

Structural and optoelectronic properties of CsSnBr₃ metal halide perovskite as promising materials toward novel-generation optoelectronics

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In this study, first-principles density functional theory (DFT) calculations of the structural and optoelectronic properties of Sn-based inorganic metal halide perovskite CsSnBr₃ are carried out and discussed in details. The Wu-Cohen (WC)-Generalized Gradient Approximation (GGA) based on the full-potential linearized augmented plane-wave (FP-LAPW) method is used to optimize the geometry structure of unit cell and then find the accurate optoelectronic properties of CsSnBr₃. Analysis of structural optimization results revealed that the lattice parameters ($a_0 = 5.776 \text{ \AA}$) and unit cell volume of CsSnBr₃ are exactly consistent with the experiments reports. Based on the results of band structures and density of states, CsSnBr₃ is found to be nonmagnetic semiconductor with suitable direct band gap of ($E_g = 0.610 \text{ eV}$) along the R symmetry point. In addition, the calculations of optical properties of CsSnBr₃, such as the real $\epsilon_1(\omega)$ and imaginary $\epsilon_2(\omega)$ parts of the dielectric function, $\epsilon(\omega)$, absorption coefficient $\alpha(\omega)$, reflectivity $R(\omega)$ and refractive index $n(\omega)$, have been performed in the photonic energy range of (0.0 – 15.0 eV). Finally, the results attained in the present study, which include the stable crystal structure and the high accurate optoelectronic properties such as appropriate direct band gap and high absorption of visible radiation, confirm the possible utilization of CsSnBr₃ materials in novel optoelectronics applications as photovoltaic solar cells, photosensors, photodetectors, photodiodes and other related optoelectronics devices.

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1. Introduction

In the last few years, the distinctive family of halide perovskite solar cells (HPSCs) with an exclusive chemical formula (ABX₃) have attracted extreme interest as excellent spectra absorbers for photovoltaics and other novel optoelectronics applications. According to the sort of ion or element that occupies the A-site, the ABX₃ family can be classified into two famous classes of halide compounds: (i) organic-inorganic halide perovskites and (ii) all-inorganic halide perovskites. The crystal of the first class contains organic ions [A = Methylammonium (MA), (CH₃NH₃)BX₃; Formamidinium (FA), (HC(NH₂)₂BX₃]. While, in all-inorganic halide perovskites, A-site is often occupied by a metallic element (A = Metal). The second class is considered one of most studied compounds during the current era, where various all inorganic HPSCs with ABX₃ (A = K, Rb, Cs; B = Metal; X= Halogen) have been created and investigated. Besides studying their unique characteristics like flexible crystal structure, tunable semiconducting band-gap ($E_g < 2.5 \text{ eV}$) [1-3], high charge-carrier mobility, large optical absorption coefficient and high composition stability [4], research also seek for promising and multi-faceted thermal, electrical and optical applications that give an extraordinary power-conversion efficiency (~24.0 %) in photovoltaic solar cells technologies [5-12].

Photovoltaic solar cells are novel devices utilized mainly to convert the free solar radiation into an electrical current through the photovoltaic effect. These devices present an optoelectronics

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design based on the combination of two semiconductor slabs with different electron concentration [4,8]. As shown in (Fig. 1) these slabs are mainly made from two different electrical materials that can be characterized as N-type semiconductor material, which has an excess of negative charges, i.e. electrons, and P-type semiconductor material, which has an excess of positive charges, i.e. holes. As a result, when both N-type and P-type slabs are in contact, some energetic electrons flow from the N-type slab to the P-type slab, and some energetic holes flow conversely from the P-type slab to the N-type slab, which produces a diffusion current through the P-N junction. Moreover, the fixed ions near the two limits of P-N junction generate an electric field in the opposite direction to the diffusion of these charges, which leads to the generation of drift current. As it is well known that the potential barriers establish at the P-N junction as a result of the balance between this drift current and diffusion current at equilibrium, which makes the net current that flows through this structure equal to zero [7,8]. When the incident solar radiation strikes the surface of solar cell, the N-type electrons absorb the energy carried by its photons, which breaks their chemical bonds and creates electron-hole pairs in the N-type material. These two charge carriers are pushed up by the electric field, causing them to flow through the P-N junction solar cell, and if a load is connected, an electric potential difference between the terminals of solar cell will be established, which generates an electric current flowing through the external electrical load in the outer circuit.

