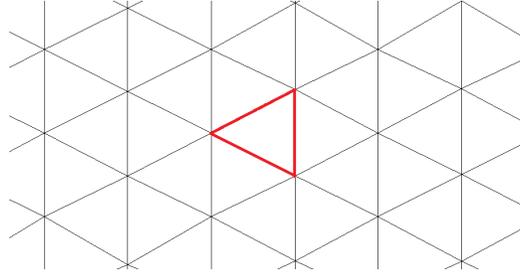


Figure 1: Illustration of the turbine position in the x-y plane on the mesh. The red triangle indicates the mesh element in which the energy extraction coefficient set is exerted.

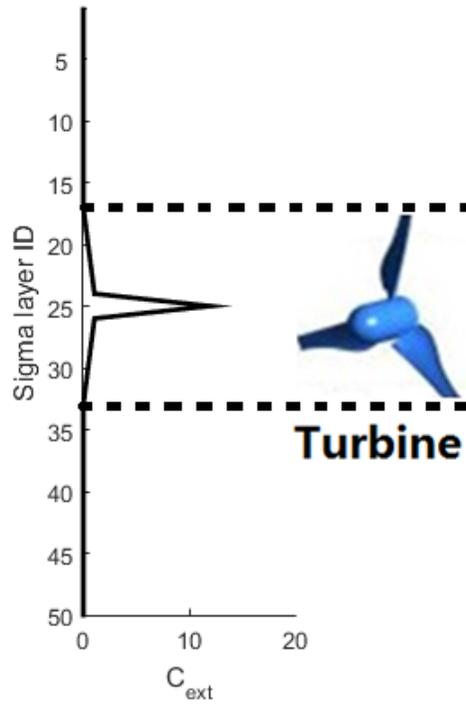


Figure 2: Illustration of three-dimensional application of C_{ext} (see Equation 21)

295 locity terms that account for the angle between the hub of the turbine and the
 296 flow direction proposed by [22] are not adopted in this research. Therefore,
 297 it is assumed that the turbine may yaw, allowing the rotor face to remain
 298 perpendicular to the incoming flow. Although this simplification is not rep-
 299 resentative of tidal turbines in general, efforts to introduce yaw controls that
 300 maximize effective rotor area are under-way e.g. [34]. Tidal turbines usually
 301 have an operational velocity window below which no power is generated and
 302 above which the power output is thresholded to the rated power output. The
 303 parameterization of this power limitation is discussed in detail in [23]. How-
 304 ever, as the operating window is often application-specific, i.e., dependent on
 305 the type of turbine, and the present study focuses on generic representation
 306 of turbines in an oceanographic model system, the limit on power output is
 307 not accounted for.

308 2.2.2. Modelling HATT in turbulence model

309 The three turbine-incurred turbulence perturbations identified in [15] are
 310 usually not accounted for in standard turbulence closures. In the present
 311 study however, each of the perturbations are represented following the terms
 312 proposed by [15] as follows:

- 313 • Turbine-induced turbulence generation, P_{tp}

$$P_{tp} = C_{tp} \cdot \frac{u^3}{\Delta x} \quad (15)$$

- 314 • Turbine-induced turbulence dissipation, P_{td}

$$P_{td} = C_{td} \cdot \frac{u \cdot k}{\Delta x} \quad (16)$$

- 315 • That of an interference for the turbulence length-scale (l), P_l

$$P_l = C_l \cdot P_s \quad (17)$$

316 C_{tp} , C_{td} and C_l in the aforementioned equations are coefficients decided
 317 empirically through parameter studies. The above mentioned terms are ac-
 318 tivated only at turbine locations.

319 With these three terms, Equations 8 and 9 become

$$\frac{\partial q^2}{\partial t} + u \frac{\partial q^2}{\partial x} + v \frac{\partial q^2}{\partial y} + w \frac{\partial q^2}{\partial z} = 2(P_s + P_b + P_{tp} - P_{td} - \varepsilon) + \frac{\partial}{\partial z} (K_q \frac{\partial q^2}{\partial z}) + F_q \quad (18)$$

320

$$\frac{\partial q^2 l}{\partial t} + u \frac{\partial q^2 l}{\partial x} + v \frac{\partial q^2 l}{\partial y} + w \frac{\partial q^2 l}{\partial z} = l(E_1(P_s + P_b) - P_l - \frac{\tilde{W}}{E_1} \varepsilon) + \frac{\partial}{\partial z} (K_q \frac{\partial q^2 l}{\partial z}) + F_l \quad (19)$$

