

# The Methodology of Calculation of Cutting Forces When Machining Composite Materials

D A Rychkov<sup>1</sup>, A S Yanyushkin<sup>1</sup>

<sup>1</sup> Bratsk State University, 40 Makarenko street, Bratsk, Russia

e-mail: rychkovda@gmail.com

**Abstract.** Cutting of composite materials has specific features and is different from the processing of metals. When this characteristic intense wear of the cutting tool. An important criterion in the selection process parameters composite processing is the value of the cutting forces, which depends on many factors and is determined experimentally, it is not always appropriate. The study developed a method of determining the cutting forces when machining composite materials and the comparative evaluation of the calculated and actual values of cutting forces. The methodology for calculating cutting forces into account specific features of the cutting tool and the extent of wear, the strength properties of the processed material and cutting conditions. Experimental studies conducted with fiberglass milling cutter equipped with elements of hard metal VK3M. The discrepancy between the estimated and the actual values of the cutting force is not more than 10%.

## Introduction

Widespread in modern industry are composite materials of polymer-based [1 – 3]. Their products in comparison with metals and alloys have a number of advantages, such as specific strength, resistance to corrosion, cost, etc. Machining composites has specific features in comparison with the processing of metals. These include increased wear of the cutting tool, the need to increase the front and rear corners of the cutting, the use of equipment with high-speed processing, the presence of local and general ventilation, etc. [4 – 10]. Modern production methods and technologies enable the manufacture of parts with high surface quality, performance, but do not always satisfy the requirements of form and dimensions of the product [11, 12]. For surfaces of different shapes is widespread milling. When milling of composite materials is recommended to use high-strength tool materials, such as cemented carbide and superhard materials [5, 13 – 15]. Difficulties in the use of these materials is the formation of a cutting edge with a small angle of sharpening, but this problem can be solved through the use of electro-technology diamond sharpening in a double etching [16 – 18].

The parameters include the milling process productivity, operability of the cutting tool, cutting power and surface finish. Urgent problem is to evaluate the cutting forces because they determine the processing capacity, the pressure on the cutting edge and chip character etc. Known research mainly aimed at finding the experimental methods for determining the cutting forces [19, 20], however, is not always advisable to conduct laboratory tests.

The aim of the study is to improve the technology for milling of composite materials, and the task is to develop methodology for calculating cutting forces, conducting an experiment for comparing the calculated and actual values of cutting forces.



### 1. Method for determining the cutting forces during milling

To determine the parameters influencing tool life in milling used the theory of strength of materials and cutting theory. We select the time when the forces acting on the "cutting tool - detail" system will have maximum values (Fig. 1). And refine them.

When cutting the material on the cutting edge of the tool by cutting layer the force of friction  $F_f^{ed}$ , which affects the degree of tool wear and the size of the chamfer wear. This force is related to the elastic resistance of the processed material and the appearance of the reaction  $N_{ed}$ . Frictional force  $F_f^{ed}$  direction is determined by the chamfer wear, which is taken tangent to the cutting surface, and the direction of reaction  $N_{ed}$  perpendicular to the direction of force  $F_f^{ed}$ .

When rotating milling cutter operates the centrifugal acceleration  $a_c^n$  and the presence of the tool imbalance can occur inertia force  $F^n$  directed in the opposite direction with respect to the centrifugal acceleration  $a_c^n$ . Since all rotating tools are subjected to balancing, the value of the imbalance in this case can be neglected, and take the position that the mass center of the cutter lies on the axis of rotation,  $F^n = 0$ .

