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₁ New Insights into Dissipation in the Electron Layer ₂ During Magnetic Reconnection

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3 Detailed comparisons are reported between laboratory observations of electron-
4 scale dissipation layers near a reconnecting X-line and direct two-dimensional
5 full-particle simulations. Many experimental features of the electron layers,
6 such as insensitivity to the ion mass, are reproduced by the simulations; the
7 layer thickness, however, is about 3 – 5 times larger than the predictions.
8 Consequently, the leading candidate 2D mechanism based on collisionless elec-
9 tron nongyrotropic pressure is insufficient to explain the observed reconec-
10 tion rates. These results suggest that, in addition to the residual collisions,
11 3D effects play an important role in electron-scale dissipation during fast re-
12 connection.

13 Despite the disruptive influences of magnetic reconnection on large-scale structures in
 14 plasmas, the crucial topological changes and their associated dissipation take place only
 15 within thin current layers. The classical collisional models, where electrons and ions flow
 16 together through a single thin and long layer, fail to explain the observed fast reconnection
 17 rates. Modern collisionless models predict [*Sonnerup*, 1979; *Mandt et al.*, 1994; *Birn*
 18 *et al.*, 2001] that ions exhaust through a thick, ion-scale layer while mobile electrons
 19 flow through a thin, electron-scale layer, allowing for efficient release of magnetic energy.
 20 These ion layers have been frequently detected in space [e.g. *Deng and Matsumoto*, 2001;
 21 *Øieroset et al.*, 2001; *Mozer et al.*, 2002] and studied in detail in the laboratory [*Ren*
 22 *et al.*, 2005; *Yamada et al.*, 2006; *Brown et al.*, 2006]. In contrast, the electron layers,
 23 where magnetic field dissipates, are rarely encountered in space and are often detected at
 24 places far from the reconnection X-line line [*Scudder et al.*, 2002; *Mozer*, 2005; *Wygant*
 25 *et al.*, 2005; *Phan et al.*, 2007]. Therefore, whether the electron layers indeed exist near
 26 the X-line, and if yes, whether their associated dissipation results predominantly from
 27 laminar two-dimensional (2D) or three-dimensional (3D) dynamics as suggested by *Xiao*
 28 *et al.* [2006, 2007], is still an open question. Here we report detailed comparisons between
 29 recent laboratory observations of the electron layers near the X-line [*Ren et al.*, 2008]
 30 and direct full-particle simulations in 2D. The measured electron layers display properties
 31 strikingly similar to predictions by 2D particle simulations, including their geometrical
 32 shape, insensitivity to ion mass, and sensitivity to the boundary conditions, but disagree
 33 on the electron layer thickness. As a consequence, the leading 2D mechanism based on
 34 collisionless electron nongyrotropic pressure is shown to be largely insufficient to explain

the observed reconnection rates. These results suggest that, in addition to the residual Coulomb collisions, 3D effects play an important role in electron-scale dissipation during fast reconnection.

The laboratory measurements were performed on the well controlled and diagnosed experiment, Magnetic Reconnection Experiment (MRX) [Yamada *et al.*, 1997], as illustrated in Fig.1. A pair of coil assemblies, known as flux-cores, are used to axisymmetrically initiate and maintain the reconnection process. Plasma is made by ionizing a pre-filled gas through pulsing toroidal field coil current within the flux-cores during the period when the current flowing in the poloidal field (PF) coils peaks. When the PF coil current is ramped down after the plasma is made, the field lines wrapped around both flux-cores are “pulled” back, reconnect, and move towards the flux-cores. Most of the important quantities can be either directly determined or indirectly inferred from these measurements in cylindrical coordinates (R, Z, θ) assuming axisymmetry: poloidal flux $\psi(R, Z, t) = \int_0^R 2\pi R' B_Z(R', Z, t) dR'$ where B_Z is the reconnecting field; the toroidal reconnection electric field $E_\theta = (\partial\psi/\partial t)/2\pi R$; and the toroidal current density $j_\theta \approx \mu_0^{-1} \partial B_Z / \partial R$. The density n and electron temperature T_e are measured by a triple Langmuir probe and the flow speeds are determined by a Mach probe. The typical plasma parameters are: $n \simeq (0.1 - 2) \times 10^{20} \text{ m}^{-3}$, $T_e \sim T_i \simeq (3 - 15) \text{ eV}$, $B < 0.5 \text{ kG}$.