321 3. Model validation

322 3.1. Extending the available experimental data with a CFD model

323 Measurements from a laboratory experiment were available for the pur-
 324 pose of model validation. This experiment took place at the University of
 325 Hull using their ‘Environment Simulator Laboratory Flume’ [6]. The flume
 326 is 11 m in length, 1.6 m wide and 0.8 m deep (the water depth was 0.6 m).
 327 The inlet flow rate was 0.5 m/s. The diameter of the horizontal axis rotor
 328 used in this experiment was 200 mm and its hub was located 300 mm above
 329 the bed. The rotor was connected to a thick cylinder which was a part of the
 330 housing structure and the cylinder extended to about 1D downstream of the
 331 rotor. Tip speed ratio (TSR) of the rotor was 5.5. Measurements of velocity
 332 and TKE were taken along the centreline from 1D to 5D downstream of the
 333 rotor.

334 Although the experimental measurements cover a wide range of data that
335 can be used for the present model validation purpose, they have apparent
336 limitations. For example, the measured data only accounts for the distance
337 down stream of the turbine up to 5D, which is not sufficient to reveal any
338 effects beyond the point at which FVCOM is assumed valid. Therefore, to
339 complement the experimental data, a CFD model based on ANSYS FLUENT
340 (Version 14.5) is built to simulate the experimental conditions. The CFD
341 model was first validated against the experimental measurements, then used
342 to generate additional data for the FVCOM model validation.

343 FLUENT solves the three-dimensional Reynolds-Averaged Navier-Stokes
344 (RANS) equations. Turbulence of the present research are calculated based
345 on the Shear Stress Transport (SST) $k - \omega$ model, following the conclusion
346 of [35, 36]. The Virtual Blade Model (VBM) is adopted in this research to
347 simulate HATTs in FLUENT [37]. Essential configurations of VBM, i.e. ge-
348 ometrical setup and running parameters of the rotor, are specified according
349 to [37].

350 3.2. CFD model validation

351 Figure 3 shows a comparison of computed streamwise flow velocity against
352 the measured experimental data. It can be seen that the velocity at the hub
353 height 1D downstream of the rotor is 0m/s which agrees with the observation
354 in the laboratory, due to the supporting shaft. The velocity profiles at the
355 other locations also match well with the laboratory data with root mean
356 square error percentage ($\%_{RMSE}$) of 14.3 at 3D, 18.4 at 4D and 20.8 at 5D
357 (These values are also presented in Table 1). The $\%_{RMSE}$ is calculated based
358 on Equation 20 for each location. However, the model predicted velocity

Table 1: $\%_{RMSE}$ for the CFD case against the experimental data

Velocity				TKE			
1D	3D	4D	5D	1D	3D	4D	5D
5.7	14.3	18.4	20.8	12.8	13.9	15.8	17.3

359 below the rotor is consistently slightly slower than the measured data. This is
 360 likely due to a combination of under-estimated bed friction and far proximity
 361 from the bed.

$$\%_{RMSE} = \frac{\sqrt{\frac{1}{n} \sum_{i=1}^n (q_i - q_{iest})^2}}{q_{max} - q_{min}} \times 100 \quad (20)$$

362 where n is the number of records in the validation data; q_i is the validation
 363 data; q_{iest} is the calculated result; q_{max} and q_{min} are the maximum and
 364 minimum records in the calculated result respectively.

365 The computed TKE results are compared with the measured data in
 366 Figure 4. At 1D downstream of the rotor, the modelled data follows the
 367 measurements very well, including the maximum and minimum values of
 368 TKE around the rotor position. Further downstream at 3D, 4D and 5D,
 369 the model predicted TKE profile shapes agree with those measured in the
 370 laboratory ($\%_{RMSE}$ refer to Table 1), i.e. the model is able to reproduce
 371 the enhanced turbulence at the rotor intercepted levels. The values at these
 372 levels, however, tend to be under-estimated by 15-20%. This is likely due to
 373 the CFD model not accounting for turbulence generated at the tip of rotor
 374 blades when in motion. Similar findings are reported in [31].

