

# Heterogeneous-Homogeneous Reaction Mechanism on the Hydro Magneticnano Fluid Flow Over a Stretching Cylinder with Prescribed Heat Flux using Hermite Wavelet Method

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## Abstract

The current work provides the Hermite wavelet method (HWM) for an incompressible Nanofluid hydromagnetic flow through a stretching cylinder associated with heterogeneous-homogeneous chemical reactions. Single-walled carbon nanotubes (SWCNTs) with multi-walled carbon nanotubes (MWCNTs) as nanoparticles in the form of arranged heat flux are accounted for currently. Regulating equations, which are highly nonlinear coupled, are changed right into non-dimensional ordinary differential equations (ODEs) using appropriate similarity transformations. The desire for exceptional flow constraints on the flow feature is finalized truthfully through tables and graphs. Graphic summaries are offered for the rheological qualities of various parameters in size for velocity, temperature, concentrations, and nanoparticles. Comparison of the numerical outcomes is made with previously available consequences under particular cases, and the results are found to be in good agreement. The Hermite wavelet technique is hugely proficient and sensible for finding outcomes to this type of coupled nonlinear ODEs. The works are in outstanding accord for coupled nonlinear ordinary differential equations (ODEs) in engineering applications.

**Keywords:** Nonlinear differential equations • Operational matrix of integration • Collocation method • Hermite wavelets.

## Introduction

The majority of the applied mathematics and engineering problems happen in highly nonlinear coupled differential equations. Several pertinent areas to wave phenomena enclose fluid mechanics, elastic media, plasma, optical fibres, etc. Also, obtaining accurate results for these problems is relatively unhurt. Nonetheless, in current years, numerical methods have drastically been urbanized to be used for a nonlinear coupled system of differential equations. A few of them were solved using different analytical and numerical methods.

The magnetic properties have significant uses in applied mathematics and engineering. For example, several manufacturing types of equipment, magnetohydrodynamic generators, bearings, pumps, and boundary layer manage are exaggerated by the contact involving the magnetic field and an electrically conducting fluid. The works of many researchers have been considered relative to these applications. One of the fundamental and significant issues around the hydromagnetic conduct of boundary layers is the length of fixed or moving surfaces within sight of a transverse magnetic field. The magnetic field and boundary layer problems are related in different industrial systems employing plasma flow transverse of magnetic fields and liquid metals [1]. Numerous scientists have contemplated the impacts of electrically conducting liquids, for example, fluid metals, water mixed with a little corrosive and different fixings within sight of an attractive field on the stream and warmth move of an incompressible gooey fluid disregarding a touching surface or an extending plate in an inactive liquid. Pavlov [2] was one of the principal pioneers in this field of study. Subsequently, a spearheading work by Pavlov [2], the flow past a moving level plate or an extending sheet within the transverse magnetic field has drawn thought, and

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a decent measure of writing has been produced on this problem ([3] and references therein).

From an energy-saving point of view, improvement of heat transfer execution in frameworks is an essential subject. The low thermal conductivity of regular heat transfer liquids, for example, water and oils, is a critical constraint for improving the exhibition and the compactness of frameworks. Solids usually have a higher warm conductivity than fluids. An imaginative and novel method to upgrade heat move is to utilize strong particles in the base liquid (for example, Nanofluids) in the scope of sizes 10–50 nm. However, in recent times Nanofluid [4], an innovative type of fluid categorize outstanding to fluid-solid understanding in non-metal or metal nanoparticle suspension; started by Choi [5], to heighten thermal conductivity of the fluid. Carbon nanotubes fundamentally are the cylinder of single or numerous sheets of grapheme. Fixated on grapheme sheets, carbon nanotubes are recognized into two kinds, viz. single and multiple-walled carbon nanotubes (SWCNTs and MWCNTs). For the most part, CNT is utilized in anodes, cathodes, impetus, and different clinical and natural applications because of its remarkable mechanical and electrical properties, just as flow conductivity. CNTs contain broad uses in aviation materials since they can likewise advance the reformist aviation materials' effects. A fluid system including CNT is exceptionally electrically conducting, suggesting that they may safeguard airplane from the lightning strike. Ample literature can be found on CNTs flow problems ([6-8] and and references therein). Sheikholeslami [9] studied the support of fixed suction occurrence on Nano fluid flow during cylinder and calculated efficient thermal conductivity in adding viscosity by KKL system. Kardri et al. [10] considered heat transfer and flow features during cylinder and recognize that the dual result exists for stretching cylinder. Nadeem et al. [11] investigated the individuality of 3D stagnation-point hybrid-Nano fluid flow during cylinder and established that heat transfer rate is advanced in hybrid Nano fluid than Nano fluid.

Heat flux is characterized as the pace transfer of heat energy during a predefined surface. Numerous scientists [12-14] exhibit flow and heat broadcast overextending cylinder utilizing recommended heat transition. Alavi et al. [15] studied endorsed heat motion to catch the quality of MHD flow over a dramatically extending sheet. Heat transfer examination utilizing recommended heat motion through stretching sheet was reviewed by Majeed et al. [15].

In various manufacturing developed, burning, paint fabricating, biomedical creation, food handling, and metal delibration from commonly discovered mineral, homogeneous, heterogeneous synthetic responses happen. Bachok et al. [17] examined stagnation flow in the form of heterogeneous-homogeneous compound response over a growing surface by allowing for indistinguishable dispersion pace of reactant and auto catalyst. Muhammad et al. [18] investigated boundary layer Ferrohydrodynamic flow within sight of heterogeneous-homogeneous responses. Newly, Nano fluid flow with heterogeneous-homogeneous reactions was concentrated by Kumar et al. [19].

Practically all arithmetical modelling involves linear or nonlinear differential equations. To determine those equations impeccably, approximately, or mathematically a few specialists employ various excellent scientific, semi-analytic plans alongside lasting label of convergence. There are different mathematical techniques to solve such nonlinear differential equations; however, a few significant information counting circular occurrence determination be misplaced throughout the process of finding the solution. Hence, analytical techniques contain emerged to solve highly nonlinear differential equations such as the

Homotopy Analysis Method (HAM) [20,21], Homotopy Analysis Sumudu Transform Method (HASTM) [22], Homotopy Perturbation Method [23,24], Variational Iteration Method[25-27], q- Homotopy Analysis Transform Method (q-HAM) [28], Energy Balance Method [29,30], new extended direct algebraic method [31,32], Homotopy Analysis Transform Method (HATM) [33], Differential Transformation Method (DTM) [34,35], Exp-function Method [36-38] and Akbari-Ganj'i's Method [39].

