

# **MINIMIZATION OF NO EMISSIONS FROM MULTI-BURNER COAL-FIRED BOILERS**

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## Program Overview

The focus of this program is to provide insight into the formation and minimization of NO<sub>x</sub> in multi-burner arrays, such as those that would be found in a typical utility boiler. Most detailed studies are performed in single-burner test facilities, and may not capture significant burner-to-burner interactions that could influence NO<sub>x</sub> emissions.

Our approach is to investigate such interactions by a combination of single and multiple burner experiments in a pilot-scale coal-fired test facility at the University of Utah, and by the use of computational combustion simulations to provide insight into the experimental results and to evaluate full-scale utility boilers. In addition, fundamental studies on nitrogen release from coal will be performed in support of the modeling effort. Improved submodels describing transformations of both volatile nitrogen species and char nitrogen species will be developed.

The program is broken into four main tasks, and reporting will be divided into these main areas:

- 1- Fundamental studies on nitrogen release from coal. These studies will be used to enhance the predictive capabilities of the combustion simulations. Studies focusing on secondary coal pyrolysis will be carried out at Brigham Young University, and studies focusing on char nitrogen will be performed at the University of Utah.
- 2- Comprehensive modeling of burner arrays. This task will be performed by Reaction Engineering International and the University of Utah.
- 3- Pilot-scale optimization of multi-burner arrays. This task will be carried out by the University of Utah.
- 4- Technology transfer. This task involves coordination with utility consultants who will provide oversight of the research program.

## **PRODUCTION OF NITROGEN OXIDE DURING CHAR OXIDATION AT PULVERIZED COAL COMBUSTION CONDITIONS**

### **SUMMARY**

During the last reporting period the experimental setup in the University of Utah Laminar-Flow Drop Tube was modified to allow for batch experiments. This modification was made in order to guarantee complete conversion of the char in the reactor. Once the setup was optimized, the effect of particle size, oxygen concentration, type of char and NO bulk concentration on the conversion of char-N to NO was evaluated.

In this report, we present the results obtained for different chars and for different NO background concentrations. The effect of oxygen and particle size is currently being analyzed and will be presented in the final report. Experiments were performed with three different carbonaceous materials and were conducted at temperatures close to that of pulverized combustion conditions (1700 K) in a laminar drop tube reactor under inert and oxidizing atmospheres. The results obtained show that the process of NO reduction on the char surface plays an important role on the total amount of char-N converted to NO<sub>x</sub>. This effect tends to reduce as the NO background concentration is reduced and doesn't seem to strongly depend on the nature of the char. Some of these results were presented at the 2nd Joint Meeting of the US Sections of the Combustion Institute, held in March of 2001. In addition to the experimental observations on char-N conversion to NO, a single particle model was developed and the predictions of the model were compared with the experimental results. Although the model predicts the linear reduction on the conversion of char-N to NO, it overpredicts the general value. A higher value for the rate of NO

destruction on char surface doesn't seem to explain this phenomenon, which may be more related to the availability of char surface for the destruction of NO.

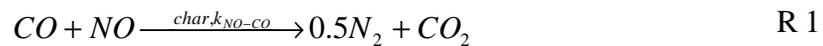
## INTRODUCTION

Production of nitrogen oxide from fuel-nitrogen during coal combustion occurs by two different phenomena: 1.) by the oxidation of the nitrogen released with the volatiles present in the char and 2.) by the oxidation of the nitrogen that remains in the char matrix. The first mechanism occurs in the homogeneous phase, and the second involves heterogeneous reactions. Research on NO<sub>x</sub> reduction has focused for many years on the homogeneous pathway and a great deal of understanding and technology has been developed for reducing NO formed as a result of volatile release from the coal. The details of heterogeneous process are less well understood, and the char nitrogen contribution is becoming of increasingly greater importance as overall NO<sub>x</sub> emissions levels decrease.

In order to attain a better understanding of the process of NO production during char oxidation, several single particle models have been proposed in the literature. Models for char-N evolution at fluidized bed combustor conditions<sup>1-3</sup> are concerned with the issue of char-N partitioning between NO and N<sub>2</sub>O and are not discussed in this paper since at pulverized combustion conditions NO is the main pollutant.<sup>4</sup> Few models are specifically targeted to the pulverized coal combustion regime. The approach of the pioneering work of Wendt and Schulze<sup>5</sup> has been followed by several different authors.<sup>6,7</sup> In Visona and Stanmore's model<sup>6</sup>, char-N may evolve as NO, HCN and N<sub>2</sub>. These authors tested different rates for NO reduction on the char, as well as the effect of CO concentration.

They concluded that most of the expressions reported in the literature for the reduction of NO on char surface were too low to predict the amount of char-N converted to NO. Jensen et al<sup>7</sup> in a fixed bed reactor study found that large sample size produced a low conversion of char N to NO as a result of NO reduction on the char surface when *in situ* generated chars were oxidized under 10% O<sub>2</sub>/N<sub>2</sub>. They also suggested that most of the rates for the NO-char reaction reported in the literature for oxygen-free conditions were too low to explain the evolution of char-N to NO and proposed the necessity for the evaluation of the NO-char reaction when oxygen is present.

