Statistical analysis of mechanical properties for main cement phases by nanoindentation technique

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Abstract. This work focuses on mechanical properties of some phases of cement-based materials, portlandite (CH), calcite and clinker. Nano-indentation experiment is done on CSM instrument to verify the values of these cement pastes, Young moduli obtained by the averaged experimental load-depth curve is close to other references. The results show that: 1) the Young's modulus of CH averaged by nano-indentation experiment is 39.88GPa, which is in relative good agreement with the 40.30GPa by Constantinides, 36.00GPa by Acker and 45.95GPa by Laugesen. 2) By nano-indentation experiment, elastic moduli of CH, LD C-S-H, HD C-S-H, limestone filler and clinker are separately within the region of 38.8-50.6 *GPa*, 17.1-27.6*GPa*, 30.54-36.50 *GPa*, 79.8-90.6*GPa* and 94.26-114.18*GPa*. The elastic moduli are determined by experiment and the SEM image of these phases are verified, which is used to describe the microstructure and mechanical properties of this typical phases in cement paste.

1. Introduction

Structural concrete is composed of cementitious composites and concrete performance is related with cementitious composites structural mechanics at different length-scales[1]. Portlandite (CH), calcite and clinker are typical constituents of hydrated cementitious of portland cement paste [2], which influences the mechanical properties and the durability of cement paste. Besides, elastic modulus of clinker phases with porosity is reliable, calculated after applying the different porosities on C_3S, C_2S, C_3A and C_4AF structures[3]. As the founding that the elastic properties of the pure phases (C_3S, C_2S) and their solid solution alite and belite found in industrial clinker has no obvious difference[4]. Young's moduli of CH, calcite and clinker are studied for the modeling of cement at the micro scale [5]. Nano-indentation experiment is used to characterize of mechanical behavior at small scale [6], thus to provide the elastic modulus of cement hydration products [7,8].

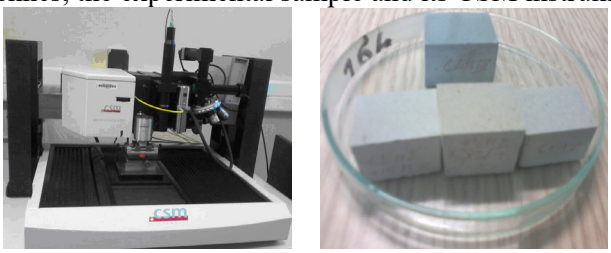
A large experimental nano-indentation campaign has been led to obtain a data basis of Young's modulus for the various phases of several cement pastes. These results may be used to validate the modeling approaches developed by the authors in previous publications. Although there are some reports on mechanical properties of cement phases, however, these reports basically focus on microstructure or qualitative analysis, and its experimental systematic research on CH, calcite and clinker at nanometers has not yet been studied. Results of nanometer cement phases during nonlinear indentation is used to compare with that of Keinde [10] and Constantinides [11]. Moreover, elastic

modulus of CH is to compare with that of the Brillouin spectroscopy measurement [12], DFT[13] and nano-iondentation[14,15]. The results of the nano-indetation tests have been already published in reference of Fu et al.[9], this new paper presents the results for pastes with CEM I and Sediments, and with CEM III. Results enable to provide elastic modulus of cement phases for the Multi-Scale Modelling of Computational Concrete platform [2,5].

2. Nano-indentation investigation of CH phase at micro-scale

2.1. Description of nano-indentation experiment

After the sample preparation and chemical composition, nano-indentation experiment is done on the instrument of INSA de Rennes, the experimental sample and its CSM instrument are in Fig.1.



a) Nano-hardness platform b) Cement paste sample

Figure 1. CSM instrument and cement paste used in experiment.

As in Figure 1 a), CSM instruments includes: ultra nano-indentation tester head, nano-indentation tester head, atomic force microscopy and optical video microscope. Samples with the dimension $1.1cm \times 1.1cm \times 1.1cm$ is in Figure 1 b). Parameters are set to be the same with reference[9].

2.2. Chemical composition and sample preparation

Composition and designation of the tested binder pastes are shown in Table 1.

