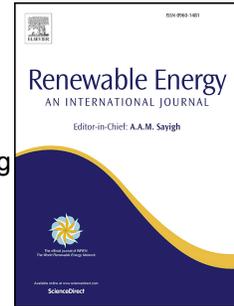


# Accepted Manuscript

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# Wind power characteristics of seven data collection sites in Jubail, Saudi Arabia using Weibull parameters

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## Abstract:

The wind characteristics of seven locations in Jubail, Saudi Arabia were analysed by using five years of wind data of six sites and three years data of one site at 10 m above ground level (AGL). The highest annual mean wind speed of 4.52 m/s was observed at Industrial area (east) and lowest of 2.52 m/s at Pearl beach with standard deviations of 2.52 and 1.1 m/s respectively. Weibull parameters were estimated using maximum likelihood, least-squares regression method (LSRM) and WASP algorithm. The most probable and maximum energy carrying wind speed were found by all the three methods. The correlation coefficient ( $R^2$ ), root mean square error (RMSE), mean bias error (MBE) and mean bias absolute error (MAE) showed that all three methods represent wind data at all sites accurately. However, the maximum likelihood method is slightly better than LSRM followed by WASP algorithm. The wind power output at all seven sites from five commercially available wind machines of rated power from 1.8 - 3.3 MW showed that Jubail industrial area (east) is most promising. The energy output from a 3 MW wind machine at this site was found to be 11,136 MWh/yr. with a plant capacity factor (PCF) of 41.3%.

36 *Keywords:* Wind power; Weibull parameters; maximum energy carrying wind speed;  
 37 most probable wind speed; plant capacity factor.

### 38 **Nomenclature**

39	$c$	scale parameter of Weibull distribution, m/s
40	$F(v)$	cumulative distribution function
41	$k$	shape parameter of Weibull distribution, dimensionless
42	$P(v)$	frequency of incidence of wind speed, $v$
43	$y_i$	frequency of actual observation
44	$x_i$	frequency of Weibull
45	$z_i$	mean wind speed, m/s
46	$\rho$	air density within the time step, kg/m <sup>3</sup>

### 48 **1. Introduction**

49 The term green energy is used for those sources of energy which do not produce any of  
 50 the harmful greenhouse gases. Further, the cleanest sources of energy are those which  
 51 utilise the natural flows of the earth. These sources are known as renewable sources of  
 52 energy and they will never die out unlike fixed reserves of fossil and nuclear fuels  
 53 which emit greenhouse gases. Wind energy is one of the promising sources of  
 54 renewable energy and is getting worldwide recognition due to its competitive cost of  
 55 production compared with traditional means.

56 Wind speed frequency distribution is an important statistical tool in predicting the  
 57 wind energy output at a particular location [1]. The Weibull distribution function is  
 58 found to represent the variable nature of wind speed better than other distributions in  
 59 most of the locations worldwide [2, 3, 4, 5]. The Weibull function is a two-parameter  
 60 function, namely, shape parameter,  $k$  and scale parameter,  $c$ . There are several methods  
 61 available in the literature for the determination of these two parameters. Stevens and  
 62 Smulders [6] found the values of  $k$  and  $c$  by five different estimation methods namely,  
 63 method of moments, method of energy pattern factor, maximum likelihood method,

64 Weibull probability paper method and percentile estimators. Almost same values were  
65 obtained by all five methods.

66 Seguro and Lambert [7] calculated the Weibull parameters using maximum likelihood  
67 method, graphical method and modified maximum likelihood method. It was reported  
68 that when wind speed data is available in time-series format, the maximum likelihood  
69 method is the recommended method for estimating the parameters. When wind speed  
70 data is available in frequency distribution format, the modified maximum likelihood  
71 method is the recommended method. The graphical method is reported to be the least  
72 accurate. Bagiorgas et al. [8] calculated the Weibull parameters using the wind data  
73 from seven different sites in Saudi Arabia. The parameter estimation methods used  
74 were least-squares regression method, method of moments, alternative maximum  
75 likelihood estimation method, maximum likelihood method, and WAsP Algorithm. The  
76 calculated values using the five different methods were found to be in good agreement  
77 at all the measurement heights. The correlation between the monthly mean values of  
78 Weibull scale parameter and the measured wind speed values was found to be linear at  
79 all the sites.

80 Rocha et al. [9] compared seven numerical methods for determining the Weibull  
81 parameters at northeast region of Brazil. The estimation methods were graphical  
82 method, maximum likelihood method, energy pattern factor method, moment method,  
83 empirical method, modified maximum likelihood method, and equivalent energy  
84 method. The equivalent energy method was found to be efficient for determining the  $k$   
85 and  $c$  parameters to fit Weibull distribution curves for wind speed data. Akdag and  
86 Dinler [10] developed a new method called power density method for estimation of  
87 Weibull parameters. This new method was compared with graphic, maximum  
88 likelihood and moment methods and it was concluded that power density method is  
89 suitable and efficient for Weibull parameters estimation for the given location.

90 Wind speed assessment of six sites in the island of Crete, Greece was done [11]. The  
91 effect of topographical features on wind characteristics was studied. The Weibull,  
92 Rayleigh, Lognormal, Gamma, and Inverse Gaussian distributions probability  
93 distributions were examined for their ability to model the wind speed frequency  
94 distributions. The most efficient methods for the estimation of the distribution  
95 parameters were found to be moments method, maximum likelihood method, and  
96 least-squares method.

97 For wind resource assessment of Selcuk University campus in Turkey, one year wind  
98 data at three different heights was analysed [12]. Energy output from a 6 MW installed  
99 capacity wind farm composed of 1.0, 1.5, and 2.0 MW rated power wind turbines was  
100 calculated and reported by Faruk et al. [12]. The minimum basic payback period was  
101 found to be 6.44 years. Onca et al. [13] presented the wind resource assessment of  
102 north-western side of the Black Sea using measured wind speed data over a period of 11  
103 years. The analysis indicated that the Romanian coastal region has more wind energy  
104 potential during the winter season, with an average annual wind speed of about 9.7  
105 m/s at 80 m and a power density of 870 W/m<sup>2</sup>. This study concluded that the north-  
106 western side of the Black Sea is a promising site for the wind farm development.

107 The forecast of energy demand in Saudi Arabia is expected to be more than double in  
108 the next one and a half decade, from 58 GW in 2015 to 121 GW in 2030 [14]. It is an  
109 urgent requirement to fill this gap of approx. 60 GW of power generation and at the  
110 same time reduce the load on diminishing oil and gas reserves. Wind energy along with  
111 solar energy - Photovoltaic (*PV*) and Concentrated Solar Power (*CSP*) are serious  
112 considerations to fill this energy gap [14]. This study aims at conducting a  
113 comprehensive and accurate wind resource assessment at seven locations of the largest  
114 industrial enterprise in middle-east by finding Weibull parameters, maximum energy  
115 carrying capacity, most probable wind speed, energy output from a few commercially  
116 available wind machines and comparing parameter estimation methods.

## 117 2. Sites, equipment and data description

118 In 1933, geologists explored oil in Jubail, Saudi Arabia. In 1983, the largest engineering  
119 and construction project ever was started at Jubail industrial city. Presently, Jubail  
120 industrial city is host to more than 160 industrial enterprises and home to almost 95,000  
121 residents. The Jubail infrastructure has the capability to operate continuously without  
122 failure of power in any of the existing facilities while meeting community requirements  
123 within high modern living standards where all the necessities of life and tourism and  
124 recreation are available.

125 To study the viability of wind power generation for the Jubail city, the historical wind  
126 data from seven weather stations was obtained from the Environment and Control  
127 Department (Royal commission for Jubail). The locations of these sites are shown in Fig.  
128 1. The photos of the wind towers at Industrial area (central), Al Bahar desalination  
129 plant, Pearl beach and Al-Reggah district are shown in Fig. 2, 3, 4 and 5 respectively. All  
130 the seven sites are located within a radius of 20 kms. The availability of long term wind  
131 speed data or an accurate forecasting method for missing data is very important in  
132 identifying suitable locations for wind turbines [15]. This governmental organisation is  
133 responsible for the maintenance, calibration and collection of meteorological data at  
134 Jubail Industrial city. The latitude/longitude and UTM coordinates of the weather  
135 station are given in Table. 1. The specifications of the wind speed sensors installed on  
136 the wind tower are given in Table 2. The list of weather parameters recorded is given in  
137 Table 3. The description of the terrain in the vicinity of all the sites is given in Table 4.

138 The coastal city of Jubail also hosts world's largest water desalination plant, Saline  
139 water conversion corporation (SWCC). This plant produces 363.4 million cubic meters  
140 of water per annum supplying it to national capital, Riyadh and Jubail [16]. The  
141 desalination in this plant is done by conventional means and out of all the alternatives  
142 of renewable energy desalination, wind powered desalination can be considered most  
143 promising [17].