Detection of the electron dissipation layer is made possible by taking advantage of the differential motions between electrons and ions or the so-called Hall effects [Sonnerup, 1979] in the reconnection region without a guide field. These differential motions (or electric current) within the reconnection plane produce out-of-plane magnetic field component

(B_θ) with a quadrupole shape. Conversely, accurate measurements of the B_θ profile can determine the in-plane electron flow because of the much slower ion flow in this region, and thus characterize the electron dissipation layer. These measurements are performed using five linear arrays of pickup coils (Fig.1); each array measures a one-dimensional profile of B_θ with a frequency response of 300kHz and with spatial resolutions up to 2.5 mm. This distance is close to the electron skin depth, c/ω_{pe} ($=0.7-1.5\text{mm}$) where ω_{pe} is the electron plasma angular frequency, and adequately resolves the electron layer whose minimum full thickness is 10 mm (see below). These arrays are housed by thin glass tubes of outer diameter of 4 mm (four arrays) or 5 mm (one array) with shielding from electrostatic noise. The presence of these probes in the plasma does not appear to affect the reconnection process, but it may cause modest overestimates of the electron layer thickness (see below).

One such example measurement is shown in Fig.2(b) where the in-plane electron flow (V_{eZ} and V_{eR}) is shown as arrows while the normalized, out-of-plane magnetic field is shown as color-coded contours in the left half of the reconnection plane. Electron outflow speed, V_{eZ} , is also shown as functions of Z in Fig.2(c) (at the current sheet center) and R in Fig.2(a) (across the reconnection region at the location where V_{eZ} peaks). The dimensions of the electron layer can be characterized by the half thickness δ_e (the radial distance during which V_{eZ} decreases by 60% from its peak value) and the half length L_e (the axial distance during which V_{eZ} increases from zero to its peak). We positively identify this region as the electron dissipation layer because both its dimensions, δ_e and L_e , are independent of ion mass, as shown in Fig.3 for δ_e .

Dissipation in the electron layer is governed by the electron equation of motion,

$$m_e n \left(\frac{\partial}{\partial t} + \mathbf{V}_e \cdot \nabla \right) \mathbf{V}_e = -en(\mathbf{E} + \mathbf{V}_e \times \mathbf{B}) - \nabla \cdot \mathbf{P}_e + en\eta_{Spitzer}\mathbf{j}, \quad (1)$$

where m_e is electron mass, \mathbf{P}_e electron pressure tensor, and $\eta_{Spitzer}$ the Spitzer resistivity due to Coulomb collisions with ions [Spitzer, 1962]. In the modern collisionless steady-state 2D models, the reconnection electric field, E_θ , can be only possibly balanced by either the Hall term $(\mathbf{V}_e \times \mathbf{B})_\theta \approx (\mathbf{j} \times \mathbf{B})_\theta/en$, the inertia terms, or the electron pressure tensor term $(\nabla \cdot \mathbf{P}_e)_\theta$. While the Hall term is important in supporting E_θ within the ion layer [Birn et al., 2001; Ren et al., 2005; Yamada et al., 2006], it diminishes within the electron layer especially near the X-line due to the vanishing \mathbf{B} . It has been shown in particle simulations [Cai and Lee, 1997; Hesse et al., 1999; Pritchett, 2001; Kuznetsova et al., 2001] that E_θ is supported primarily by the electron pressure tensor term following earlier suggestions [Vasyliunas, 1975]. This mechanism has been since widely accepted as the leading candidate to provide the required dissipation within the electron layer. It is, however, extremely difficult to confirm this pressure anisotropy, directly or indirectly, by measurements in real plasmas [Scudder et al., 2002].