Table 1. Composition and designation of the tested binder pastes

Composition (Kg/m^3)	B-CEMIII	B-CEMI SD
CEMI	-	303.6
CEMIII	330	-
Limeston filler	240	240
water	210	210
Sediment	-	26.4
water/binder	0.368	0.368

The chemical composition of the cements and mineral admixtures (limestone filler) are in Table 2.

Table 2. Composition and properties of cements and mineral admixtures

Components	CEMIII (%)	CEMI (%)	Limeston filler (%)
CaO	49.9	64.53	-
$CaCO_3$	-	-	96.8
SiO_2	29.1	20.12	0.9
Al_2O_3	8.5	5.03	-
Fe_2O_3	1	3.12	-
MgO	5	0.98	-
K_2O	0.32	0.98	-
Na_2O	0.4	0.16	-
SO_3	2.67	3.34	-
clinker content (%)	36	98	-
slag content (%)	62	-	-
Specific surface (cm^2/g)	4263	3649.9	4190

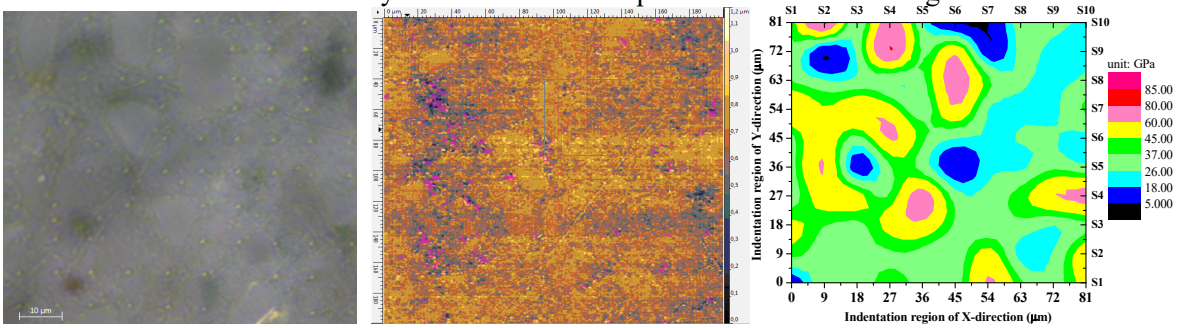
Specific gravity (g/cm^3)	2.98	3.15	2.7

3. Results analysis and discussion

3.1. Regional indentation analysis of B-CEM (III)

Nano-indentation experiment is carried out to determine elastic moduli of cement phases. Bountiful tests is applied to obtain mechanical properties of different phases [18]. The reduced modulus is used. For obtaining Young's modulus, the assumption on the value of the Poisson ratio is required to transform from the reduced modulus to Young's modulus, which should be clearly precise.

During data processing of B-CEM(III) sample, we focus on the analysis of hardness range of hydration products, the unhydrated particles will not be considered in statistics. By the order of elastic modulus and hardness from small to large, cement paste ingredients are: a mixture of pores and hydrates, low-density C-S-H gel, high density C-S-H gel and calcium hydroxide, slag hydrates, limestone grains, unhydrated slag particles and unhydrated clinker grains. The value of the Poisson coefficient is set to 0.2. The evolution of the elastic modulus E_{HIT} (unit: GPa) and maximum depth h_{max} (unit: *nm*) as a function of the indented position of the untreated sample are recorded. Typical regional indentation of the B-CEM(III) matrix area (100 indents, $81\times81\mu m^2$, indent distance $9\mu m$, force $1.5mN$) and elastic modulus distribution by nano-indentation experiments is shown in Figure 2.