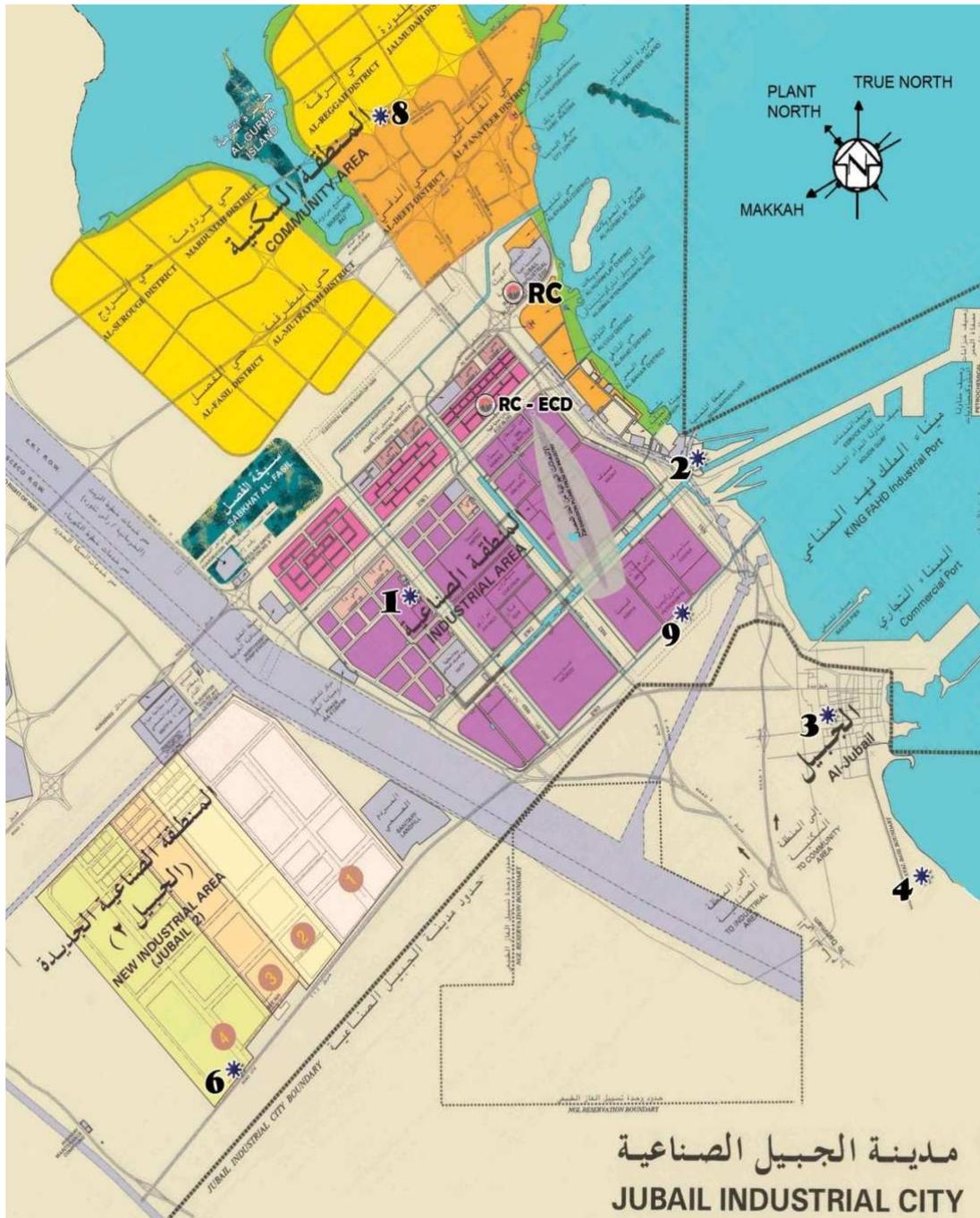


Fig. 1. Weather stations in Jubail industrial city

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152 Table 1

153 Latitude/longitude and UTM coordinates of weather data collection sites.

Site Code	Site name	Degrees, Minutes, Seconds	Station height, m AGL
Site 1	Industrial area (Central)	27° 2'15.76"N	10, 50 & 90
		49°32'2.56"E	
Site 2	Al-Bahar desalination plant	27° 4'27.49"N	10
		49°36'3.24"E	
Site 3	Pearl beach	27° 0'36.85"N	10
		49°39'9.56"E	
Site 4	Naval Base	26°55'39.92"N	10
		49°42'42.89"E	
Site 6	Industrial area 2 (South)	26°55'13.40"N	10
		49°29'0.10"E	
Site 8	Al-Reggah District	27° 7'54.03"N	10
		49°31'57.02"E	
Site 9	Industrial area (East)	27° 1'49.95"N	10
		49°36'41.14"E	

154 Table 2

155 Specifications of the wind speed sensor at data collection site.

PERFORMANCE CHARACTERISTICS	
Maximum Operating Range:	0 - 125 mph (0 - 60 m/s)
Starting Speed:	0.5 mph (0.22 m/s)
Calibrated Range:	0 - 100 mph (0 - 50 m/s)
Accuracy:	±1% or 0.15 mph (0.07 m/s)
Resolution:	<0.1 mph or m/s
Temperature Range:	-50°C to +65°C (-58°F to +149°F)
Distance Constant:	less than 5 ft (1.5m) of flow (meets EPA specifications)
ELECTRICAL CHARACTERISTICS	
Power Requirements:	12 VDC at 10 mA, 12 VDC at 350 mA for internal heater
Output Signal:	11 volt (pulse frequency equivalent to speed)
Output Impedance:	100 Ω maximum
PHYSICAL CHARACTERISTICS	
Weight:	1.5 lbs (.68 kg)
Finish:	Clear anodised aluminium; Lexan cup assembly.
CABLE & MOUNTING	
PN 1953 Mounting:	Cable Assembly; specify length in feet or metres PN 191 Crossarm Assembly

156

157 Table 3

158 Parameter list of the weather data collection tower.

Sr.No	Parameter Code	Description	Unit
1	ATM	Atmospheric Temperature	DegC
2	PRE	Precipitation	mm
4	RH	Relative Humidity	%
6	VWD10	Vector Wind Direction 10m	deg
9	VWS10	Vector Wind Speed 10m	m/s



Fig. 2. Wind tower at Industrial area (Central)



Fig. 3. Wind tower at Al-Bahar desalination plant



Fig. 4. Wind tower at Pearl beach



Fig. 5. Wind tower at Al-Reggah district

159 Table 4  
160 Description of the terrain in the vicinity of weather stations.

Site	Description
Industrial area (Central)	Only station where weather data is available at three heights AGL. Surrounded mainly by plain terrain with some warehouses of 8 - 10 m height about 200 m away in west direction.
Al-Bahar desalination plant	Located on sea shore near desalination plant. Terrain is mostly plain and surrounded by very small shrubs.
Pearl beach	Located in Jubail residential area and surrounded by 3-4 story buildings. This station recorded minimum wind speed out of all weather stations.
Naval Base	Located near Dhahran-Jubail highway. Terrain is mostly plain and surrounded by very small shrubs and few residential buildings 200 m away towards east.
Industrial area 2 (South)	Surrounded mainly by plain terrain with some warehouses of 8 - 10 m height about 300 m away in west and north direction.
Al-Reggah District	Location mostly surrounded by shrubs. Surrounding clear with a 3 story building around 150 m away in north-eastern direction.
Industrial area (East)	Surrounded mainly by plain terrain with some warehouses of 8 - 10 m height about 150 m away in north - west direction

1613. This study presents the analysis of wind characteristics from seven different sites at  
 162 Jubail city in Saudi Arabia at 10 m height above ground level (AGL). The wind data is  
 163 collected over a period of 5 years (2008 – 2012) for all sites except the site at Naval base  
 164 where the data was available for 3 years (2010 – 2012).

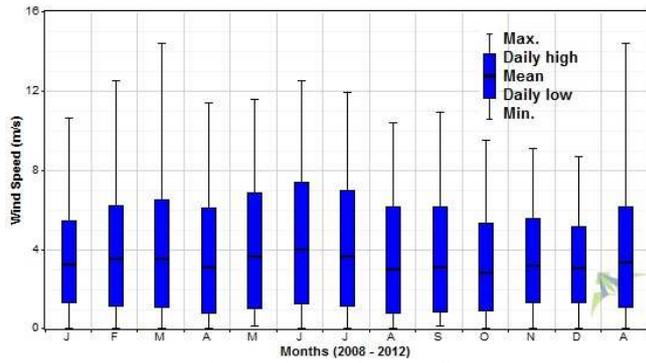
### 165 2.1 Statistics of Wind Speed

166 The hourly average wind speed values over entire period of data collection for all the  
 167 seven sites at 10 m height are presented in Table 5. The highest annual mean wind  
 168 speed of 4.53 m/s was observed at Industrial area (East) and the lowest of 2.25 m/s at  
 169 Pearl beach with standard deviations of 2.52 and 1.1 m/s respectively. To assess the  
 170 seasonal variation of wind speed over all sites, the data is sorted month-wise and the  
 171 monthly maximum, daily high/low (in that month), mean, and monthly minimum  
 172 wind speeds are plotted. These plots are shown in Fig. 6. It was observed that the  
 173 highest monthly mean wind speed was witnessed in February/June at all sites; this  
 174 period coincides with the high energy demand period for the region due to air  
 175 conditioning load. The lowest mean wind speed was witnessed in September/October  
 176 at all sites. To visualize the wind patterns at all the sites, the wind rose charts, showing  
 177 the frequency and speed of wind blowing from each of 16 cardinal directions were  
 178 plotted as shown in Fig. 7. These rose plots for a particular site can help in wind  
 179 machine design decisions. It can be observed from these plots that the most prevailing  
 180 wind direction at all sites was from the north-west.

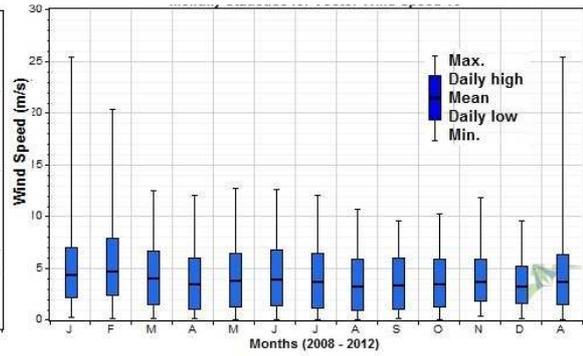
181 Table 5  
 182 Wind speed statistics of all sites.