375 Overall, the agreement between FLUENT based CFD model results and

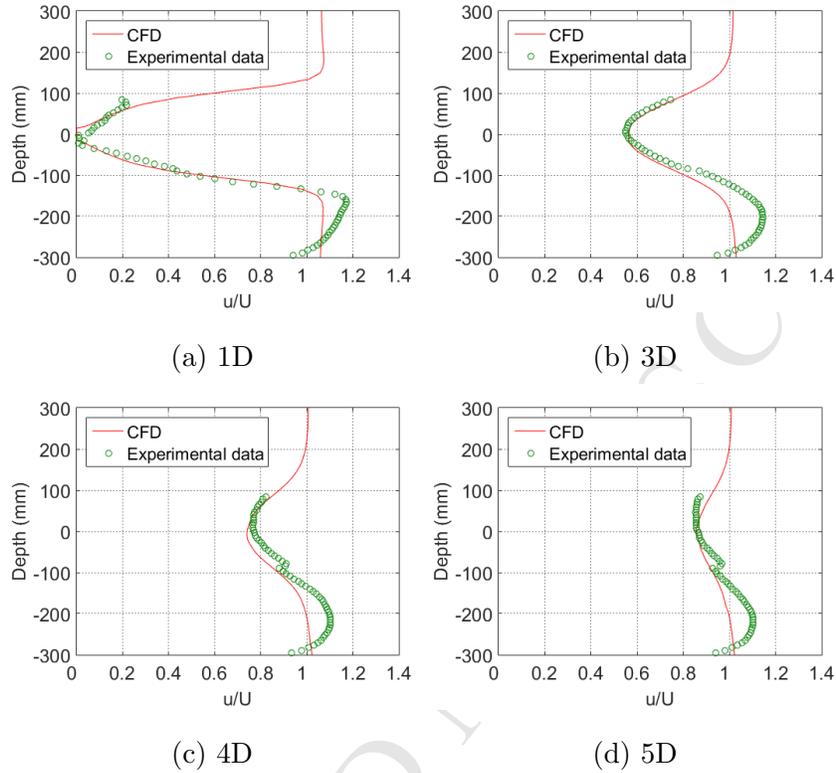


Figure 3: Normalized velocity profiles of the CFD case against those measured in the laboratory at 1D, 3D, 4D and 5D downstream of the rotor

376 measured data are considered to be satisfactory at all sites. The CFD pre-
 377 dicted results within the rotor intersected region from 5D downstream can
 378 be used with confidence for FVCOM model validation.

379 3.3. Validation of the FVCOM model

380 With the validated CFD model available to complement the experimental
 381 data, it was possible to perform a thorough validation of the turbine sim-
 382 ulation method developed within FVCOM. In the following, a number of
 383 validation tests are documented in which the FVCOM model is compared

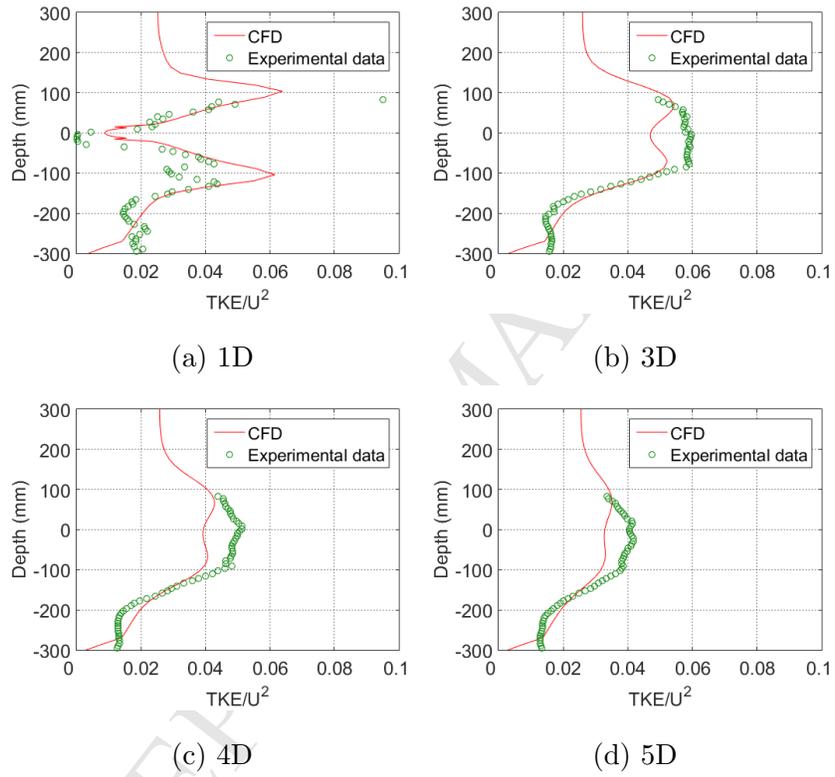


Figure 4: Normalized TKE profiles of the CFD case against those measured in the laboratory at 1D, 3D, 4D and 5D downstream of the rotor

384 with the CFD model and where available, the original experimental data.