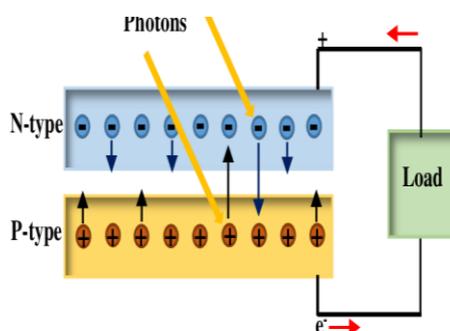


Fig. 1. The photovoltaic effect and schematic illustration of P-N junction solar cell.

Therefore, the current challenge is to synthesize ABX_3 solid materials that provide suitable properties, include notable chemical stability at high temperatures, high electrical power conversion efficiency, broad emission and tunable semiconducting E_g [13]. Motivated by the effect of A- and B-site substitution in ABX_3 unit cell, we extended this concept to produce a promising compound of $CsSnBr_3$ and explore its structural, and optoelectronic properties. Recently, several research studies have been done on numerous cubic compounds within ABX_3 family, which is the most common structure in materials science and solid state physics. Due to the possibility of substituting the three positions A, B and X in ABX_3 by suitable metallic elements and halogens, respectively, these compounds can have all potentials to become promising materials with multifunctional properties [14-16]. Thus, most ABX_3 compounds can have remarkable performances in many fields of future applications, such as in photovoltaic solar cells (Fig. 1) [17], memories, sensors and diode devices [3,7], electrodes [15], as well as in ferroelectricity, superconductivity and piezoelectricity applications [14]. These physical properties have attracted widespread attention of scientists, engineers and researchers to devote enormous efforts on these ABX_3 materials to investigate and detect novel and useful properties for different future applications [1,8,11,14].

In this work, in order to contribute and develop the materials research in this field as well as to explore new properties among the HPSC compounds that are not yet predicted experimentally or theoretically, we have intended to investigate the main physical properties of ABX_3 by choosing its sites as: A is an alkali-metal, i.e. Cesium atom ($A = Cs$), B is post-transition metal ($B = Sn$) and X is a halogen element ($X = Br$). This study proves a distinguished contribution in this field by examining the effect of site substitution ($A = Cs$, $B = Sn$) and applying WC method on the structural and optoelectronic properties of ABX_3 compared to the published

properties of related halide perovskites. The main goal of this study, is to provide GGA theoretical bases to realize all these physical properties of cesium bromide CsSnBr_3 and their dependence on the type of B-site. All these calculations were carried out by utilizing the WC method based on the Generalized Gradient Approximation (GGA), to well examine the structural, electronic and optical properties of CsSnBr_3 . As a result of this work and based on their obtained chemical and physical properties, we can expect the possible applications of CsSnBr_3 halide perovskites in photovoltaic solar cells, photodetectors, photodiodes and other related optoelectronics.

2. Computational methods

The ground state properties of CsSnBr_3 are calculated using the first-principles density functional theory (DFT) [18], as executed in the WIEN2k [19] package. Full-potential linearized augmented plane-wave (FP-LAPW) method is utilized. The Wu-Cohen (WC) [18-20] method based on the Generalized Gradient Approximation (GGA) [21] is implemented to modulate the structural and optoelectronic properties of this compound. Non spin-polarized version of the WC-GGA calculations are performed to obtain the appropriate results of these properties.