These two studies cast doubt on the utility of most of the kinetic expressions for the rate of NO reduction on the surface when predicting char-N conversion to NO. This reduction reaction seems therefore to be a critical element in modeling NO production during char combustion. Since it is not the main objective of this paper to discuss this reaction, the reader is referred to different reviews on this topic.<sup>8-10</sup> Nevertheless it may be helpful for further discussion to draw attention to two points. First the effect of CO through the reaction:



R 1 occurs in parallel to the global NO-char reaction:

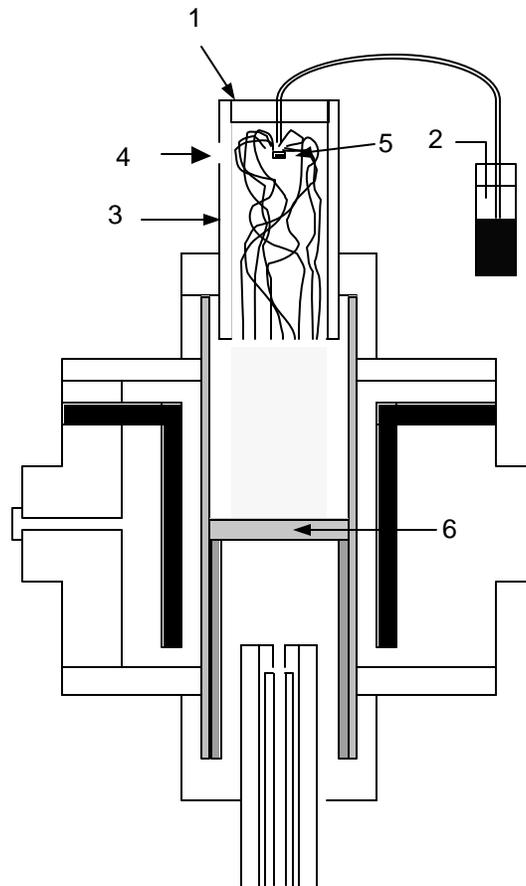


Secondly, the effect of O<sub>2</sub>. Chambrion et al<sup>11</sup> found that O<sub>2</sub> has a catalytic effect on R 2. The fact that their experiments were at 600°C and low O<sub>2</sub> concentration (0.4%) makes the comparison of the results to the PC conditions difficult. No analytical expression was found in the reviewed literature for the quantification of the effect of O<sub>2</sub> on this reaction.

This study proposes a single particle model that predicts the formation of NO from char-N. This model is compared to the experimental data obtained in a drop tube reactor, at temperatures similar to those of pulverized bed combustors. The rate of NO reduction on char was also evaluated in order to allow its use as an input for the model.

### REACTOR AND EXPERIMENTAL SETUP

The experiments were carried out in an electrically-heated laminar flow drop tube reactor with a cross sectional diameter of  $5.08 \times 10^{-2}$  m. The conventional setup of the drop-tube was modified to allow the implementation of batch experiments and *in situ* char formation.



**Figure 1. Experimental setup for the Batch experiment.** 1. Quartz window. 2. Carrying gas input. 3. Distributor. 4. Distributor radial gas. 5. Bluff disk. 6. Alumina/silica non-woven fabric

Figure 1 presents a schematic of the experimental setup. During the experiments, a known amount of coal or char was introduced to the reactor under inert or oxidizing atmosphere by means of a custom-built distributor, which consists of a disk located in front of the char injection tube. The purpose of the disk is to cause a deflection that spreads the coal uniformly over the entire cross-sectional area of the drop tube reactor, minimizing the chance of particle-particle interactions in the reaction zone. To prevent the deposition of coal on the walls of the distributor, a radial gas stream is injected through the walls of the distributor surrounding the coal injection zone. After the disk, uniform flow develops before the gases enter the drop tube reaction zone and the coal stream is dispersed over the entire cross sectional area. Since the flow inside the reacting section is laminar, no deposition of coal on the reactor walls occurs. The solid stream is then collected over an alumina/silica non-woven fabric that was placed in the middle of the reacting zone. A quartz window on the top of the drop tube allowed visual examination of the particle distribution. The exhaust gases are collected by a water-cooled probe placed immediately under the non-woven fabric. Analysis of CO, CO<sub>2</sub>, NO, NO<sub>2</sub>, N<sub>2</sub>O and HCN was performed by FTIR. For some experiments, CO and CO<sub>2</sub> FTIR concentrations were verified with an NDIR analyzer, and NO FTIR concentration was verified by a chemiluminescent analyzer.

Three different experiments were conducted:

1. **Oxygen-free experiments.** The objective of this set of experiments was to evaluate the rate of NO reduction on char surface. In this case, coal or char was injected into an NO/He stream and then collected on the non-woven fabric. The rate of NO reduction by the char was computed as follows:

$$k_{NO} = \ln \left( \frac{C_{NO}^{in}}{C_{NO}^{out}} \right) \frac{n}{w_{char}} \quad \text{E 1}$$

E 1 assumes a first order reaction between NO and char. After five minutes, O<sub>2</sub> is injected in the reactor and the value of  $w_{char}$  is obtained from the integral of the concentrations of carbon oxides detected in the product gases.

**2. *In situ* char experiments.** For these experiments, coal was introduced to the reactor under inert atmosphere. After 60s under inert atmosphere, an O<sub>2</sub>-containing stream is introduced to the drop tube and the chars are rapidly consumed during oxidation. The purpose of this experiment was to evaluate the conversion of char-N to NO for chars prepared *in situ*. However, NO reduction in the downstream section of the reactor due to the fuel-rich conditions in the combustion gas after char oxidation complicated the interpretation of this set of experiments.

