

Hyperfine-changing transitions in $^3\text{He II}$ and other one-electron ions by electron scattering

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Synopsis We present short-range phase shifts and spin-exchange cross sections for elastic electron scattering from selected one-electron ions from He^+ to Fe^{25+} . The results are explained in a simple physical picture based on quantum defect theory.

The hyperfine-changing transition in $^3\text{He}^+$ at 3.46 cm (8.665 GHz) is used for precise determination of the $^3\text{He}/\text{H}$ abundance in the interstellar medium [1]. In models to obtain the $^3\text{He}/\text{H}$ ratio, non-LTE effects and line broadening due to electron collisions should be included [2]. Spin-exchange effects in highly charged ions are also of interest for many storage ring experiments.

Calculations using the Coulomb-Born and static exchange approximation, both in non-relativistic and relativistic form, were carried out by Augustin *et al* [3]. They focused on the angle-integrated spin-exchange cross section [4]

$$\sigma_{\text{SE}} = \frac{\pi}{k^2} \sum_{\ell=0}^{\infty} (2\ell + 1) \sin^2(\delta_{\ell}^t - \delta_{\ell}^s) \quad (1)$$

for elastic collisions, where k and ℓ denote the electron's linear and angular momenta while the superscripts on the short-range potential phase shifts, δ_{ℓ}^t and δ_{ℓ}^s , refer to triplet (t) and singlet (s) scattering with total electron spin $S = 1$ or $S = 0$, respectively.

In a recent paper [5], we showed how highly accurate results for this problem can be obtained using Rydberg energy levels of neutral helium or those of the respective two-electron ions. The essential idea is to write the energy levels as

$$E_{n\ell} = -\frac{1}{2} \frac{Z^2}{n_{\ell}^*}, \quad (2)$$

with an effective quantum number $n_{\ell}^* = n - \bar{\mu}_{\ell}$, and obtain the phaseshift from the relation

$$\lim_{E \rightarrow 0} \delta_{\ell}(E) = \pi \bar{\mu}_{\ell}. \quad (3)$$

Figure 1 exhibits some examples. Spin-exchange cross sections for H and $^3\text{He}^+$ are shown in Fig. 2. Note the entirely different energy dependence, particularly at low energies.

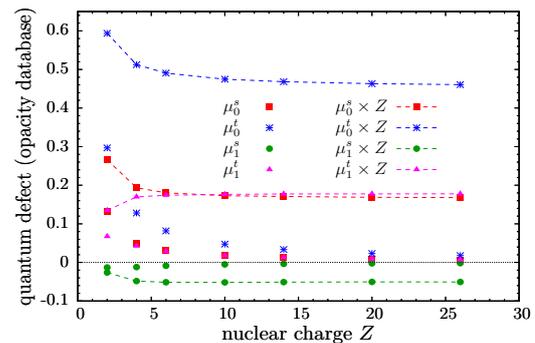


Figure 1. Quantum defects for two-electron systems as a function of the nuclear charge Z , based on data from the Opacity Project [6]. As expected, the quantum defects scale as $1/Z$.

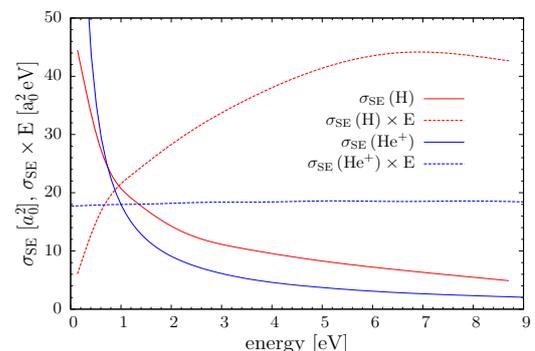


Figure 2. Spin-exchange cross sections for He^+ and atomic hydrogen [5].

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