385 The FVCOM based model was firstly set up according to the experimental
386 conditions mentioned above. The spatial resolution of the mesh is uniform
387 in both stream-wise and cross-stream directions with a mesh size of 0.2 m
388 (1D). Vertically, the water column is evenly divided into 50 sigma layers,
389 this was found to provide a good trade-off between vertical resolution and
390 simulation efficiency, i.e. it allows the evolving shapes of the velocity and
391 TKE profiles over the water depth to be well captured without making the
392 model computationally prohibitive. A uniform flow speed is achieved through
393 maintaining a constant water level difference between the two ends of the
394 channel.

395 As stated in Section 2, the turbine is represented by assigning C_{ext} values
396 individually to the sigma layers. In this case, 17 out of 50 sigma layers are
397 occupied by the turbine. The values of C_{ext} were decided through a process of
398 iterative curve-fitting tests. Hence, the validation results presented represent
399 the identified minimum $\%_{RMSE}$ of these tests. The proposed approach was
400 to have a vertically symmetrical linear increase over the layers occupied by
401 the turbine, and a single dominating coefficient in the centre (see Equation
402 21). This C_{ext} profile shape was determined empirically to produce velocity
403 profiles that fitted well with the validation data. However, this definition of
404 the C_{ext} profile shape may not be suitable in other applications and hence it
405 is noted here that a wider study of possible profile shapes in general would
406 be an interesting avenue for future research.

Table 2: C_{ext} profile parameters and values of C_{tp} , C_{td} and C_l

$C_{ext_{\max A}}$	$C_{ext_{\max B}}$	σ_{\min}	σ_{centre}	C_{tp}	C_{td}	C_l
12	1.2	17	25	0.08	0.1	2.8

$$C_{ext} = \begin{cases} m_1\sigma + c_1, & \sigma_{\text{centre}} > \sigma \geq \sigma_{\min} \\ m_2\sigma + c_2, & \sigma_{\max} > \sigma \geq \sigma_{\text{centre}} \\ C_{ext_{\max A}}, & \sigma = \sigma_{\text{centre}} \\ 0, & \text{otherwise} \end{cases} \quad (21)$$

407 where $m_1 = C_{ext_{\max B}}/(\sigma_{\text{centre}} - \sigma_{\min})$, $m_2 = -m_1$, $c_1 = -m_1\sigma_{\min}$, $c_2 =$
408 $m_1\sigma_{\max}$, and $\sigma_{\max} = 2\sigma_{\text{centre}} - \sigma_{\min}$. $C_{ext_{\max A}}$ is the dominant central coeffi-
409 cient, $C_{ext_{\max B}}$ is the height of the C_{ext} profile not considering $C_{ext_{\max A}}$ and
410 $\sigma_{\min} < \sigma < \sigma_{\max}$ is the domain covered by the rotor. The C_{ext} profile used
411 in the current study is shown in Figure 2. For completeness, the parameters
412 introduced in Equation 21 used in this study are given in Table 2 along with
413 coefficients to simulate impact of the turbine on the turbulence, C_{tp} , C_{td} and
414 C_l ; again, these are determined empirically based on the validation data.
415 Finally, note that the depth-averaged value C_{ext} is 0.408.

416 To validate the FVCOM model, two cases are run for velocity and TKE
417 validation: with and without the additional turbulence terms activated at
418 the turbine location. These two cases are hereafter named TbM (with the
419 terms) and TbO (without the terms).

420 Comparison of velocity profiles at 5D, 7D, 9D and 11D downstream of
421 the turbine are shown in Figure 5 (for $\%_{RMSE}$ of these results refer to Table
422 3). This range is chosen due to the fact that up to 5D the model is highly

Table 3: $\%_{RMSE}$ for the four FVCOM cases

Cases	Velocity				TKE			
	5D	7D	9D	11D	5D	7D	9D	11D
TbM	20.4	13.3	16.7	23.4	16.3	28.0	25.1	15.3
TbO	26.9	22.1	12.9	22.1	41.3	22.1	21.7	29.6

Errors at 5D are given against the experimental data; and against CFD results otherwise