Station	Annual mean wind speed, m/s		
	Mean	Maximum	Standard Deviation
Industrial area (Central)	3.27	11.90	1.985
Al-Bahar desalination plant	3.74	2.40	2.193
Pearl beach	2.26	8.70	1.109
Naval Base	3.78	13.80	2.220
Industrial area 2 (South)	4.31	27.00	2.983
Al-Reggah District	2.91	13.60	1.511
Industrial area (East)	4.53	19.30	2.520

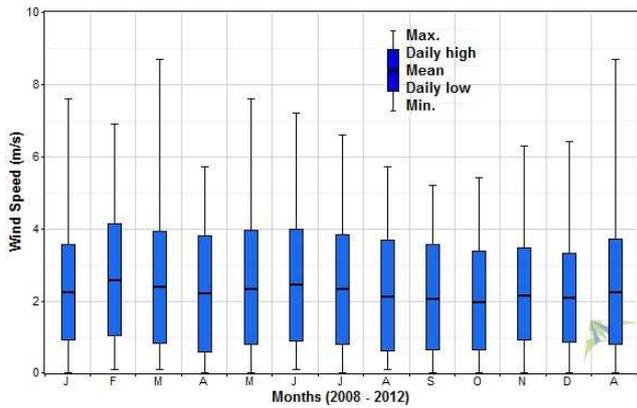
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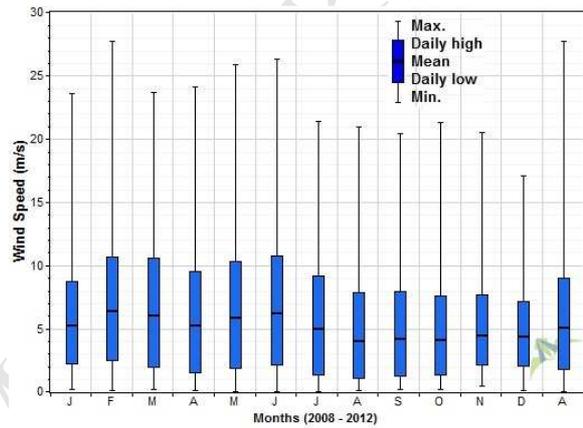
Industrial area (Central)



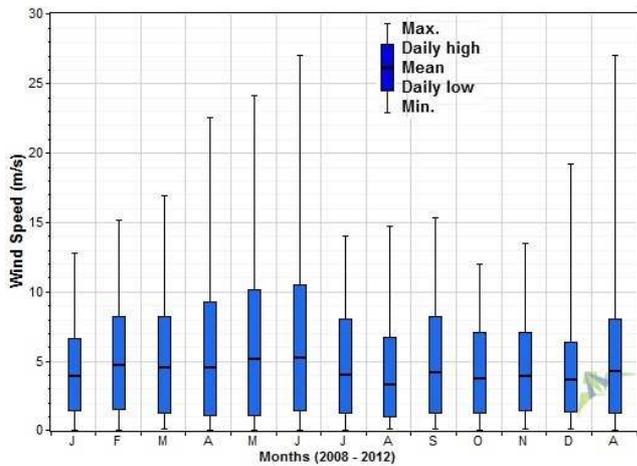
Al-Bahar desalination plant



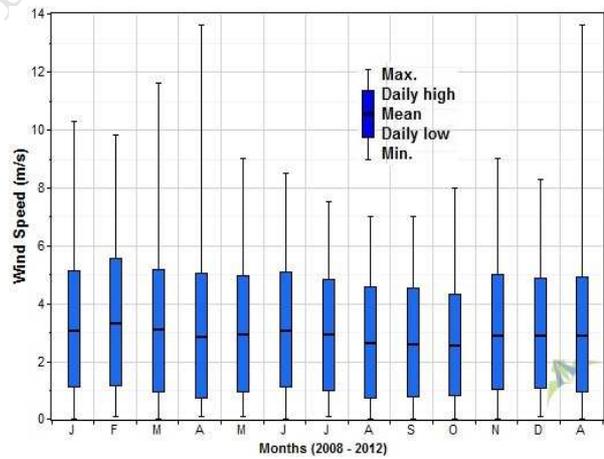
Pearl beach



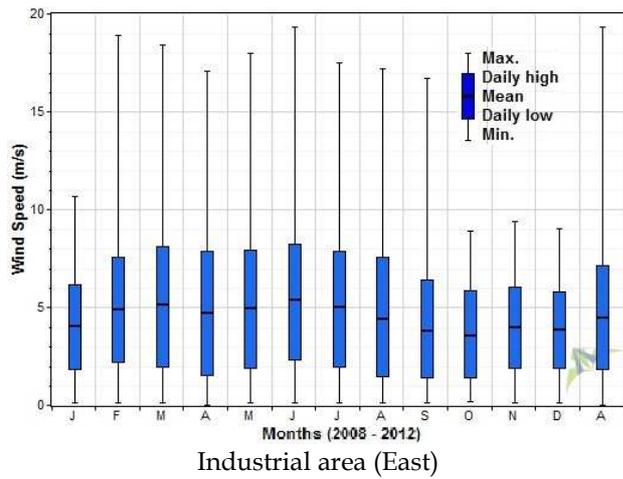
Naval Base



Industrial area 2 (South)



Al-Reggah District



184

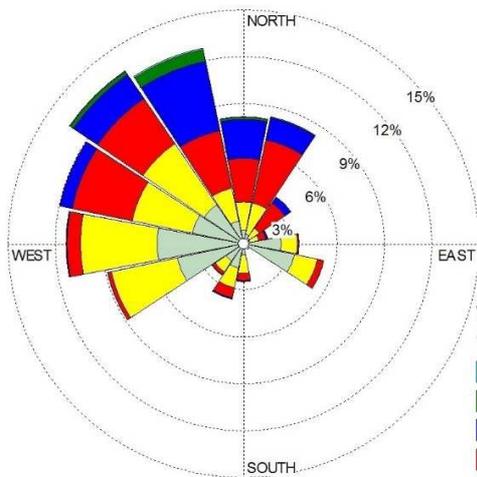
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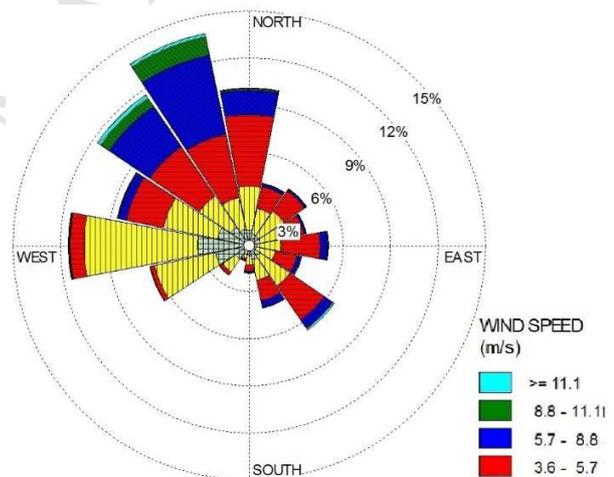
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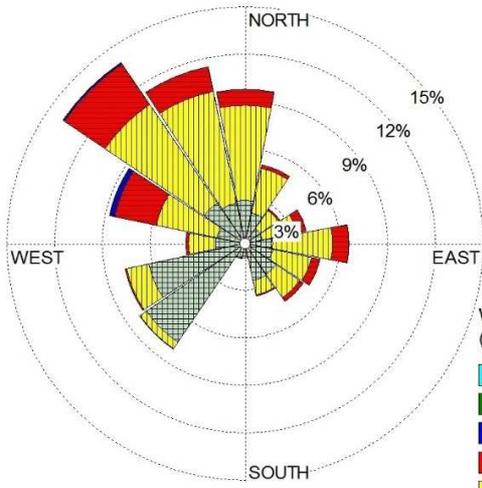
Fig. 6. Monthly maximum, daily high, daily mean, daily low and minimum wind speed at all sites.



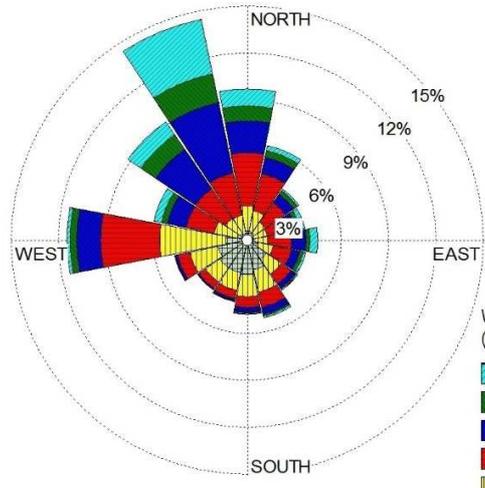
Industrial area (Central)



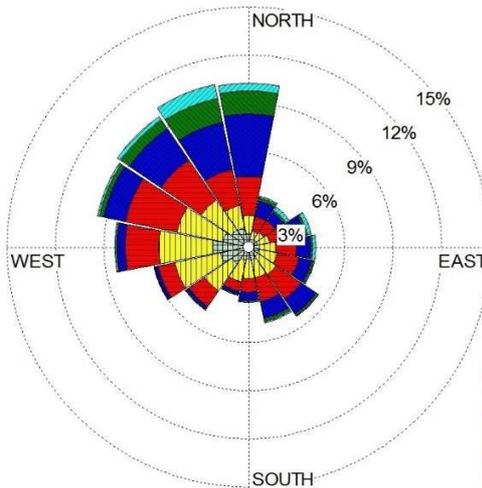
Al-Bahar desalination plant



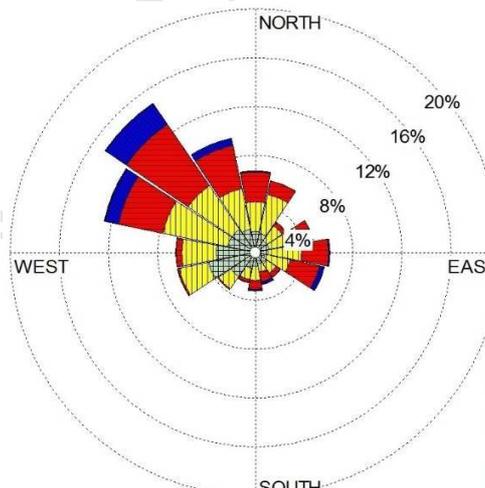
Pearl beach



Naval Base



Industrial area 2 (South)