To the very best of our understanding, no study was performed in an incompressible Nano fluidhydro magnetic flow during stretching cylinders associated with heterogeneous- homogeneous chemical reactions by using the wavelet technique. Wavelet theory is one of the recent emerging approaches in applied mathematics. It has a wide range of applications in the following fields as Signal analyses, computer science, mathematical modeling, image processing, and applied sciences. Many mathematicians' contributions towards wavelets based numerical methods are as follows: Laguerre wavelets method [40], Hermite wavelets method [41], B-spline approach [42], Wavelet collocation method [43], Generalized Hermite wavelets method [44], etc. SWCNTs and MWCNTs as nanoparticles in the look of set heat transfer motion are considered here. It has significant uses in anodes, cathodes, semiconductors, microelectronics, paper creation, glass blowing, plastic sheets, polymer preparation, food handling, ignition, aviation materials, paint industry, and mechanical different clinical and biomedical innovation, and ecological investigations. The numerical simulations have been employed using a numerical method recognized as HWM (see, for details, [41]). The Velocity and temperature distribution are advanced in MWCNT than SWCNT, and the opposite trend could be seen for concentration circulations presented in tables and graphs. The results gotten are compared to the earlier findings, which are in excellent agreement with the current work. It is expected that modern literary works will undoubtedly offer better details for the science and industrial sectors.

The organization of this paper is as follows; section 2 is devoted to the problem formulation. The progress of the Hermite matrix of integration is available in section 3. Section 4 reveals the method of solution, and the results are discussed in section 5. Finally, the conclusion is drawn in section 6.

**Problem formulation**

The basic highly nonlinear coupled ordinary differential equations (ODEs), which described in an incompressible nanofluid hydro magnetic flow through stretching cylinder associated with heterogeneous- homogeneous chemical reaction, can be summarized as introduced by ShankarGerl et al. [45]:

$$(1 + 2\gamma t)f''' + 2\gamma f'' + (1 - \phi)^{2.5} \left\{ (1 - \phi) + \phi \left( \frac{\rho_{CNT}}{\rho_f} \right) \right\} [f f'' - (f')^2] - M f' = 0 \quad (2.1)$$

$$\left[ \frac{\kappa_{nf}/\kappa_f}{(1 - \phi) + \phi \left( \frac{\rho_{CNT}}{\rho_f} \right)} \right] \{ (1 + 2\gamma t)\theta'' + 2\gamma\theta' \} + Pr(f\theta' - f'\theta) = 0 \quad (2.2)$$

$$\frac{1}{Sc} \{ (1 + 2\gamma t)g'' + 2\gamma g' \} + f g' - \lambda g G^2 = 0 \quad (2.3)$$

$$\frac{\delta}{Sc} \{ (1 + 2\gamma t)G'' + 2\gamma G' \} + f G' + \lambda g G^2 = 0 \quad (2.4)$$

$$f(0) = 0, f'(0) = 1, \theta'(0) = -1, g'(0) = K_s g(0), \delta G'(0) = -K_s g(0) \left. \vphantom{f(0)} \right\} \quad (2.5)$$

$$f'(t) \rightarrow 0, \theta(t) \rightarrow 0, g(t) \rightarrow 1, G(t) \rightarrow 0 \text{ as } t \rightarrow \infty$$

Where the prime (') represents differentiation with respect to t.

Without loss of generality, we suppose that the molecular diffusion rates of chemical species A and B are of a similar size. Besides, we think that  $D_A = D_B$ , i.e.  $\delta = 1$ ; so we believe from the hypothesis that  $g(t) + G(t) = 1$ . Thus, (2.3) and (2.4) gather together to

$$(1 + 2\gamma t)g'' + 2\gamma g' + Sc f g' - \lambda Sc g(1 - g)^2 = 0 \quad (2.6)$$

With the rehabilitated boundary conditions

$$f(0) = 0, f'(0) = 1, \theta'(0) = -1, g'(0) = K_s g(0) \left. \vphantom{f(0)} \right\} \quad (2.7)$$

$$f'(t) \rightarrow 0, \theta(t) \rightarrow 0, g(t) \rightarrow 1, \text{ as } t \rightarrow \infty$$

**Hermite wavelet operation matrix of integration**

**Hermite wavelet**

Hermite wavelets are defined in detail (Shiralashetti and Kumbinaraaiah [42]).

**Approximation of function**

We would approximate  $y(x)$  under Hermite space by elements of Hermite wavelet basis as follows:

$$y(x) = \sum_{n=1}^{\infty} \sum_{m=0}^{\infty} C_{m,n} \phi_{m,n}(x), \quad (3.1)$$

Where  $\phi_{m,n}(x)$  is given in (3.1).

We approximate  $y(x)$  by truncating the series as follows

$$y(x) \approx \sum_{m=1}^{2^{k-1}} \sum_{n=0}^{N-1} C_{m,n} \phi_{m,n}(x) = A^T \phi(x), \quad (3.2)$$

Where  $A$  and  $\phi(x)$  are  $2^{k-1} N \times 1$  matrix,

$$A^T = [C_{1,0}, \dots, C_{1,N-1}, C_{2,0}, \dots, C_{2,N-1}, \dots, C_{2^{k-1},0}, \dots, C_{2^{k-1},N-1}],$$

$$\phi(x) = [\phi_{1,0}, \dots, \phi_{1,N-1}, \phi_{2,0}, \dots, \phi_{2,N-1}, \dots, \phi_{2^{k-1},0}, \dots, \phi_{2^{k-1},N-1}]^T.$$

