

# Effect of $\beta^-$ -charged eradiation and its calculation in the nuclear electrodynamics theory

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**Abstract.** The study of own fields and charged particles motion and also charged fission splinters of a heavy nucleuses into nonrelativistic approximation is the subject of this paper research. The main efforts are concentrated in quest of charged share components by the radioactive  $\beta^-$ -disintegration. The corresponding field equations and equations of motion in the nuclear electrodynamics processes are obtained and their solutions are found. Analysis of the microscopic equations is generalized to the level of the macroscopic description of continuous medium electrodynamics and is accompanied by quantumomechanical additions.

## 1. Introduction

The important peculiarity of presented work is a definition and solution of fields equations and motion equations for fission splinters in consideration of charged share of radioactive inside nucleon  $\beta^-$ -disintegration effect, i. e. in consideration of emitted cascaded electrons but without consideration of  $\gamma$ -radiation [1], [2], [3]. The obtained theoretical results can be a basis for the further mathematical modelling of generation phenomenon of a virulent directional electromagnetical fields on the toroid (the nuclear electrogenerator) in the process of nuclear chain fission [4], [5], [6]. We propose the toroid is the solenoid with the external winding. Moreover inside of this toroid all fragments of the nuclear disintegration remain in force. That is why light charges don't may escape the system and therefore enter the formalism.

## 2. The fields and motion of charged fission particles

We are interested by the calculation recipe of electrical  $E_*(R, t) \in R^3$  and magnetical  $B_*(R, t) \in R^3$  fields in the point with coordinate  $R \in R^3$  at time moment  $t$  which are produced by the particles with charges  $Z_i$ , coordinates  $R_i(t)$  and velocities  $\dot{R}_i(t) = v_i(t)$ ,  $i = 1, 2, \dots$ . It is known that given fields into Gaussian units system (taking into account of values in order  $1/c$ , where  $c$  is velocity of light, and of multiplicator  $4\pi$  in the expression for potentials) can be written with the aid of microscopic Maxwell-Lorenz equations system in the form

$$\begin{aligned} \nabla E_* &= \sum_i Z_i \delta(R_i - R), & -E'_* + \nabla \times B_* &= \frac{1}{c} \sum_i Z_i \dot{R}_i \delta(R_i - R), \\ \nabla B_* &= 0, & B'_* + \nabla \times E_* &= 0. \end{aligned} \quad (1)$$



We denote here: for the vector  $\nabla$  (the differential Hamiltonian operator) is the differentiation on coordinate  $R$ , the feature on top is the differentiation on  $ct$ ;  $\delta(R_i - R)$  is the delta-function from  $R_i - R$  included in the field sources.

Taking into account of the vector potential  $a(R, t) : B_* = \nabla \times a$ , the scalar potential  $\varphi(R, t) : E_* = -\nabla\varphi - a'$  and the Lorenzian calibrated condition:  $\nabla a + \varphi' = 0$  also, the solution for system (1) in the form of nonrelativistic electromagnetical field can be found

$$E_* = \sum_i E_i, \quad E_i = -\nabla \frac{Z_i}{4\pi\sigma_i}, \quad B_* = \sum_i B_i, \quad B_i = \frac{1}{c} \nabla \times \frac{Z_i \dot{R}_i}{4\pi\sigma_i},$$

where through  $\sigma_i = |R_i - R|$  is denoted the distance between points with coordinates  $R_i$  and  $R$  in the space  $R^3$ .

The equation of  $i$ -th particle motion with the mass  $m_i$  under the influence Lorenzian force has the form

$$m_i \ddot{R}_i = Z_i [E(R_i, t) + \frac{1}{c} \dot{R}_i \times B(R_i, t)], \quad (2)$$

where  $E(R_i, t) = \sum_j E_j + E_0$ ,  $B(R_i, t) = \sum_j B_j + B_0$ ;  $(E, B)$  is full electromagnetical field in the point  $R_i$  at time moment  $t$ ;  $(E_0, B_0)$  is external field,  $(E_*, B_*)$  is internal field of the charged particles in the given point, moreover  $i \neq j$ .

For equation (2) can be attached the canonical form:  $\partial H / \partial P_i = \dot{R}_i$ ,  $\partial H / \partial R_i = -\dot{P}_i$  with the aid of the Hamiltonian

$$H = \sum_i \frac{P_i^2}{2m_i} + \sum_i \sum_j \frac{Z_i Z_j}{8\pi\sigma_{ij}} + \sum_i Z_i \left[ \varphi_0(R_i, t) - \frac{P_i}{cm_i} A_0(R_i, t) \right], \quad \sigma_{ij} = |R_i - R_j|,$$

where  $i \neq j$ , into the terms of impulse variables  $P_i$ , coordinate variables  $R_i$  and potentials (scalar  $\varphi_0$  and vector  $A_0$ ) of external field.