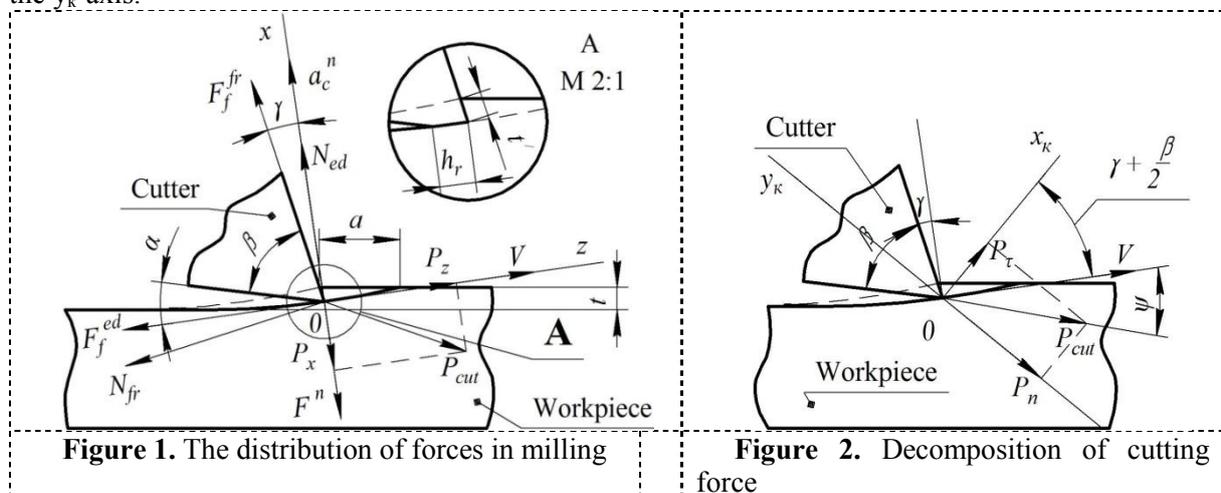
Also at the cutting edge the force of friction  $F_f^{fr}$ , which is connected with the elastic resistance of the treated material and the appearance of the reaction  $N_{fr}$ . The force  $F_f^{fr}$  is directed along the front surface of the cutting wedge and the reaction  $N_{fr}$  is directed perpendicular to the friction force  $F_f^{fr}$ .

Removal of material from the surface is effected by the cutting force  $P_{cut}$  which can be decomposed into two components:  $P_z$  and  $P_x$ , directed along the axes OX and OZ respectively. The axes of the projections are directed as follows: OZ axis is parallel to the vector velocity  $V$ ; and OX - perpendicular to the OZ axis.

Cutting force  $P_{cut}$  is determined by the formula, knowing its components:

$$P_{cut} = \sqrt{P_z^2 + P_x^2} \quad (1)$$

The cutting force  $P_{cut}$  affects flexural and compressive cutting edge of the tool axes  $y_k$  and  $x_k$  (Fig. 2). The  $y_k$ -axis is directed along the bisector of the angle wedge, on the  $x_k$ -axis perpendicular to the  $y_k$ -axis.



Thus, the force  $P_n$  directed along the  $y_k$  axis, will affect the value of the compressive stress in the cutting edge during milling, and the force  $P_\tau$ , directed along the  $x_k$  axis, - the value of the bending stress. Moreover, the direction of the cutting force  $P_{cut}$  is deflected from the direction of the velocity vector  $V$  on the angle  $\psi$ . According to the scheme in Fig. 2, this angle is  $\psi = \arctg\left(\frac{P_x}{P_z}\right)$ .

The value of the stress caused by the influence of the cutting forces will be:

$$\sigma_n = \frac{P_n}{B \cdot h_r} = \frac{P_{cut} \cdot \sin(\psi + \gamma + \beta/2)}{B \cdot h_r} \quad (2)$$

$$\sigma_\tau = \frac{P_\tau}{B \cdot h_r \cdot \sin \gamma} = \frac{P_{cut} \cdot \cos(\psi + \gamma + \beta/2)}{B \cdot h_r \cdot \sin \gamma} \quad (3)$$

where  $h_r$  – value chamfer wear along the rear surface of the cutting tool, mm;  $B$  – the width of the shear layer, mm;  $\gamma$  – the rake angle of the cutting tool;  $\beta$  – sharpening angle of the cutting edge.

Under normal conditions, the cutting stress must not exceed the strength properties of the cutting blade.

Cutting forces are determined based on the fact that the sum of the projections of the forces on the axis OZ and OX is equal to zero:

$$\sum F_i(z) = 0: P_z = N_{fr} \cdot \cos \gamma + F_f^{fr} \cdot \sin \gamma + F_f^{ed} \quad (4)$$

$$\sum F_i(x) = 0: P_x = -N_{ed} - F_f^{ed} \cdot \cos \gamma + N_{fr} \cdot \sin \gamma \quad (5)$$

$$F_f^{ed} = N_{ed} \cdot f \quad (6)$$

$$F_f^{fr} = N_{fr} \cdot f \quad (7)$$

where  $f$  – the coefficient of friction between the tool and the workpiece.

