

# Four- and three-body breakup mechanism of ${}^6\text{Li}$ elastic scattering

S Watanabe<sup>1</sup>, T Matsumoto<sup>2</sup>, K Ogata<sup>3</sup> and M Yahiro<sup>2</sup>

<sup>1</sup>RIKEN Nishina Center, Wako, Saitama 351-0198, Japan

<sup>2</sup>Department of Physics, Kyushu University, Fukuoka 812-8581, Japan

<sup>3</sup>Research Center for Nuclear Physics (RCNP), Osaka University, Ibaraki, Osaka 567-0047, Japan

E-mail: shin.watanabe.vf@riken.jp

**Abstract.** We investigate a breakup mechanism of  ${}^6\text{Li}$  elastic scattering on heavy targets ( $T = {}^{209}\text{Bi}$  or  ${}^{208}\text{Pb}$ ) with the four-body version of the continuum-discretized coupled-channels method (four-body CDCC). Four-body CDCC successfully reproduces measured elastic cross sections with no adjustable parameter, and we can then clearly discuss the four-body dynamics. Our analysis shows that  $d\alpha$  breakup ( ${}^6\text{Li} + T \rightarrow d + \alpha + T$ ) is much more essential than  $np\alpha$  breakup ( ${}^6\text{Li} + T \rightarrow n + p + \alpha + T$ ) in  ${}^6\text{Li}$  scattering.

## 1. Introduction

In reactions of weakly-bound nuclei, projectile breakup plays an important role and the treatment of projectile-breakup effects is essential to describe scattering. The continuum-discretized coupled-channels method (CDCC) was proposed as a method for treating breakup effects [1, 2, 3]. Nowadays, CDCC is applied to not only three-body scattering (two-body projectile + T) but also four-body scattering (three-body projectile + T) [4, 5, 6, 7], where T denotes a target. CDCC for three- and four-body scattering are now called three- and four-body CDCC, respectively.

${}^6\text{Li} + {}^{209}\text{Bi}$  scattering near the Coulomb barrier energy ( $E_b^{\text{Coul}} \approx 30$  MeV) was first analyzed with three-body CDCC based on the  $d+\alpha + {}^{209}\text{Bi}$  three-body model [8]. However, the calculation could not reproduce the measured elastic cross section without introducing a normalization factor for the optical potentials. This problem was solved by four-body CDCC based on the  $n + p + \alpha + {}^{209}\text{Bi}$  four-body model [6]. The four-body calculation describes the experimental data without introducing any adjustable parameter. As an interesting finding, we showed that three-body CDCC can reproduce the cross section if the phenomenological  $d$ -optical potential is replaced by the single-folding potential that does not include  $d$ -breakup effects [6]. This suggests that  $d$  (*i.e.* the  $n$ - $p$  subsystem of  ${}^6\text{Li}$ ) hardly breaks up during  ${}^6\text{Li}$  scattering. In this work, we investigate the breakup mechanism within the four-body CDCC framework and validate the evidence.

## 2. Decomposition of the CDCC model space

We only recapitulate the treatment of model space in four-body CDCC; see Ref. [3, 7] for the detail. In four-body CDCC, the Schrödinger equation is solved in the model space  $P$  spanned by



the ground and discretized-continuum states of  ${}^6\text{Li}$ :  $P = \sum_{\gamma=0}^N |\Phi_\gamma\rangle \langle\Phi_\gamma|$ , where  $\Phi_\gamma$  represents the  $\gamma$ -th eigenstate, and the  $\gamma = 0$  and  $\gamma = 1-N$  correspond to the ground and discretized-continuum states, respectively. The  $\Phi_\gamma$  are obtained as pseudostates by using the Gaussian expansion method [9].