In PFLAPW method, the unit cell of CsSnBr_3 contains two main regions; the first of which is a spherical region, muffin-tin (MT), where the potential is expected to be spherically symmetric, this region is definite by ($r \leq R_{\text{MT}}$) where R_{MT} is the muffin-tin radius. In all WC-GGA calculations, the R_{MT} values of the individual elements in CsSnBr_3 are set as [$R_{\text{MT}}(\text{Cs}) = 2.2$, $R_{\text{MT}}(\text{Sn}) = 2.0$ and $R_{\text{MT}}(\text{Br}) = 1.8$ a.u.]. In the MT region, the solution of the Schrödinger equation is given by a radial function times a spherical harmonic, whereas in the interstitial region (IR), the potential is considered constant and the Schrödinger equation is solved by plane wave functions.

The ground state energy convergence to (0.00001 Ry) was achieved using the total number of (k-points = 2000) in the first Brillouin zone (BZ) with a cutoff value ($R_{\text{MT}}K_{\text{max}} = 8.0$), where R_{MT} corresponds to smallest MT radius and K_{max} is the largest reciprocal lattice vector [19]. The structural optimizations of CsSnBr_3 were carried out as a first stage, where the unit cell energy has been varied with respect to its unit cell volume.

3. Results and discussion

As an initial utilization of the skills provided by the WIEN2k code, the optimized structural parameters of perovskite CsSnBr_3 are obtained from the *Energy vs. Volume* calculation in nonmagnetic (NM) and ferromagnetic (FM) phases . Fig. 2 show the predicted results of structural optimization by fitting the variation of the total energy per unit cell of CsSnBr_3 as a function of its corresponding volume by means of the Murnaghan equation of state:

$$E - E_0 = \frac{B_0 V}{B'_0} \left[\frac{(V_0/V)^{B'_0}}{(B'_0 - 1)} + 1 \right] - \left[\frac{B_0 V_0}{(B'_0 - 1)} \right] \quad (1)$$

where, E = the total energy per unit cell of CsSnBr_3 , E_0 = the ground state energy, V = the unit cell volume of CsSnBr_3 , V_0 = the equilibrium unit cell volume with lattice constants of ($a_0 = b_0 = c_0$), B_0 = the bulk modulus, and B'_0 = the pressure derivative of bulk modulus.

It is clearly that the crystal structure of CsSnBr_3 in NM phase is more stable than in FM phase because it shows less energy ($E_{\text{NM}} < E_{\text{FM}}$). Table 1 summarizes the structural data of CsSnBr_3 extracted from the optimization calculations compared with the available experimental and previous DFT results.

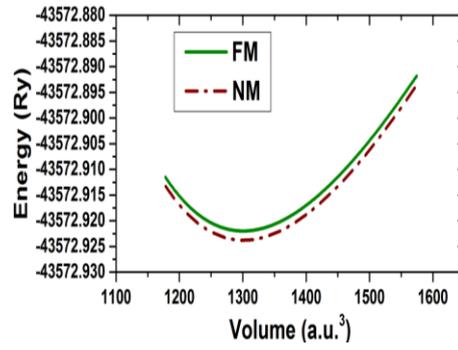


Fig. 2. The optimized of energy vs. unit cell volume of metal halide perovskite CsSnBr_3 .

Table 1. The optimized structural data of metal halide perovskite CsSnBr_3 .

Parameter	Present	Other [25,26]
S. G.	Pm-3m	Pm-3m
a_0 (Å)	5.776	5.883, 5.800
V_0 (Å ³)	192.7	
B_0 (GPa)	22.19	
B'_0 (GPa)	4.634	
T_F	1.006	
Sn-Br (Å)	2.888	
E_0 (Ry)	-43572.92	
E_g (eV)	0.610	0.600, 0.626