Given that the reactions  $N_{ed}$  and  $N_{fr}$  are dependent on the elastic properties of the material being processed, we obtain:

$$N_{ed} = \sigma_{el}^{pr} \cdot S_{cut} \quad (8)$$

$$N_{fr} = \sigma_{com}^{pr} \cdot S_{pr} \quad (9)$$

where  $\sigma_{com}^{pr}$  – the compressive strength of the processed material, MPa;  $\sigma_{el}^{pr}$  – elastic stress arising from the cutting material, MPa;  $S_{pr}$  – sectional area of a cut-off stratum in the direction, perpendicular to the reaction  $N_{fr}$ ,  $\text{mm}^2$ ;  $S_{cut}$  – sectional area of a cutting element in the direction, perpendicular to the reaction  $N_{ed}$ ,  $\text{mm}^2$ .

$$S_{pr} = B \cdot t' \quad (10)$$

where  $t'$  – the maximum thickness of cutting layer for milling, mm.

Maximum thickness of cutting layer depends on cutting conditions and cutter diameter and is defined by the formula:

$$t' = \frac{S_z \cdot t}{R \sin\left(\arccos\left(1 - \frac{t}{R}\right)\right)} \quad (11)$$

where  $S_z$  – feed to the cutter tooth, mm/tooth;  $R$  – cutter radius, mm;  $t$  – cutting depth, mm.

$$S_{cut} = B \cdot h_r \quad (12)$$

## 2. Method of the experiment

To establish the conformity of the calculated and the actual measurements of cutting forces set up an experiment to process composite glass fiber brand STEF-1 cutting tool equipped with inserts made of sintered carbide VK3M.

The study was conducted on the test bench, created on the base of the machine 3D642E model modernized under the processes of milling of composite materials with the possibility of establishing a high spindle speed and equipped with a number of local ventilation. The limits of variation of cutting conditions are set as follows: cutting depth  $t = 0.5 - 1.5$  mm, feed to the cutter tooth  $S_z = 0.16 - 0.33$  mm/tooth. Cutting speed  $V$  was set as much as possible that provide installation spindle speed  $n = 6000 \text{ min}^{-1}$ . Given that the torque from the motor to the spindle of the machine is carried by a belt transmission, characterized by belt slippage, and the cutting diameter of 150 mm and the cutting speed  $V = 45 \pm 2$  m/s.

The limits of variation, tool and processed materials are selected based on the recommendations on the treatment of polymeric materials reinforced with high-strength fibers and fabrics [5, 13 – 15].

When processing polymeric composite materials characterized by tool wear on the back surface, so the process stability criterion is the value chamfer wear along the rear surface of the cutting tool  $h_r = 0.35$  mm. Its further increase would lead to poor quality of the machined surface [5]. The value of chamfer is optically controlled.

During the experiment were monitored using cutting power meter K506. Calculation of cutting forces when power measurements carried out according to the formula:

$$P_{cut} = \frac{N_{cut}}{V} \quad (13)$$

where  $V$  – cutting speed, m/s.

