

# Nondestructive Determination of $^{235}\text{U}$ Enrichment of Uranium Samples in the Presence of Actinides ( $^{232}\text{Th}$ , $^{236}\text{U}$ , $^{237}\text{Np}$ )

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**Abstract.** The measurements were performed using a planar Ge detector. The multi-group analysis (MGA) for the determination isotopic abundances in low enriched uranium samples is applied in this study. In order to perform the analysis of complex gamma-spectrums, were taken a number of gamma-spectrums of single reference samples, containing  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{232}\text{Th}$ ,  $^{236}\text{U}$ ,  $^{237}\text{Np}$  with declared isotopic abundance. The gamma-ray spectrums in the range of low energy X-ray and gamma-ray peaks of these samples were obtained and analyzed.

## 1. Introduction

The determination of  $^{235}\text{U}$  enrichment is of great importance of nuclear technology. The MGA for uranium (MGAU) method for non-destructive assay of  $^{235}\text{U}$  enrichment does not require the use of any nuclear material standards [1].

The MGAU-code is based on the analysis of the 89-120 keV region of Ge detector spectrum. There are some limitations of using of MGAU-code: the resolution at  $E\gamma=122$  keV of Germanium detector less than 700 eV; it requires from the daughter isotopes be in activity equilibrium with the  $^{235}\text{U}$  and  $^{238}\text{U}$  parent isotopes (it require up to six months after chemical separation); the accuracy of the method diminishes when the thickness of sample container becomes excessive; the abundances of actinides ( $^{232}\text{Th}$ ,  $^{236}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{239}\text{Pu}$ ) and other gamma-emitter nuclides (fission products, et all) must be very little. The MGAU-code was designed to operate with little or no user interaction, that is as «complete secrecy»-code (we can not change the parameters of the code). Hence the conclusion: it is necessary to perform a preliminary analysis of the gamma-ray spectrums of the samples for the presence of «interfering» impurities - gamma emitters (actinides) [1-2].

The first task of this investigation is to perform the analysis of gamma-spectrums of single reference samples containing  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{232}\text{Th}$ ,  $^{236}\text{U}$ ,  $^{237}\text{Np}$  with declared isotopic abundance.

The second task – using the MGAU-code to obtain the results of the  $^{235}\text{U}$  enrichment of samples: a) «pure» U-samples and b) «dirty» U-samples, containing different concentrations of actinides ( $^{232}\text{Th}$ ,  $^{236}\text{U}$ ,  $^{237}\text{Np}$ ). Before each using of the MGAU-code it is necessary to analyze gamma-spectrum of sample.

The third task – to obtain the results of the  $^{235}\text{U}$  enrichment sample using the gamma-spectrum of investigated sample without use of MGAU-code. In order to decide this task the «peak-ratio» technique was applied [3] in the narrow 89-99-keV energy range. The peak 89.95-keV in spectrum of the sample is a measure of the  $^{235}\text{U}$  concentration (X-ray Th X<sub>Kα2</sub>). The intensities of 92.4 and 92.8-



keV lines of  $^{234}\text{Th}$  are used as a measure of  $^{238}\text{U}$  concentration of the sample. The 93.35-keV thorium  $\text{K}\alpha_1$  line was used as a measure of  $^{235}\text{U}$  concentration. The contribution of 93.35-keV line was taken into account by using the special procedure.

## 2. Experimental description

### 2.1. Equipment

Spectrums were taken in planar Ge detector with resolution 460 eV at  $E_\gamma=122$  keV (full width at half maximum, FWHM). The multichannel digital analyzer DSA-1000 Canberra and Genie-2000 (including MGAU-code) soft were used. The spectrums were stored in 4096 channels with a gain of 0.75 keV/channel. During the measurements there was performed the control of the position of the X-ray and gamma-ray peaks at energies of 63.1 and 185.72 keV, respectively belonging  $^{234}\text{Th}$  and  $^{235}\text{U}$ . The maxima of the peaks were situated respectively in the channels (844±1) and (2476±4).

### 2.2. The Gamma and X-rays Nuclear Data

The Gamma and X-rays nuclear data are presented in Table 1.

