

# Simulation of femtosecond pulsed laser ablation of metals

**R V Davydov, V I Antonov**

Peter the Great St.Petersburg Polytechnic University, Saint Petersburg, Russia

E-mail: davydovroman@outlook.com

**Abstract.** In this paper a mathematical model for femtosecond laser ablation of metals is proposed, based on standard two-temperature model connected with 1D hydrodynamic equations. Wide-range equation of state has been developed. The simulation results are compared with experimental data for aluminium and copper. A good agreement for both metals with numerical results and experiment shows that this model can be employed for choosing laser parameters to better accuracy in nanoparticles production by ablation of metals.

## 1. Introduction

There is a growing interest in the nanofabrication of materials and their applications in various fields of life and technology, such as electronics, energy generation, health care and storage. A great deal of progress in this field has relied on the use of lasers. Production of nanoparticles can be done in several ways, one of them is laser ablation [1].

Despite extensive research work, accurate prediction of the ablation process is still lacking, because it significantly depending on laser parameters, surrounding medium and target material characteristics. To analyze the physical processes at high energy densities, when laser is used, an adequate description of the thermodynamic properties of matter over a broad region of states including the normal conditions and plasma at high pressures and temperatures is required.

Nowadays a two-temperature model (TTM) has been widely employed for solving ultrashort laser processing of metals [2-5]. This continuous model describes the energy transfer inside a metal with two coupled generalized heat conduction equations for the temperatures of the electrons and the lattice. To describe the material removal processes TTM is often inserted into a hydrodynamic code. But the choice of an equation of state, required for solving hydrodynamic equations, can significantly affect the results.

The article is organized as follows. It begins with describing the mathematical model, then we construct the appropriate semi-empirical two-temperature equation of state for model. Finally, we demonstrate the results for aluminium and copper and compare it with experimental data.

## 2. Mathematical model of laser ablation

In this work we describe the evolution of material parameters using the conservation of mass, momentum and energy of electron, and ion subsystems in a two-temperature single-fluid 1D Lagrangian form:

$$\frac{\partial}{\partial t} \left( \frac{1}{\rho} \right) + \frac{\partial v}{\partial m} = 0 \quad (1)$$

$$\frac{\partial v}{\partial t} + \frac{\partial P}{\partial m} = 0, v = \frac{\partial x}{\partial t} \quad (2)$$



$$\frac{\partial \varepsilon_e}{\partial t} + P_e \frac{\partial v}{\partial m} = \frac{\partial}{\partial m} \left( k \rho \frac{\partial T_e}{\partial m} \right) - \frac{\alpha_{ei}}{\rho} (T_e - T_i) + J_L \quad (3)$$

$$\frac{\partial \varepsilon_i}{\partial t} + P_i \frac{\partial v}{\partial m} = \frac{\alpha_{ei}}{\rho} (T_e - T_i) \quad (4)$$

where  $m$  is the mass coordinate,  $dm = \rho dx$ ,  $m = \int_{x_0}^x \rho dx$ , direction of  $x$ -axis is chosen perpendicular to the irradiated surface of the metal,  $\rho$  is the density,  $\rho_0$  is the initial density,  $v$  is the velocity,  $t$  is the time,  $P_e$  and  $P_i$  are the pressures of electrons and ions,  $\varepsilon_e$  and  $\varepsilon_i$  are the internal energies of electrons and ions,  $P = P_e + P_i$  and  $\varepsilon = \varepsilon_e + \varepsilon_i$  are the full pressure and the internal energy,  $T_e$  and  $T_i$  are the temperatures of electrons and ions.

For the coefficient of electron-ion relaxation  $\alpha_{ei}$  we use formula from work [6] and energy of the absorbed laser radiation  $J_L$ , described by:

$$J_L = \frac{F_{abs}}{\tau_L \delta \sqrt{\pi} \rho} \exp\left(-\frac{t^2}{\tau_L^2}\right) \exp\left(-\frac{x(m,t) - x(m_0,t)}{\delta}\right) \quad (5)$$

where  $\tau_L$  is the laser pulse duration,  $F_{abs}$  is the laser radiation energy,  $\delta$  is the skin depth of metal.