423 likely to be invalid due to previously mentioned limitations of FVCOM, and
 424 beyond 11D there is little variation in the velocity profile. Within the turbine
 425 swept area, velocity profiles of both TbM and TbO show a satisfactory agree-
 426 ment with the experimental measurements at 5D. Slight under-prediction is
 427 observed in the near bed boundary layer, which is attributed to the under-
 428 predicted bed friction. Further downstream, there is significant overall agree-
 429 ment between the FVCOM and CFD predicted velocities, especially beyond
 430 7D downstream of the turbine. Hence, the new model system is capable of
 431 predicting the far-wake of the turbine correctly in terms of velocity, given ap-
 432 propriate C_{ext} values assigned. Beyond 9D downstream, both FVCOM and
 433 CFD model results show near uniform distributions of the velocity across
 434 the depth, indicating that the flow is less affected by both bottom and upper
 435 boundaries as well as the turbine operations in the far-wake.

436 Comparison of TKE profiles at 5D, 7D, 9D and 11D downstream of the
 437 turbine are shown in Figure 6, again, for $\%_{RMSE}$ of these results refer to
 438 Table 3. In Figure 6 (a) case TbM predicted TKE matches better with the
 439 experimental data than the CFD model. This is due to the tendency of

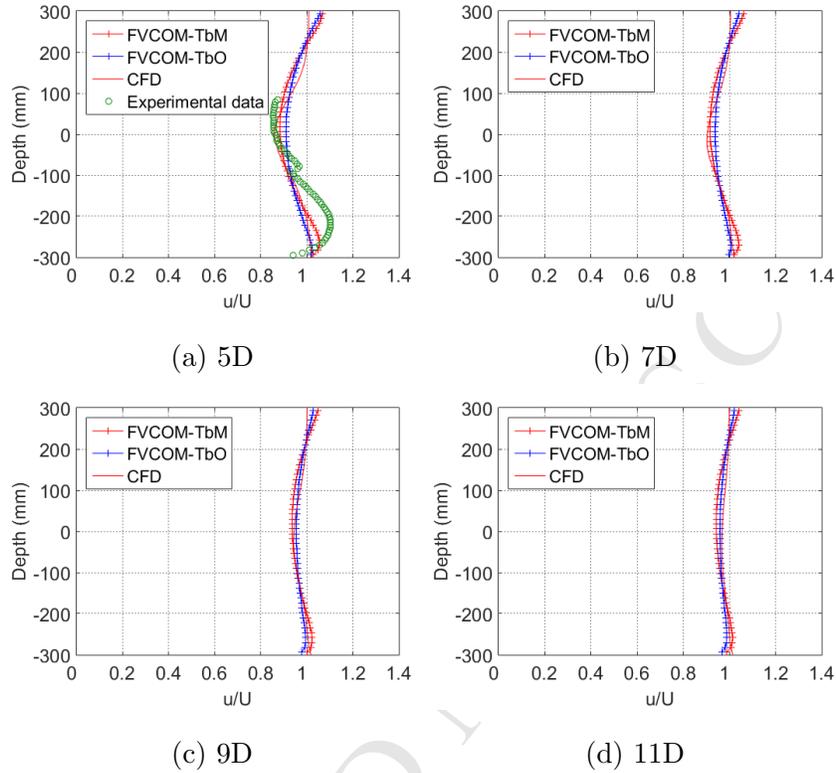


Figure 5: Normalized velocity profiles of two FVCOM cases (with and without turbulence modification terms) against those predicted by the CFD case and measured in the laboratory at 5D, 7D, 9D and 11D downstream of the rotor

440 the CFD result underestimate TKE levels as identified in Section 2. For
 441 this reason, it is assumed that at locations 7D and 9D where experimental
 442 data were not available, although case TbO more closely matches the CFD
 443 results, case TbM presents a more likely reflection of reality. Further, the
 444 differences in the computed TKE level between cases TbM and TbO become
 445 less significant as the wake recovers further downstream.

