

Four- and three-body breakup mechanism of ${}^6\text{Li}$ elastic scattering

S Watanabe¹, T Matsumoto², K Ogata³ and M Yahiro²

¹RIKEN Nishina Center, Wako, Saitama 351-0198, Japan

²Department of Physics, Kyushu University, Fukuoka 812-8581, Japan

³Research Center for Nuclear Physics (RCNP), Osaka University, Ibaraki, Osaka 567-0047, Japan

E-mail: shin.watanabe.vf@riken.jp

Abstract. We investigate a breakup mechanism of ${}^6\text{Li}$ elastic scattering on heavy targets ($T = {}^{209}\text{Bi}$ or ${}^{208}\text{Pb}$) with the four-body version of the continuum-discretized coupled-channels method (four-body CDCC). Four-body CDCC successfully reproduces measured elastic cross sections with no adjustable parameter, and we can then clearly discuss the four-body dynamics. Our analysis shows that $d\alpha$ breakup (${}^6\text{Li} + T \rightarrow d + \alpha + T$) is much more essential than $n p \alpha$ breakup (${}^6\text{Li} + T \rightarrow n + p + \alpha + T$) in ${}^6\text{Li}$ scattering.

1. Introduction

In reactions of weakly-bound nuclei, projectile breakup plays an important role and the treatment of projectile-breakup effects is essential to describe scattering. The continuum-discretized coupled-channels method (CDCC) was proposed as a method for treating breakup effects [1, 2, 3]. Nowadays, CDCC is applied to not only three-body scattering (two-body projectile + T) but also four-body scattering (three-body projectile + T) [4, 5, 6, 7], where T denotes a target. CDCC for three- and four-body scattering are now called three- and four-body CDCC, respectively.

${}^6\text{Li} + {}^{209}\text{Bi}$ scattering near the Coulomb barrier energy ($E_b^{\text{Coul}} \approx 30$ MeV) was first analyzed with three-body CDCC based on the $d + \alpha + {}^{209}\text{Bi}$ three-body model [8]. However, the calculation could not reproduce the measured elastic cross section without introducing a normalization factor for the optical potentials. This problem was solved by four-body CDCC based on the $n + p + \alpha + {}^{209}\text{Bi}$ four-body model [6]. The four-body calculation describes the experimental data without introducing any adjustable parameter. As an interesting finding, we showed that three-body CDCC can reproduce the cross section if the phenomenological d -optical potential is replaced by the single-folding potential that does not include d -breakup effects [6]. This suggests that d (*i.e.* the n - p subsystem of ${}^6\text{Li}$) hardly breaks up during ${}^6\text{Li}$ scattering. In this work, we investigate the breakup mechanism within the four-body CDCC framework and validate the evidence.

2. Decomposition of the CDCC model space

We only recapitulate the treatment of model space in four-body CDCC; see Ref. [3, 7] for the detail. In four-body CDCC, the Schrödinger equation is solved in the model space P spanned by



the ground and discretized-continuum states of ${}^6\text{Li}$: $P = \sum_{\gamma=0}^N |\Phi_\gamma\rangle \langle\Phi_\gamma|$, where Φ_γ represents the γ -th eigenstate, and the $\gamma = 0$ and $\gamma = 1-N$ correspond to the ground and discretized-continuum states, respectively. The Φ_γ are obtained as pseudostates by using the Gaussian expansion method [9].

In this paper, we investigate the breakup mechanism by restricting the model space P . For this purpose, we first specify whether the breakup state Φ_γ ($\gamma = 1-N$) is the $d\alpha$ -dominant or $np\alpha$ -dominant breakup state by calculating the squared overlap between Φ_γ and the d ground state $\phi^{(d)}$: $\Gamma_\gamma^{(d\alpha)} = |\langle\phi^{(d)}|\Phi_\gamma\rangle|^2$. If $\Gamma_\gamma^{(d\alpha)}$ is larger (smaller) than 0.5, the state is defined as a $d\alpha$ -dominant state $\Phi_\gamma^{(d\alpha)}$ ($np\alpha$ -dominant state $\Phi_\gamma^{(np\alpha)}$). With the $d\alpha$ - and $np\alpha$ -dominant state above, the CDCC model space P can be decomposed into the three parts $P = P_0 + P_{d\alpha} + P_{np\alpha}$, where

$$P_0 = |\Phi_0\rangle \langle\Phi_0|, \quad P_{d\alpha} = \sum_{\beta} |\Phi_\beta^{(d\alpha)}\rangle \langle\Phi_\beta^{(d\alpha)}|, \quad P_{np\alpha} = \sum_{\delta} |\Phi_\delta^{(np\alpha)}\rangle \langle\Phi_\delta^{(np\alpha)}|. \quad (1)$$

In the following discussion, we calculate cross sections by switching on and off to clarify the reaction dynamics.

3. Results

First, we show the validity of four-body CDCC. Figure 1 shows the angular distribution of elastic cross section for ${}^6\text{Li} + {}^{209}\text{Bi}$ scattering at 32.8 MeV. The three-body CDCC calculation (dashed line) underestimates the experimental data as reported in Ref. [8]. We then apply four-body CDCC in order to explain this discrepancy. Four-body CDCC (solid line) perfectly reproduces the experimental data without introducing any adjustable parameter. ${}^6\text{Li} + {}^{209}\text{Bi}$ scattering near the Coulomb barrier energy is thus described by four-body CDCC. Therefore, we can clearly discuss the breakup mechanism below.