**Operational matrix**

**Operational matrix of integration**

Here, we extracted some Hermite wavelet basis at  $k = 1$  as follows:

$$\phi_{1,0}(x) = \frac{2}{\sqrt{\pi}}$$

$$\phi_{1,1}(x) = \frac{1}{\sqrt{\pi}}(8x - 4)$$

$$\phi_{1,2}(x) = \frac{1}{\sqrt{\pi}}(32x^2 - 32x + 4)$$

$$\phi_{1,3}(x) = \frac{1}{\sqrt{\pi}}(128x^3 - 192x^2 + 48x + 8)$$

$$\phi_{1,4}(x) = \frac{1}{\sqrt{\pi}}(512x^4 - 1024x^3 + 384x^2 + 128x - 40)$$

$$\begin{aligned} \phi_{1,5}(x) &= \frac{1}{\sqrt{\pi}}(2048x^5 - 5120x^4 + 2560x^3 + 1280x^2 - 800x + 16) \\ \phi_{1,6}(x) &= \frac{1}{\sqrt{\pi}}(8192x^6 - 24576x^5 + 15360x^4 + 10240x^3 - 9600x^2 + 384x + 368) \\ \phi_{1,7}(x) &= \frac{1}{\sqrt{\pi}}(32768x^7 - 114688x^6 + 86016x^5 + 71680x^4 - 89600x^3 + 5376x^2 + 10304x - 928) \\ \phi_{1,8}(x) &= \frac{1}{\sqrt{\pi}}(131072x^8 - 524288x^7 + 458752x^6 + 458752x^5 - 716800x^4 + \\ &\quad 57344x^3 + 164864x^2 - 29696x - 3296) \\ \phi_{1,9}(x) &= \frac{1}{\sqrt{\pi}}(524288x^9 - 2359296x^8 + 2359296x^7 + 2752512x^6 - 5160960x^5 + 516096x^4 + \\ &\quad 1978368x^3 - 534528x^2 - 118656x + 21440) \\ \phi_{1,10}(x) &= \frac{1}{\sqrt{\pi}}(2097152x^{10} - 10485760x^9 + 11796480x^8 + 15728640x^7 - 34406400x^6 + \\ &\quad 4128768x^5 + 19783680x^4 - 7127040x^3 - 2373120x^2 + 857600x + 16448) \\ \phi_{1,11}(x) &= \frac{1}{\sqrt{\pi}}(8388608x^{11} - 46137344x^{10} + 57671680x^9 + 86507520x^8 - 216268800x^7 + \\ &\quad 30277632x^6 + 174096384x^5 - 78397440x^4 - 34805760x^3 + 18867200x^2 + 723712x - 461696) \\ \phi_{1,12}(x) &= \frac{1}{\sqrt{\pi}}(33554432x^{12} - 201326592x^{11} + 276824064x^{10} + 461373440x^9 - 1297612800x^8 + 207618048x^7 + \\ &\quad 1392771072x^6 - 752615424x^5 - 417669120x^4 + 301875200x^3 + 17369088x^2 - 22161408x + 561536) \end{aligned}$$

Where,

$$\phi_9(x) = [\phi_{1,0}(x), \phi_{1,1}(x), \phi_{1,2}(x), \phi_{1,3}(x), \phi_{1,4}(x), \phi_{1,5}(x), \phi_{1,6}(x), \phi_{1,7}(x), \phi_{1,8}(x)]^T$$

Now integrate above first nine basis concerning x limit from 0 to x, then express as a linear combination of Hermite wavelet basis as,

$$\begin{aligned} \int_0^x \phi_{1,0}(x) &= \left[ \frac{1}{2} \quad \frac{1}{4} \quad 0 \right] \phi_9(x) \\ \int_0^x \phi_{1,1}(x) &= \left[ \frac{-1}{4} \quad 0 \quad \frac{1}{8} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \phi_{1,2}(x) &= \left[ \frac{-1}{3} \quad 0 \quad 0 \quad \frac{1}{12} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \phi_{1,3}(x) &= \left[ \frac{5}{4} \quad 0 \quad 0 \quad 0 \quad \frac{1}{16} \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \phi_{1,4}(x) &= \left[ \frac{-2}{5} \quad 0 \quad 0 \quad 0 \quad 0 \quad \frac{1}{20} \quad 0 \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \phi_{1,5}(x) &= \left[ \frac{-23}{3} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad \frac{1}{24} \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \phi_{1,6}(x) &= \left[ \frac{116}{7} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad \frac{1}{28} \quad 0 \right] \phi_9(x) \\ \int_0^x \phi_{1,7}(x) &= \left[ \frac{103}{2} \quad 0 \quad \frac{1}{32} \right] \phi_9(x) \\ \int_0^x \phi_{1,8}(x) &= \left[ \frac{-2680}{9} \quad 0 \right] \phi_9(x) + \frac{1}{36} \phi_{1,9}(x) \end{aligned}$$

Hence,

$$\int_0^x \phi(x) dx = H_{9,9} \phi_9(x) + \bar{\phi}_9(x)$$

Where,

$$H_{9,9} = \begin{bmatrix} \frac{1}{2} & \frac{1}{4} & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{-1}{4} & 0 & \frac{1}{8} & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{-1}{3} & 0 & 0 & \frac{1}{12} & 0 & 0 & 0 & 0 & 0 \\ \frac{5}{4} & 0 & 0 & 0 & \frac{1}{16} & 0 & 0 & 0 & 0 \\ \frac{-2}{5} & 0 & 0 & 0 & 0 & \frac{1}{20} & 0 & 0 & 0 \\ \frac{-23}{3} & 0 & 0 & 0 & 0 & 0 & \frac{1}{24} & 0 & 0 \\ \frac{116}{7} & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{28} & 0 \\ \frac{103}{2} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{32} \\ \frac{-2680}{9} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}, \bar{\phi}_9(x) = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ \frac{1}{36} \phi_{1,9}(x) \end{bmatrix}$$