The electron wide-range thermal conductivity coefficient  $k$  is constructed as an interpolation between limiting metal and hot plasma cases [7]. The viscosity and thermal conductivity of the ions are neglected in this model. To calculate the ablation depth, we perform an integration of the mass flux through the surface using the expression:

$$d = \frac{1}{\rho_0} \int_0^t (\rho v)|_{x=x_0} dt' \quad (6)$$

### 3. Equation of state

To solve the system of hydrodynamic equations (1) – (4) we construct the wide-range semi-empirical two-temperature equation of state. The metal is expected to consist of the same electrically neutral atomic cells with atomic weight  $A$  and charge  $Z$ . The Helmholtz free energy of a single atomic cell is the sum of three terms, describing the electronic and ionic components, and the interaction between them:

$$F = F_e + F_i + F_{ei} \quad (7)$$

As the main thermodynamic parameters we use atomic cell volume  $V$  and temperatures  $T_e$ ,  $T_i$ . The number of free electrons in one atomic cell we call the degree of ionization and denote by the letter  $y$ . The pressure of the electrons is assumed to be the pressure of an ideal Fermi gas of electrons with density  $y/V$  and temperature  $T_e$ , where  $y$  is the solution of the modified equation of ionization:

$$\mu_F\left(\frac{y}{V}, T_e\right) + I(y) - B(V, T_e) = 0 \quad (8)$$

Here  $\mu_F$  - the chemical potential of an ideal Fermi gas,  $I(y)$  - ionization potential, which is a smooth function of  $y$  and is constructed as a smoothing spline on the known experimental values of the successive stages of ionization  $I(1)$ ,  $I(2)$  etc.

$B(V, T_e)$  - negative correction, which purpose is the description of cold ionization of highly compressed matter:

$$B(V, T_e) = b \left(\frac{Z}{V}\right)^\beta (1 + \mu T_e V^\sigma)^{-1} \quad (9)$$

where  $b$ ,  $\beta$ ,  $\sigma$ ,  $\mu$  - parameters, determined from shock compression data of metals.

For the free energy of an ideal Fermi gas we use approximation:

$$F_e = y T_e \left[ \frac{3}{5} \varphi - \frac{3}{2} \ln \left( 1 + \frac{5}{2\varphi} \right) \right] \quad (10)$$

where

$$\varphi = \frac{1}{2} (3\pi^2)^{\frac{2}{3}} \left(\frac{y}{V}\right)^{\frac{2}{3}} / T_e \quad (11)$$

From (10) we get formulas for the chemical potential, pressure and internal energy of the free electrons:

$$\mu_F = \frac{1}{2} (3\pi^2)^{\frac{2}{3}} \left(\frac{y}{V}\right)^{\frac{2}{3}} + T_e \left[ \left(1 + \frac{2}{5} \varphi\right)^{-1} - \frac{3}{2} \ln\left(1 + \frac{5}{2\varphi}\right) \right] \quad (12)$$

$$P_e = \frac{1}{5} (3\pi^2)^{\frac{2}{3}} \left(\frac{y}{V}\right)^{\frac{5}{3}} + T_e \left(\frac{y}{V}\right) \left(1 + \frac{2}{5} \varphi\right)^{-1} \quad (13)$$

$$E_e = \frac{3}{2} VP \quad (14)$$

$F_i$  is describing the transition from the crystal state at low temperatures to the state of an ideal ion gas at high temperatures:

$$F_i = \frac{3}{2} T_i \ln \frac{1+\lambda G}{V^{\frac{1}{3}} T_i} \quad (15)$$

where

$$G = \left(\frac{4\pi}{3}\right)^{\frac{1}{3}} \frac{y_c^2(V)}{V^{\frac{1}{3}} T_i} \quad (16)$$

and  $y_c(V)$  assumed to be a known function of the atomic volume  $V$ , defined by the equation of ionization,  $\lambda$  - parameter of interpolation.

From (15) we get:

$$P_i = \frac{T_i}{V} \frac{1+3\lambda \left(\frac{1}{2} \frac{d \ln y_c(V)}{d \ln V}\right) G}{1+\lambda G} \quad (17)$$

$$E_i = \frac{3}{2} T_i \frac{1+2\lambda G}{1+\lambda G} \quad (18)$$

And finally, for  $P_{ei}$  we take into account that it must not affect the equation of ionization, full pressure should be equal zero at normal density and zero temperature, component of the internal energy must take into account the Coulomb attraction between the free electrons, at low densities  $P_{ei}$  must decrease rapidly, electron-ion interaction at a fixed density should decrease as the temperature increases.

$$P_{ei} = -\frac{1}{5} (3\pi^2)^{\frac{2}{3}} \left(\frac{y_0}{V_0}\right)^{\frac{5}{3}} \left(\frac{V_0}{V}\right)^{\frac{4}{3}} \frac{1+\delta}{1+[\delta+(1+\delta)T_e/T^*] \left(\frac{V}{V_0}\right)^{\gamma}} \quad (19)$$

Here  $V_0$ ,  $\gamma$ ,  $\delta$ ,  $T^*$  are the parameters, determined from the known values of density, sublimation energy, isothermal compressibility and thermal expansion coefficient.