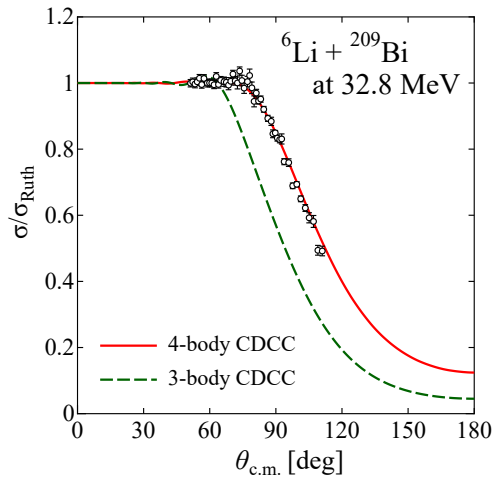


Figure 1. (Color online) Elastic cross sections (divided by the Rutherford cross section) for ${}^6\text{Li} + {}^{209}\text{Bi}$ scattering at 32.8 MeV. The solid (dashed) line represents the result of four-body CDCC (three-body CDCC) calculation. The experimental data is taken from Refs.[10, 11].

Next, we show ${}^6\text{Li} + {}^{208}\text{Pb}$ scattering at 39 MeV in Fig 2, which is almost the same as ${}^6\text{Li} + {}^{209}\text{Bi}$ scattering at 32.8 MeV. The solid and dotted lines correspond to the full and 1ch calculations, respectively. These are nothing but the calculations in P and P_0 , respectively. The difference comes from breakup effects and the full calculation reproduces the experimental data well by virtue of breakup effects.

Now, we switch on only the subspace $P_{np\alpha}$ or $P_{d\alpha}$ from P_0 in order to investigate the breakup mechanism. The dot-dashed line (a) represents the calculation of $P_0 + P_{np\alpha}$ and it is close to 1ch calculation (dotted line). On the other hand, the dashed line (b) corresponds to the calculation of $P_0 + P_{d\alpha}$ and it simulates the full calculation (solid line) almost perfectly. It should be noted

that the number of $d\alpha$ -dominant states is much less than that of $np\alpha$ -dominant states in the present model space P . As seen above, $d\alpha$ breakup is favored in ${}^6\text{Li}$ scattering. This property is now called $d\alpha$ -dominance, and we have found that the $d\alpha$ -dominance is realized in a wide energy range [7]. It has been thus confirmed that d (*i.e.* the n - p subsystem of ${}^6\text{Li}$) hardly breaks up during ${}^6\text{Li}$ scattering.

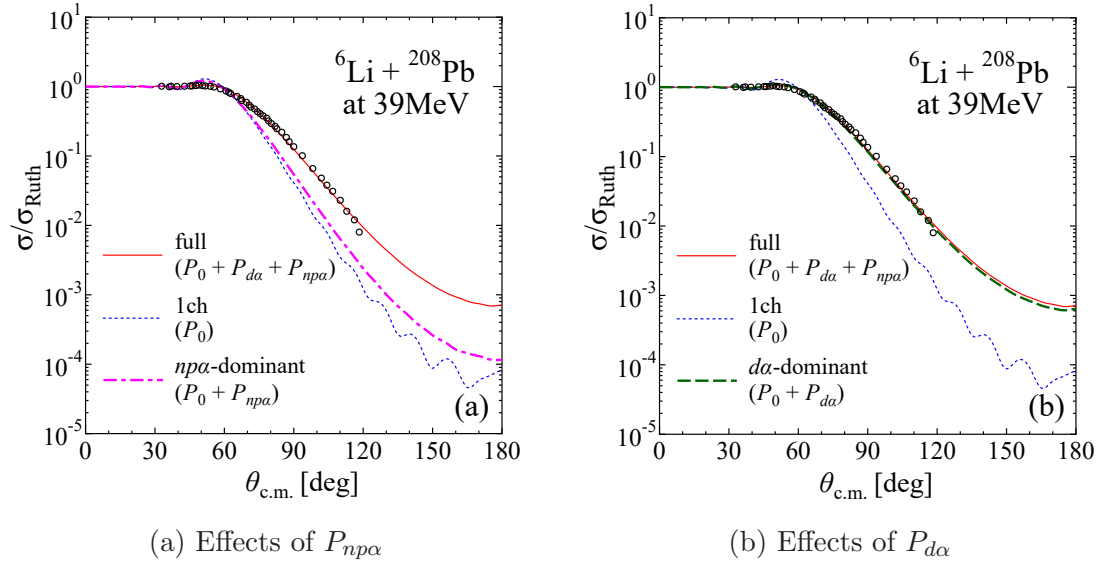


Figure 2. (Color online) Elastic cross sections for ${}^6\text{Li} + {}^{208}\text{Pb}$ scattering at 39 MeV. The solid and dotted lines correspond to the results of full and 1ch calculations, respectively. The dot-dashed line (a) represents the calculation with the model space $P_0 + P_{np\alpha}$, whereas the dashed line (b) shows the calculation with $P_0 + P_{d\alpha}$. The experimental data is taken from Ref. [12].

4. Summary

We have investigated four-body dynamics of ${}^6\text{Li}$ elastic scattering ($n + p + \alpha + \text{T}$, $\text{T} = {}^{209}\text{Bi}$ or ${}^{208}\text{Pb}$). The elastic scattering are successfully described in the four-body CDCC framework without introducing any adjustable parameter. We can then clearly analyze the breakup mechanism. Our analysis shows that the $d\alpha$ -dominant breakup is much more essential compared with the $np\alpha$ -dominant breakup for describing the scattering ($d\alpha$ -dominance). This justifies the fact that d (*i.e.* the n - p subsystem of ${}^6\text{Li}$) hardly breaks up during ${}^6\text{Li}$ scattering.

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