Next, twice integration of above nine basis is given below

$$\begin{aligned} \int_0^x \int_0^x \phi_{1,0}(x) dx dx &= \left[ \frac{3}{16} \quad \frac{1}{8} \quad \frac{1}{32} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \int_0^x \phi_{1,1}(x) dx dx &= \left[ \frac{-1}{6} \quad \frac{-1}{16} \quad 0 \quad \frac{1}{96} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \int_0^x \phi_{1,2}(x) dx dx &= \left[ \frac{-1}{16} \quad \frac{-1}{12} \quad 0 \quad 0 \quad \frac{1}{192} \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \int_0^x \phi_{1,3}(x) dx dx &= \left[ \frac{3}{5} \quad \frac{5}{16} \quad 0 \quad 0 \quad 0 \quad \frac{1}{320} \quad 0 \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \int_0^x \phi_{1,4}(x) dx dx &= \left[ \frac{-7}{12} \quad \frac{-1}{10} \quad 0 \quad 0 \quad 0 \quad 0 \quad \frac{1}{480} \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \int_0^x \phi_{1,5}(x) dx dx &= \left[ \frac{-22}{7} \quad \frac{-23}{12} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad \frac{1}{672} \quad 0 \right] \phi_9(x) \\ \int_0^x \int_0^x \phi_{1,6}(x) dx dx &= \left[ \frac{81}{8} \quad \frac{29}{7} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad \frac{1}{896} \right] \phi_9(x) \\ \int_0^x \int_0^x \phi_{1,7}(x) dx dx &= \left[ \frac{148}{9} \quad \frac{103}{8} \quad 0 \right] \phi_9(x) + \frac{1}{1152} \phi_{1,9}(x) \\ \int_0^x \int_0^x \phi_{1,8}(x) dx dx &= \left[ \frac{-773}{5} \quad \frac{-670}{9} \quad 0 \right] \phi_9(x) + \frac{1}{1440} \phi_{1,10}(x) \end{aligned}$$

Hence,

$$\int_0^x \int_0^x \phi(x) dx dx = H'_{9,9} \phi_9(x) + \bar{\phi}'_9(x)$$

Where,

$$H'_{9,9} = \begin{bmatrix} \frac{3}{16} & \frac{1}{8} & \frac{1}{32} & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{-1}{6} & \frac{-1}{16} & 0 & \frac{1}{96} & 0 & 0 & 0 & 0 & 0 \\ \frac{-1}{16} & \frac{-1}{12} & 0 & 0 & \frac{1}{192} & 0 & 0 & 0 & 0 \\ \frac{3}{5} & \frac{5}{16} & 0 & 0 & 0 & \frac{1}{320} & 0 & 0 & 0 \\ \frac{-7}{12} & \frac{-1}{10} & 0 & 0 & 0 & 0 & \frac{1}{480} & 0 & 0 \\ \frac{-22}{7} & \frac{-23}{12} & 0 & 0 & 0 & 0 & 0 & \frac{1}{672} & 0 \\ \frac{81}{8} & \frac{29}{7} & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{896} \\ \frac{148}{9} & \frac{103}{8} & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{-773}{5} & \frac{-670}{9} & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}, \bar{\phi}'_9(x) = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ \frac{1}{1152} \phi_{1,9}(x) \\ \frac{1}{1440} \phi_{1,10}(x) \end{bmatrix}$$

Again triple integration of above nine basis is given by,

$$\begin{aligned} \int_0^x \int_0^x \int_0^x \phi_{1,0}(x) dx dx dx &= \left[ \frac{5}{96} \quad \frac{3}{64} \quad \frac{1}{64} \quad \frac{1}{384} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \int_0^x \int_0^x \phi_{1,1}(x) dx dx dx &= \left[ \frac{-7}{128} \quad \frac{-1}{24} \quad \frac{-1}{128} \quad 0 \quad \frac{1}{1536} \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \int_0^x \int_0^x \phi_{1,2}(x) dx dx dx &= \left[ \frac{-1}{80} \quad \frac{-1}{64} \quad \frac{-1}{96} \quad 0 \quad 0 \quad \frac{1}{3840} \quad 0 \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \int_0^x \int_0^x \phi_{1,3}(x) dx dx dx &= \left[ \frac{19}{96} \quad \frac{3}{20} \quad \frac{5}{128} \quad 0 \quad 0 \quad 0 \quad \frac{1}{7680} \quad 0 \quad 0 \right] \phi_9(x) \\ \int_0^x \int_0^x \int_0^x \phi_{1,4}(x) dx dx dx &= \left[ \frac{-13}{56} \quad \frac{-7}{48} \quad \frac{-1}{80} \quad 0 \quad 0 \quad 0 \quad 0 \quad \frac{1}{13440} \quad 0 \right] \phi_9(x) \\ \int_0^x \int_0^x \int_0^x \phi_{1,6}(x) dx dx dx &= \left[ \frac{133}{36} \quad \frac{81}{32} \quad \frac{29}{56} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) + \frac{1}{32256} \phi_{1,9}(x) \\ \int_0^x \int_0^x \int_0^x \phi_{1,6}(x) dx dx dx &= \left[ \frac{133}{36} \quad \frac{81}{32} \quad \frac{29}{56} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) + \frac{1}{32256} \phi_{1,9}(x) \\ \int_0^x \int_0^x \int_0^x \phi_{1,7}(x) dx dx dx &= \left[ \frac{193}{40} \quad \frac{37}{9} \quad \frac{103}{64} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) + \frac{1}{46080} \phi_{1,10}(x) \\ \int_0^x \int_0^x \int_0^x \phi_{1,8}(x) dx dx dx &= \left[ \frac{-1211}{22} \quad \frac{-773}{20} \quad \frac{-335}{36} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \right] \phi_9(x) + \frac{1}{46080} \phi_{1,11}(x) \end{aligned}$$

Hence,

$$\int_0^x \int_0^x \int_0^x \phi(x) dx dx dx = H_{9 \times 9}'' \phi_9(x) + \bar{\phi}_9''(x)$$

where,

$$H_{9 \times 9}'' = \begin{bmatrix} \frac{5}{96} & \frac{3}{64} & \frac{1}{64} & \frac{1}{384} & 0 & 0 & 0 & 0 & 0 \\ \frac{7}{128} & \frac{1}{24} & \frac{1}{128} & 0 & \frac{1}{1536} & 0 & 0 & 0 & 0 \\ \frac{11}{80} & \frac{1}{64} & \frac{1}{96} & 0 & 0 & \frac{1}{3840} & 0 & 0 & 0 \\ \frac{19}{96} & \frac{3}{20} & \frac{5}{128} & 0 & 0 & 0 & \frac{1}{7680} & 0 & 0 \\ \frac{13}{56} & \frac{7}{48} & \frac{1}{80} & 0 & 0 & 0 & 0 & \frac{1}{13440} & 0 \\ \frac{65}{64} & \frac{11}{14} & \frac{23}{96} & 0 & 0 & 0 & 0 & 0 & \frac{1}{21504} \\ \frac{133}{36} & \frac{81}{32} & \frac{29}{56} & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{193}{40} & \frac{37}{9} & \frac{103}{64} & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{1211}{22} & \frac{273}{20} & \frac{335}{36} & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}, \bar{\phi}_9''(x) = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ \frac{1}{32256} \phi_{1,9}(x) \\ \frac{1}{46080} \phi_{1,10}(x) \\ \frac{1}{63360} \phi_{1,11}(x) \end{bmatrix}$$

In the same way, we can create matrices for our convenience. In the result section, the third-order highly nonlinear coupled ordinary differential equations are solved using N=6 and 9. So, we generated matrices of order 9\*9 up to a triple operational matrix of integration.