**3. Direct injection.** To avoid any reduction of the NO produced during reaction, char or coal was injected into an O<sub>2</sub>-containing stream. In this way char oxidation begins while the particle is falling in the reactor. The residence time for the particle in suspension is less than 300 ms. Since this is less than the time for oxidation, the reaction is completed in the non-woven fabric. The sample size for all experiments was ~ 5 mg. The total gaseous flow was 4000 sccm.

#### **COAL AND CHAR SAMPLES**

In order to understand the effect of the carbonaceous material on reaction R 2 as well as on the amount of char-N that is converted to NO, an Illinois No. 6 coal and two different chars were used in the experiments. An activated char with low nitrogen content was

included for comparison. Table 1 presents the ultimate and proximate analysis of the samples. Coal refers to the raw Illinois No. 6 coal. Char DT refers to char produced by injection of coal in a **Drop Tube** reactor without the presence of the non-woven fabric (continuous injection mode); the char from the drop tube provides the elemental and proximate analysis for the initial condition of the char in the *in situ* experiment explained above. Char U-Furnace is char produced in a pulverized coal bench-scale furnace<sup>12</sup> with Illinois No.6 coal produced using a self-sustained flame under typical pulverized combustor conditions. And finally, activated char is a commercial activated char produced from coconut shell.

**Table 1. Coal and Char analysis**

	Proximate Analysis				Ultimate Analysis (daf)				
	Moist.	Ash	Volatile Matter	Fixed Carbon	C	H	N	S	O
Coal	6.91	5.56	46.38	41.15	80.67	5.30	1.87	0.98	11.19
Char DT	5.30	10.86	4.07	85.07	95.70	0.56	1.84	0.72	1.18
Char U-Furn.	0.89	17.85	N.A.	N.A.	92.63	1.48	1.96	0.62	3.31
Activat. char	6.06	5.23	N.A.	N.A.	91.56	2.06	0.14	0.02	6.21

N.A. Not available

#### **SINGLE PARTICLE MODEL**

The single particle model developed in this study solves the species conservation equation (E 2) for all the gaseous species involved in the system (CO, N<sub>2</sub>, NO, O<sub>2</sub> and He) and for one solid species, carbon in the char. It assumes the system to be isothermal. The particle temperature was assumed to be 100 K higher than the gas temperature as suggested from the experimental results of Hurt<sup>13</sup> for Illinois No. 6 char.

$$\frac{\partial}{\partial t} c_i = - \left( \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 N_i) \right) + R_i^v \quad \text{E 2}$$

E 2 was solved by applying a control volume technique as described by Patankar.<sup>14</sup> The molar flux,  $N_i$  is assumed to be in the Knudsen regime, therefore it is approximated to be a diffusion flux, as given by E 3

$$J_i = -D_{k,i} \frac{dC_i}{dr} \quad \text{E 3}$$

The coefficient of Knudsen diffusivity is the one recommended by Satterfield<sup>15</sup> (E 4) and was computed for every species. The tortuosity was assumed to be 2.

$$D_{K,i} = \frac{8}{3} \left( \frac{q}{A_s r_p} \right) \sqrt{\frac{2R_g T}{pMW_i}} \quad \text{E 4}$$

For the carbon oxidation, the intrinsic reaction rate of Smith<sup>16</sup> was used.

$$R_i = 3050 \exp(-179.4 / RT) \frac{kgC}{m^2 s (101325 Pa O_2)}, \text{ original expression} \quad \text{E 5}$$

$$R_i^C = 2.5061 \exp(-2.1578 \times 10^4 / T) \frac{gmolC}{m^2 s Pa O_2}, \text{ Expression for } R_i \quad \text{E 6}$$

$$R_C^v = R_i^C * C_{O_2} * R_g * T * A_{s-v} \frac{gmolC}{m^3 s} \quad \text{E 7}$$

Where

$$A_{s-v} = C_C * MW_C * \frac{1}{C_{\%}} * A_s * \frac{1}{1000} \frac{m^2}{m^3} \quad \text{E 8}$$

The char surface area ( $A_s$ ) was considered to change with char conversion as defined by<sup>17</sup>:

$$A_s = A_s^o (1 + 2.5X)(1 - X) \quad \text{E 9}$$

An initial particle surface area of 100 m<sup>2</sup>/gm for the coal chars and of 1400 m<sup>2</sup>/gm for the activated char was used for all the models.

The rate of NO production was assumed to be proportional to the rate of  $C_s$  consumption.

With  $N/C$ , (atomic ratio of N to C in the char at 0 burnout) as proportionality constant.

$$R_{NO}^v = R_C^v * N/C \frac{gmolNO}{m^3s} \quad E 10$$

The volumetric void pore fraction of the particle, or char porosity is taken from Stanmore<sup>17</sup> as:

$$\mathbf{q} = \mathbf{q}_o + X(1 - \mathbf{q}_o)\mathbf{q}_c \quad E 11$$

With  $\mathbf{q}_o$  as 0.41.