In view of these, it can conclude that the obtained value of a_0 is in a good agreement with those results. Also, the value of B_0 illustrates the mechanical stiffness of CsSnBr_3 which makes it more rigid material and less compressible. Alike expectation was reported for analogous metal halide perovskites within GGA studies [22]. Also, the atomic distances and positions in the cubic unit cell of CsSnBr_3 are shown in (Fig. 3), Cs at 1a (0,0,0), Sn at 1b (0.5,0.5,0.5) and Br at 3d (0.5,0,0), (0,0.5,0) and (0,0,0.5). Moreover, two important characteristics that determine the suitability of CsSnBr_3 material for the manufacture of photovoltaics solar cells and related optoelectronics devices are quantum efficiency and chemical stability. Tolerance factor [23] evaluates the chemical stability of CsSnBr_3 by means of ionic radii, as:

$$T_F = \frac{0.71 (r_{\text{Cs}} + r_{\text{Br}})}{(r_{\text{Sn}} + r_{\text{Br}})} \quad (2)$$

where, ($r_{\text{Cs}} = 2.02$ Å) in XII-coordinate system, and ($r_{\text{Sn}} = 0.89$ Å) and ($r_{\text{Br}} = 1.82$ Å) in the VI-coordinate system [24]. As a result of applying this formula, it is found that the stable cubic crystal structure of halide perovskite CsSnBr_3 gives a value close to the standard value ($T_F \approx 1.00$), which matches also the (Pm-3m; #221) symmetry.

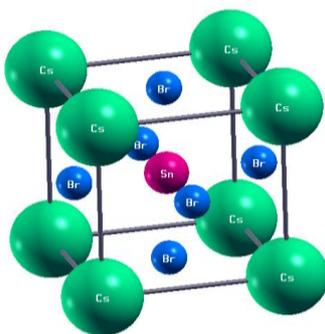


Fig. 3. The cubic crystal structure of metal halide perovskite CsSnBr_3 .

In order to study the electronic properties of CsSnBr_3 , its 2D charge density, band structure, total density of states (TDOS) and partial density of states (PDOS) have been calculated and discussed deeply as follow. First, Fig. 4 represents the charge density in (100) plane of the unit cell of CsSnBr_3 , which gives a clear picture of the chemical bonding nature between the three atoms Cs, Sn and Br in their unit cell CsSnBr_3 as well as allows to explain the charge transfer mechanisms through these bonds. It can be seen that there is formation of orbital hybridizations between p-states of cations Sn-5p and anions Br-4p. The condensed contour lines around Sn and Br indicates their covalent bond nature whereas the formation of other bonds Cs– Br have an ionic nature with minor contour lines.

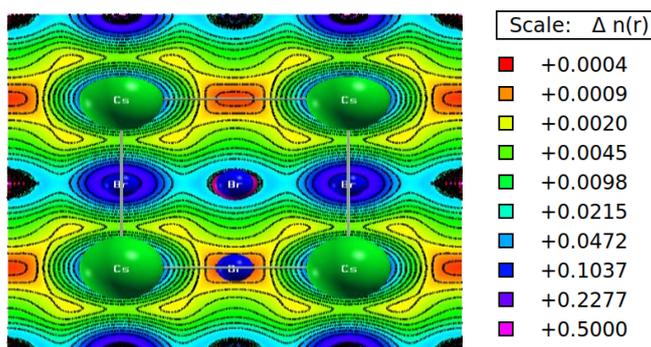


Fig. 4. The 2D charge density in (100) plane for the unit cells of metal halide perovskite CsSnBr_3 .

Second, an important parameter of semiconductor is the value of band gap (E_g), can be extracted from the results of calculated band structures, which can be used to evaluate the potential of this compound for optoelectronics applications. Fig. 5 shows the calculated band structures of CsSnBr_3 along their high cubic symmetry points within the first BZ. The key remark here, that perovskite CsSnBr_3 shows semiconductor property with a direct E_g at R-point of about ($E_g \approx 0.610$ eV) in good agreement with the experimental value ($E_g \approx 0.600$ eV) and smaller than GGA result ($E_g \approx 0.626$ eV) [25,26]. The indirect E_g of CsSnBr_3 locates between the valence band maxima and conduction band minima, which both lie along the R symmetry point. Where, the valence band maxima line touch the Fermi level ($E_F = 0.0$ eV). Compared with its analogous Ge and Pb based halide perovskites [1,22], the narrow E_g shown by the CsSnBr_3 crystal increases its significance for P-N junction (Fig. 1) in optoelectronics devices and photovoltaic solar cells applications.

