

# Intermultiplet transitions in filled skutterudite $\text{SmFe}_4\text{P}_{12}$

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**Abstract.** The intermultiplet transitions in filled skutterudite  $\text{SmFe}_4\text{P}_{12}$  are studied by magnetization and time-of-flight inelastic neutron scattering experiments. In neutron scattering experiments by using high energy neutrons for reducing huge neutron absorption of natural Sm, a small inelastic peak has been observed around  $\sim 80$  meV at low temperature. The scattering vector dependence of intensity of this peak agrees with the theoretical inelastic structure factor for the intermultiplet transition from the ground  $J = 5/2$  multiplet to the excited  $J = 7/2$  multiplet in  $\text{Sm}^{3+}$  ion. Interestingly, the energy splitting is much smaller than the free  $\text{Sm}^{3+}$  ion value. This is also comparable with that estimated by the inverse magnetic susceptibility. This large reduction of the energy splitting might be due to the strong  $c-f$  mixing in  $\text{SmFe}_4\text{P}_{12}$ .

## 1. Introduction

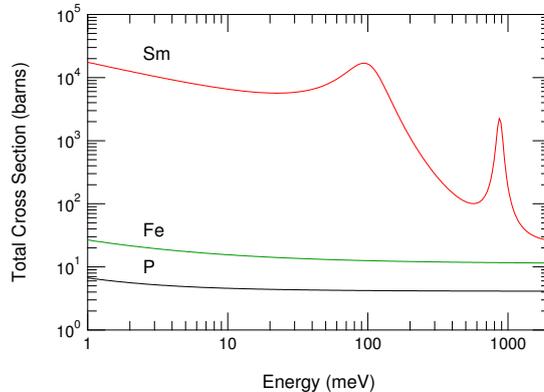
Filled skutterudites  $\text{RT}_4\text{X}_{12}$  (R = rare-earth, T = transition metal, X = pnictogen) have been intensively studied because they exhibit unusual low temperature properties, such as the heavy fermion (HF) behavior, the multipolar ordering and the unconventional superconductivity [1]. Among them,  $\text{SmFe}_4\text{P}_{12}$  is reported to be the first Sm-based ferromagnetic Kondo-lattice compound exhibiting a ferromagnetic transition at the Curie temperature 1.6 K [2]. It shows the unconventional HF state with the large electronic specific-heat coefficient  $\gamma = 370$  mJ/mol K<sup>2</sup>, which is the second heaviest in Sm-based compound next to  $\text{SmOs}_4\text{Sb}_{12}$  [3, 4]. As is the case with  $\text{SmOs}_4\text{Sb}_{12}$ , the  $\gamma$  value of  $\text{SmFe}_4\text{P}_{12}$  also seems to be robust against magnetic fields. The electrical resistivity of  $\text{SmFe}_4\text{P}_{12}$  shows the characteristic feature of Kondo lattice with Kondo temperature of about 30 K [2, 5]. It shows the clear metamagnetism at 22 T and the magnetization does not saturate even at high magnetic fields up to 42 T [6]. The magnetization  $0.4\mu_B$  at 42 T is considerably less than the free  $\text{Sm}^{3+}$  value of  $0.71\mu_B$ . The valence of Sm ions is reported to be almost trivalent [2, 10], in contrast to the intermediate valence state of  $\text{SmOs}_4\text{Sb}_{12}$  [10]. The ground  $J$  multiplet of  $\text{Sm}^{3+}$  ion is the  ${}^6H_{5/2}$  multiplet, which splits to a  $\Gamma_5$  doublet and a  $\Gamma_{67}$  quartet by the crystal field (CF) with  $T_h$  symmetry [7], where the characteristic 6th-order term in the CF Hamiltonian does not affect the ground multiplet. The CF level scheme of  $\text{SmFe}_4\text{P}_{12}$  is considered to be the  $\Gamma_5$  ground state and the  $\Gamma_{67}$  excited state with the energy separation of about 6 meV by the specific heat [8] and NMR measurements [9].