**Method of solution**

Now, assume that

$$f'''(x) = A^T \psi(x) \tag{4.1}$$

Integrate Eq. (4.1) with respect to x form 0 to x, we get,

$$f''(x) = f''(0) + A^T [P\psi(x) + \bar{\psi}(x)] \tag{4.2}$$

Integrate (4.2) with respect to x form 0 to x

$$f'(x) = f'(0) + x f''(0) + A^T [P'\psi(x) + \bar{\psi}'(x)] \tag{4.3}$$

Integrate (4.3) concerning x form 0 to x

$$f(x) = f(0) + x f'(0) + \frac{x^2}{2} f''(0) + A^T [P''\psi(x) + \bar{\psi}''(x)] \tag{4.4}$$

$$f(x) = x + \frac{x^2}{2} f''(0) + A^T [P''\psi(x) + \bar{\psi}''(x)] \tag{4.5}$$

Put  $x = \eta$  in (4.3) we get

$$f'(\eta) = 1 + \eta f''(0) + A^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \tag{4.6}$$

$$f''(0) = \frac{1}{\eta} \left\{ -1 - A^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right\} \tag{4.7}$$

Fit (4.7) in (4.2, 4.3, 4.5) we get

$$f''(x) = \frac{1}{\eta} \left\{ -1 - A^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right\} + A^T [P\psi(x) + \bar{\psi}(x)] \tag{4.8}$$

$$f'(x) = 1 + \frac{x}{\eta} \left\{ -1 - A^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right\} + A^T [P'\psi(x) + \bar{\psi}'(x)] \tag{4.9}$$

$$f(x) = x + \frac{x^2}{2} \frac{1}{\eta} \left\{ -1 - A^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right\} + A^T [P''\psi(x) + \bar{\psi}''(x)] \tag{4.10}$$

Again put

$$\theta''(x) = B^T \psi(x) \tag{4.11}$$

Integrate (4.11) with respect to x form 0 to x

$$\theta'(x) = -1 + B^T [P\psi(x) + \bar{\psi}(x)] \tag{4.12}$$

Integrate (4.12) concerning x form 0 to x

$$\theta(x) = \theta(0) - x + B^T [P'\psi(x) + \bar{\psi}'(x)] \tag{4.13}$$

Put  $x = \eta$  in the above equation, we get

$$\theta(\eta) = \theta(0) - \eta + B^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \tag{4.14}$$

$$\theta(0) = \eta - B^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \tag{4.15}$$

Form (4.15) and (4.13), we get

$$\theta(x) = \eta - B^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} - x + B^T [P'\psi(x) + \bar{\psi}'(x)] \tag{4.16}$$

Again put

$$g''(x) = C^T \psi(x) \tag{4.17}$$

Integrate (4.17) concerning x form 0 to x

$$g'(x) = g'(0) + C^T [P\psi(x) + \bar{\psi}(x)] = K_s g(0) + C^T [P\psi(x) + \bar{\psi}(x)] \tag{4.18}$$

Integrate (4.18) concerning x form 0 to x

$$g(x) = g(0) + K_s g(0)x + C^T [P'\psi(x) + \bar{\psi}'(x)] \tag{4.19}$$

Put  $x = \eta$  in the above equation, we get

$$g(\eta) = g(0) [1 + K_s \eta] + C^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \tag{4.20}$$

$$g(0) = \frac{1}{[1 + K_s \eta]} \left( 1 - C^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right) \tag{4.21}$$

form (4.21) and (4.18), (4.19) we get

$$g'(x) = K_s \frac{1}{[1 + K_s \eta]} \left( 1 - C^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right) + C^T [P\psi(x) + \bar{\psi}(x)] \tag{4.22}$$

$$g(x) = \frac{[1 + K_s x]}{[1 + K_s \eta]} \left( 1 - C^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right) + C^T [P'\psi(x) + \bar{\psi}'(x)] \tag{4.23}$$

Again put

$$G''(x) = D^T \psi(x) \tag{4.24}$$

Integrate (4.24) concerning x form 0 to x

$$G'(x) = G'(0) + D^T [P\psi(x) + \bar{\psi}(x)] = -\frac{K_s}{\delta} g(0) + D^T [P\psi(x) + \bar{\psi}(x)] \tag{4.25}$$

$$G'(x) = -\frac{K_s}{\delta} \frac{1}{[1 + K_s \eta]} \left( 1 - C^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right) + D^T [P\psi(x) + \bar{\psi}(x)] \tag{4.26}$$

Integrate (4.26) concerning x form 0 to x

$$G(x) = G(0) - \frac{K_s}{\delta} \frac{x}{[1 + K_s \eta]} \left( 1 - C^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right) + D^T [P\psi(x) + \bar{\psi}(x)] \tag{4.27}$$

Put  $x = \eta$  in the above equation, we get

$$G(\eta) = G(0) - \frac{K_s}{\delta} \frac{\eta}{[1 + K_s \eta]} \left( 1 - C^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right) + D^T [P\psi(x) + \bar{\psi}(x)]_{x=\eta} \tag{4.28}$$

$$G(0) = \frac{K_s}{\delta} \frac{\eta}{[1 + K_s \eta]} \left( 1 - C^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right) - D^T [P\psi(x) + \bar{\psi}(x)]_{x=\eta} \tag{4.29}$$

form (4.29) and (4.27), we get

$$G(x) = \frac{K_s}{\delta} \frac{\eta}{[1 + K_s \eta]} \left( 1 - C^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right) - D^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} - \frac{K_s}{\delta} \frac{x}{[1 + K_s \eta]} \left( 1 - C^T [P'\psi(x) + \bar{\psi}'(x)]_{x=\eta} \right) + D^T [P\psi(x) + \bar{\psi}(x)] \tag{4.30}$$

Substitute  $f''', f'', f', f, g'', g', g, \theta'', \theta', \theta, G'', G', G$  in a given system of highly nonlinear coupled ODEs. Then collate each ODE by the following collocation points  $x_i = \frac{2i-1}{2N}$ . Where  $i = 1, 2, 3, \dots, N$  and

$N$  represents the size of the operational matrix. Then we get a nonlinear algebraic equations system and solve this system by Newton's method that yields the Hermite wavelet's unknown coefficients. Substitute these unknown coefficients to  $f, \theta, g$  and  $G$  will reflect the Laguerre wavelet-based numerical solutions for a given system of nonlinear coupled ODEs.