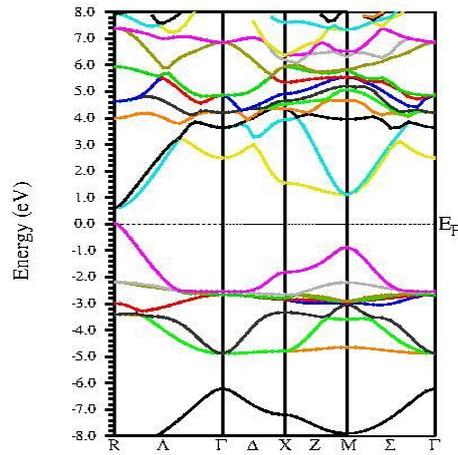


Fig. 5. The calculated band structures of metal halide perovskite CsSnBr_3 .

Third, in order to evaluate the atomic contribution to the density of states and nature of the atomic bonding in CsSnBr_3 , the total density of states (TDOS) and partial density of states (PDOS) are calculated using the WC method and shown in Figs. 6 and 7. It is obvious that TDOS (Fig. 6(a)) shows an E_g at the E_F , which also predicts the semiconducting behavior obtained from band structures. Also, the different contributions come from the TDOS per atom of Cs, Sn and Br to the TDOS per unit cell of CsSnBr_3 are plotted in (Fig. 6(b)).

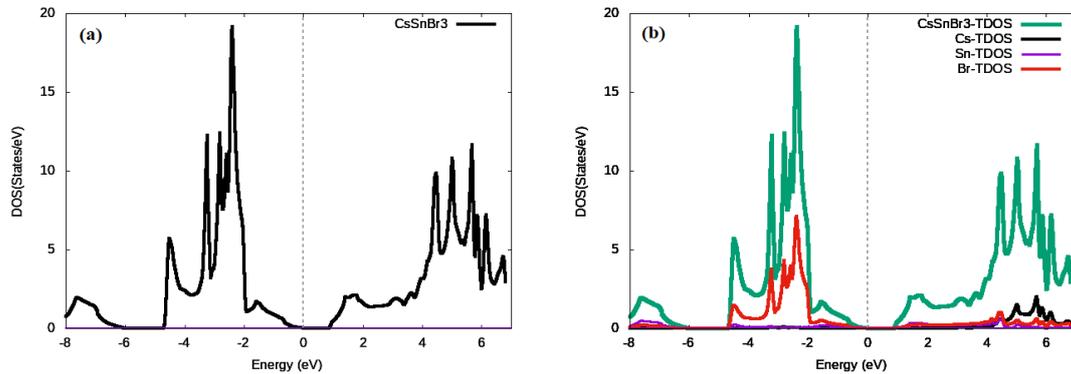


Fig. 6. The calculated total density of states; (a) TDOSs of CsSnBr_3 , and (b) TDOSs of Cs, Sn and Br of atoms, per unit

Moreover, the PDOSs per atom (Fig. 7(a,b, c)) confirm that the valence bands create from the partial hybridizations between Sn (5s, 5p) and Br (4p) states extend between -5.0 eV and E_F , whereas the conduction bands are generally dominated also by the Sn (5p) and Br (4p) hybridizations. The top of valence bands is yielded by partial 5s and 4p states, Sn (5s) – Br (4p), and the bottom of conduction bands are occupied by 5p and 4p states with no contribution come from Cs (5p) and Cs (4d) states. The prediction of semiconducting property gives complete confidence of the tenability to develop such the proposed CsSnBr_3 compound as promising candidate materials for novel light-emitting diodes, optoelectronic and photovoltaic technologies [27].