## 3. Results and Discussion

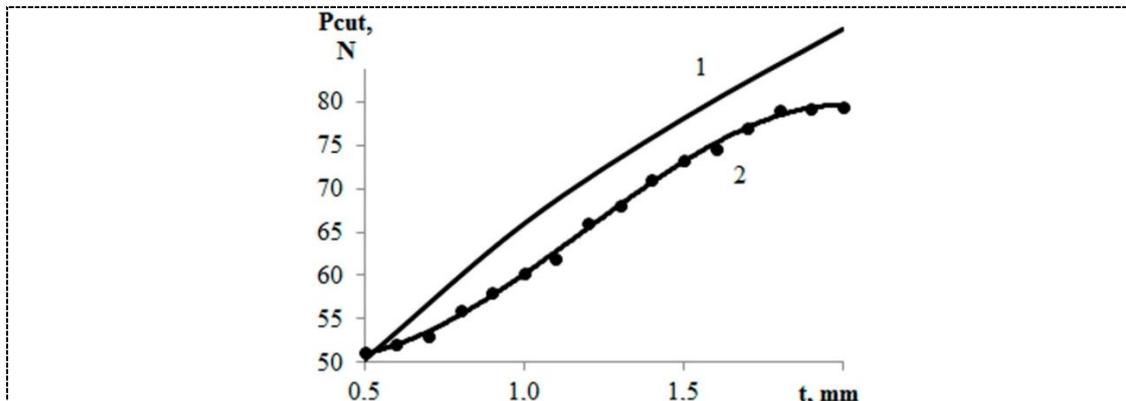
According to the experimental results obtained by mathematical relationship of the cutting force of the processing modes:

$$P_{cut} = 4.2 + 166S_z - 3t + 168S_z t \quad (14)$$

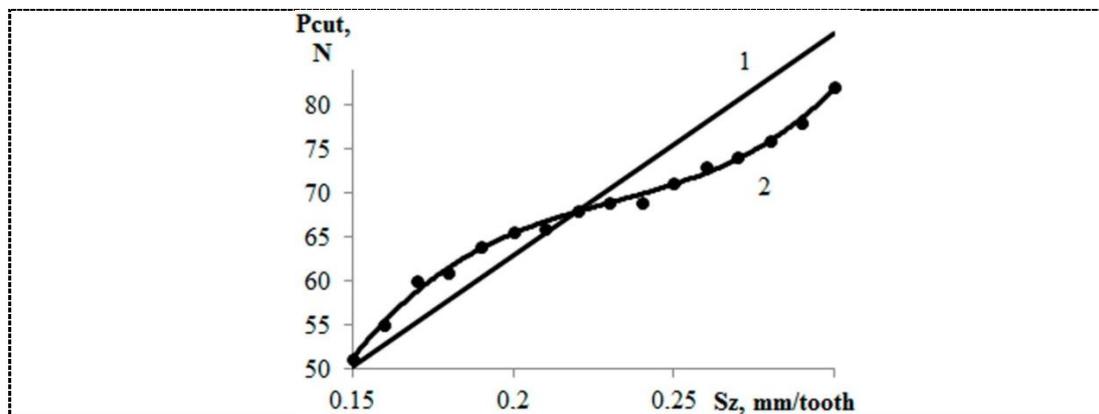
According to the above method calculated the cutting forces during milling fiberglass brand STEF-1 hard alloy VK3M with varying treatment regimens. The input parameters for the calculation were as follows: the rake angle  $\gamma = 25^\circ$ ; Compressive strength  $\sigma_{com}^{pr} = 400$  MPa; Cutter radius  $R = 62.5$  mm; The cutting width  $B = 10$  mm; the coefficient of friction  $f = 0.5$ ; chamfer wear along the rear surface  $h_r = 0.35$  mm.

For comparison of the calculated and experimental data plotted as the cutting force of the feed and depth of cut (Fig. 3, 4).

With increasing feed and depth of cut, the cutting force increases due to the increased thickness of the shear layer of the processed material and the load on the cutting tool. The values of the calculated and experimental curves do not differ by more than 10%. This makes it possible to predict with sufficient certainty value cutting forces at varying grades of composite materials, process conditions and constructional features of the cutting tool.



**Figure 3.** The dependence of the cutting force by the cutting depth: 1 – calculated dependence; 2 – experimental dependence



**Figure 4.** The dependence of the cutting force by the feed per tooth: 1 – calculated dependence; 2 – experimental dependence

## Conclusions

Conclusions and recommendations were made on the results of research:

1. An analysis of the scientific literature shows that the composite cutting issues are not well understood, not fully presented studies of the characteristics of their processing.
2. A method for calculating cutting forces during milling of materials based on the provisions of the mechanics and the theory of cutting. The method allows to calculate the cutting force with high accuracy and is used to determine the optimum cutting performance composite materials.
3. The mathematical dependence of the cutting force on the treatment regimes in order to assess the difference between calculated and experimental values. It was found that the error rate of not more than 10%, which is acceptable to the theoretical studies of the process of milling of composite materials and designing manufacturing operations.