### 3. The fields and motion of charged fission splinters

Let us set the problem about conclusion of field equations and motion equations of the charged splinters (the united particles with internal nuclear structure) which are made in consequence of the chain nuclear fission reaction. These compound united particles can be considered as many time ionized positive ions for the reason electrons upsetting of the atom outer skin of divided substance.

We proceed from the field equation of individual particles (1). Add to the index  $i$  the index  $k$ . Then instead of vector  $R_i$  we take the vector  $R_{ki}$ , where  $R_{ki} = R_k + r_{ki}$ ; where  $k$  is the splinter index,  $i$  is the index of the particle of given splinter,  $r_{ki}$  is the internal coordinate of  $ki$ -th particle concerning the fixed point of  $k$ -th splinter.

The charged fission splinters are not "the stable complexes" but are the powerfully nonsteady particles groups are exposed the pronounced instantaneous radioactive fission (the  $\beta^-$ -fission accompanied by the  $\gamma$ -radiation). We have in the  $k$ -th fission splinter the individual charged particles in the point  $R_{ki}$  with the charges  $Z_{ki}$  and the charged nucleus in the point  $R_k$  is exposed  $\beta^-$ -fission with the charge  $Z_k : Z_k = X_k + Y_k$ , where  $X_k$  is the proton charge of nucleus (i. e. the original proton charge of splinter + the proton charge of  $\beta^-$ -fission products),  $Y_k$  is the electron charge of  $\beta^-$ -fission products.

The solutions  $E_*$  and  $B_*$  of field equations can be approximated as converged rows on parameter  $|r_{ki}|/|R_k - R|$ , i. e. the dimensions of a splinter  $R_{ki}$  smaller a distance  $\sigma_k$  from the observation point  $R$  to fixed point (nucleus)  $R_k$  of  $k$ -th splinter. Transform equations (1) taking

into account all expansions, included the  $\delta$ -function expansion into the Taylor's row on  $r_{ki}$  in the locality of the point  $(R_k - R)$

$$\begin{aligned} \nabla E_* &= \sum_k \sum_i Z_{ki} \sum_{n=0}^{\infty} \frac{(-1)^n}{n!} (r_{ki} \nabla)^n \delta(R_k - R) + \sum_k X_k \delta(R_k - R) + \sum_k Y_k \delta(R_k - R), \\ -E'_* + \nabla \times B_* &= \frac{1}{c} \sum_k \sum_i Z_{ki} (\dot{R}_k + \dot{r}_{ki}) \sum_{n=0}^{\infty} \frac{(-1)^n}{n!} (r_{ki} \nabla)^n \delta(R_k - R) \\ + \frac{1}{c} \sum_k X_k \dot{R}_k \delta(R_k - R) + \frac{1}{c} \sum_k Y_k \dot{R}_k \delta(R_k - R), \quad \nabla B_* &= 0, \quad B'_* + \nabla \times E_* = 0. \end{aligned}$$

The motion equation of  $ki$ -th particle into  $k$ -th splinter with the charge  $Z_{ki}$ , the mass  $m_{ki}$  and the coordinate  $R_{ki}$  at the time moment  $t$  into full electromagnetical field  $(E(R_{ki}), B(R_{ki}, t))$  has a form of equation (2), where  $R_i \rightarrow R_{ki}$ , i. e.

$$m_{ki} \ddot{R}_{ki} = Z_{ki} [E(R_{ki}, t) + \frac{1}{c} \dot{R}_{ki} \times B(R_{ki}, t)] \quad (3)$$

and

$$\begin{aligned} E(R_{ki}, t) &= - \sum_j \nabla_{ki} \frac{Z_{kj}}{4\pi \sigma_{k,ij}} - \nabla_{ki} \frac{(X_k + Y_k)}{4\pi \sigma_{k,ik}} - \sum_l \sum_j \nabla_{ki} \frac{Z_{lj}}{4\pi \sigma_{kl,ij}} \\ &- \sum_l \nabla_{ki} \frac{(X_l + Y_l)}{4\pi \sigma_{kl,il}} + E_0(R_{ki}, t), \quad B(R_{ki}, t) = B_0(R_{ki}, t), \end{aligned} \quad (4)$$

where  $j \neq i$ ,  $l \neq k$ ;  $\nabla_{ki}$  is the gradient vector on the elements of vector  $R_{ki}$ . In the system (4) are denoted

$$\begin{aligned} \sigma_{k,ij} &= |R_{ki} - R_{kj}|, \quad \sigma_{k,ik} = |R_{ki} - R_{kk}| = |R_{ki} - R_k|, \\ \sigma_{kl,ij} &= |R_{ki} - R_{lj}|, \quad \sigma_{kl,il} = |R_{ki} - R_{ll}| = |R_{ki} - R_l|, \end{aligned}$$

and moreover  $|R_{ki} - R_k| = |r_{ki}|$ .