In general, the energy from the ground  $J$  multiplet to the first excited  $J$  multiplet in Sm and Eu compounds is known to be not large compared to  $k_B T$  at room temperature [11]. Therefore it is necessary to consider the influence of the excited  $J$  multiplet for these compounds. Although it is reported that the local environment surrounding rare-earth ions has little effect on the energy between the  $J$  multiplets split by the spin-orbit interaction [12], it may be important to examine the energy splitting in the Sm-based HF compounds for understanding the unusual electronic states of these materials.

## 2. Experimental

Single crystals of  $\text{SmFe}_4\text{P}_{12}$  were grown by the tin-flux method using the raw materials of 99.9%(3N)-pure naturally occurring Sm, 3N-Fe, 6N-P and 5N-Sn. Dimensions of most crystals were less than 1 mm. X-ray powder diffraction measurements confirmed that our sample has the filled skutterudite crystal structure (space group  $\text{Im}\bar{3}$ ) with a lattice parameter  $a = 7.803\text{\AA}$ , which agrees with the reported values [2, 13, 14], and no impurity phase except small amount of  $\text{FeP}_2$  less than about 3% in volume. Magnetization measurement on the single crystal in a constant magnetic field 1 kOe parallel to [100] was performed in Quantum Design SQUID magnetometer between 2 K and 300 K. Inelastic neutron scattering (INS) experiments were done by using the time-of-flight high resolution chopper spectrometer HRC at J-PARC [15]. Many small single crystals of  $\text{SmFe}_4\text{P}_{12}$  were combined for a total mass of 2.38 g. They were wrapped in thin Al foil and formed into a thin plate (30 mm $\times$ 30 mm $\times$ 1 mm) with the main plate plane perpendicular to the direction of the incident neutron beam. Then, it was enclosed in an Al container and mounted in a closed cycle refrigerator. Usually it is difficult to do INS

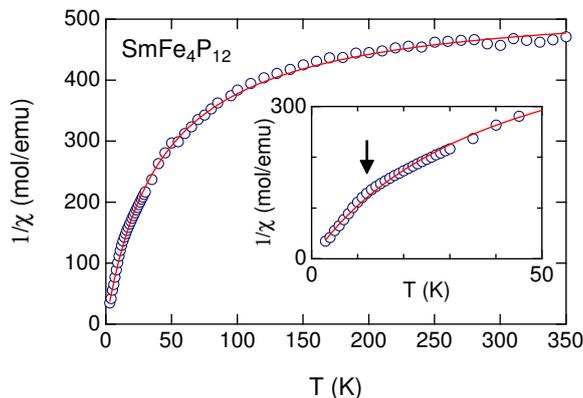


**Figure 1.** Energy dependence of the neutron cross sections of natural Sm, Fe and P.

experiments on the Sm containing materials because of huge thermal-neutron absorption by natural Sm, but, it is possible to reduce the effects of the neutron absorption by using higher energy neutrons. As shown in Fig. 1, there is a transmission window between the strong  $^{149}\text{Sm}$  nuclear resonances which peak at  $\sim 100$  meV and  $\sim 900$  meV. Therefore we chose an high incident neutron energy of 514.1 meV and a chopper frequency of 600 Hz, where the scattered neutrons also have low absorption cross sections. In this experimental set up, the instrument resolution at zero energy transfer was a full width at half maximum of 19 meV.

## 3. Results and discussion

The temperature dependence of inverse magnetic susceptibility  $1/\chi(T)$  is shown in Fig. 2. At low temperatures, there is a broad hump at  $\sim 12$  K as denoted by the arrow in the inset of Fig. 2.



**Figure 2.** Temperature dependence of inverse magnetic susceptibility  $1/\chi(T)$  of  $\text{SmFe}_4\text{P}_{12}$ . The line denotes a fit of Eq. (1) to the  $1/\chi(T)$  data. The low temperature behavior is shown in the inset.