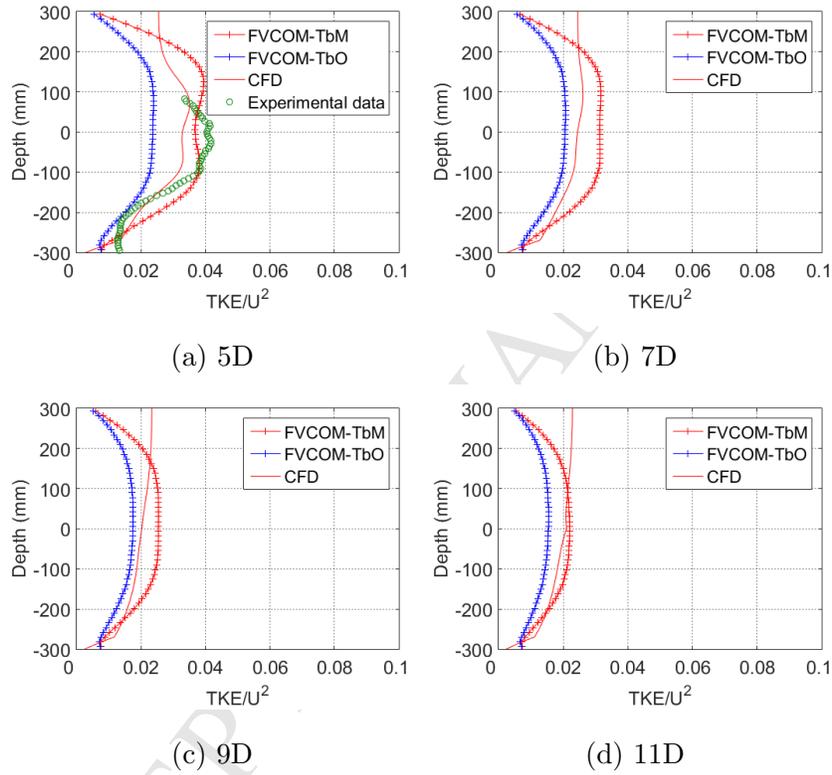


Figure 6: Normalized TKE profiles of two FVCOM cases, TbM and TbO, against those predicted by the CFD case and measured in the laboratory at 5D, 7D, 9D and 11D downstream of the rotor

446 4. Application —Influence of turbulence closure terms

447 A series of tests are carried out in FVCOM to reveal impacts of a single
448 turbine on the surroundings using a prototype 15 m diameter turbine model
449 as the test bed. Water depth of these cases is 45 m and the turbine hub is
450 located at a depth of 22.5 m. The flow conditions are set to reflect those of
451 the Anglesey coast, North Wales, UK. This site is of particular interest for
452 potential introduction of tidal turbine farms [38]. A water velocity of 1.0 m/s
453 is defined, given by a time-average over one full tide cycle at the location [39].
454 These tests are conducted with and without the turbine implementations, i.e.
455 the coefficients represent turbine effects being switched on and off, in order
456 to reveal the differences between the baseline case (no turbine) and cases
457 with turbine effects. Particular attention is given to the effects of enhanced
458 turbulence.

459 Free-surface elevation, normalized depth-averaged velocity, water flow ve-
460 locity in the bottom boundary layer and bed shear stress along the centreline
461 are calculated under different scenarios: TbM15 (with turbulence terms),
462 TbO15 (without turbulence terms) and undisturbed flow. These are shown
463 in Figure 7.

464 In Figure 7, the turbine is placed at 0D and the horizontal axis shows
465 distance in terms of turbine diameters ($1D = 15$ m). It can be seen that water
466 level upstream of the turbine is higher than the undisturbed flow in both
467 TbM15 and TbO15 (Figure 7 (A)), accompanied by a substantial ($\sim 20\%$)
468 drop of water velocity (Figure 7 (B)). The passing flow is slowed down due
469 to energy loss. The decelerated water accumulates in front of the turbine,
470 causing the water level rise upstream of the turbine. Free-surface elevation

471 drop is observed at the turbine location. The water level keeps dropping
472 until 1D downstream of the turbine. These behaviours are consistent with
473 measurements from a previously published laboratory experiment [7].

474 It is observed that only a very slight difference is caused by the turbulence
475 closure terms to the calculated free surface elevation and depth-averaged ve-
476 locity ($< 0.1\%$ mean square difference between TbM15 and TbO15 in Figure
477 7 (A) & (B)). Also, both free surface elevation and depth-averaged velocity re-
478 cover over a relatively short distance. Specifically, the depth-averaged veloc-
479 ity recovered to 96% of its original value within 2D downstream of the turbine
480 for both TbM15 and TbO15 before recovery begins to stagnate. The recovery
481 of surface water elevation also goes into stagnancy beyond 3D downstream
482 the turbine. The water elevation is still slightly ($\sim 1\%$) below its undisturbed
483 value at 25D downstream of the turbine. Similarly, depth-averaged velocity
484 does not completely recover within a distance of 25D. Similar non-localized
485 far-field impact is also reported in [40].