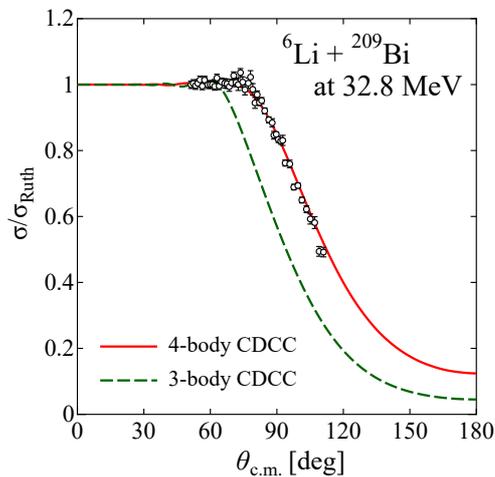
In this paper, we investigate the breakup mechanism by restricting the model space  $P$ . For this purpose, we first specify whether the breakup state  $\Phi_\gamma$  ( $\gamma = 1-N$ ) is the  $d\alpha$ -dominant or  $np\alpha$ -dominant breakup state by calculating the squared overlap between  $\Phi_\gamma$  and the  $d$  ground state  $\phi^{(d)}$ :  $\Gamma_\gamma^{(d\alpha)} = |\langle\phi^{(d)}|\Phi_\gamma\rangle|^2$ . If  $\Gamma_\gamma^{(d\alpha)}$  is larger (smaller) than 0.5, the state is defined as a  $d\alpha$ -dominant state  $\Phi_\gamma^{(d\alpha)}$  ( $np\alpha$ -dominant state  $\Phi_\gamma^{(np\alpha)}$ ). With the  $d\alpha$ - and  $np\alpha$ -dominant state above, the CDCC model space  $P$  can be decomposed into the three parts  $P = P_0 + P_{d\alpha} + P_{np\alpha}$ , where

$$P_0 = |\Phi_0\rangle \langle\Phi_0|, P_{d\alpha} = \sum_{\beta} |\Phi_{\beta}^{(d\alpha)}\rangle \langle\Phi_{\beta}^{(d\alpha)}|, P_{np\alpha} = \sum_{\delta} |\Phi_{\delta}^{(np\alpha)}\rangle \langle\Phi_{\delta}^{(np\alpha)}|. \quad (1)$$

In the following discussion, we calculate cross sections by switching on and off to clarify the reaction dynamics.

### 3. Results

First, we show the validity of four-body CDCC. Figure 1 shows the angular distribution of elastic cross section for  ${}^6\text{Li} + {}^{209}\text{Bi}$  scattering at 32.8 MeV. The three-body CDCC calculation (dashed line) underestimates the experimental data as reported in Ref. [8]. We then apply four-body CDCC in order to explain this discrepancy. Four-body CDCC (solid line) perfectly reproduces the experimental data without introducing any adjustable parameter.  ${}^6\text{Li} + {}^{209}\text{Bi}$  scattering near the Coulomb barrier energy is thus described by four-body CDCC. Therefore, we can clearly discuss the breakup mechanism below.