The boundary conditions were symmetry at  $r = 0$  and at  $r = R_p$  the flux is given by the following expression:

$$N_{i,r=R_p} = -k_g (c_i^{bulk} - c_i^{nr}) \quad E 12$$

$k_g$ , the mass transfer coefficient was computed as:<sup>18</sup>

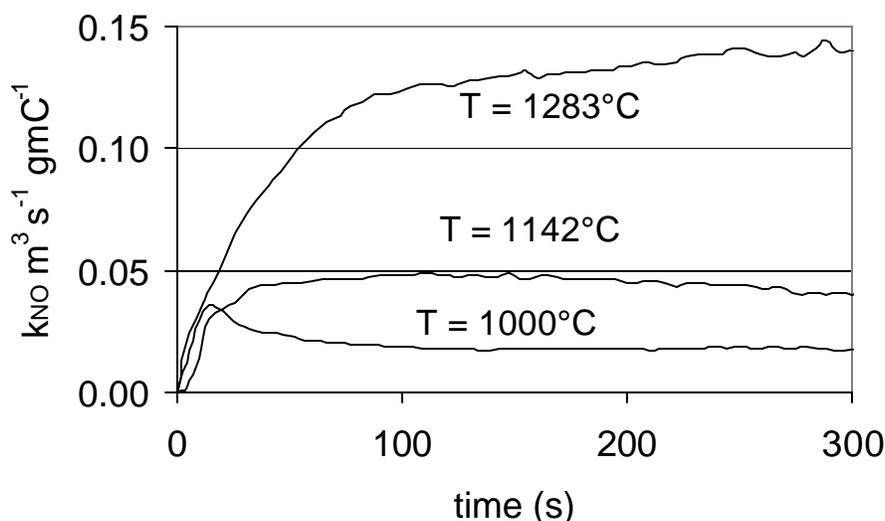
$$k_g = D_{eff} / (2 * R_p) \quad E 13$$

$D_{eff}$ , the mass transfer effective multicomponent effective diffusion coefficient, was computed by CHEMKIN II transport package.<sup>19</sup>

## RESULTS AND DISCUSSION

### 1. Oxygen-free experiments

Since several of the values present in the literature for the rate of NO reduction on char surface (e.g.<sup>20-23</sup>) have been considered to be too low to account for the conversion of char-N to NO in recent studies<sup>6,7</sup>, experiments to establish the value of  $k_{NO}$  for the present set-up and chars were carried out.



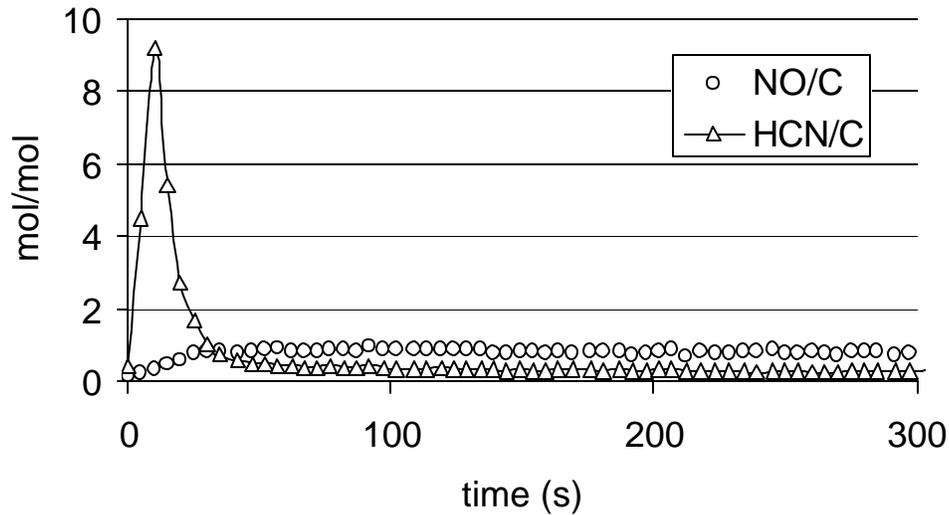
**Figure 2. Rate of NO reduction on char produced from Illinois No.6 coal. Coal was injected on the top of the reactor into a 740ppm NO/He stream at time 0.**

Figure 2 presents the rate of NO reduction as calculated using equation E 1 for Illinois No.6 chars. In this experiment, coal was injected at time 0 and the rate was computed from this initial time. The first item to point out in Figure 2 is the result for 1000°C. At this temperature, and at the initial time there is a small increase in the reaction rate. These results are similar to those of Jensen et al.<sup>7</sup>

However, at higher temperatures this effect is not observed. Figure 3 presents the molar ratio of NO/C (C refers to the sum of the carbonaceous species, mainly CO, in the product gases) and HCN/C for the experiment at 1000°C in Figure 2. The results suggest a high HCN production during the first initial period of the reaction, when pyrolysis is occurring. After the pyrolysis reactions decay, the NO/C ratio increases to one, as is expected from R 2, and the HCN/C ratio drops to a very low value. Plots similar to Figure 3 were prepared at other temperatures and the values of HCN/C were considerably lower for the other two cases. This information suggests that the evaluation of  $k_{NO}$  at times prior to completion of pyrolysis may be biased by the reactions of NO with

pyrolysis products. Given the nature of the expression for the evaluation of  $k_{NO}$  (E 1), the value of the  $w_{char}$  is critical for the final results of  $k_{NO}$ . If the mass of char is underestimated by neglecting the production of carbon-containing species (as HCN) the value of  $k_{NO}$  increases, in the case of Figure 2 by 30%. This effect may be less pronounced at higher temperatures since the effect of late devolatilization reactions may be lower, as well as the time required for pyrolysis. The value  $k_{NO}$  was computed when a plateau in the value of  $k_{NO}$  was obtained for all the temperatures in order to eliminate the transient initial reaction with the pyrolysis products.