Al-Reggah District

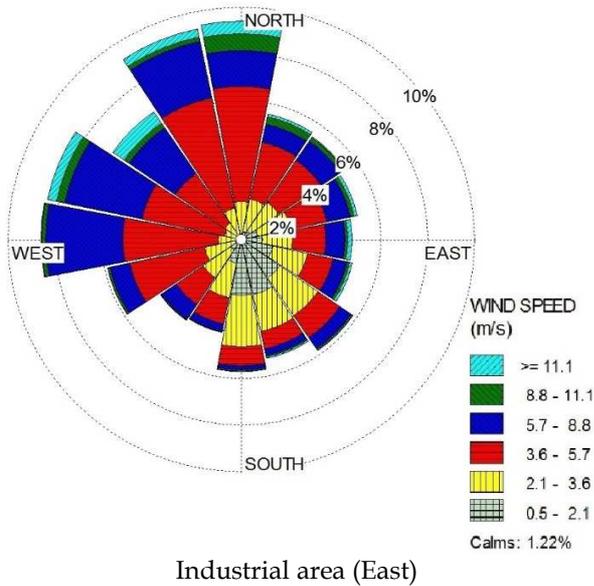


Fig. 7. Wind rose plots at 10 m AGL at all sites

189

190

### 191 3. Numerical methods for determining the Weibull parameters

192 The two-parameter Weibull distribution is frequently used to characterise wind  
 193 behaviour because it provides a good representation of wind data [2, 3, 4, 5]. This  
 194 distribution function shows the probability of the wind speed in a 1 m/s bins centered  
 195 on a particular wind data time series. The Weibull distribution function is expressed as  
 196 [18]:

$$197 \quad P_{(v)} = \frac{k}{v} \left(\frac{v}{c}\right)^{k-1} \exp\left\{-\left(\frac{v}{c}\right)^k\right\}, \quad (1)$$

198 Where  $P_{(v)}$  is the frequency of incidence of wind speed,  $v$ . The scale factor,  $c$  in m/s, is  
 199 indicative of mean wind speed and  $k$  is the dimensionless shape factor, which describes  
 200 the shape and width of the distribution. The Weibull distribution is therefore  
 201 determined by the parameters,  $c$  and  $k$ . The cumulative Weibull distribution,  $P_{(v)}$ , which  
 202 gives the probability of the wind speed greater than the value,  $v$ , is expressed as:

$$203 \quad P_{(v)} = \exp\left\{-\left(\frac{v}{c}\right)^k\right\}, \quad (2)$$

204 There are several methods to estimate Weibull parameters. Three methods commonly  
 205 used are discussed in this study.

206 *3.1 Maximum Likelihood Method*

207 Maximum likelihood method was suggested by Stevens and Smulders [6]. This method  
 208 requires extensive iterative calculations. Shape and scale parameters of Weibull  
 209 distribution are estimated by these two equations

$$210 \quad k = \left( \frac{\sum_{i=1}^n v_i^k \ln(v_i)}{\sum_{i=1}^n v_i^k} - \frac{\sum_{i=1}^n \ln(v_i)}{n} \right)^{-1} \quad (3)$$

$$211 \quad c = \left( \frac{\sum_{i=1}^n (v_i)^k}{n} \right)^{\frac{1}{k}} \quad (4)$$

212 Where  $v_i$  is the wind speed and  $n$  is the number of nonzero wind speeds. This method is  
 213 implemented by taking care of zero wind speeds which make logarithm indefinite and  
 214 then calculate shape parameter. The scale parameter is found using a numerical  
 215 technique in order to find the root of Eq. (3) around  $k = 2$ .

216

217 *3.2 Least-Squares Regression Method (LSRM)*

218 The equation of the probability density function, after a double logarithmic  
 219 transformation, can be written as follows:

$$220 \quad \ln[-\ln(1 - F(v))] = k \ln(c) \quad (5)$$

221 The above equation is linear and can be fitted using the LSRM [19]. The cumulative  
 222 distribution function  $F(v)$  can be estimated easily, using an estimator, which is the  
 223 median rank.

224 The wind power density, WPD, for maximum likelihood method and least-squares  
 225 regression method is computed using the following equation:

$$226 \quad WPD = \frac{1}{2} \rho c^3 \quad (6)$$

227 Where:

228  $\rho$ : air density within the time step, kg/m<sup>3</sup>.

229  $c$ : weibull scale parameter, measure of average wind speed within the time step, m/s.

230

231 3.3 WAsP Algorithm

232 There are two requirements of WAsP algorithm

233 (1) The power density of the fitted Weibull distribution is equal to that of the  
234 observed distribution and

235 (2) The proportion of values above the mean is the same for the fitted Weibull  
236 distribution as for the observed distribution.

237 Let  $X$  represents the proportion of the observed wind speeds that exceed the mean wind  
238 speed. The cumulative distribution function  $F(U)$  gives the proportion of values that are  
239 less than  $U$ , so  $1-F(U)$  is the proportion of values that exceed  $U$ . One can therefore write  
240 the second requirement as follows:

$$241 \quad X = 1 - F(\bar{U}) \quad (7)$$

242 Since the mean wind speed is given by the following equation:

$$243 \quad \bar{U} = c\Gamma\left(\frac{1}{k} + 1\right) \quad (8)$$

244 Substitute the aforementioned mean value in the expression of the cumulative  
245 distribution function to get second requirement:

$$246 \quad X = \exp\left[-\Gamma\left(\frac{1}{k} + 1\right)^k\right] \quad (9)$$

247 Taking the natural logarithm of both sides gives

$$248 \quad -\ln X = \Gamma\left(\frac{1}{k} + 1\right)^k \quad (10)$$

249 In performing the WAsP algorithm to fit the Weibull distribution, WindoGrapher [20]  
250 software (<http://www.mistaya.ca/>) calculates  $X$  and then solves the above equation  
251 iteratively by using the Brent method, in order to find the  $k$  parameter. Requirement (1)  
252 allows us to calculate the  $c$  parameter. On the basis of the Weibull distribution, in WAsP  
253 algorithm, the mean WPD, assuming constant air density, is calculated as follows:

$$254 \quad WPD = \frac{1}{2}\rho c^3 \Gamma\left(\frac{3}{k} + 1\right) \quad (11)$$

255 We can also write an equation for the mean power density of the observed wind speeds  
256 as follows:

$$257 \quad WPD = \frac{1}{2N} \rho \sum_N U_i^3 \quad (12)$$

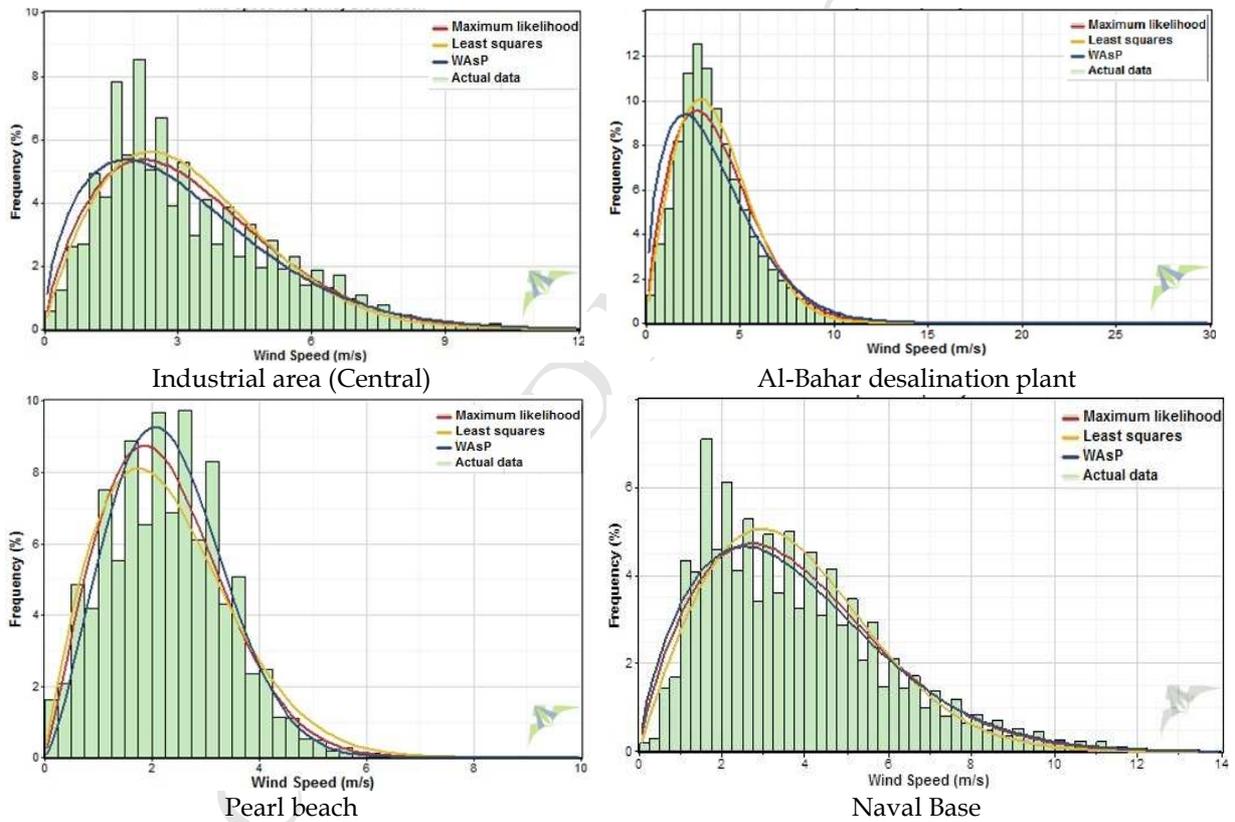
258 As per requirement (1), these must be equal, so one can write,