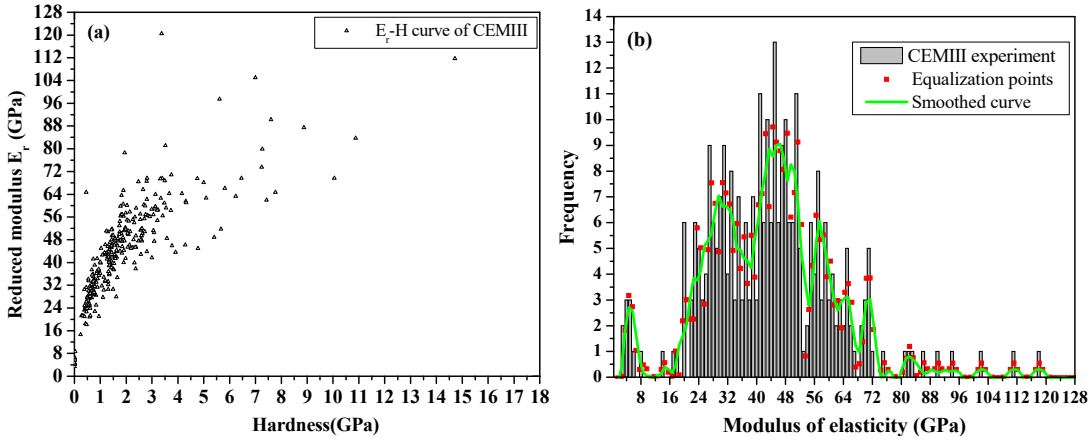


a) Indentation region b) Conscan map of the specimen c) The fitting areas of elastic modulus distribution

Figure 2. Indentation analysis of B-CEM(III) matrix in experiment

Figure 2 a) shows the distribution of 10×10 indents performed on the matrix. The marked plane area in Figure 2 b) is about $50nm\times50nm$. The indented area is visualized using an optical microscope, whereas the cement matrix region (the distance between two indents is $9\mu m$) is assigned to the smoothed surface surrounded by the outlined indent area enclosed by the color lines. Figure 2 c) presents the fitting of the contour areas to show the possible surround areas by all data of the indentation points with contrast to Figure 2 a). The real E_{HIT} distribution of individual indentation points in the indent region to divide the modulus into several ranges. The averaged Young's modulus on the determined 100 indents enable to obtain an approximate mean value of the matrix modulus.

Meanwhile, the mapping matrices and E_r-H curves according to the experiment data can be used to analyse the main phases in the indentation area. The number of total indents on surface is 363. The E_r-H curve and elastic modulus distribution by nano-indentation experiments are separately in Figure 3.



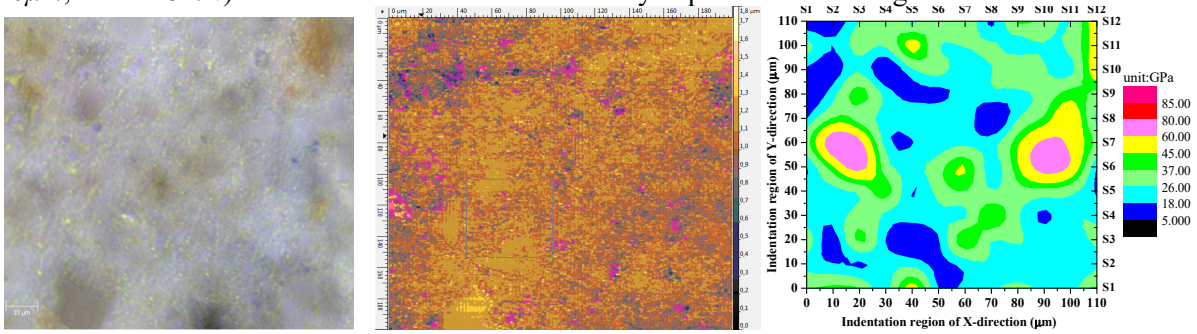
a) Distribution of the reduced modulus versus hardness b) Frequency histogram of elastic modulus

Figure 3. E_r-H curve and elastic modulus frequency histogram of B-CEM(III) sample

As is shown in Figure 3 a), the E_r-H curve basically turns to a kind of linear relationship. Besides, the averaged elastic modulus E_{HIT} of all the individual indents is about 36.695GPa and the averaged maximum depth h_{max} value is about 194.57nm. Moreover, we can suppose from Figure 3 b) that elastic moduli of different phases are as follows: LD C-S-H is 26GPa, HD C-S-H is 32GPa, CH and slag hydrate (probably stratlingite …) is 48GPa, Calcite and slag grains is in the range of 60-80 GPa.