Table 2 presents the results of Arrhenius plots obtained from data similar to Figure 2 for other materials.



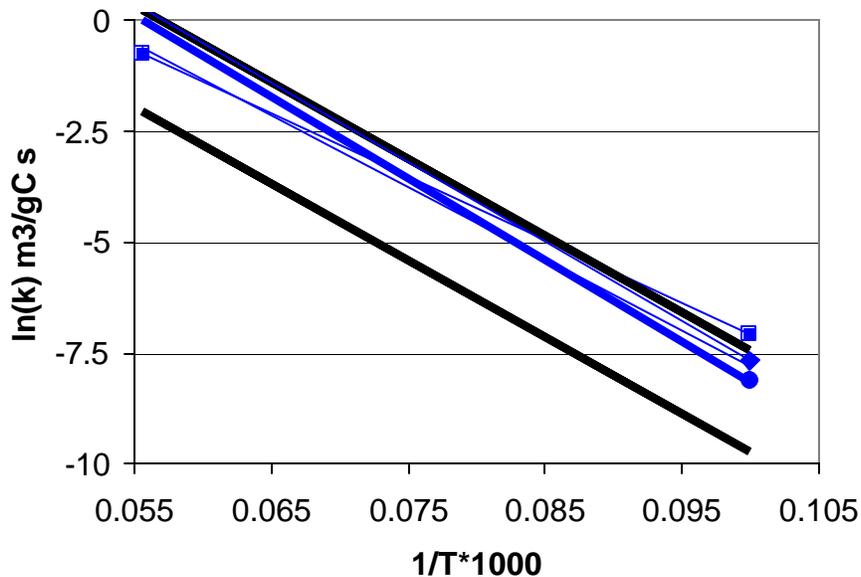
**Figure 3. NO/C and HCN/C ratios for the NO-char reaction.  
Coal Illinois No. 6. T = 1000°C**

**Table 2. Values for the reaction of char with NO for different chars**

	$k_0$ (m <sup>3</sup> /s gm C)	$E_a$ (J/gmol K)	$r$
Char U furnace	26439	152306	0.9972
Coal Illinois No. 6	1323	118589	0.9947
Activated char	27515	148748	0.9995

Figure 4 presents the comparison of the kinetic expressions of Table 2 to those of the general expression derived by Aarna and Suuberg<sup>8</sup>. The char-NO kinetics differ by less than one order of magnitude. Most of the results are in the upper range of the generalized expression given by E 14. Furthermore, there is not a great difference between the values reported for NO reduction on char for *in situ* chars and the one prepared *a priori*.

$$k_{NO} = 5.5 \times 10^6 \exp(-15939/T) \text{ g}_{NO} \text{ m}^{-2} \text{ h}^{-1} \text{ atm}_{NO}^{-1} \quad \text{E 14}$$



**Figure 4. Arrhenius plots for the reaction NO-char for four different solids. Bold lines represent general expression by Aarna and Suuberg<sup>8</sup> and one order of magnitude this value. Squares: Coal; Circles: Char U furnace; Diamonds: Activated char**

## 2. Experiments in the presence of oxygen

As discussed before, the rate of NO reduction on char surface seems to have a strong influence on the prediction of single particle models on the amount of char-N converted

to NO. Since this rate has been found first order with respect to NO, particularly in the high temperature regime,<sup>24</sup> it follows that it would be important to check the conversion of char-N to NO for different bulk-NO concentrations.

In order to do this, the variable  $\mathbf{a}_{NO}$ , as defined by E 15, was chosen to represent the amount of char-N converted to NO. Note that  $\mathbf{a}_{NO}$  can be negative in case when the char is reducing the NO injected as background gas.

$$\mathbf{a}_{NO} = \frac{\int_{t_1}^{t_2} \mathbf{n}(C_{NO}^{out} - C_{NO}^{in}) dt}{(N/C)_{solid} \int_{t_1}^{t_2} \mathbf{n}(C_{CO}^{out} + C_{CO_2}^{out}) dt} \quad \text{E 15}$$

Figure 5 presents the concentration of combustion products from the combustion of char U-Furnace when NO background was zero. Similar results were obtained from the other solid samples.

Although the duration of the char oxidation reaction is in the order of 1 second, the residence time in the analysis trail accounts for the broad peak in Figure 5. It is clear that the FTIR doesn't allow resolving the concentrations in time. However, the data is enough for the calculation of  $\mathbf{a}_{NO}$  and the carbon balance was between 85% and 110% for all the experiments. No specific trend in carbon balance was observed as the NO concentration was increased.