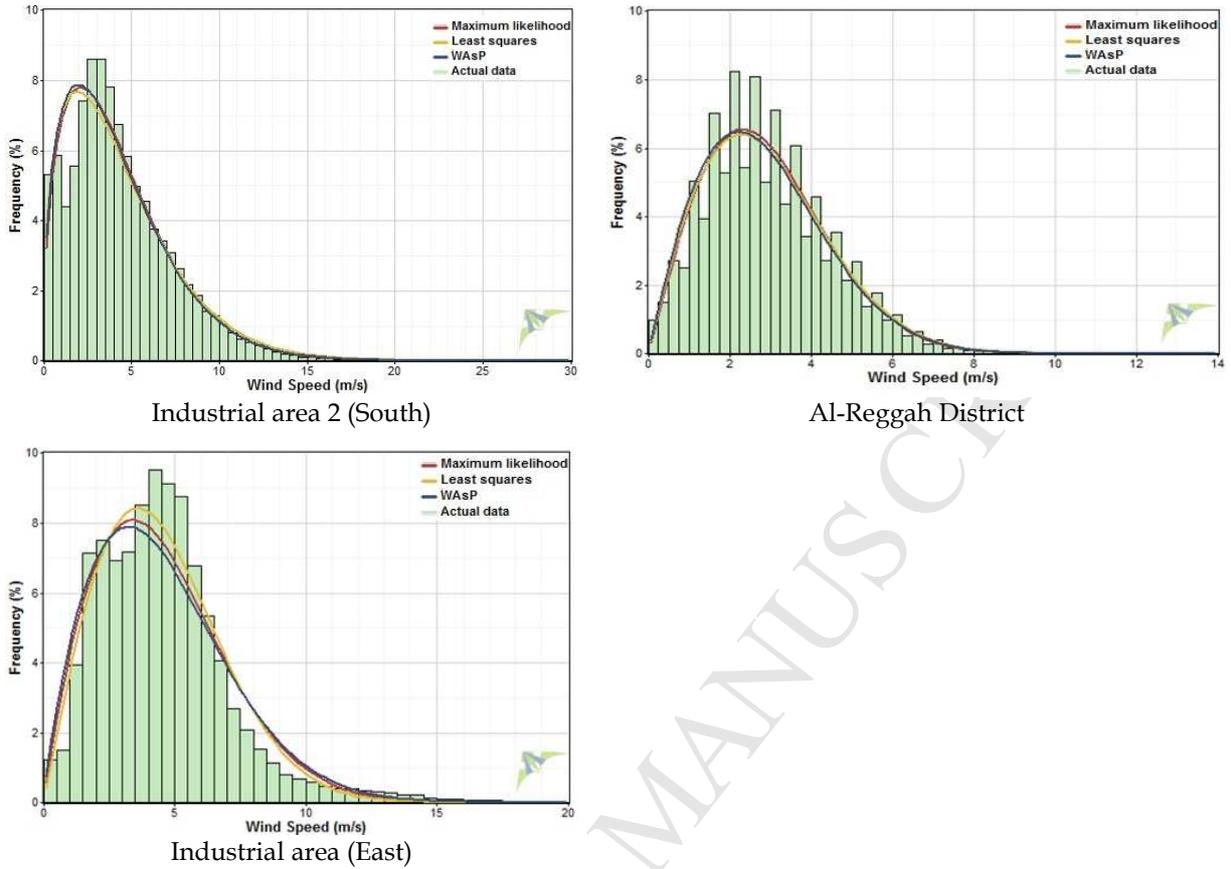
$$259 \quad c^3 \Gamma\left(\frac{3}{k} + 1\right) = \frac{1}{N} \sum_N U_i^3 \quad (13)$$

260 Solving this for  $c$  gives us the following:

$$261 \quad c = \sqrt[3]{\frac{\sum_N U_i^3}{N \Gamma\left(\frac{3}{k} + 1\right)}} \quad (14)$$

262 The actual wind data and Weibull curves at all seven sites (maximum likelihood  
263 method, least squares regression methods and WAsP method) are also shown in Fig. 8.





264 Fig. 8. Weibull probability distributions (three methods) and actual data at all sites.

265

#### 266 4. Goodness-of-fit tests

267 To analyse the efficiency of the aforementioned Weibull parameter estimation methods,  
 268 the following tests were conducted:

269 Coefficient of determination,  $R^2$ , is the square of correlation between the frequencies of  
 270 Weibull to that of actual observations.

271 The coefficient of determination is computed according to the following equation [21,  
 272 9]:

$$273 R^2 = \frac{\sum_{i=1}^N (y_i - z_i)^2 - \sum_{i=1}^N (y_i - x_i)^2}{\sum_{i=1}^N (y_i - z_i)^2} \quad (15)$$

274 The root mean square error,  $RMSE$  is the measure of the residuals of frequency of  
 275 Weibull and actual observations [20].

$$276 RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - x_i)^2} \quad (16)$$

277 The mean bias error, *MBE* and mean bias absolute error, *MAE* are a measure of how  
 278 closely frequency of Weibull match the actual observations [21, 9].

$$279 \quad MBE = \frac{1}{N} \sum_{i=1}^N (y_i - x_i) \quad (17)$$

280

$$281 \quad MAE = \frac{1}{N} \sum_{i=1}^N |y_i - x_i| \quad (18)$$

282 Where:

283 *N* is the number is observations, *y<sub>i</sub>* is the frequency of observation, *x<sub>i</sub>* is the frequency of  
 284 Weibull and *z<sub>i</sub>* is the mean wind speed.

285

## 286 5. Results and discussion

287 The Weibull scale and shape parameters (*c* and *k*), wind power density (WPD) and  
 288 statistical results (*R<sup>2</sup>*, *RSME*, *MBE* and *MAE*) for all sites estimated by Maximum  
 289 likelihood method, least square regression method and WAsP method are shown in  
 290 Tables 6 - 12. Considering overall data at all sites, the average error in calculating the  
 291 WPD was found to be 0.25% for maximum likelihood method, 6.8% for LSRM and 5.7%  
 292 for WAsP method. It can be clearly validated by goodness-of-fit test indicators, i.e., *R<sup>2</sup>*,  
 293 *RSME*, *MBE* and *MAE* at all sites that maximum likelihood method is the best method  
 294 to represent the wind regime in Jubail, very closely followed by least square regression  
 295 and WAsP method. The monthly and annual Weibull parameters obtained by the most  
 296 accurate method, maximum likelihood method are given in Table 13 and 14  
 297 respectively. The monthly and annual variation of Weibull parameters *k* and *c* is shown  
 298 in Figs. 9, 10, 11 and 12.

299

300 Table 6

301 Weibull parameters, WPD and statistical results for Industrial area (Central).

Parameter estimation method	<i>k</i>	<i>c</i> (m/s)	WPD (w/m <sup>2</sup> )	<i>R<sup>2</sup></i>	<i>RMSE</i>	<i>MBE</i>	<i>MAE</i>
Maximum likelihood method	1.724	3.675	48.5	0.86	0.1750	-0.0046	0.3132
Least-Squares Regression Method	1.845	3.640	43.1	0.85	0.1811	-0.0047	0.3228
WAsP method	1.563	3.519	49.6	0.85	0.1849	-0.0048	0.3547

302

303

304 Table 7

305 Weibull parameters, WPD and statistical results for Al-Bahar desalination plant.

Parameter estimation method	$k$	$c$ (m/s)	WPD (w/m <sup>2</sup> )	$R^2$	RMSE	MBE	MAE
Maximum likelihood method	1.800	4.218	69.2	0.96	0.0720	-0.0042	0.1758
Least-Squares Regression Method	1.952	4.200	61.9	0.96	0.0725	-0.0045	0.1784
WAsP method	1.548	4.012	74.8	0.91	0.1449	-0.0030	0.2274

306

307 Table 8

308 Weibull parameters, WPD and statistical results for Pearl beach.

Parameter estimation method	$k$	$c$ (m/s)	WPD (w/m <sup>2</sup> )	$R^2$	RMSE	MBE	MAE
Maximum likelihood method	2.104	2.539	12.7	0.91	0.0180	-0.0047	0.1155
Least-Squares Regression Method	1.924	2.582	14.6	0.90	0.0230	-0.0048	0.1433
WAsP method	2.367	2.611	12.5	0.90	0.0235	-0.0050	0.1208

309

310 Table 9

311 Weibull parameters, WPD and statistical results for Naval Base.

Parameter estimation method	$k$	$c$ (m/s)	WPD (w/m <sup>2</sup> )	$R^2$	RMSE	MBE	MAE
Maximum likelihood method	1.799	4.263	71.4	0.86	0.1600	-0.0050	0.3521
Least-Squares Regression Method	1.973	4.205	61.4	0.85	0.1717	-0.0049	0.3619
WAsP method	1.718	4.218	73.7	0.84	0.1574	-0.0050	0.3522

312

313 Table 10

314 Weibull parameters, WPD and statistical results for Industrial area 2 (South).

Parameter estimation method	$k$	$c$ (m/s)	WPD (w/m <sup>2</sup> )	$R^2$	RMSE	MBE	MAE
Maximum likelihood method	1.450	4.740	139.2	0.92	0.0970	-0.0034	0.1482
Least-Squares Regression Method	1.392	4.788	155.9	0.92	0.0958	-0.0032	0.1624
WAsP method	1.421	4.678	139.4	0.92	0.0970	-0.0030	0.1491

315

316 Table 11

317 Weibull parameters, WPD and statistical results for Al-Reggah District

Parameter estimation method	$k$	$c$ (m/s)	WPD (w/m <sup>2</sup> )	$R^2$	RMSE	MBE	MAE
Maximum likelihood method	2.008	3.286	28.8	0.94	0.1770	-0.0048	0.3504
Least-Squares Regression Method	1.957	3.304	30.1	0.93	0.1782	-0.0048	0.3497
WAsP method	1.938	3.242	28.7	0.93	0.1780	-0.0050	0.3485

318 Table 12

319 Weibull parameters, WPD and statistical results for Industrial area (East)

Parameter estimation method	$k$	$c$ (m/s)	WPD (w/m <sup>2</sup> )	$R^2$	RMSE	MBE	MAE
Maximum likelihood method	1.876	5.098	116.0	0.94	0.0700	-0.0048	0.2339
Least-Squares Regression Method	1.999	5.096	107.8	0.94	0.0705	-0.0048	0.2139
WAsP method	1.799	5.100	122.3	0.93	0.0902	-0.0050	0.2491