486 Changes incurred by the enhanced turbulent mixing (TbM15) to the flow
487 velocity in the boundary layer and the bed shear stress, however, are obvious
488 (Figure 7 (C) & (D)). When compared to the undisturbed flow, the presence
489 of the turbine increases the water velocity in the bottom layer, regardless
490 of the turbulence calculation scheme. However, the increase is $\sim 8\%$ larger
491 when the turbulence terms are activated (TbM15). Flow velocity and bed
492 shear stress reach their maximum at roughly 1D downstream of the turbine.
493 The downstream influential range of the turbine is beyond 25D for bottom
494 layer water velocity and bottom shear stress in both TbM15 and TbO15.
495 Further, it is important to note that a $2 N/m^2$ increase in bottom shear stress

496 beyond the undisturbed flow level can be seen in Figure 7 (D) for TbM15,
497 which exceeds the critical shear stress of medium sand, coarse sand and a
498 range of fine gravel, as defined in [41]. This is mainly due to the accelerated
499 flow near the bottom in the turbine wake. Increased bottom shear stress
500 is also reported in laboratory work [42, 6] as well as CFD simulations [37].
501 This is contrary to reduced bottom shear stress observations in previous
502 two-dimensional studies [25, 26], in which the bottom shear stress is derived
503 from reduced depth-averaged velocity. The bottom layer water velocity and
504 bottom shear stress difference caused by the turbulence calculation scheme
505 starts to become negligible beyond 10D downstream of the turbine.

506 **5. Discussion and research outlook**

507 This study has highlighted the need of additional terms in the momen-
508 tum equations and the turbulence closure (MY-2.5) of the three-dimensional
509 FVCOM to simulate accurate hydrodynamics in the wake of turbines. The
510 results demonstrate that an augmented FVCOM can produce satisfactory
511 velocity and TKE profiles in the wake of a turbine (refer to Table 3 for com-
512 parison results of computed and measured profiles). However, one should
513 note that in the current state of the proposed method, simulated wake still
514 lacks rotational motion, which may result in inaccurate suspended sediment
515 distribution.

516 Another important finding in this research is the increased bed shear
517 stress predicted by the three-dimensional FVCOM, which agrees with re-
518 sults reported in physical experiment studies [6, 42]. This is a result of the
519 flow acceleration near the bed being identified by a three-dimensional model.