## Results and Discussions

To find the Hermite wavelet functional matrix method's efficiency, we solved highly nonlinear coupled ordinary differential equations and compared the calculated outcomes with other methods available in the literature. From Table 2, we compare the Runge-Kutta method, Finite difference method, DTM, and HWM methods when  $M = \gamma = \phi = 0$  and in the nonexistence of a chemical reaction. Hence we can be fulfilled that HWM is a more suitable method for solving highly nonlinear coupled ODEs (2.1–2.5). The physical behaviour of different known physical parameters in the confirmed flow problem on the velocity, temperature, and concentration fields is presented in Figures 1-10.

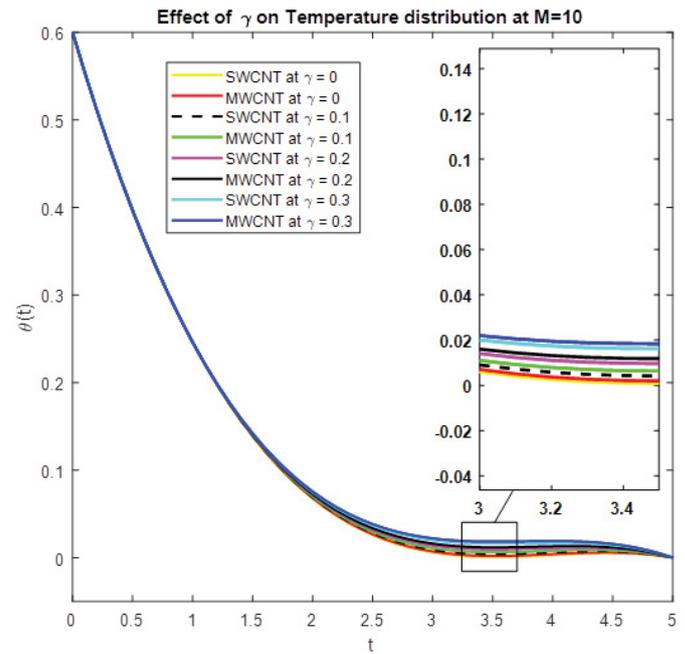
The velocity curves for different values of curvature parameter  $\gamma$  are presented in Figure 1. We noticeable the increase in fluid velocity during growth. Temperature dispersion because of curvature parameter  $\gamma$  have been depicted in Figure 2. Temperature dispersion enhances like velocity profiles for increasing  $\gamma$ . Velocity and temperature curves are superior in MWCNT than SWCNT. The concentration curves (Figure 3) support an undefined way like temperature curves when  $\gamma$  heightens and afterward concentration boundary layers obtain thicker. The velocity curves for different values of nanoparticle concentration  $\phi$  are presented in Figure 4. We evident the improvement in liquid velocity for increasing  $\phi$  and henceforth impetus boundary layer gets thicker. Figure 5 shows that the temperature curves for various nanoparticle concentration values  $\phi$ , and it uncovered that temperature curves increase with the increase in  $\phi$ . This choice with an actual component that  $\phi$  increases shows thermal conductivity quickens and in like manner thermal boundary layer width gets increased. Velocity

**Table 1.** The dimensionless parameters are introduced in equations (2.1-2.5).

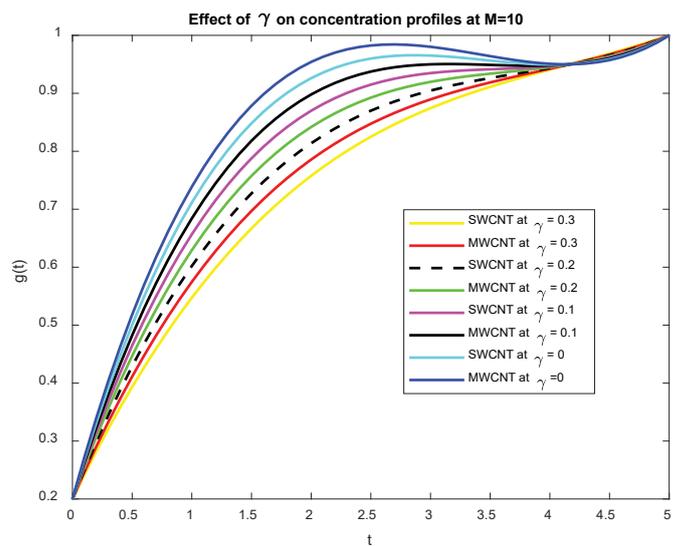
Definition	Notation	Parameter
$\left(\frac{v_f L}{U_0}\right)^{0.5}$	$\gamma$	curvature parameter
$\frac{D_B}{D_A}$	$\delta$	the ratio of the mass diffusion coefficient
$\frac{\mu_f (C_p)_f}{\kappa_f}$	$Pr$	Prandtl number
$\frac{v_f}{D_A}$	$Sc$	Schmidt number
$\frac{k_r a_0^2 L}{U_0}$	$\lambda$	Homogeneous chemical reaction factor
$\frac{k_s \sqrt{v_f L}}{D_A U_0}$	$K_s$	Heterogeneous chemical reaction factor
$\frac{\sigma_{nf} B_0^2 L}{\rho_f U_0}$	$M$	Revised magnetic parameter