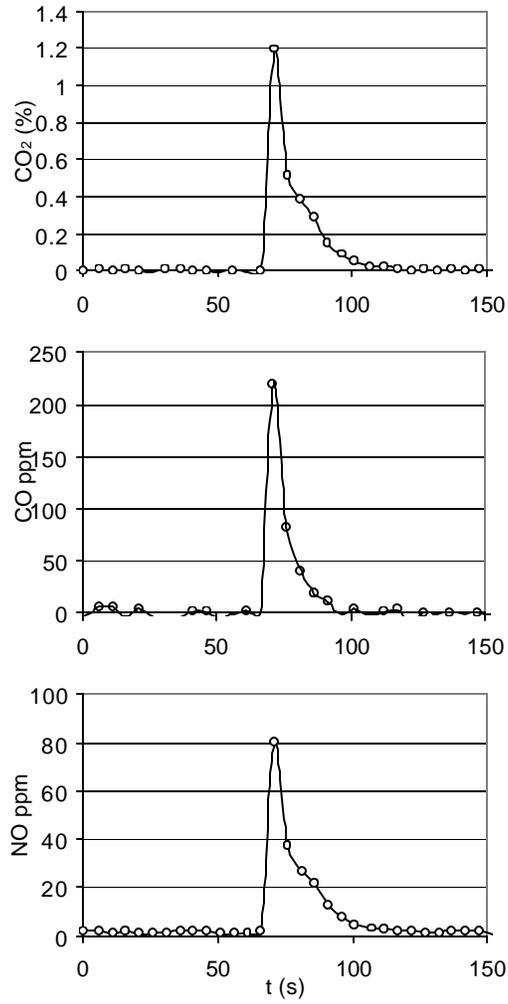
Figure 6 presents the results of  $\mathbf{a}_{NO}$  for three different solids: chars U-furnace, coal and activated char. The first striking result is that the plot of  $\mathbf{a}_{NO}$  vs. NO concentration in the background formed straight lines for all three solids. An almost linear relation was also obtained by Spinti<sup>25</sup> in similar experiments performed in a bench-scale pulverized coal

furnace.<sup>12</sup> This result, although surprising, may be explained in a rather simple way by considering the effect of the rate of NO reduction on the char surface.  $\mathbf{a}_{NO}$  can also be defined by:

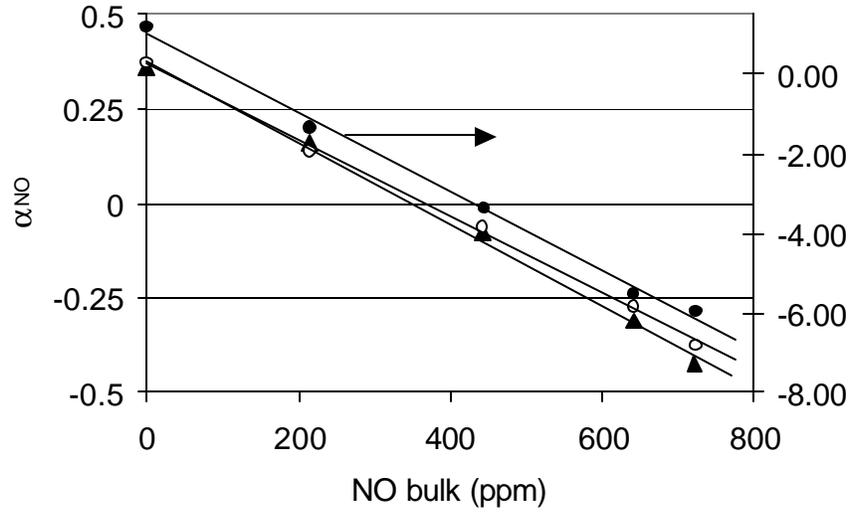
$$\mathbf{a}_{NO} = \frac{NO^{out} - NO^{in}}{NO_{solid}^{tot}} \quad \text{E 16}$$

Where  $NO_{solid}^{tot}$  represents the amount of NO produced from the solid if all the nitrogen in the solid were converted to NO, and  $NO^{out}$  and  $NO^{in}$  represent the NO leaving and entering the reactor respectively. Note that  $NO^{in} = NO^{bkg} + NO^{solid}$ , where  $NO^{bkg}$  represents the NO injected in the background and  $NO^{solid}$  the one produced by the solid. Since for these experiments, a rather small sample was used compared to the total gas flow,  $NO^{bkg} \gg NO^{solid}$ , therefore  $NO^{in} \sim NO^{bkg}$ . From E 1 and E 16 it follows that:

$$\mathbf{a}_{NO} = \frac{NO^{bkg} \left( \exp\left(\frac{-k_{NO} W_{char}}{\mathbf{n}}\right) - 1 \right)}{NO_{solid}^{tot}} \quad \text{E 17}$$



**Figure 5. Combustion gases concentration during char U-furnace oxidation.  
 $T_g=1698\text{K}$ . 4%O<sub>2</sub>/He.  $D_p= 58\mu\text{m}$ .**



**Figure 6. Variation of the conversion of solid-N to NO during oxidation experiments.  $T_g = 1698$  K. 4%O<sub>2</sub>.  $D_p = 58\mu\text{m}$ . ○: Char U-Furnace(left axis); △:Coal Illinois No. 6 (left axis); ●:Activated char (right axis)**