**Table 1.** Gamma and X-rays nuclear data [4].

	Energy (keV)	Photon emission probability (%)
$\gamma\text{-ray}(^{235}\text{U}/^{231}\text{Th})$	89.95±0.2	1.00±0.6
Th $\text{K}\alpha_2$	89.957	28.2±0.6
Pa $\text{K}\alpha_2$	92.282	28.3±0.6
$\gamma\text{-ray}(^{238}\text{U}/^{234}\text{Th})$	92.38	2.8±0.3
$\gamma\text{-ray}(^{238}\text{U}/^{234}\text{Th})$	92.80	2.8±0.3
$\gamma\text{-ray}(^{235}\text{U}/^{231}\text{Th})$	93.02	0.047±0.006
Th $\text{K}\alpha_1$	93.35	46.0±0.9
U $\text{K}\alpha_3$	93.844	0.098±0.003

### 2.3. The Procedure of the Experimental Investigation

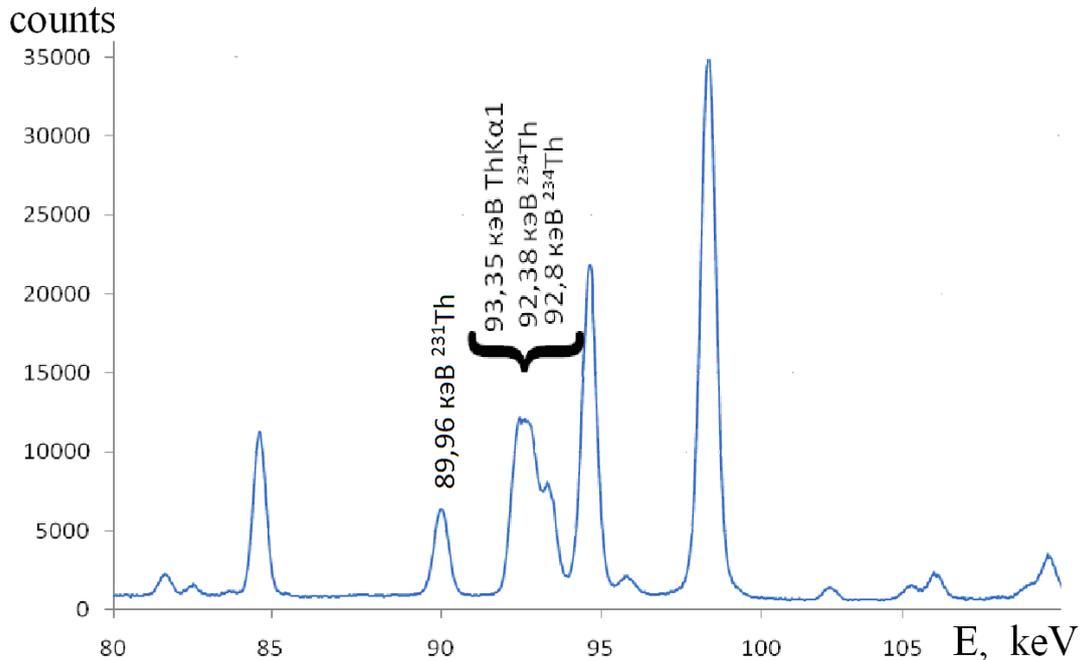
#### 2.3.1. The Investigation of Influence of Different Concentrations of $^{232}\text{Th}$ and $^{236}\text{U}$ Presence in $\text{UO}_2$ -Samples on the Results of $^{235}\text{U}$ Enrichment Determination by MGAU-code

The  $^{235}\text{U}$  enrichment of the reference  $\text{UO}_2$ -sample ( $^{235}\text{U}$  enrichment  $x=6.50$  wt%) was determined by MGAU-code (Table 2).

**Table 2.** The results of  $^{235}\text{U}$  enrichment using MGAU-code analysis for  $\text{UO}_2$ -sample ( $x=6.50$  wt%).

Nuclide	Weight fraction of nuclide, (%)	Derivation
$^{234}\text{U}$	0.045	0.010 (22.2 %)
$^{235}\text{U}$	6.352	0.084 (1.3%)
$^{238}\text{U}$	93.603	0.084 (0.1%)

The gamma-spectrum of the reference UO<sub>2</sub>-sample (<sup>235</sup>U enrichment x=6.50 wt%) was taken. The peak 89.95-keV in spectrum of this sample is a measure of the <sup>235</sup>U concentration (X-ray Th X<sub>Kα2</sub>) (Figure 1).



**Figure 1.** Gamma and X-ray spectrum of enriched uranium sample (x=6.50 wt%).

The gamma-spectrum of <sup>232</sup>Th sample was taken. In this spectrum the peak of sample 89.95-keV is a measure of <sup>232</sup>Th concentration.