One of the predictions of these 2D particle simulations is that the half thickness of the electron layer, δ_e , scales as $(1 - 2)c/\omega_{pe}$ [Pritchett, 2001]. The measured δ_e in MRX, however, scales as $\sim 8c/\omega_{pe}$ (Fig.3). Current blockage due to the probes is estimated to lead to a 6 – 44% increase in the measured δ_e , depending on the ratio of δ_e to the glass tube radius. Applying these corrections leads to $\delta_e = (5.5 - 7.5)c/\omega_{pe}$. To better compare with the experiment, on the other hand, we have constructed a kinetic numerical model [Dorfman et al., 2008] using boundary conditions similar to the MRX based on

101 the existing NPIC 2D code [*Daughton et al.*, 2006]. A 75cm×150cm simulation box is
 102 used with conducting boundary conditions for fields and elastic reflection for particles
 103 at the walls. Two current carrying coils of radius 1.3 cm are contained within a larger
 104 concentric flux core of radius 9.4 cm. The flux cores are spaced 40 cm apart as in the
 105 experiment. The flux core surface is approximated as an insulating boundary; particles
 106 may be absorbed or reflected. Due to constraints on computation resources, the number
 107 of the Debye lengths per c/ω_{pe} is limited compared to the experiment, but there is strong
 108 evidence that the reconnection rate and electron layer scalings are insensitive to this
 109 number as long as the initial plasma beta is fixed [*Dorfman et al.*, 2008]. As the current
 110 is ramped down according to a sinusoidal waveform modeled on the PF coil current of
 111 MRX and reconnection is driven, both ion and electron dissipation layers are formed.
 112 Simulation parameters are chosen such that the global reconnection rate and the current
 113 sheet thickness on the ion scale match the observations. An example run is shown in
 114 Fig.2(d-f) in the same format as in Fig.2(a-c), and most of the observed features, including
 115 geometrical shapes and out-of-plane magnetic component, are reproduced.

116 The quantitative agreement between experiment and simulation is, however, found for
 117 only the global ion dynamics but not the local electron dynamics. The experimentally
 118 observed independence of δ_e and L_e on ion mass was reproduced as shown for δ_e by the
 119 open squares in Fig.3 for a fixed but artificially heavy electron mass. The values of δ_e
 120 in units of c/w_{pe} (evaluated using a line-averaged density at $Z = 0$), however, are much
 121 smaller in simulations than in experiments, as illustrated by an alternative ordinate in
 122 Fig.2(a) and (d). In Fig.3, a case at higher mass ratio (400) with a different electron mass

is also plotted along with simulations with a realistic hydrogen mass ratio but a smaller simulation domain and open boundary conditions [Daughton *et al.*, 2006]. All of these cases, including more recent simulations using different open boundary conditions [Huang and Ma, 2008], confirm a linear relation of $\delta_e = (1.5 - 2)c/\omega_{pe}$ which is about 3 – 5 times thinner than the experiment. In contrast, the dependence of the length of the electron layer (L_e) on c/ω_{pe} is less robust; it can change significantly when the reflection coefficient parameter on the flux core surface is varied [Dorfman *et al.*, 2008] as expected from the observed dependence of the reconnection process on boundary conditions [Kuritsyn *et al.*, 2007].