320

321 Table 13

322 Monthly Weibull parameters at all sites (Maximum likelihood method)

Location	Industrial area (Central)		Al-Bahar desalination plant		Pearl beach		Naval Base		Industrial area 2 (South)		Al-Reggah District		Industrial area (East)	
	$k$	$c$	$k$	$c$	$k$	$c$	$k$	$c$	$k$	$c$	$k$	$c$	$k$	$c$
Jan	1.892	3.691	1.572	4.869	2.016	2.539	2.013	4.202	1.666	4.443	1.845	3.467	2.415	4.591
Feb	1.680	3.962	1.697	5.254	2.126	2.913	1.880	4.913	1.556	5.247	1.893	3.760	1.942	5.579
Mar	1.700	4.003	1.835	4.556	2.108	2.698	1.730	5.053	1.566	5.058	1.942	3.483	1.910	5.817
Apr	1.649	3.504	1.871	3.938	2.118	2.509	1.896	4.203	1.528	5.117	2.045	3.246	1.938	5.363
May	1.662	4.106	1.759	4.247	2.253	2.644	1.825	4.409	1.382	5.662	2.178	3.314	1.909	5.644
Jun	1.673	4.476	1.731	4.442	2.047	2.785	1.704	4.876	1.351	5.800	2.063	3.484	1.721	6.133
Jul	1.675	4.133	1.885	4.159	2.307	2.651	1.692	4.279	1.266	4.378	2.259	3.313	1.940	5.706
Aug	1.608	3.392	2.035	3.724	2.267	2.406	1.787	3.556	1.356	3.686	2.229	2.966	1.938	5.060
Sep	1.762	3.533	2.033	3.802	2.256	2.343	1.888	3.543	1.643	4.753	2.165	2.950	1.473	4.244
Oct	1.759	3.189	2.044	3.941	2.118	2.229	1.821	3.755	1.697	4.237	2.127	2.883	2.410	4.095
Nov	2.056	3.639	2.169	4.180	2.258	2.436	2.101	4.237	1.625	4.436	2.024	3.290	2.699	4.516
Dec	2.020	3.492	2.231	3.643	1.989	2.355	2.009	4.191	1.461	4.101	1.912	3.282	2.535	4.380

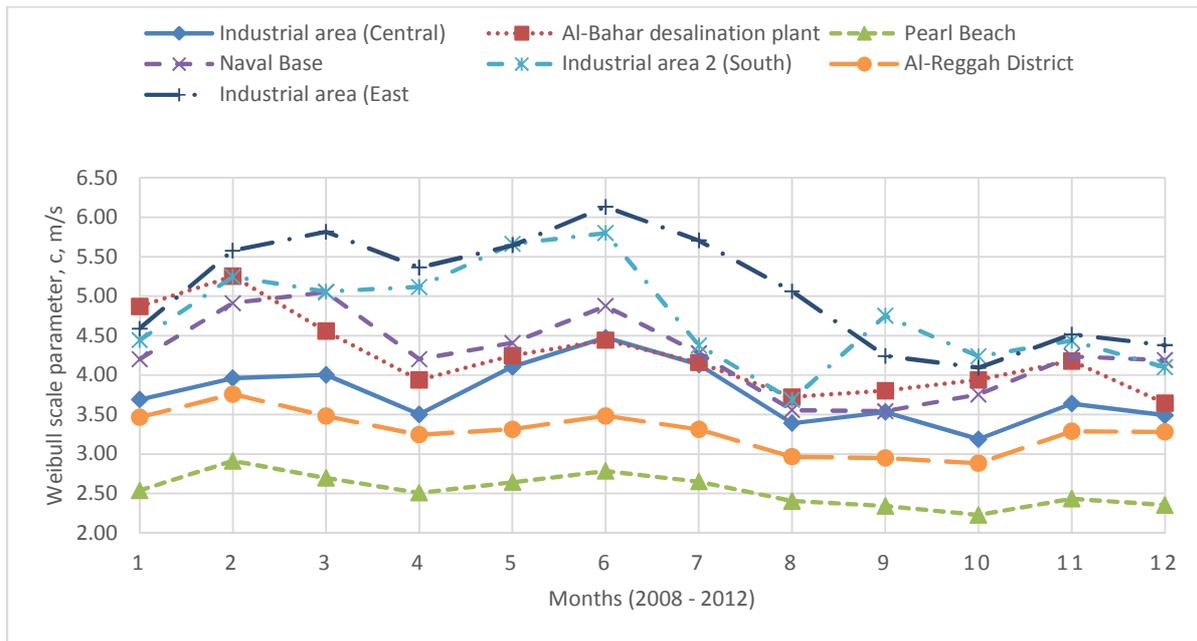
323

324 Table 14

325 Annual Weibull parameters at all sites (Maximum likelihood method)

Year	Industrial area (Central)		Al-Bahar desalination plant		Pearl beach		Naval Base		Industrial area 2 (South)		Al-Reggah District		Industrial area (East)	
	$k$	$c$	$k$	$c$	$k$	$c$	$k$	$c$	$k$	$c$	$k$	$c$	$k$	$c$
2008	1.714	3.971	1.603	4.777	2.128	2.667	-	-	1.989	5.480	1.941	3.363	2.434	4.757
2009	1.700	3.658	1.899	4.301	2.109	2.548	-	-	1.875	5.251	1.992	3.318	2.318	4.450
2010	1.701	3.611	1.913	4.163	2.111	2.443	1.811	4.151	1.660	4.338	1.996	3.141	2.457	4.671
2011	1.743	3.880	1.927	3.641	2.178	2.578	1.834	4.429	1.194	3.849	2.104	3.343	2.320	4.563
2012	1.724	3.675	1.987	4.229	2.057	2.467	1.763	4.212	1.096	4.685	2.025	3.261	1.876	5.098

326

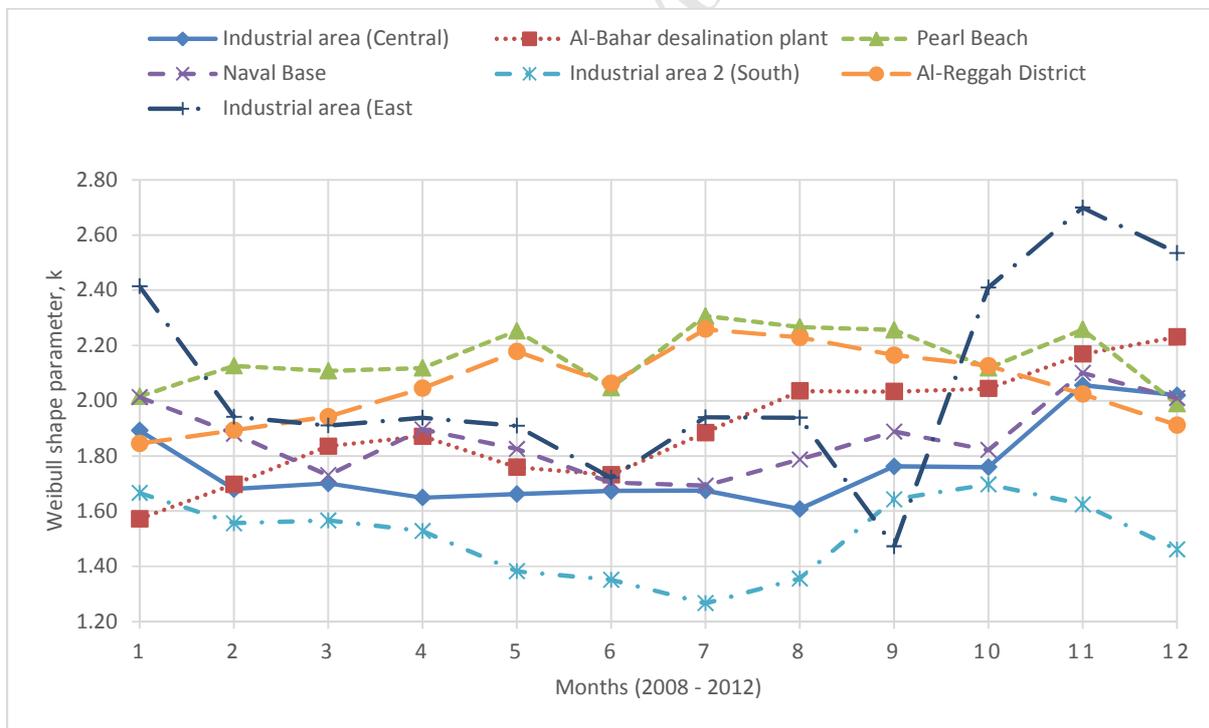


327

328

Fig. 9. Monthly variation of Weibull scale parameter,  $c$ , m/s at all sites.