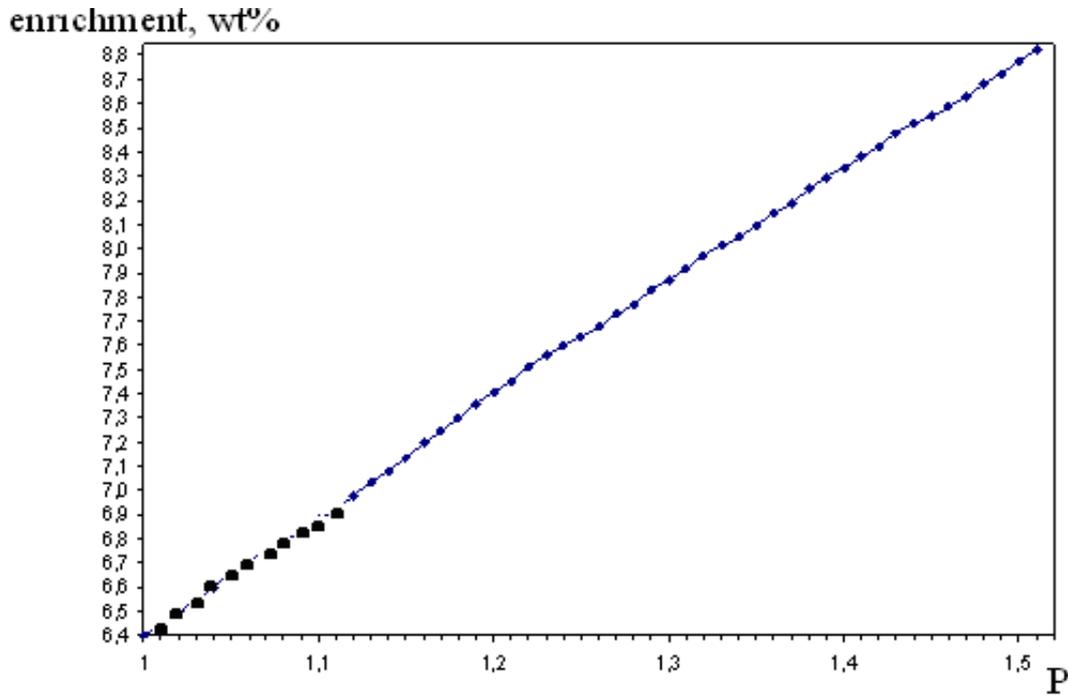
The count rate in peaks 89.95 keV in both samples was determined (measuring peak intensity in counts/s). The time of measuring <sup>232</sup>Th sample spectrum, corresponding the increasing the value of count rate in peak 89.95 keV in the spectrum of UO<sub>2</sub>-sample (<sup>235</sup>U enrichment x=6.50 wt%) is obtained.

Using the gamma-spectrum of UO<sub>2</sub>-sample contained in the memory of multi-channel analyzer, the UO<sub>2</sub>-sample was removed from Ge - detector and then the <sup>232</sup>Th-sample was put on the detector. After the spectrum measurement of <sup>232</sup>Th-sample during the necessary time the count rate in the peak 89.95-keV increased by 1%. That corresponds to an increase of weight fraction <sup>232</sup>Th in the mixture of (UO<sub>2</sub>+<sup>232</sup>Th). A new treatment of obtained spectrum was performed by MGAU-code, ect. Step by step we obtain the response function of MGAU-code of increasing 89.95 keV count rate peak by gamma-emitter (<sup>232</sup>Th-sample). This count rate depends from parameter P:

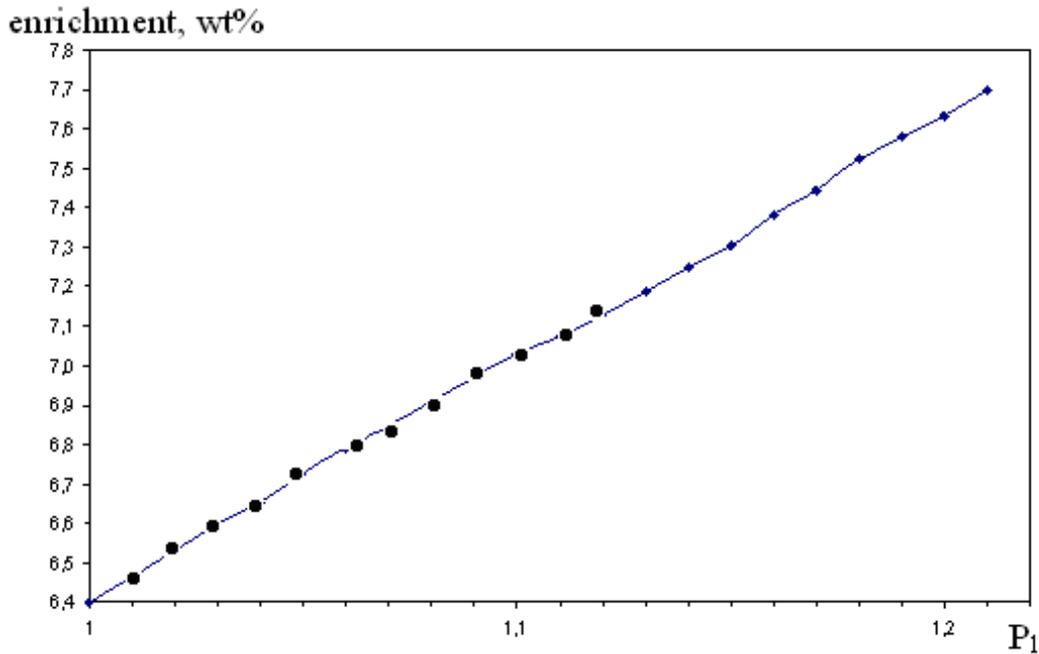
$$P = \frac{S^{90\text{ keV}}(UO_2(6.5\%) + {}^{232}\text{Th})}{S^{90\text{ keV}}(UO_2(6.5\%))} \tag{1}$$

The dependence of <sup>235</sup>U enrichment (obtained using MGAU-code analysis) from parameter P is presented on Figure 2. The number of the «big points» on the Figure 2 corresponds that there are no message from MGAU-code «gamma-emitting nuclides are present in investigated sample» on measure of increase of parameter P before certain moment. The analogical procedure was performed with <sup>236</sup>U sample. The results are presented in Figure 3 in dependence of the

$$P_1 = \frac{S^{90\text{ keV}}(UO_2(6.5\%) + {}^{236}\text{U})}{S^{90\text{ keV}}(UO_2(6.5\%))}.$$



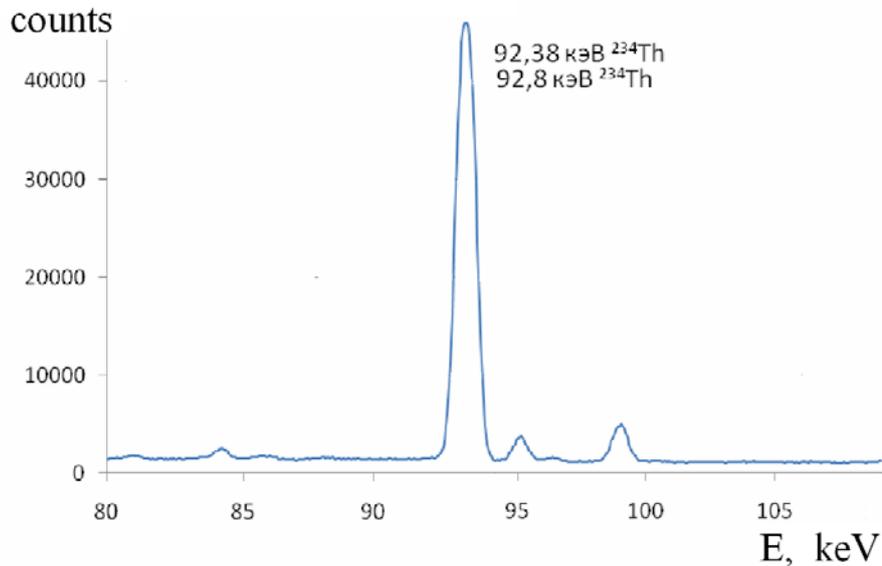
**Figure 2.** Dependence of  $^{235}\text{U}$  enrichment (obtained using MGAU-code analysis) from parameter P:  $^{232}\text{Th}$  gamma-emitting nuclide is present in investigated sample.