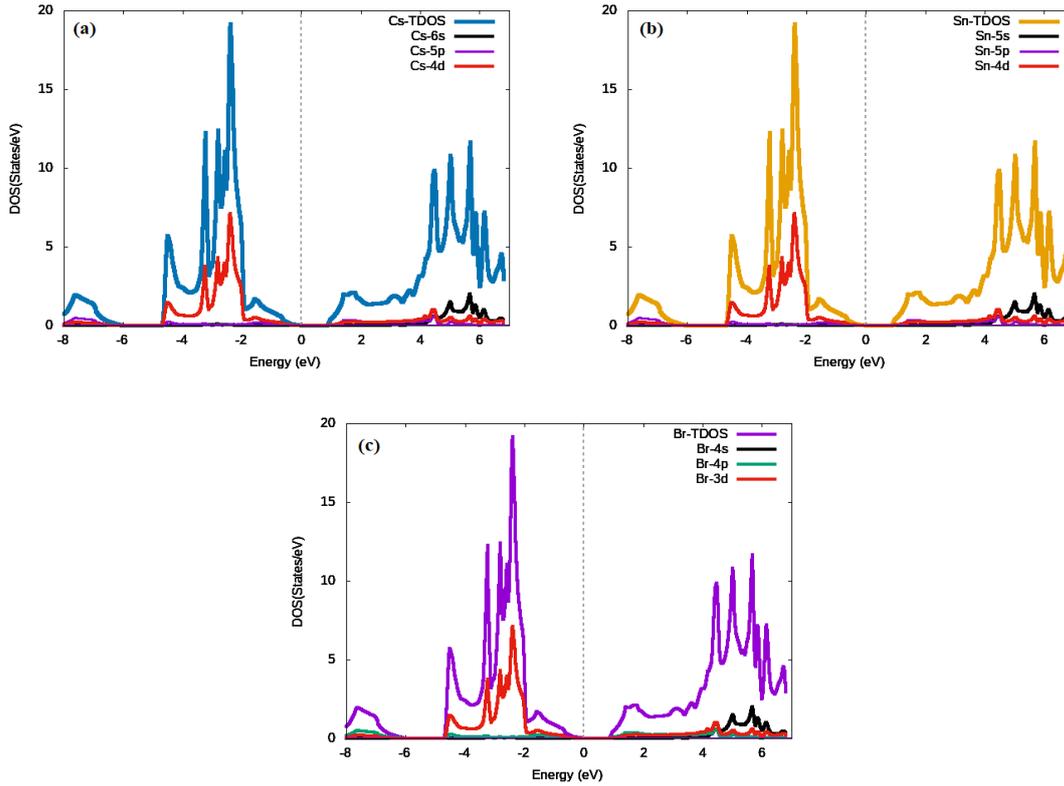


Fig. 7. The calculated partial density of states; PDOSs of (a) Cs, (b) Sn and (c) Br, per atom in metal halide perovskite CsSnBr_3 .

Studying of the optical properties allows us to determine the response of a certain material as a result of its interaction with the electromagnetic radiation. Thus, to examine this response, the key optical parameters of CsSnBr_3 like real part $\varepsilon_1(\omega)$ of the dielectric function, the absorption coefficient $\alpha(\omega)$, the refractive index $n(\omega)$ and the reflectivity $R(\omega)$ are calculated and discussed in detail. The optical results obtained in the meaningful photonic energy range of (0.0 – 15.0 eV) are plotted in Figs. 8 and 9.