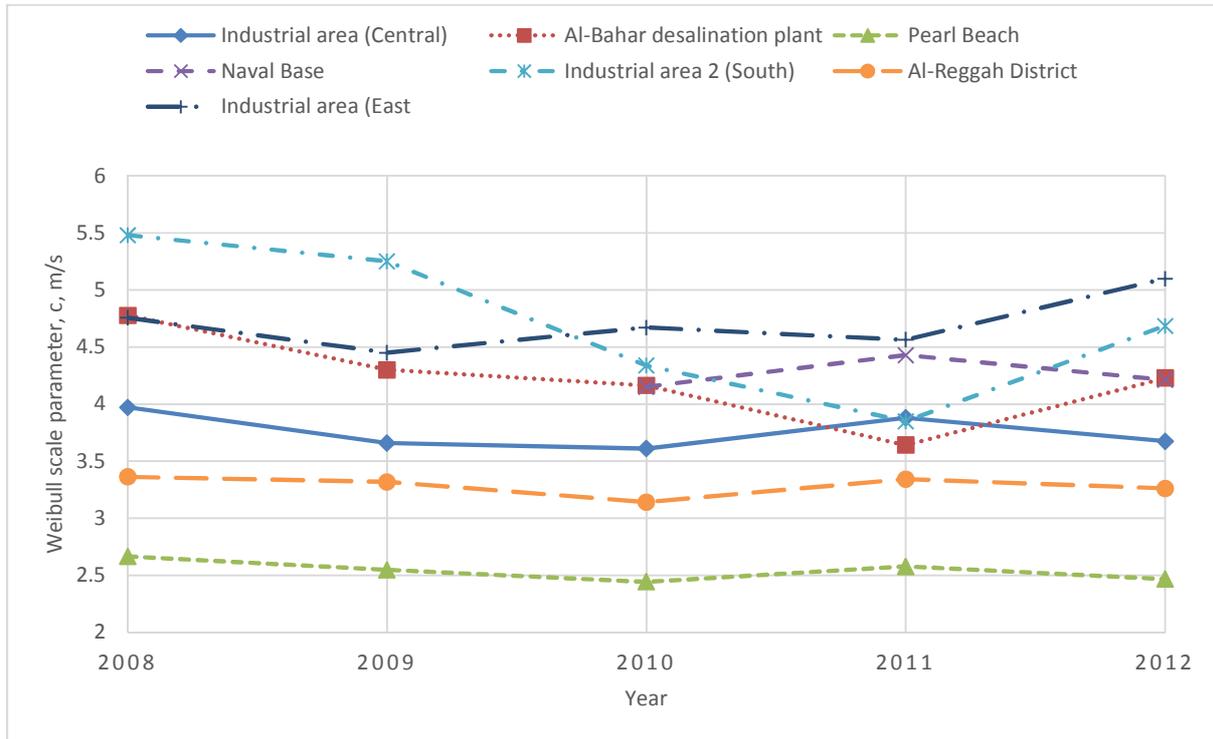
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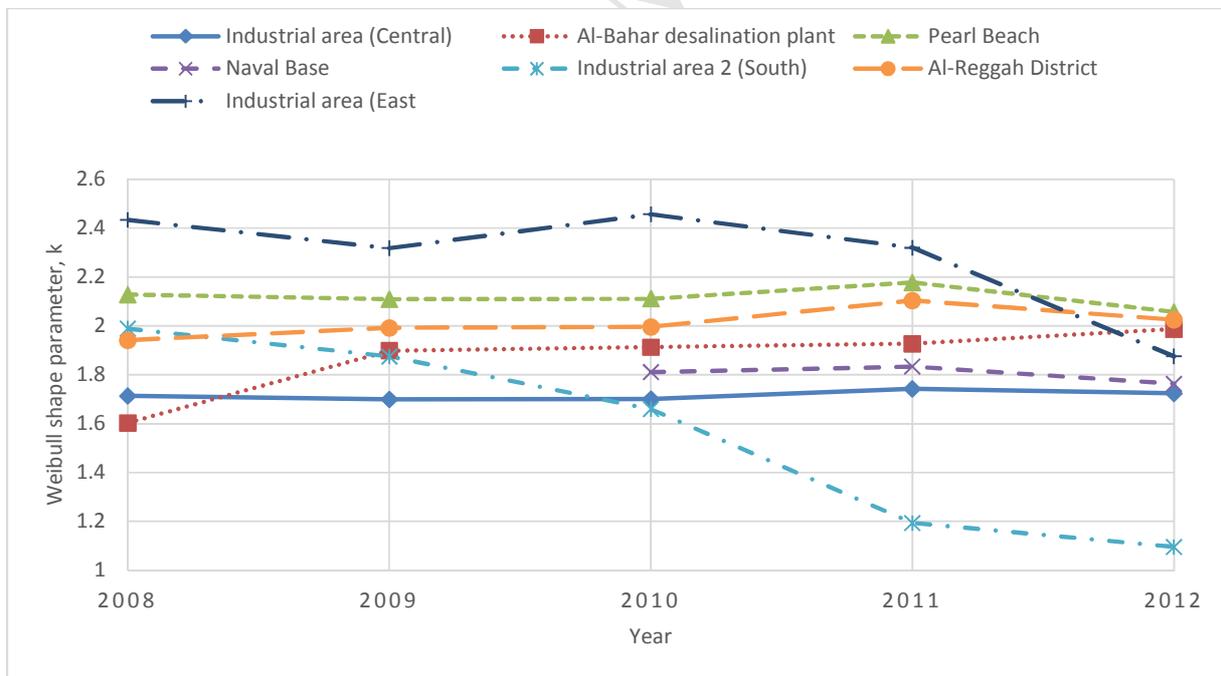
331

Fig. 10. Monthly variation of Weibull shape parameter,  $k$  at all sites.



332

333

Fig. 11. Annual variation of Weibull scale parameter,  $c$ , m/s at all sites.

334

335

Fig. 12. Annual variation of Weibull shape parameter,  $k$  at all sites.

336

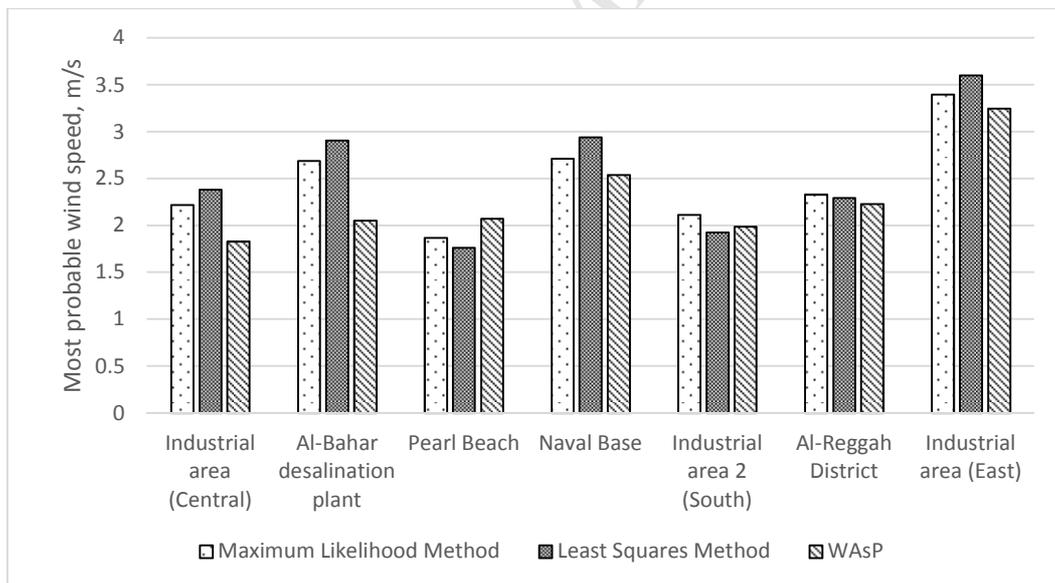
337 *5.1 Most Probable Wind Speed*

338 The most probable wind speed simply provides the most frequently occurring wind  
 339 speed for a given wind probability distribution. In high wind potential sites, the most  
 340 probable wind speed is close to the rated wind speed for a given wind machine. The  
 341 most probable wind speed can be calculated using the Weibull shape and scale  
 342 parameters via the following equation [22]:

$$343 \quad V_{mp} = c \left(1 - \frac{1}{k}\right)^{\frac{1}{k}} \quad (14)$$

344 The most probable wind speed at all the seven locations at 10 m AGL was found using  
 345 all three estimation methods and is shown in Fig. 13. All three estimation methods  
 346 showed similar results. The highest most probable wind speeds determined by  
 347 maximum likelihood method, least-square regression methods and WAsP are 3.39, 3.6  
 348 and 3.24 m/s respectively and were observed at Industrial area (east).

349



350

351 Fig. 13. Most probable wind speed at all sites.

352

353

354

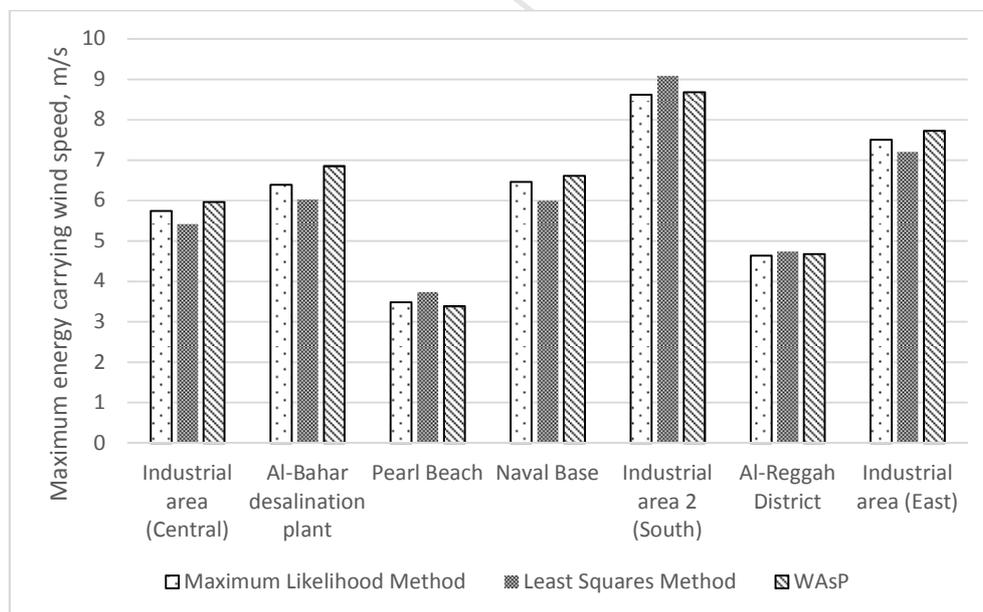
355 *5.2 Maximum Energy Carrying Wind Speed Estimation*

356 The maximum energy carrying wind speed is the speed which generates maximum  
 357 energy. This can be estimated from the Weibull parameters through the following  
 358 relationship [22]:

$$359 \quad V_{max,E} = c \left(1 + \frac{2}{k}\right)^{\frac{1}{k}} \quad (15)$$

360 The maximum energy carrying wind speed at all the seven locations at 10 m AGL was  
 361 found using all three estimation methods is shown in Fig. 14 below. All three estimation  
 362 methods showed similar results. The highest maximum energy carrying wind speed  
 363 values of 8.61, 9.0 and 8.68 m/s; determined by maximum likelihood method, least-  
 364 square regression methods and WAsP; were observed at Industrial area 2 (south). While  
 365 at Industrial area (east) the respective values were found to be 7.5, 7.2 and 7.7 m/s  
 366 respectively. These wind speeds are indicative of producing maximum energy in  
 367 industrial area 2 (south) and industrial area (east).

368



369

370

Fig. 14. Maximum energy carrying wind speed at all sites.

371

372

### 373 5.3 Energy Output

374 The wind energy output from five different commercially available wind machines with  
 375 rated power of 1.8 to 3.3 MW was determined at all the sites. The wind speed frequency  
 376 at different hub heights at all sites was determined by vertical extrapolation of wind  
 377 speed using the local wind shear exponent value of 0.217. This value of wind shear  
 378 coefficient was obtained by using measured wind speed at 10, 50 and 90 m heights AGL  
 379 at Industrial area (central).

380 The wind shear coefficient,  $\alpha$ , was calculated using the following equation [23]:

$$381 \quad \alpha = \frac{\ln(V_2) - \ln(V_1)}{\ln(Z_2) - \ln(Z_1)} \quad (16)$$

382 Where  $V_1$  and  $V_2$  are wind speeds at height  $Z_1$  and  $Z_2$  respectively.

383 The air density used in energy output calculations, was calculated using the local  
 384 pressure and temperature measurements at Industrial area (central).