3.2. Regional indentation analysis of B-CEM (I)_SD

Similarly, during data processing of B-CEM(I)_SD sample, the Poisson coefficient is set to 0.2. regional indentation of the B-CEM(I)_SD matrix area (144 indents, 110×110μm^2, indent distance 10μm, force 1.5mN) and elastic modulus distribution by experiments is in Figure 4.

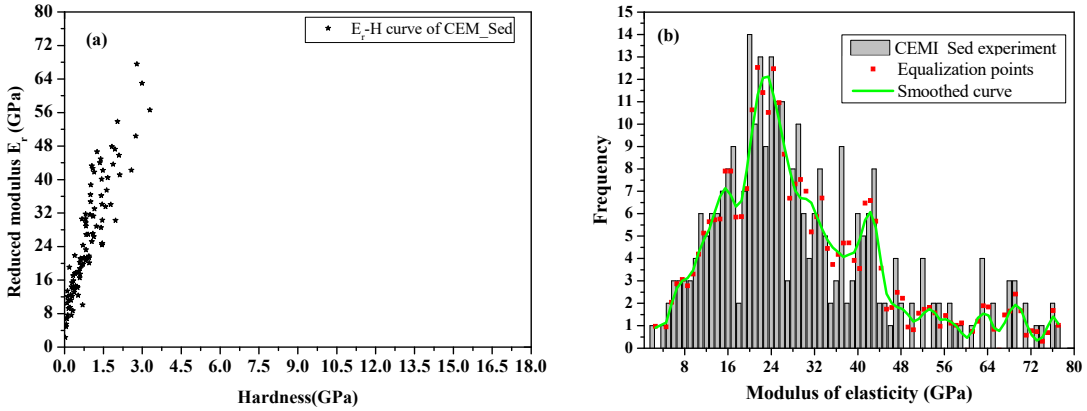


a) Indentation region b) Indentation area in the plane area c) The distribution of elastic modulus areas

Figure 4. Elastic modulus distribution of B-CEM(I)_SD by nano-indentation experiments

Figure 4 a) shows the distribution of 12×12 indents performed on the matrix of the B-CEM(I)_SD sample. The marked plane area in Figure 4 b) is about 50nm×50nm. The cement matrix region (the distance between two indents is 10μm) is assigned to the smoothed. Figure 4 c) presents the fitting of the contour areas to show the possible surround areas by all data of the indentation points with contrast to Figure 4 a). The indentation hardness HIT (equivalent to Meyer Hardness and similar to HV for a Vickers indenter) is introduced. The average of Young's moduli on the determined 144 indents enable to obtain an approximate mean value of the matrix modulus.

Meanwhile, the mapping matrices and E_r-H curves according to the experiment data can be used to analyse the main phases in the indentation area. The number of total indents on surface is 296. The E_r-H curve and elastic modulus distribution by nano-indentation experiments are in Figure 5.



a) Distribution of the reduced modulus versus hardness b) Frequency histogram of elastic modulus

Figure 5. E_r-H curve and elastic modulus frequency histogram of B-CEM(I)_SD sample

As is in Figure 5 a), the E_r-H curve basically turns to a kind of linear relationship. Besides, the averaged elastic modulus E_{HIT} of all the individual indents is about 30.08GPa and the averaged maximum depth h_{max} value is about 309.20nm. We can suppose from Figure 5 b) that elastic modulus of phases are as: LD C-S-H is 24GPa, HD C-S-H is 33GPa, CH is 43GPa,Calcite is 60-76GPa.

3.3. XRD spectra results of cement pastes

For various cement pastes, different phases can be determined according to their microstructures. Ye G. et al. [16]have investigated the microstructure of cementitious materials by experiment and simulation. There are different kinds of matrix components in our cement pastes: unhydrated clinker particles and mainly C_2S or C_3S, C-S-H gels (including low density, high density and pouzolanic), CH phase, ettringite phase (needles shape) and other phases (moncarboaluminates, stratlingite and slag etc.). X-ray experiments is proved to be effective, pastes are discussed by Davood [17] , in Figure 6.