First, from the $\varepsilon_1(\omega)$ curve (Fig. 8 (a)), which illustrates the degree of optical polarization of CsSnBr_3 when the electromagnetic radiation interacts with its crystal, it can be seen that $\varepsilon_1(\omega)$ starts at zero energy ($\omega = 0$). This value corresponds to the electronic E_g that defined by Kramers-Kronig relations and Penn model [22]. $\varepsilon_1(0) - 1 = \left(\frac{E_p}{E_g}\right)^2$, where the plasma energy ($E_p = \hbar\omega_p$), so, the narrow E_g gives a larger value of its $\varepsilon_1(0)$ and vice versa. The static value of CsSnBr_3 is ($\varepsilon_1(0) = 6.74$), which is in complete agreement with the conclusion drawn from the Penn's theoretical model. The $\varepsilon_1(\omega)$ curve increases to its first peak 7.09 at 0.42 eV and maximum value 7.63 at 0.72 eV, then it reaches its negative value next 11.4 eV. This indicates that the electromagnetic radiation is reflected from the CsSnBr_3 crystal and its photonic beam is totally reduced in this optical medium, making it as candidate materials for the protective shields from this radiation in the above specific energy range [25].

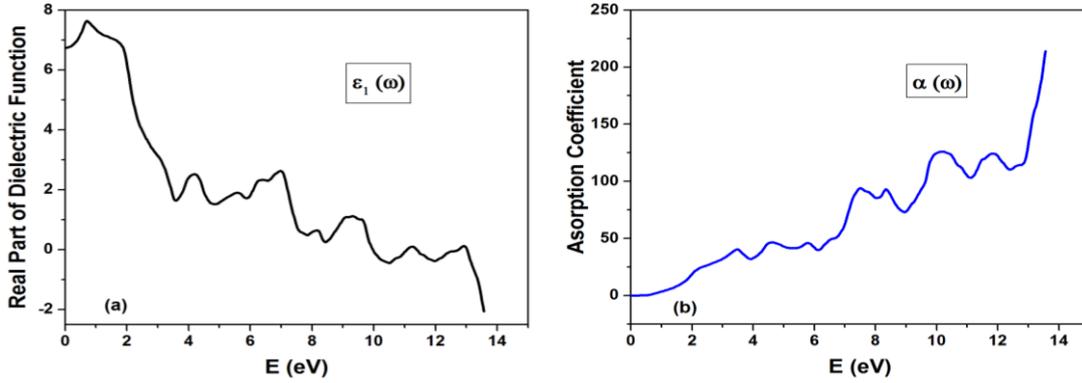


Fig. 8. The optical results of metal halide perovskite CsSnBr_3 (a) real part of dielectric function $\varepsilon_1(\omega)$, (b) absorption coefficient $\alpha(\omega)$, (c) refractive index $n(\omega)$ and (d) reflectivity $R(\omega)$.

The absorption coefficient $\alpha(\omega)$ (Fig. 8 (b)), which describes the optoelectronic interaction between the incident photons and the electrons in crystal of CsSnBr_3 , thus, it can provide important evidence for the application prospects of this material. It is clear that $\alpha(\omega)$ curve increases with the increase of E (eV), through four main peaks at 4.42 eV, 7.44 eV, 10.11 eV and 13.56 eV, in the visible range. CsSnBr_3 shows high light absorption in the visible range due to its narrow E_g , which indicates that CsSnBr_3 can be considered as suitable potential semiconductor crystal structures for many novel optoelectronics applications like photovoltaic solar cells, optical sensors and detectors [45]. The curve of reflectivity $R(\omega)$ for CsSnBr_3 (Fig. 9 (a)) is consistent with the behavior of $\alpha(\omega)$, the static value is ($R(0) \approx 0.20$) and its maximum value corresponds to the negative values of $\varepsilon_1(\omega)$ at $E > 11.4$ eV, where the percentage of $R(\omega)$ is found to be 24.7%. Finally, from the curve of refractive index $n(\omega)$ of CsSnBr_3 in (Fig. 9 (b)), it is clearly seen that the static and calculated values of refractive index are equal, $n(0) \approx 2.60$, and $n(0) = \sqrt{\varepsilon_1(0)} \approx 2.596$, respectively.