On the analogy of (2) ( $i \rightarrow k$ ) can be written the motion equation of the nucleus of  $k$ -th splinter with the charge  $Z_k = X_k + Y_k$ , the mass  $m_k$ , the coordinate  $R_k$  into full electromagnetical field  $(E(R_k, t), B(R_k, t))$

$$m_k \ddot{R}_k = Z_k [E(R_k, t) + \frac{1}{c} \dot{R}_k \times B(R_k, t)], \quad (5)$$

where

$$\begin{aligned} E(R_k, t) &= - \sum_j \nabla_k \frac{Z_{kj}}{4\pi \sigma_{k,kj}} - \sum_l \sum_j \nabla_k \frac{Z_{lj}}{4\pi \sigma_{kl,kj}} \\ &- \sum_l \nabla_k \frac{(X_l + Y_l)}{4\pi \sigma_{kl,kl}} + E_0(R_k, t), \quad B(R_k, t) = B_0(R_k, t), \quad l \neq k. \end{aligned} \quad (6)$$

After the summarizing of equations (3) on  $i$  and the adding with equation (5) for description of the motion of  $k$ -th splinter with the mass  $\bar{m}_k$  and the coordinate of masses center  $\bar{R}_k$

$$\bar{m}_k = \sum_i m_{ki} + m_k, \quad \bar{R}_k = \frac{\sum_i m_{ki} R_{ki} + m_k R_k}{\bar{m}_k}$$

we obtain the equation

$$\bar{m}_k \ddot{\vec{R}}_k = \sum_i Z_{ki} [E(R_{ki}, t) + \frac{1}{c} \dot{\vec{R}}_{ki} \times B(R_{ki}, t)] + Z_k [E(R_k, t) + \frac{1}{c} \dot{\vec{R}}_k \times B(R_k, t)]. \quad (7)$$

Substitute the expressions (4) and (6) into the equation (7). Then the resultant force corresponding the intrasplinter field for the set of central forces is equal zero. Consequently the equation (7) acquires the form

$$\begin{aligned} \bar{m}_k \ddot{\vec{R}}_k = & - \sum_l \sum_i \sum_j \nabla_{ki} \frac{Z_{ki} Z_{lj}}{4\pi \sigma_{kl,ij}} - \sum_l \sum_i \nabla_{ki} \frac{Z_{ki} (X_l + Y_l)}{4\pi \sigma_{kl,il}} - \sum_l \sum_j \nabla_k \frac{Z_{lj} (X_k + Y_k)}{4\pi \sigma_{kl,kj}} \\ & - \sum_l \nabla_k \frac{(X_l + Y_l)(X_k + Y_k)}{4\pi \sigma_{kl,kl}} + \sum_i Z_{ki} [E_0(R_{ki}, t) + \frac{1}{c} \dot{\vec{R}}_{ki} \times B_0(R_{ki}, )] \\ & + (X_k + Y_k) [E_0(R_k, t) + \frac{1}{c} \dot{\vec{R}}_k \times B_0(R_k, t)], \quad l \neq k. \end{aligned} \quad (8)$$

For all that external field  $(E_0, B_0)$  satisfies the homogeneous equations

$$\nabla B_0 = 0, \quad B'_0 + \nabla \times E_0 = 0.$$

Thus, the equation (8) is the motion equation of  $k$ -th splinter into electromagnetical field of other splinters and external sources.

It is important to note the received equations on a level with the traditional items in the right part of the Lorenzian force contain also the items are made a force connected with radioactive charged radiation of nucleuses into fission splinters (the accounting of  $\beta^-$ -charged radiation by the radioactive electrodynamical effect).

#### 4. Conclusions

Chain fission of heavy nuclei is one of many physical phenomena which proceed in an avalanche scheme. In fission there is an impetuous increase in the numbers of neutrons, charged particles and fission splinters with enormous kinetic energy. The present theory aims to describe the above process quantitatively. In the future it could find an application in powerful reactors operating exclusively on the basis of electronuclear conversions.

#### References

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