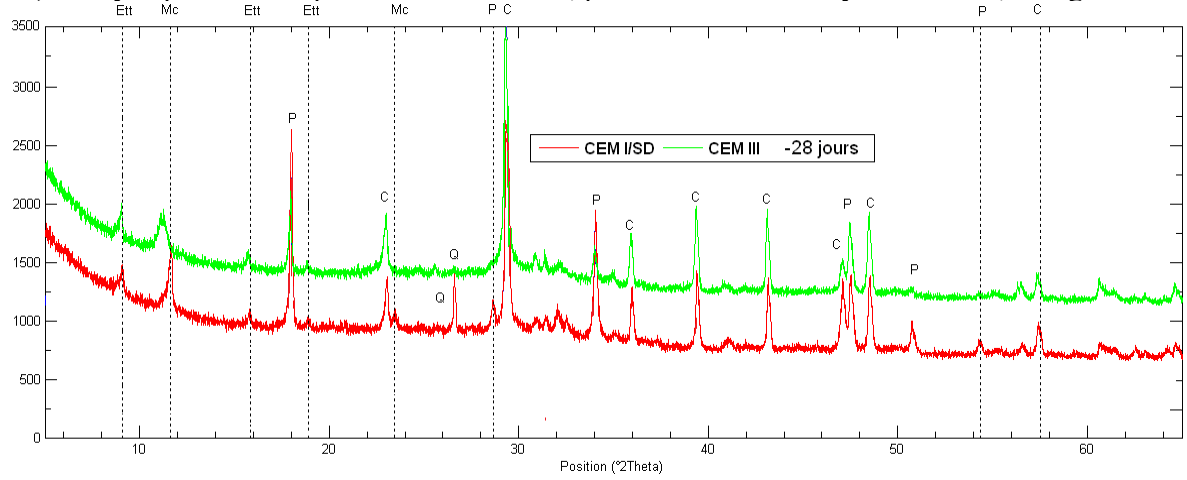
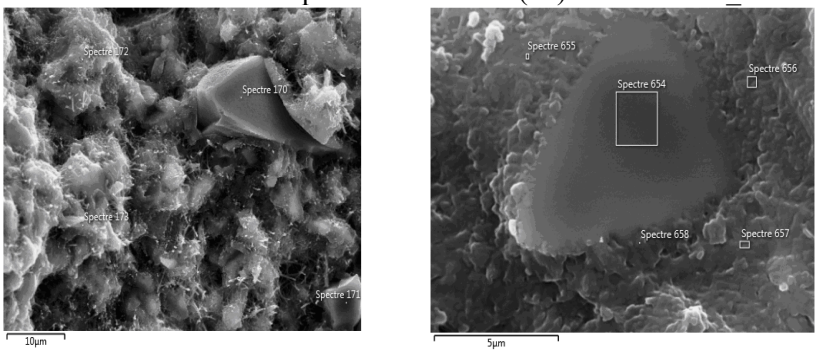


Figure 6. XRD spectra of different pastes at the ages of 28 days

Figure 6 shows the XRD spectra results of different pastes, including B-CEM(III), B-CEM(I)_SD with an age of 28 days. From Fig.6, the diffraction patterns on samples of binder pastes aged 28 days and 90 days are obtained. It also shows a series of intensive peaks of various substances in the X-ray diffraction curve (the 2θ angle is 28.60°). It can be seen that a certain amount of calcite, portlandite, ettringite and monocarbonatealuminate are presented and characterized in pastes of CEMI_SD. Besides, the quartz is also detected in CEMI_SD pastes. Moreover, the peak of portlandite is much less intense for the pastes in which a low content of clinker is also predictable like CEM III paste.