**Table 2.** Variation of  $\theta(0)$  for different values of  $Pr$ .

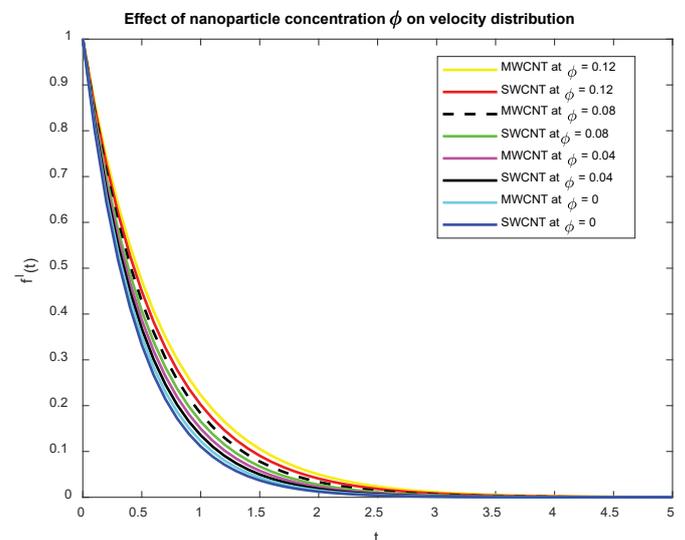
$Pr$	Bachok and Ishak [14]	Elbashbeshy [13]	SankarGiri et al. [45]	Present Method	
				HWM (N=6)	HWM(N=12)
0.72	1.2367	1.2253	1.236582	1.20374	1.23667
1.00	1.0000	1.0000	0.999999	0.98872	1.00000
6.70	0.3333	-	0.333303	0.30131	0.33331
10.0	0.2688	0.2688	0.268768	0.27621	0.26887



**Figure 1.** Velocity curves for different values of curvature parameter.



**Figure 2.** Temperature curves for different values of curvature parameter.



**Figure 3.** Concentration curves for different values of curvature parameter.

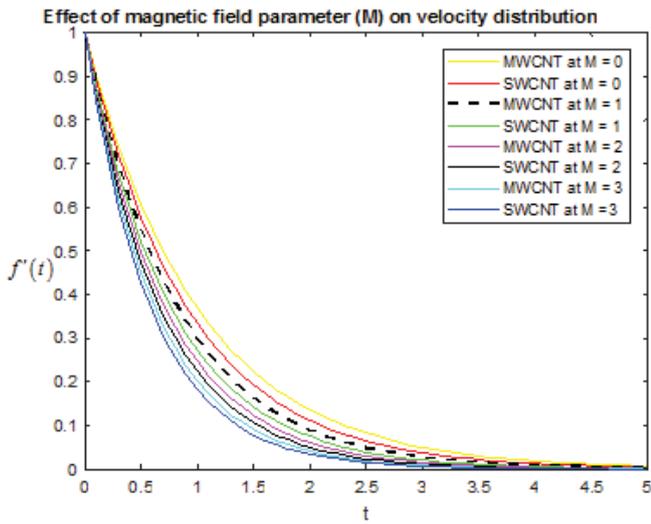


Figure 4. Velocity curves for different values of nanoparticle concentration.

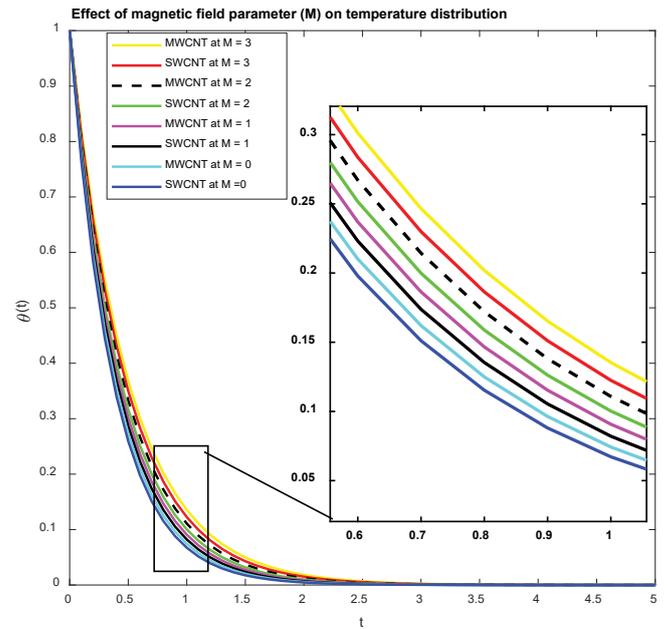


Figure 7. Temperature curves for different values of the magnetic field parameter.

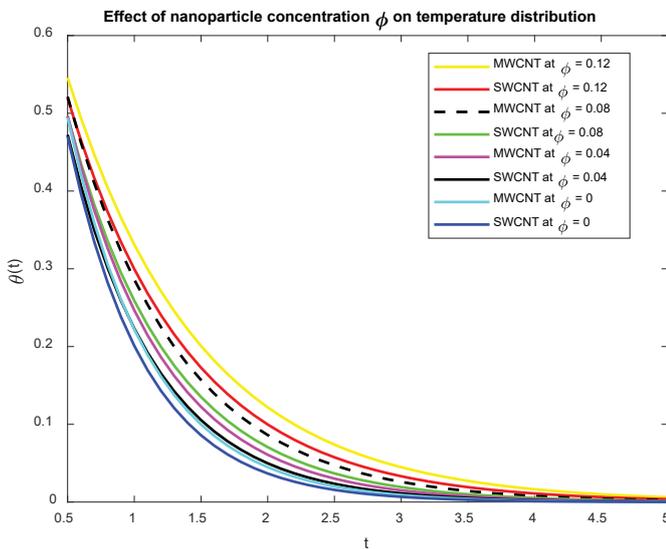


Figure 5. Temperature curves for different values of nanoparticle concentration.

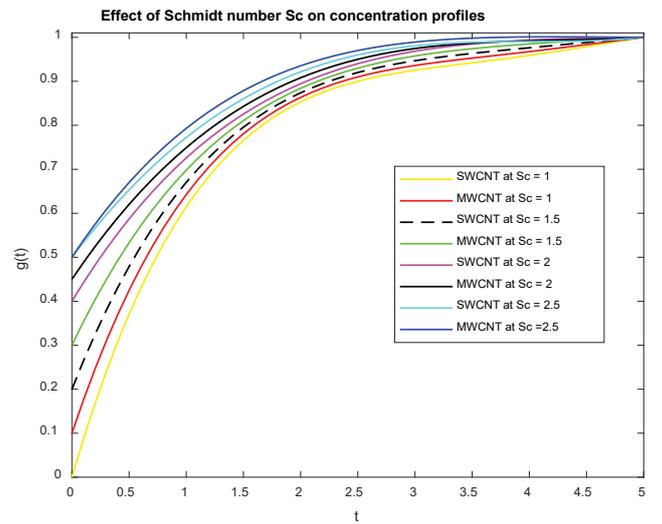


Figure 8. Concentration curves for different values of Schmidt number.