The fact that the observed electron layers are substantially thicker than the numerical predictions implies different dissipation mechanisms operating between these two cases. In fact, our collisionless simulation model does not include the residual collisions between electrons and ions or neutrals. But in MRX only a fraction of E_θ can be accounted for by the classical resistivity, $E_\eta \equiv \eta_{Spitzer} j_\theta$ (Fig.4). Collisions between electrons and neutrals, and electron collisional viscous effects are also estimated to be unimportant in these discharges with low fill pressure. The electron inertia terms, $(m_e/e)[(V_{eR}\partial/\partial R) + (V_{eZ}\partial/\partial Z)]V_{e\theta}$, are estimated to be on the order of 1 V/m, which is negligibly small. Near the X-line, the effects due to electron nongyrotropic pressure can be well approximated by [Hesse *et al.*, 1999]

$$E_{NG} \equiv - \left(\frac{\nabla \cdot \mathbf{P}_e}{en} \right)_\theta \approx \frac{1}{e} \frac{\partial V_{eZ}}{\partial Z} \sqrt{2m_e T_e}, \quad (2)$$

as also validated in our kinetic model. Direct evaluations of E_{NG} using the measured profile, $V_{eZ}(Z)$ as in Fig.2, gives values only a small fraction of $E_\theta - E_\eta$ (Fig.4). This leaves

the majority of E_θ still unexplained, and therefore there must exist additional dominant dissipation mechanisms. Because our kinetic model contains all possible collisionless kinetic mechanisms operative in 2D, these dominant mechanisms must be 3D in character, including effects due to current sheet deformation or plasma turbulence through wave-particle interactions within the current sheet. The latter was indeed already suggested by the detection of electromagnetic fluctuations [*Ji et al.*, 2004] when dissipation increases at low collisionalities [*Ji et al.*, 1998]. This subject is also under intensive theoretical and numerical investigation, such as recently by *Moritaka et al.* [2007], in the search for mechanisms for fast reconnection. Lastly, we comment that these 3D effects, in addition to the residual collisions, may diffuse substantially the predicted two-scale structures seen in the profiles of the reconnecting magnetic field, which remain undetected thus far in the experiment.

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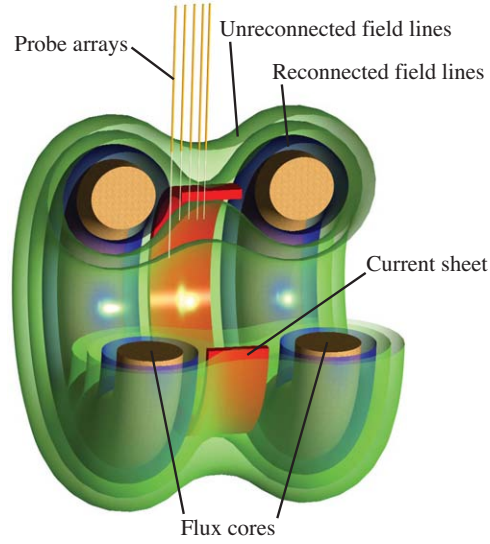


Figure 1. Experimental set-up of MRX device. The toroidal direction points along the current sheet while the poloidal direction wraps around the flux cores.