3.4. Morphology, composition analysis and microstructure

To highlight the cement phases in samples, SEM analysis are made in university of Rennes 1. Figure 7 shows typical microstructures of different phases in B-CEM (III) and B-CEMI_SD samples.



a) The test point 170 of slag in B-CEM (III) b) The Slag of the point 654 in B-CEMI_SD

Figure 7. Image of typical microstructures in B-CEM (III) and B-CEMI_SD samples

As can be seen from Figure 7 a), the test points of 170 and 171 are both slag particles with various particle sizes, with a higher elastic modulus in theory. Besides, the test point 173 with the sheet-like structure at the top of the microcrystalline position is possible for C-S-H phase. Meanwhile, in the Figure 7 b), the point 658 correspond to slash hydration product probably stratlingite or slag C-S-H phase and the point 654 corresponds to slag phase.

3.5. E_{HIT} frequency histogram of cement phases by nano-indentation experiment

Elastic moduli of LD and HD C-S-H structures by molecular dynamic simulation[9,18] and elastic modulus of CH and calcite by density functional theory[19] have been investigated in previous studies. However, these phases are not always detectable by simple observation. Then the comparison of E_{HIT} frequency histogram of samples is drawn, shown in Figure 8.

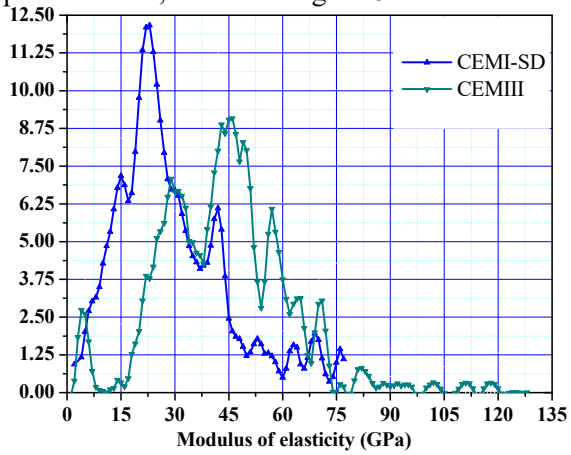


Figure 8 Comparison of E_{HIT} frequency histogram of two samples

Figure 8 shows comparison of frequency histogram of elastic modulus under various samples. For CH phase, the area of the histogram is within the range of 38.8-50.6 *GPa* and the averaged Young's modulus is about 40.2-49.2*GPa*, which is close to the values of 36.3-44.3*GPa* by Constantinides [10] and 33.0-39.0*GPa* by Acker [20]. For LD C-S-H and HD C-S-H phases, the area of the histogram is within the range of 17.1-27.6*GPa* (averaged to be 19.65-25.05*GPa*) and 30.54-36.50 *GPa* (averaged to be 29.92-37.12*GPa*) ,which is close to the values of LD C-S-H 14.0-22.4 *GPa* and HD C-S-H 27.0-32.8*GPa* by Constantinides [10] as well as to the values of LD C-S-H 18.0-22.0*GPa* and HD C-S-H 27.0-35.0*GPa* by Acker [20]. Furthermore, the latter two peaks which are probably limestone filler and clinker phases, there are some peaks in the range of 60-141*GPa*. The ranges of limestone filler and

clinker phases are separately 79.8-90.6*GPa* and 94.26-114.18*GPa*, and the averaged Young's modulus are separately 85.2±5.3*GPa* and 104.22±3.2*GPa*.

4. Conclusion

Nano-indentation experiments are carried out and regional indents are analyzed combined with the observation of morphology and analysis of the E_{HIT} frequency histogram. The experimental curves are analyzed and Young moduli are determined by the *P-h* curves. Conclusions are as follows:

1) Young's modulus of CH averaged by nano-indentation experiment is 39.88*GPa*, which is in good agreement with 40.30*GPa* by Constantinides, 36.00*GPa* by Acker and 45.95*GPa* by Laugesen..

2) By nano-indentation experiment, elastic moduli of CH, LD C-S-H, HD C-S-H, limestone filler and clinker are separately within the region of 38.8-50.6 *GPa*, 17.1-27.6*GPa*, 30.54-36.50 *GPa*, 79.8-90.6*GPa* and 94.26-114.18*GPa*.

In all, these parameters provide evidence to obtain the mechanical properties of certain cement phases, thus to establish an accurate multi-scale model of concrete on MuMoCC platform.

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