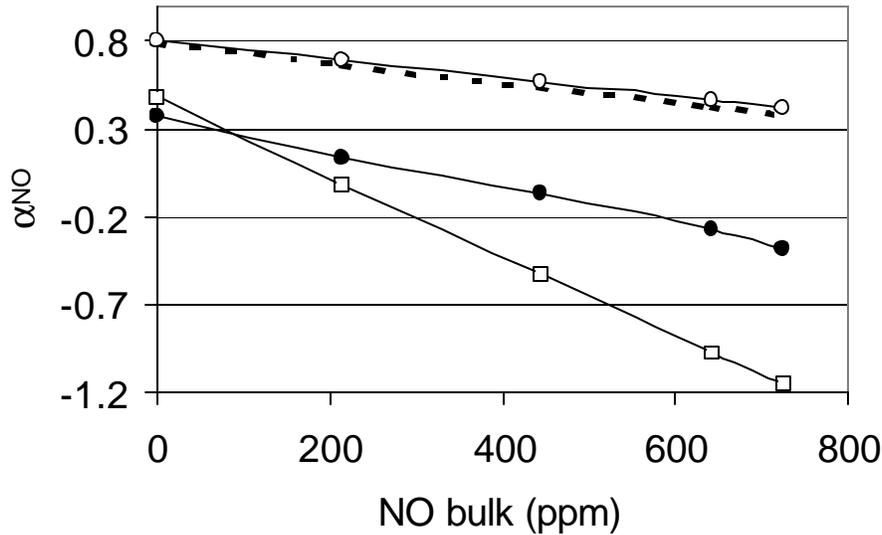
E 17 presents a linear relation between  $a_{NO}$  and  $NO^{bkg}$  and explains why the plot is so similar for the coal Illinois No. 6 and the char U-furnace. In the previous section,  $k_{NO}$  was found to be similar for the *in situ* prepared char from coal Illinois No. 6 and for the char U-furnace. If this is the case, for a given  $NO^{in}$ ,  $a_{NO}$  will only differ from the two solids in the value of  $NO_{solid}^{tot}$ , and given similar sample weights and since the nitrogen content of both solids is comparable (Table 1),  $a_{NO}$  will be similar for both samples. E 17 also predicts, in accordance to the results in Figure 6, that the activated carbon, with a lower value of  $NO_{solid}^{tot}$ , will present a higher slope for the plot of  $a_{NO}$  vs.  $NO^{bkg}$ .

Although expression E 17 gives explanation to many of the experimental facts observed during the combustion of the carbonaceous materials used in this study, it may not be easily applied to the combustion of a char particle, since it was designed for a steady-state system. Nevertheless, the important information obtained from E 17 is that any single

particle model for the prediction of char-N evolution to NO should consider a first order reaction of NO with char.

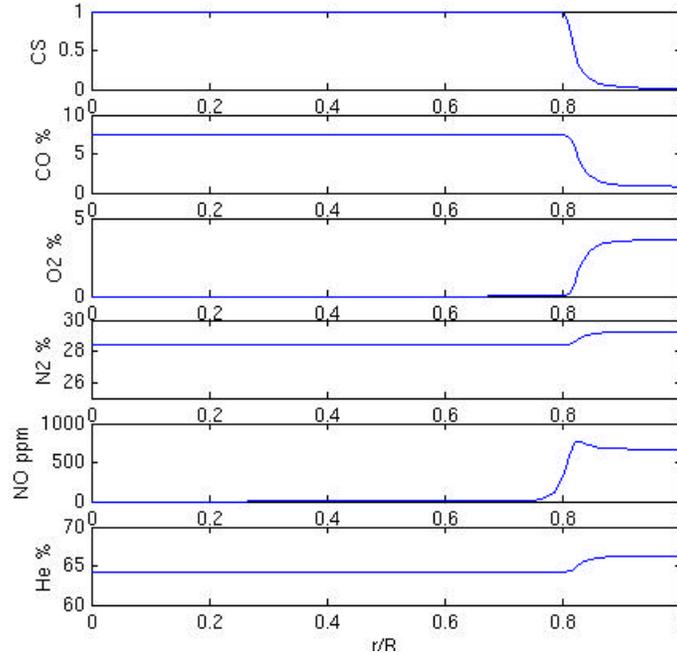
### **3. Single particle model and prediction of char-N evolution**

As a final part in the analysis, the single particle model described before was applied to the combustion of char with NO as background gas. From the prior discussion, it is clear that the rate of NO reduction on char surface is a very important parameter in the model. Therefore, as first approach, the values of  $k_{NO}$  determined in the oxygen-free experiments were used as inputs for the model and only reaction R 2 was considered for the destruction of NO on char surface. The open symbols in Figure 7 represent the results of this comparison. Although the model predicts the reduction of  $a_{NO}$  when the NO bulk concentration increased in a linear way, the estimated values for  $a_{NO}$  are higher than the values found experimentally. Similar results were obtained for the other chars. To provide more insight on the model predictions, Figure 8 presents the predicted variation of the species concentrations during char oxidation when char conversion was 0.4.  $C_s$  represents the ratio of carbon concentration at time  $t$  to that at the beginning of the reaction. According to the model predictions, the reaction of carbon oxidation occurs in a narrow range in the external part of the particle. This result is in agreement with the traditional approach of computing the rate of the carbon-oxygen reaction on an external surface area basis.<sup>26</sup>



**Figure 7. Comparison of model prediction with experimental data for the oxidation of char U-furnace  $T_p = 1800$  K.  $D_p = 58\mu\text{m}$ . 4.0%O<sub>2</sub>/640 ppm NO/29.4%N<sub>2</sub>/66%He**  
**●: Experimental data ○Model (Only R 2); Dotted line: Model (R 2 and R 1) □: Model (R 2 and R 1) and  $k_{NO} \cdot 10$**

NO is produced in the same narrow region of carbon oxidation, and it can diffuse inside the particle, where it is rapidly reduced on the char, or it can escape to the boundary layer. Due to the fast reaction of carbon with oxygen, the carbon concentration in this region is low, and a considerable amount of NO escapes to the boundary layer without been reduced by the particle. Figure 8 also shows that in the same region, the CO concentration is high, as is to be expected from the char oxidation. Under these conditions, reaction R 1 may be important in the process of NO destruction. Therefore, the kinetics of NO destruction by CO on the char surface was incorporated into the model. For R 1, Aarna and Suuberg<sup>27</sup> found that the reaction was zero order with respect to CO, particularly for high CO concentrations, and first order with respect to NO at high temperatures. They also suggested expression E 18 as a possible value for reaction R 1.