#### 4. Results

To verify the model we determine the dependence of ablation depth on the laser pulse duration after a single laser shot and compare with experimental data for aluminium and copper. Ultrashort laser pulses are generated by an amplified all solid-state Ti:Sapphire laser chain [8].

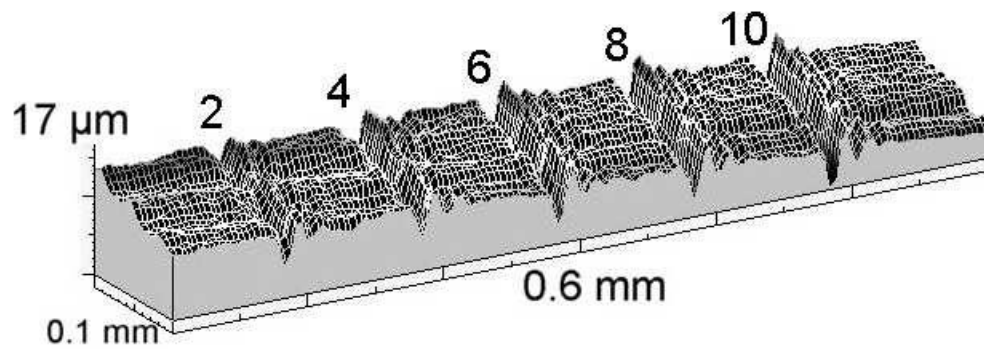
Low energy pulses are extracted from a mode-locked oscillator (1.6 nJ/pulse, 80 MHz, 800 nm, 120 fs). The pulses are then injected into an amplifying chain including: an optical pulse stretcher, a regenerative amplifier associated with a two-pass amplifier using a 20 W Nd:YLF laser as pumping source, and a pulse compressor. Linearly polarized pulses with wavelength centered on 800 nm, an energy of 1.5 mJ at 1 kHz repetition rate and typical duration of 170 fs were delivered.

The samples are mounted on a three-motorized-axes system with 0.5  $\mu\text{m}$  accuracy. Experiments are performed in the image plane of an aperture placed before the objective. Focusing objectives of 25 mm or 10 mm focal lengths to obtain fluences in a range of 0.5 to 35 J/cm<sup>2</sup> with the same beam size, 16  $\mu\text{m}$  in diameter, in the image plane.

For ablation depth measurements, grooves are machined by moving the sample, which is adapted such that each point on the groove axis undergoes 8 consecutive irradiations at each target pass. The

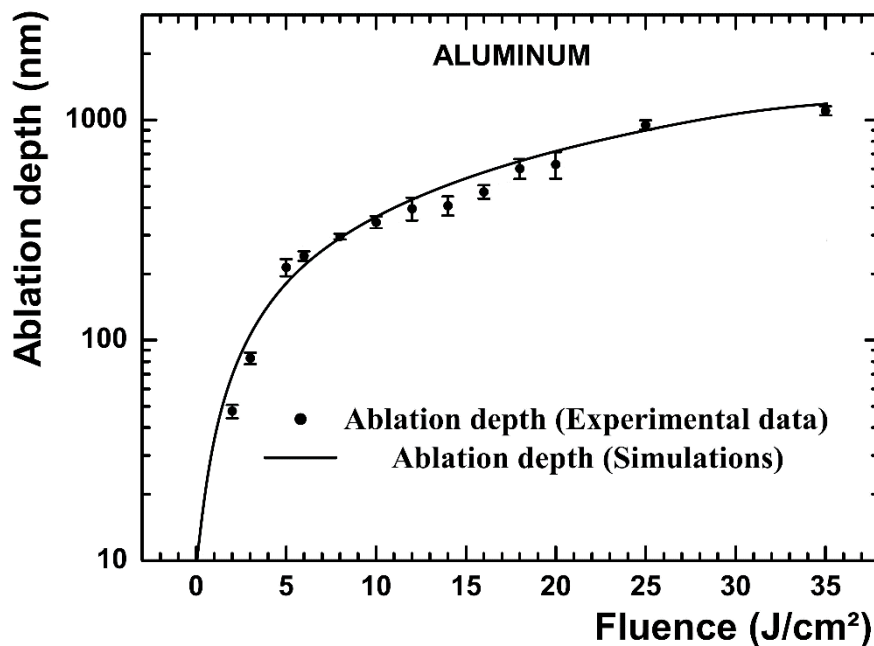
number of times the sample passes in front of the fixed beam can be adjusted. Figure 1 shows a scanning electron microscopy (SEM) picture of the machined grooves on copper for 2, 4, 6, 8 and 10 passes.