385 The air density,  $\rho$  was calculated using the following equation:

$$386 \quad P = \frac{\rho}{RT} \quad (\text{Kg/m}^3) \quad (17)$$

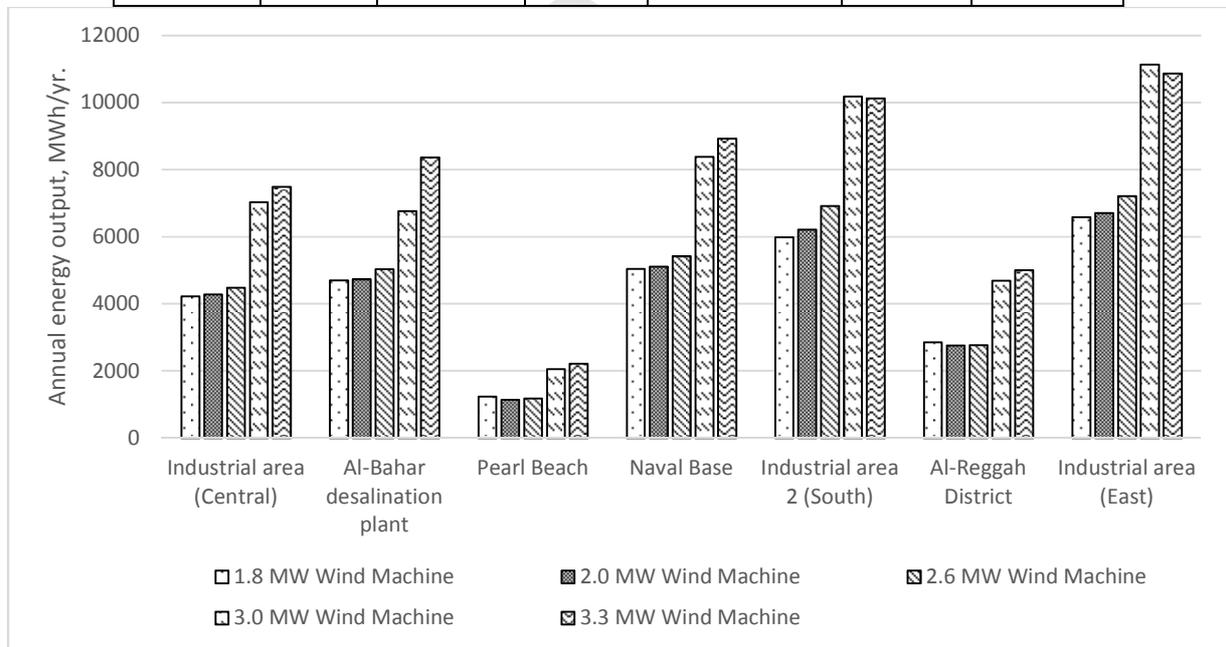
387 Where  $P$  is the air pressure in Pascals,  $R$  is the specific gas constant of air, 287.05 J/kg.K  
 388 and  $T$  is the local air temperature in degrees Kelvin. An overall mean air density at this  
 389 station was found to be 1.17 kg/m<sup>3</sup>. To find the energy output from selected wind  
 390 turbine, the number of hours the wind speed remained in different wind speed bins is  
 391 determined at the turbine hub height. Then using the power curve data of the selected  
 392 wind machine, the energy output is calculated. In this study, the energy output is  
 393 calculated using Windographer [20] software. The plant capacity factor, PCF is the ratio  
 394 of its actual annual output, to its rated output. The technical specifications of wind  
 395 machines used in this study are summarised in Table 15. The annual energy output in  
 396 MWh/year and Plant capacity factor, PCF in % is presented in Figure 15 and 16  
 397 respectively. It can be observed from these figures that the most feasible site for wind

398 farm development in Jubail city is Industrial area (East). At this site, the maximum  
 399 energy output of 11,135 MWh/year was obtained at a PCF of 41.3% from a  
 400 commercially available wind machine of 3 MW rated power.

401 The comparison of %PCF of these five wind machines at all sites reveals that wind  
 402 machine 5 (1.8 MW rated power) is most efficient at all sites in Jubail. A low rated  
 403 power wind machine is more efficient for low or mediocre wind potential areas [23].  
 404 Wind machines 1, 2 and 4 of rated power 3.3, 3.0 and 2.0 MW respectively were found  
 405 to have similar mediocre efficiency. Wind machine 3 (2.6 rated power) is found to be  
 406 least efficient for all sites Jubail.

407 Table 15 Technical data of wind machines [19]

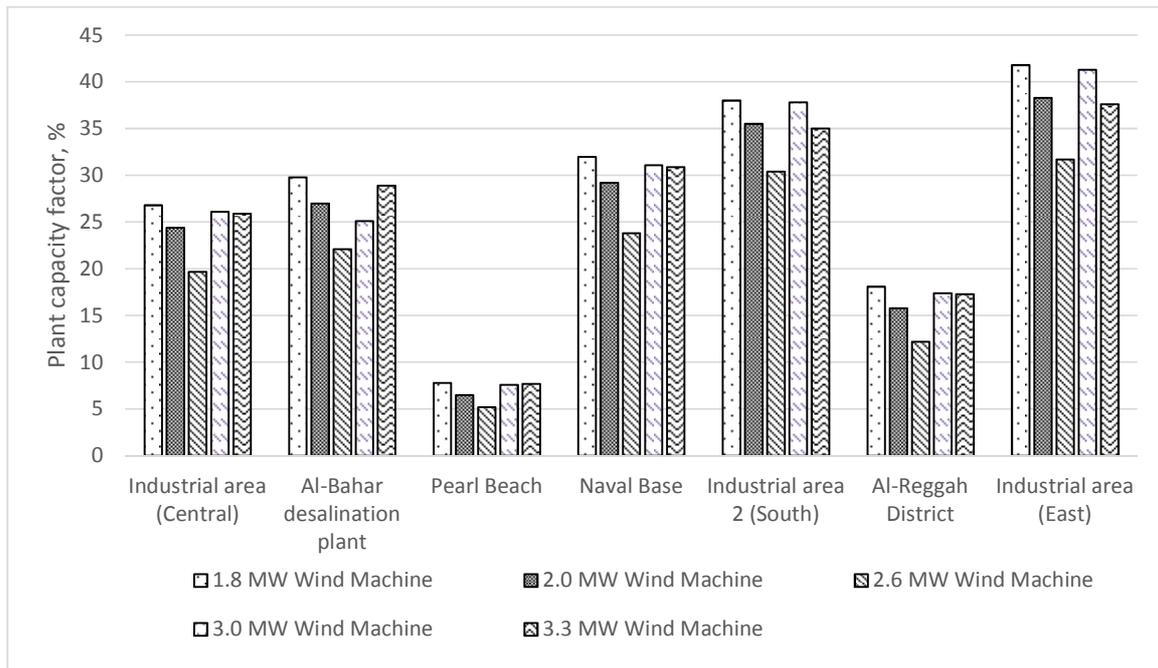
Wind machine	Cut-in speed (m/s)	Cut-out speed (m/s)	Rated output (kW)	Rated wind speed (m/s)	Hub height (m)	Rotor diameter (m)
WM 1	3	25	3300	12	117	126
WM 2	3	22.5	3000	12	119	126
WM 3	4	23	2600	15	75	100
WM 4	3	25	2000	11.5	80	110
WM 5	4	20	1800	12	80	100



408

409 Fig. 15. Annual energy output of different wind machines at all sites.

410



411

412

Fig. 16. Plant capacity factor of different wind machines at all sites.

413

## 414 6. Concluding Remarks

415 The following main observations can be drawn from this study:

416 The wind characteristics of seven locations in Jubail, Saudi Arabia were analysed. At 10  
 417 m AGL, the annual mean wind speeds varied from 2.25 m/s (standard deviation 1.109  
 418 m/s) at Pearl beach to 4.52 m/s (standard deviation 2.52 m/s) at Industrial area (east).  
 419 In general, at all sites, the highest monthly mean wind speed was observed in  
 420 February/June and the lowest in September/October. The period of higher winds  
 421 availability coincides with high power demand period of the area due to air  
 422 conditioning load. The most prevailing wind direction was from the north-west which  
 423 means that the wind machines can spread facing the prevailing wind direction.

424 The goodness-of-fit test indicators, i.e.,  $R^2$ ,  $RSME$ ,  $MBE$  and  $MAE$  show that the  
 425 maximum likelihood method is the most efficient method of Weibull parameter  
 426 estimation for Jubail region followed by least square regression method and WAsP. The

427 highest value of most probable wind speed was found to be in the range 3.2 m/s to 3.6  
428 m/s at industrial area (east) by three estimation methods. The highest value of  
429 maximum energy carrying wind speed was found to be in the range 8.6 m/s to 9.0 m/s  
430 at industrial area 2 (south) by three estimation methods.

431 The wind energy output from five different commercially available wind machines with  
432 rated output ranging from 1.8 to 3.3 MW at all the sites shows that most feasible site for  
433 wind farm development in Jubail city is Industrial area (East). At this site, the  
434 maximum energy output of 11,135 MWh/year with a PCF of 41.3% from a 3 MW rated  
435 power wind machine was obtained. The second best site for wind farm development is  
436 Industrial area 2 (south). At this site, the maximum energy output of 10,180 MWh/year  
437 with a PCF of 37.8 % from a 3 MW rated power wind machine was obtained. From  
438 %PCF, it can be concluded that Wind machine 5 (1.8 MW rated power) is most efficient  
439 at all sites in Jubail as a low rated power wind machine is more efficient for mediocre  
440 wind potential areas.

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**Highlights:**

- The wind characteristics of seven locations in Jubail, Saudi Arabia.
- Estimation of Weibull parameters by maximum likelihood, least-squares regression method (LSRM), and WASP algorithm.
- The most probable and maximum energy carrying wind speed based on Weibull scale and shape parameters at all sites.
- The goodness-of-fit test indicators like  $R^2$ , RSME, MBE and MAE.
- The energy output from a 3 MW wind machine was 11,136 MWh/yr. with a plant capacity factor (PCF) of 41.3%.