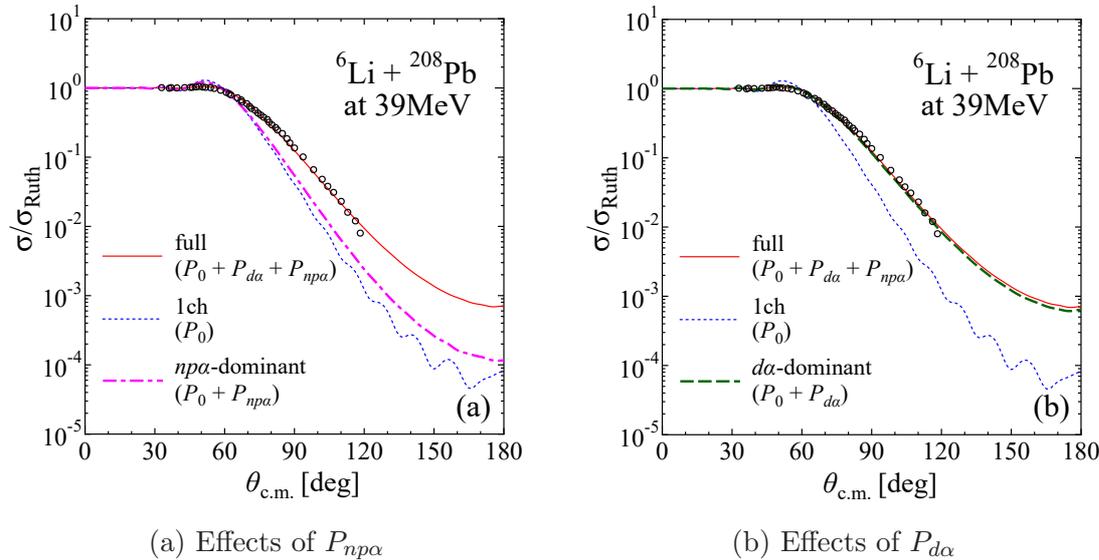


**Figure 1.** (Color online) Elastic cross sections (divided by the Rutherford cross section) for  ${}^6\text{Li} + {}^{209}\text{Bi}$  scattering at 32.8 MeV. The solid (dashed) line represents the result of four-body CDCC (three-body CDCC) calculation. The experimental data is taken from Refs.[10, 11].

Next, we show  ${}^6\text{Li} + {}^{208}\text{Pb}$  scattering at 39 MeV in Fig 2, which is almost the same as  ${}^6\text{Li} + {}^{209}\text{Bi}$  scattering at 32.8 MeV. The solid and dotted lines correspond to the full and 1ch calculations, respectively. These are nothing but the calculations in  $P$  and  $P_0$ , respectively. The difference comes from breakup effects and the full calculation reproduces the experimental data well by virtue of breakup effects.

Now, we switch on only the subspace  $P_{np\alpha}$  or  $P_{d\alpha}$  from  $P_0$  in order to investigate the breakup mechanism. The dot-dashed line (a) represents the calculation of  $P_0 + P_{np\alpha}$  and it is close to 1ch calculation (dotted line). On the other hand, the dashed line (b) corresponds to the calculation of  $P_0 + P_{d\alpha}$  and it simulates the full calculation (solid line) almost perfectly. It should be noted

that the number of  $d\alpha$ -dominant states is much less than that of  $np\alpha$ -dominant states in the present model space  $P$ . As seen above,  $d\alpha$  breakup is favored in  ${}^6\text{Li}$  scattering. This property is now called  $d\alpha$ -dominance, and we have found that the  $d\alpha$ -dominance is realized in a wide energy range [7]. It has been thus confirmed that  $d$  (*i.e.* the  $n$ - $p$  subsystem of  ${}^6\text{Li}$ ) hardly breaks up during  ${}^6\text{Li}$  scattering.



**Figure 2.** (Color online) Elastic cross sections for  ${}^6\text{Li} + {}^{208}\text{Pb}$  scattering at 39 MeV. The solid and dotted lines correspond to the results of full and 1ch calculations, respectively. The dot-dashed line (a) represents the calculation with the model space  $P_0 + P_{np\alpha}$ , whereas the dashed line (b) shows the calculation with  $P_0 + P_{d\alpha}$ . The experimental data is taken from Ref. [12].

#### 4. Summary

We have investigated four-body dynamics of  ${}^6\text{Li}$  elastic scattering ( $n + p + \alpha + \text{T}$ ,  $\text{T} = {}^{209}\text{Bi}$  or  ${}^{208}\text{Pb}$ ). The elastic scattering are successfully described in the four-body CDCC framework without introducing any adjustable parameter. We can then clearly analyze the breakup mechanism. Our analysis shows that the  $d\alpha$ -dominant breakup is much more essential compared with the  $np\alpha$ -dominant breakup for describing the scattering ( $d\alpha$ -dominance). This justifies the fact that  $d$  (*i.e.* the  $n$ - $p$  subsystem of  ${}^6\text{Li}$ ) hardly breaks up during  ${}^6\text{Li}$  scattering.

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