The groove depth is measured by an optical profilometer with a 10 nm depth resolution. The ablation rates for each groove are deduced taking into account the sample speed, the repetition rate of the laser, the beam size and the number of passes. For each energy density an ablation depth averaged over a few tens of laser shots.

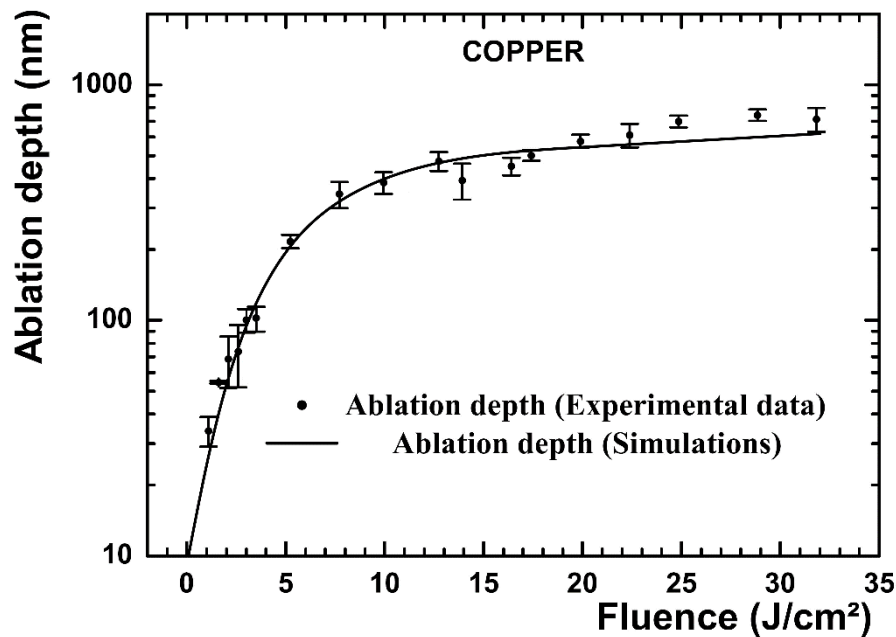


**Figure 1.** SEM picture of machined-groove profiles, from 2 to 10 passes, on a copper sample.

As we can see in figure 2 and in figure 3 results of the simulation are pretty close to experimental data both for copper and aluminium in a range of 0.5 to 35 J/cm<sup>2</sup>.



**Figure 2.** Experimental and numerical ablation depth as a function of the laser fluence on an aluminum target obtained with a 170 fs laser pulse.



**Figure 3.** Experimental and numerical ablation depth as a function of the laser fluence on a copper target obtained with a 170 fs laser pulse.

## 5. Conclusion

In this paper a mathematical model for femtosecond laser ablation of metals is proposed, based on standard two-temperature model connected with 1D hydrodynamic equations. Wide-range equation of state has been developed. The simulation results are compared with experimental data for aluminium and copper. A good agreement for both metals with numerical results and experiment shows that this model can be employed for choosing laser parameters to better accuracy in nanoparticles production by ablation of metals.

## References

- [1] Makarov G N 2013 *Phys. Usp.* **56** 643–682
- [2] Li Q, Lao H, Lin J, Chen Y and Chen X 2011 *Appl. Phys. A*. **105** 125-129
- [3] Ren Y, Chen J and Zhang Y 2012 *J. Heat Mass Transfer* **55** 1620-1627
- [4] Mishra S and Yadava V 2013 *Opt. Laser Technol.* **48** 461-474
- [5] Zhang J, Chen Y, Hu M and Chen X 2015 *Appl. Phys.* **117** 063104
- [6] Petrov Yu V 2005 *J. Laser and Particle Beams* **23** 283-289
- [7] Povarnitsyn M E, Andreev N E, Levashov P R, Khishchenko K V and Rosmej O N 2012 *Phys. Plasmas* **19** 023110
- [8] Colombier J P, Combis P, Bonneau F, Harzic R Le and Audouard E 2005 *Phys. Rev. B* **71** 165406