Table 2 summarizes the calculated results and static values (Figs. 8 and 9) of the main optical parameters for the metal halide perovskite CsSnBr_3 at zero energy ($E = 0$). These data include the maximum value real part of dielectric function $\varepsilon_1(0)$, the static value of reflective index $R(0)$, the static and calculated values of refractive index $n(0)$, and the evaluation rate of the optical absorption $\alpha(\omega)$.

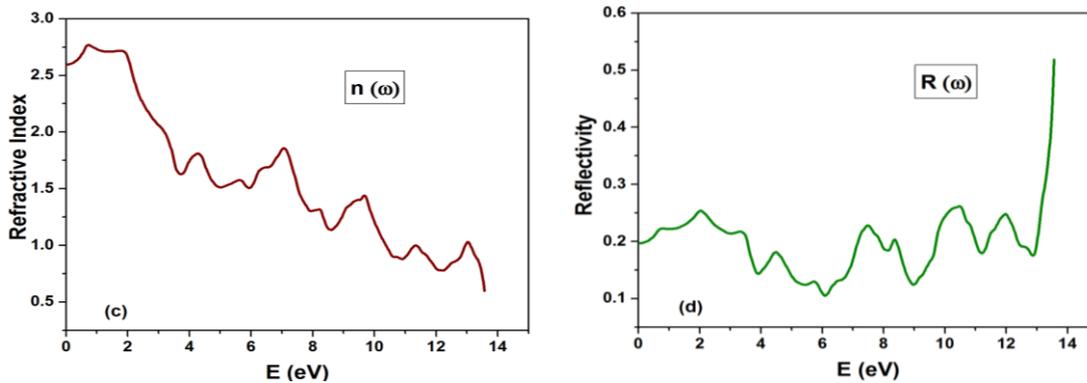


Fig. 9. The optical results of metal halide perovskite CsSnBr_3 (a) real part of dielectric function $\varepsilon_1(\omega)$, (b) absorption coefficient $\alpha(\omega)$, (c) refractive index $n(\omega)$ and (d) reflectivity $R(\omega)$.

Table 2. The main optical data with semiconductor nature of the metal halide perovskite CsSnBr₃.

Optical Parameter	Symbol	Value
Maximum value of real part	$\epsilon_1(0)$	6.740
Static reflective index	$R(0)$	0.200
Static refractive index	$n(0)$	2.600
Calculated refractive index	$n(0) = \sqrt{\epsilon_1(0)}$	2.596
Absorption rate	$\alpha(\omega)$	High

4. Conclusions

In this work, the structural, electronic and optical properties of all-inorganic metal halide perovskite CsSnBr₃ were examined for novel optoelectronics applications by execution of density functional theory (DFT) based on the FP-LAPW-WIEN2k method. To highlight these properties, the WC method based on the Generalized Gradient Approximation (GGA) has been used in all calculations. The results obtained from structural optimizations that carried out using WC method, show that the compound CsSnBr₃ stable in cubic structure (Pm-3m; no. 221) with ($a_0 = 5.776 \text{ \AA}$).

Also, the calculation results of band structures, density of states and 2D charge density show that the present perovskite CsSnBr₃ exhibits nonmagnetic and semiconductor properties and characterized by an appropriate direct band gap of ($E_g \approx 0.610 \text{ eV}$) lie along the R-R symmetry point. Moreover, the results obtained for the optical properties, the real part of the dielectric function, the absorption coefficient $\alpha(\omega)$, the refractive index $n(\omega)$ and the reflectivity $R(\omega)$, confirm that the crystal of CsSnBr₃ is a good light absorber with high light absorption extends in the visible range.

Accordingly, the exclusive properties of CsSnBr₃, that include high structural stability, high ductility and elasticity, suitable value of direct band gap and high optical absorption, make it a promising material for various novel applications. The present theoretical results provide a basis for the future experimental studies of Cs-based halide perovskites and related compounds, which have structural and optical properties may be necessary in novel fields of optoelectronics industries such as in photovoltaic solar cells, photodetectors, photodiodes and other photovoltaics devices.

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