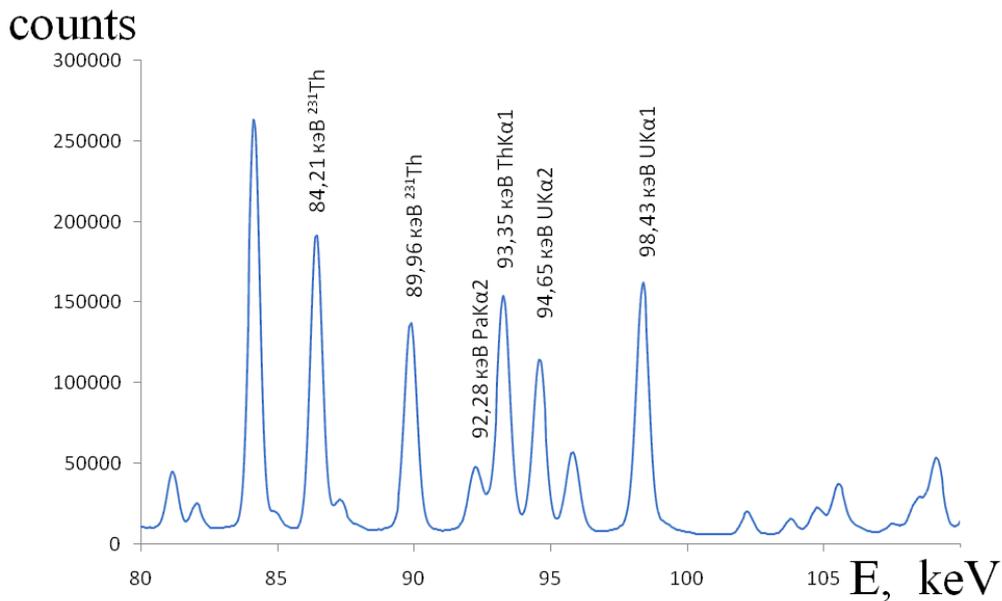
**Figure 3.** Dependence of  $^{235}\text{U}$  enrichment (obtained using MGAU-code analysis) from parameter P<sub>1</sub>:  $^{236}\text{U}$  gamma-emitting nuclide is present in investigated sample.

2.2.2. The «Peak-Ratio» Technique for  $^{235}\text{U}$  Enrichment Determination in Samples (Without Using of MGAU-Code)

On the Figure 4 is presented the gamma and X-ray spectrum of depleted uranium sample ( $x=0.0025$  wt%). On the Figure 5 is presented the gamma and X-ray spectrum of enriched uranium sample ( $x=98$  wt%)



**Figure 4.** Gamma and X-ray spectrum of depleted uranium sample ( $x=0.0025$  wt%).



**Figure 5.** Gamma and X-ray spectrum of enriched uranium sample ( $x=98$  wt%).

The «strip» function of the multichannel analyzer was used as follows: 1) store an «enriched» spectrum of uranium enriched to 99.5 % in  $^{235}\text{U}$ ; 2) obtain the sample spectrum, then normalize the «enriched» spectrum to the 89.96 keV X-ray of the sample spectrum; and 3) subtract the normalized «enriched» spectrum from the sample spectrum. The resultant stripped spectrum contains the cleanly resolved  $^{238}\text{U}$  gamma-ray doublet at 92-keV peak from the stripped spectrum and the 89.96-keV X-ray peak area from the original sample spectrum are used to obtain the  $^{238}\text{U}/^{235}\text{U}$  ratio. A relationship between enrichment,  $X$ , and the  $^{238}\text{U}/^{235}\text{U}$  ratio,  $R$ , can be obtained as follows:

$$X = \frac{100 \cdot w.f.^{235}\text{U}}{w.f.^{234}\text{U} + w.f.^{235}\text{U} + w.f.^{236}\text{U} + w.f.^{238}\text{U}} \quad (2),$$

where  $w.f.^{234}\text{U}$ ,  $w.f.^{235}\text{U}$ ,  $w.f.^{236}\text{U}$ ,  $w.f.^{238}\text{U}$  - weight fraction of  $^{234}\text{U}$ ,  $^{235}\text{U}$ ,  $^{236}\text{U}$ ,  $^{238}\text{U}$ , respectively

Substitutive the following approximation into the above equation:

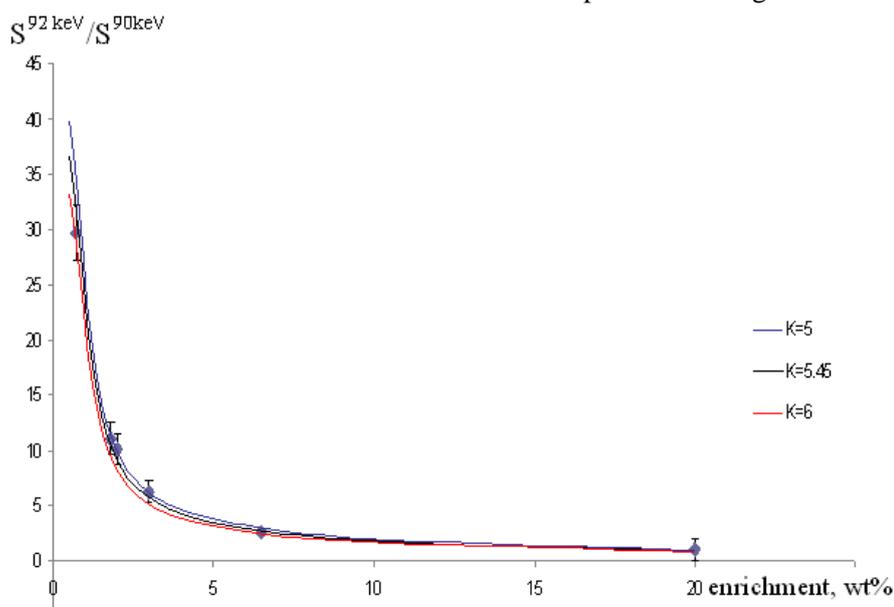
$$w.f.^{234}\text{U} + w.f.^{236}\text{U} = 0.01 \cdot w.f.^{235}\text{U} \quad (3).$$

Than rearrange the terms to obtain:

$$X = \frac{100}{1.01 + \frac{w.f.^{238}\text{U}}{w.f.^{235}\text{U}}} = \frac{100}{1.01 + K \cdot R},$$

where  $R = \frac{S^{92\text{keV}}}{S^{90\text{keV}}}$ ;  $K = 5,46$  is an experimental constant. The constant  $K$  is determined in by

iterative way to give the best fit to the calibration data where  $R = \frac{S^{92\text{keV}}}{S^{90\text{keV}}}$ . The relationship between peak area ratios  $S^{92\text{keV}}/S^{90\text{keV}}$  and  $^{235}\text{U}$  enrichment are presented in figure 6.



**Figure 6.** (color online) Relationship between peak area ratios  $S^{92\text{keV}}/S^{90\text{keV}}$  and  $^{235}\text{U}$  enrichment.

### 3. Conclusions

Using the high resolution planar Ge detector it is possible to take the gamma-spectrums of «clean» uranium samples and «unknown» «dirty» uranium samples, containing some concentrations of actinides. Using a single reference samples, containing  $^{232}\text{Th}$ ,  $^{236}\text{U}$ ,  $^{237}\text{Np}$  etc. with declared isotopic abundance, it is possible to increase the count rates in corresponding gamma-spectrum peaks of «unknown» «dirty» uranium samples and obtain the response function of MGAU-code from the  $^{235}\text{U}$  enrichment (using MGAU-code) in dependence of parameter **P**. At last, now it is possible to estimate the number of steps, that corresponds the increasing of **P** on 1%, when the MGAU-code message «gamma-emitters are present in sample» will be obtain.

The «peak-ratio» technique description, presented in this paper, allows explaining the procedure of  $^{235}\text{U}$  enrichment determination of uranium samples without using of MGAU-code and its allows obtaining the  $^{235}\text{U}$  enrichment of investigated samples.

The study of nondestructive determination of  $^{235}\text{U}$  enrichment of uranium samples in the presence of actinides will be continued.

### 4. References

- [1] Gunnik R *et al* 1994 A New Analysis Code for Measuring U-235 Enrichments in Arbitrary Samples *IAEA Symposium on International Safeguards, Vienna, Austria. Lawrence Livermore National Laboratory. Report UCRL-JC-114713 Livermore, California*
- [2] Yucel H 2007 The Applicability of MGA Method for Depleted and Natural Uranium Isotopic Analysis in the Presence of Actinides ( $^{232}\text{Th}$ ,  $^{237}\text{Np}$ ,  $^{233}\text{Pa}$  and  $^{241}\text{Am}$ ) *Applied Radiation and Isotopes* **65** p 1269-1280
- [3] Passive Nondestructive Assay of Nuclear Materials 1991 NUREG/CR-5550 LA-UR-90-732 Edited by: Reilly D, Ensslin N and Smith H
- [4] Firestone R B, Shirley V S 1996 Table of Isotopes. *Wiley, New-York*