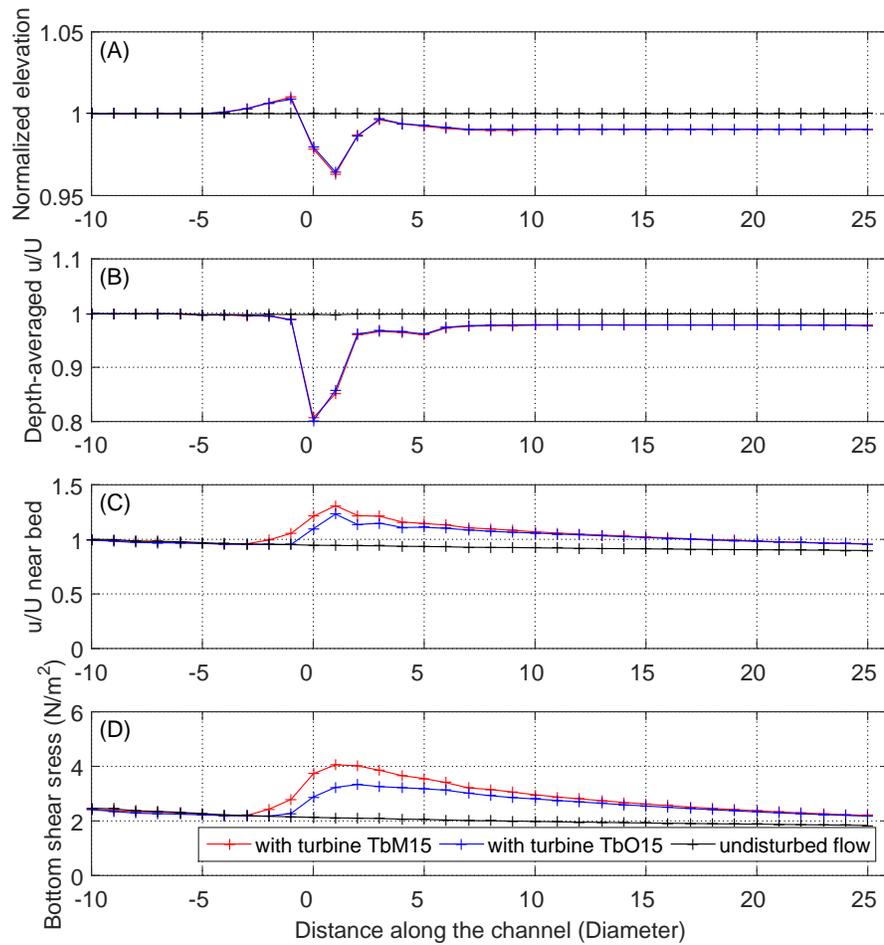


Figure 7: (A) Normalized free-surface elevation (B) Normalized depth-averaged velocity (C) Normalized water velocity in the bottom layer and (D) Bottom shear stress along the centreline calculated under different scenarios: TbM15 - Retarding force + turbulence terms, TbO15 - Retarding force and undisturbed flow . (The turbine is positioned at 0D)

520 This lies in contrast to a generally reduced flow in the wake predicted by a
521 depth-averaged two-dimensional model, which commonly leads to bed stress
522 weakening in the wake [25, 26]. A precise prediction of bed shear stress is of
523 particular importance, as it largely decides the sediment morphology [41].

524 Furthermore, it is noted that there is currently a gap in the literature on
525 the implementation of effects of turbines on waves in large scale numerical
526 modelling. However, small scale CFD simulations carried out by [37] showed
527 that the wave height was reduced by roughly 17% and the wave length was
528 increased by 19% due to the presence of a turbine rotor ($D=0.5$ m) with its
529 hub located 0.39 m away from the free surface. Therefore, effects of turbines
530 on surface waves are recommended as an important and interesting avenue
531 of investigation in future large scale numerical modelling studies in order to
532 obtain a more complete simulation of tidal turbines. An introduction to this
533 topic, presented by one of the authors can be found in [39].

534 6. Conclusions

535 In this study, a numerical model based on FVCOM for simulating far-field
536 impacts of tidal turbines has been developed according to understandings
537 obtained from laboratory measurements [6] and small scale CFD simulations.
538 Apart from the widely acknowledged flow deceleration in the wake, TKE level
539 in the wake was found to be increased due to the presence of turbines. Under-
540 estimated TKE level predicted by small scale CFD and large scale FVCOM
541 simulations without turbulence terms (case TbO) demonstrated the need of
542 further treatment to the turbulence closures.

543 In more detail, to simulate the impact identified above in FVCOM, a body

544 force was employed in the current module to account for the turbine-induced
545 water deceleration. Three terms were added into the three-dimensional MY-
546 2.5 turbulence closure to model turbine-related turbulence generation, dissi-
547 pation and turbulence length-scale interference.

548 An idealized water channel was built to test the reliability of the developed
549 turbine simulation system. The mesh resolution at the turbine location was
550 set to the diameter of the prototype turbine used in the experiment so that
551 turbines could be simulated individually. The validation results indicate
552 that the three-dimensional retarding force method was able to address water
553 velocity reduction effectively and correctly. The turbulence terms were shown
554 to be necessary for accurate turbulent mixing prediction; without them being
555 activated at the turbine location, under-prediction of TKE level behind the
556 turbine was observed.

557 The standalone turbine tests demonstrated behaviours similar to those
558 observed in a laboratory experiment [7] in terms of free surface elevation
559 and depth-averaged velocity. The additional turbulence terms have little
560 effect on the calculation of these two variables. An encouraging finding is
561 that the enhanced bottom shear stress results were qualitatively consistent
562 with laboratory observations. In reality, the increase in bottom shear stress
563 is likely to be caused by the accelerated flow near the bottom as well as
564 intensified mixing in the wake due to the turbine rotor in motion. These
565 two processes could be simulated accurately in the present study due to the
566 three-dimensional modelling system used.

567 To finalize, in this paper a numerical tool for impact assessment of large
568 scale tidal turbine farms is presented. The turbine simulating platform is

569 developed based on a three-dimensional large scale modelling system. When
570 considering potential future work in the area of three-dimensional sediment
571 transport modelling, the herein proposed treatment of flow velocity and tur-
572 bulence level leading to accurate prediction of vertical flow structure and
573 mixing in the wake of tidal turbines is of particular importance.

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- A three dimensional turbine simulation platform is built based on a three-dimensional wave-current-sediment fully coupled oceanographic model.
- Accurate simulation of velocity structure and turbulent mixing in the wake is obtained.
- Enhanced bottom shear stress due to the turbine is obtained.

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