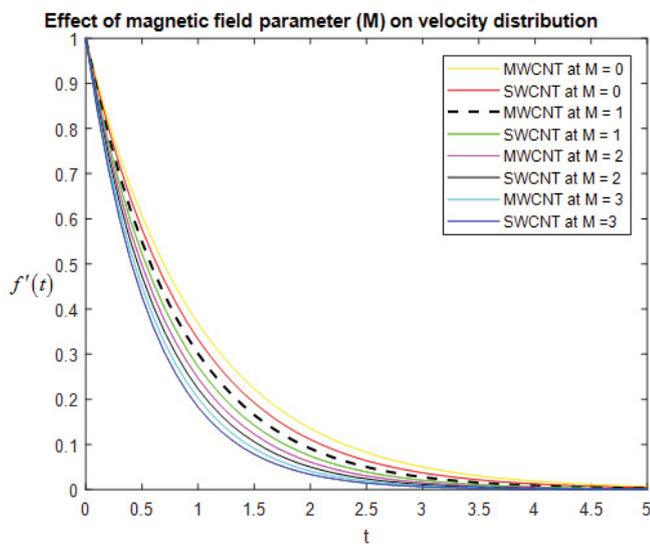


Figure 6. Velocity curves for different values of the magnetic field parameter.

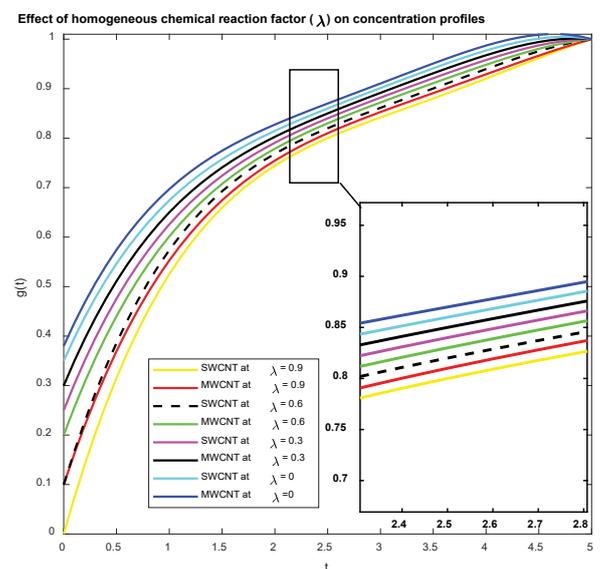
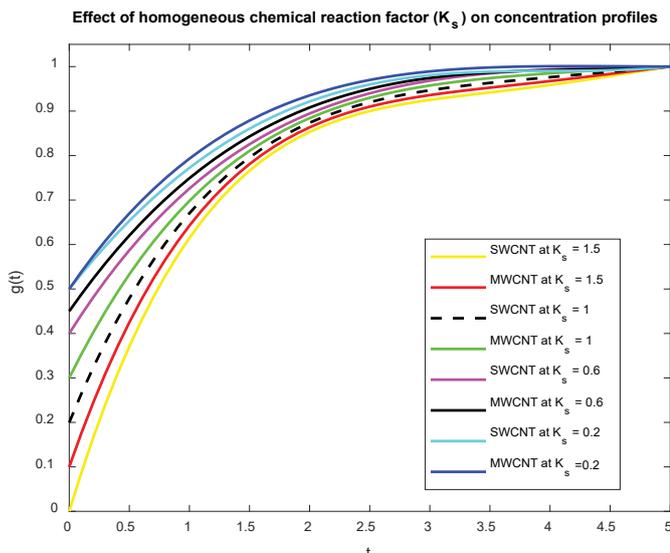


Figure 9. Concentration curves for different values of homogeneous chemical reaction factor.



**Figure 10.** Concentration curves for different values of heterogeneous chemical reaction factor.

and temperature curves are advanced in MWCNT than SWCNT. The velocity curves for different values of the magnetic-field parameter  $M$  are presented in Figure 6. The graphical agreement embraces the rejection of liquid speed while the potency of the magnetic field gets engorged. Figure 7 revealed how magnetic-field parameter  $M$  follows up on temperature field. We comprehend that temperature dispersion is supported with  $M$ . While extra work total needed to loosen up nanofluid contrary to the magnetic field's purpose, heats transport nanofluid and improve temperature curves. Velocity and temperature curves are advanced in MWCNT than SWCNT. Schmidt number is perceived as a proportion of the rate of momentum diffusivity to the rate of mass diffusivity; thus, higher estimations of  $Sc$  suggest little mass distribution and as an aftereffect concentration curves refute, which are depicted in Figure 8. Concentration curves are superior in SWCNT than MWCNT. Uniform chemical reaction factor  $\lambda$  intensifies the spices  $B$ , which balanced nanoparticles in it. Like this nanoparticles' creation upgrades. This legitimizes that  $g$  is increased in the scheme as explained in Figure 9. In Figure 10, we reveal the thump of heterogeneous chemical reaction factor ( $K_s$ ) on the flow. The first-order heterogeneous response happens in the endurance of solid engrossing warmed heated surface, which absorbs  $A$  and  $B$  and afterward a reply happens and following flavours  $B$  emerged from the divider thermally energizing nanoparticle in it. Consequently  $g$  upturns. Concentration curves are greater in SWCNT than MWCNT.

## Conclusion

This manuscript enlarges heterogeneous-homogeneous chemical reaction in an incompressible nanofluid hydromagnetic flow through a stretching cylinder. SWCNTs, as well as MWCNTs nanoparticles, are considered at this point. We reformed coupled PDEs to couple highly nonlinear ODEs using the similarity technique and then resolved by HWM. The outcome process of HWM shows the competence of HWM for solving highly nonlinear differential equations, which is shown in the tables and figures. The computed solution via this technique is close to a numerical solution. Moreover, the HWM is more capable than any numerical method to solve this type of equations. The critical outcomes of the foregoing study may be summarized as follows:

The velocity curves are the same for different values  $\gamma$  and  $\phi$ .

Temperature curves are improved with  $\gamma$ ,  $M$ , and  $\phi$ .

Velocity and temperature curves are advanced in MWCNT than SWCNT, and opposite results are seen in the case of concentration curves.

Concentration curves increase for chemical reaction factor.

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