## References

- [1] Gallant F M, Bruck H A, Prickett S E and Cesarec M 2006 Graded polymer composites using twin-screw extrusion: a combinatorial approach to developing new energetic materials *Composites Part A: Applied Science and Manufacturing* **6** 957–969.
- [2] Gorokhovskiy A V, Escalante-Garcia J I, Gashnikova G Yu, Nikulina L P and Artemenko S E 2005 Composite materials based on wastes of flat glass processing *Waste Management* **7** 733–736.
- [3] Dhand V, Mittal G, Rhee K Y, Park S J and Hui D 2015 A short review on basalt fiber reinforced polymer composites *Composites Part B: Engineering* **73** 166–180.

- [4] Lobanov D V and Yanyushkin A S 2011 Analysis of structural precast solutions milling tools for machining composite materials *Engineering Technology* **5** 20–25.
- [5] Lobanov D V, Yanyushkin A S, Rychkov D A and Petrov N P 2011 Optimal organization of tools for machining composites *Russian Engineering Research* **2** 156–157.
- [6] Bailleul J L, Sobotka V, Delaunay D and Jarny Y 2003 Inverse algorithm for optimal processing of composite materials *Composites Part A: Applied Science and Manufacturing* **8** 695–708.
- [7] Lemma E, Chen L, Siores E and Wang J 2002 Study of cutting fiber-reinforced composites by using abrasive water-jet with cutting head oscillation *Composite Structures* **1-4** 297–303.
- [8] Fomin V N, Malyukova E B and Berlin A A 2004 Criteria for optimization of processing and fabrication of polymer composite materials *Doklady Chemistry* **4-6** 39–41.
- [9] Matis I G 1991 Methods and means of inspecting the quality of composite materials *Russian Journal of Nondestructive Testing* **4** 277–285.
- [10] Bakulin V N, Larin A A and Reznichenkod V I 2015 Improving the quality of manufacture of polymer-composite products using computed tomography as a nondestructive-testing method *Journal of Engineering Physics and Thermophysics* **2** 556–560.
- [11] Skeebe V Yu, Ivancivsky V V and Pushnin V N 2015 Numerical modeling of steel surface hardening in the process of high energy heating by high frequency currents *Applied Mechanics and Materials* **698** 288–293.
- [12] Plotnikova N V, Losinskaya A A, Skeebe V Yu and Nikitenko E 2015 Perspective of high energy heating implementation for steel surface saturation with carbon *Applied Mechanics and Materials* **698** 351–354.
- [13] Yuanyushkin A S, Rychkov D A and Lobanov D V 2014 Surface quality of the fiberglass composite material after milling *Applied mechanics and materials* **682** 183–187.
- [14] Davim J P, Reis P and António C C 2004 A study on milling of glass fiber reinforced plastics manufactured by hand-lay up using statistical analysis (anova) *Composite Structures* **3-4** 493–500.
- [15] Yanyushkin A S, Lobanov D V and Rychkov D A 2015 Automation tool preparation in the conditions of production *Applied Mechanics and Materials* **770** 739–743.
- [16] Arkhipov P V, Yanyushkin A S, Lobanov D V and Petrushin S I 2013 The effect of diamond tool performance capability on the quality of processed surface *Applied mechanics and materials* **379** 124–130.
- [17] Yanyushkin A S, Saprykina N A and Medvedeva O I 2014 Mechanism of protective membrane formation on the surface of metal-bonded diamond disks *Applied Mechanics and Materials* **682** 327–331.
- [18] Yanyushkin A S, Lobanov D V, Arkhipov P V and Ivancivsky V V 2015 Contact processes in grinding *Applied Mechanics and Materials* **788** 17–21.
- [19] Kalla D, Twomey J and Sheikh-Ahmad J 2010 Prediction of cutting forces in helical end milling fiber reinforced polymers *International Journal of Machine Tools and Manufacture* **10** 882–891.
- [20] McKenzie W M, Ko P, Cvitkovic R and Ringler M 2001 Towards a model predicting cutting forces and surface quality in routing layered boards *Wood Science and Technology* **6** 563–569.