**Figure 8. Model prediction of species concentration vs. non-dimensional particle radius for the oxidation of char U-furnace  $T_p = 1800$  K.  $D_p = 58\mu\text{m}$ . 4.0%O<sub>2</sub>/640 ppm NO/29.4%N<sub>2</sub>/66%He Char conversion was 0.40.**

$$k_{NO-CO} = 1.2 \times 10^6 \exp(-13919/T) \text{ g}_{NO} \text{ m}^{-2} \text{ h}^{-1} \text{ atm}_{NO}^{-1} \quad \text{E 18}$$

Expression E 18 was incorporated into the model, but there was no significant improvement in model predictions (see Figure 7). Finally, for comparison, the effect of an increase in one order of magnitude in  $k_{NO}$  was evaluated. The results in Figure 7 show that although there is a reduction on the value of  $a_{NO}$  at low NO bulk concentrations, the slope of the plot differs from the one found in the experiments. This suggests, that the reason for the disagreement between model predictions and experimental results may not be only related to the value of  $k_{NO}$ , but also to another factor, possible a larger area of char in contact with NO than the one predicted by the relation for the Knudsen diffusivity.

## CONCLUSIONS

It is important to ensure that the pyrolysis reactions have neared completion prior to the determination of the rate of NO reduction on char surface. Otherwise, unrealistically high values of  $k_{NO}$  will result due to underestimation of the char sample and due to reactions between NO and the pyrolysis byproducts.

The different rates of NO reduction on char for the various carbonaceous materials used in this study were similar. These results, coupled with the first order reaction of NO with the char surface, explained why plots for the conversion of char-N to NO vs. NO bulk concentration lie on a linear plot, and why the results were almost independent of the nature of the carbon material used. This result underscores the importance of the reactions of char-N to form NO since it suggests that char particles surrounded by low NO concentrations, such as those produced in new low-NO<sub>x</sub> burners, will produce more NO from char-N than particles exposed to higher boundary layer NO concentrations. The similarity of the curves of conversion of char-N to NO vs. NO concentration (Figure 7) suggests that under the experimental conditions of this study, the heterogeneous reactions are the most important for the reduction of the NO that evolves during char oxidation.

A single particle model for the evolution of char-N to NO was developed. The model predicts correctly the linear decrease of char-N conversion to NO as the NO bulk concentration is increased. However, the model overpredicts NO production. The reason for this overprediction is unclear, but may be related to the availability of char surface for NO reduction during char combustion.

## NOMENCLATURE

$A_s$ :	Surface area of the particle ( $\text{kg m}^{-2}$ )
$A_{s_v}$ :	Internal surface area of the char per reactor volume ( $\text{m}^2 \text{m}^{-3}$ )
$C_i^{in}$ :	Concentration of species $i$ at reactor's entrance ( $\text{mol/m}^3$ )
$C_i^{out}$ :	Concentration of species $i$ at reactor's exit ( $\text{mol/m}^3$ )
$c_i$ :	Molar concentration of species $i$ ( $\text{gmol m}^{-3}$ )
$D_{eff}$ :	Mass transfer effective multicomponent diffusion coefficient ( $\text{m s}^{-2}$ )
$D_p$ :	Particle average diameter (m)
$D_{k,i}$ :	Knudsen diffusivity of species $i$
$J_i$ :	Molar diffusive flux of species $i$ ( $\text{mol m}^{-2} \text{s}^{-1}$ )
$k_g$ :	Mass transfer coefficient ( $\text{m s}^{-1}$ )
$k_{NO}$ :	Rate of NO-char reaction ( $\text{m}^3/\text{gmC s}$ )
$(N/C)_{solid}$ :	Nitrogen to carbon molar ratio in the injected solid (-)
$N_i$ :	Molar flux of species $i$ ( $\text{gmol m}^{-2} \text{s}^{-1}$ )
$R_i^v$ :	Volumetric molar rate of formation of species $i$ ( $\text{gmol m}^{-3} \text{s}^{-1}$ )
$R_i^C$ :	Intrinsic rate for the reaction carbon oxygen
$v$ :	Volumetric flow ( $\text{m}^3/\text{seg}$ )
$w_{coal}$ :	Weight of sample in the reactor (gm of C)
$T_g$ :	Gas temperature (K)
$r$ :	Particle radius at time $t$ (m)
$q$ :	Char porosity (-)
$q_o$ :	Char porosity at beginning of reaction (-)
$q_c$ :	Ratio char solid volume to char total volume (-)
$q_c = 1 - f_{ash} \frac{\mathbf{r}_p}{\mathbf{r}_{ash}}$	
$f_{ash}$ :	Initial ash mass fraction of the char
$\mathbf{r}_{ash}$ :	Ash density ( $\text{kg m}^{-3}$ )
$\mathbf{r}_p$ :	Particle density ( $\text{kg m}^{-3}$ )

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