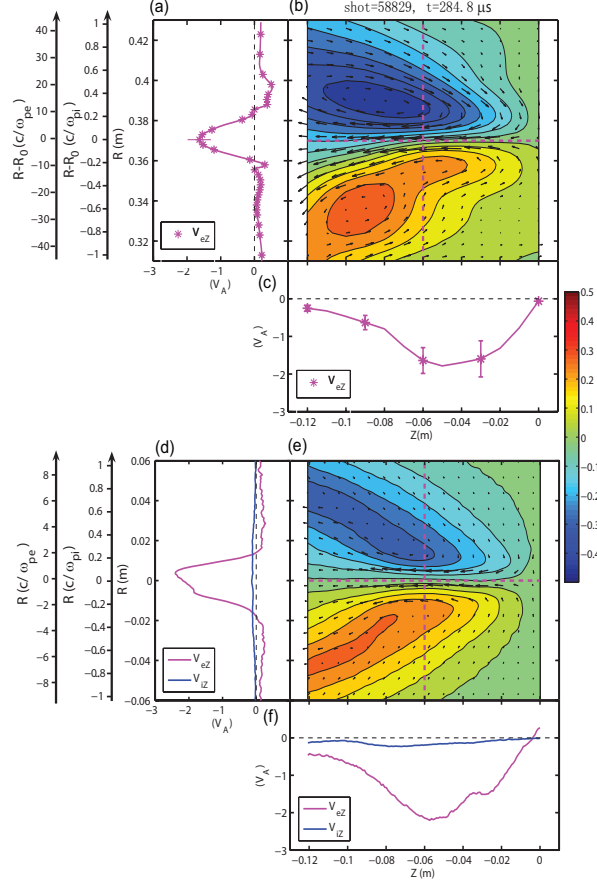


Figure 2. Identification of electron dissipation layer. The top three panels (a-c) show an experimental example taken from a hydrogen plasma with a fill pressure of 2 mTorr. Results from a corresponding simulation are shown in the same format in the lower three panels (d-f). The parameters used in the simulation are: 864×1728 cells with 0.5 billion particles per species, initial density of $2.6 \times 10^{19} \text{m}^{-3}$, $m_i = m_{\text{hydrogen}}$, $m_e = m_{\text{hydrogen}}/75$, a time scale for the coil current ramp down is 185 initial ion cyclotron times, and no particle reflections at the flux core surface.

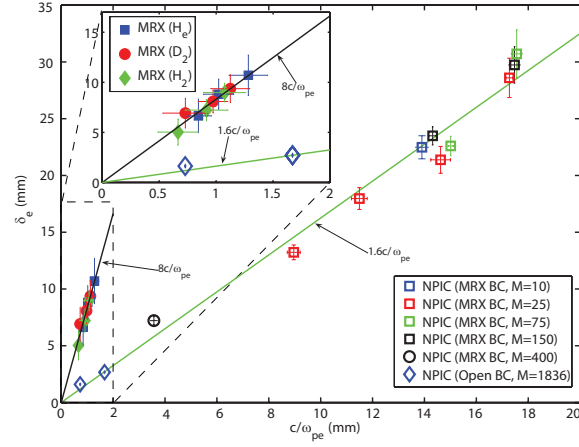


Figure 3. Scaling of width of electron dissipation layer. Filled symbols show the experimentally measured δ_e as a function of the electron skin depth (c/ω_{pe}) for three different ion species. The error bars result mainly from shot-to-shot variations. Open symbols show δ_e determined from 2D PIC simulations.

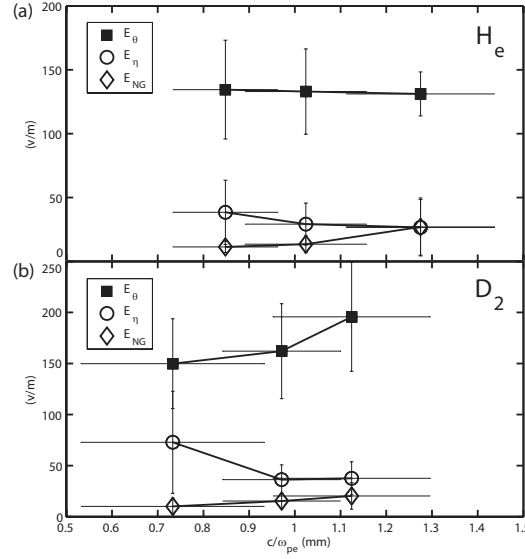


Figure 4. Composition of reconnecting electron field, E_θ , for (a) helium and (b) deuterium plasmas. Total reconnecting electric field in MRX, E_θ , and the part of it due to electron-ion collisions, $E_\eta = \eta_{Spitzer} j_\theta$ near the X-line are plotted as a function of c/ω_{pe} . The estimated electric field due to electron nongyrotropic pressure, E_{NG} , is also shown.

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