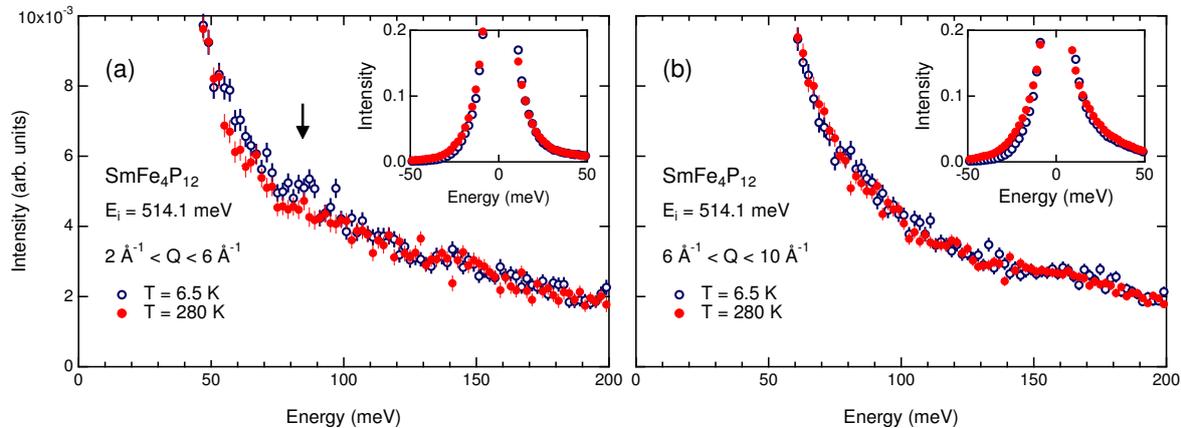
This may be due to the CF effects. Assuming that the  $\Gamma_5$  ground doublet and the  $\Gamma_{67}$  excited quartet with the energy splitting of 6 meV, the CF calculation of the temperature dependence of  $1/\chi(T)$  reproduces the observed hump. This is another piece of evidence that the  $\Gamma_5$  doublet is a CF ground state because the CF calculation assuming the  $\Gamma_{67}$  quartet as a CF ground state does not reproduce such hump of  $1/\chi(T)$ . In order to get microscopic information about this CF splitting, we have tried to do INS experiment by using thermal neutrons with  $E_i = 30$  meV, but, no signal was observed because of the influence of neutron absorption of Sm.

Overall temperature dependence of  $1/\chi(T)$  in  $\text{SmFe}_4\text{P}_{12}$  apparently does not follow the simple Curie-Weiss law. This is consistent with the small energy gap  $\Delta$  between the ground  $J = 5/2$  multiplet and the first excited  $J = 7/2$  multiplet in the  $\text{Sm}^{3+}$  ion. Therefore a fit of the data was made with the modified Curie-Weiss law without considering the small CF splitting

$$\chi(T) = \frac{N\mu_{\text{eff}}^2}{3k_{\text{B}}(T - \Theta)} + \chi_0 \quad (1)$$

where  $N$  is Avogadro's number,  $\mu_{\text{eff}}$  is the effective magnetic moment,  $\Theta$  is the Curie-Weiss temperature and  $\chi_0$  is a temperature-independent Van-Vleck term due to coupling with the excited  $J = 7/2$  multiplet, which is calculated to be  $\frac{20N\mu_{\text{B}}^2}{7\Delta k_{\text{B}}}$ . The fit yields  $\Theta = 0.1$  K,  $\mu_{\text{eff}} = 0.79\mu_{\text{B}}$ , which is relatively less than  $0.85\mu_{\text{B}}$  expected for the  $\text{Sm}^{3+}$  free ion, and the energy splitting  $\Delta = 569$  K (49 meV). This  $\Delta$  value is much less than the free  $\text{Sm}^{3+}$  ion value  $\sim 130$  meV [11]. For more exact estimation of  $\Delta$ , the contribution of the Pauli paramagnetism of conduction electrons to  $\chi_0$  should be taken into account. Such small energy splitting is also reported in another Sm-based HF skutterudite  $\text{SmOs}_4\text{Sb}_{12}$  by the bulk magnetic susceptibility measurement [4].

Figure 3 shows the INS energy spectra of  $\text{SmFe}_4\text{P}_{12}$  at temperature 6.5 K and 280 K for  $2\text{\AA}^{-1} \leq Q \leq 6\text{\AA}^{-1}$  and  $6\text{\AA}^{-1} \leq Q \leq 10\text{\AA}^{-1}$ , where  $Q$  is the magnitude of the scattering vector. At low  $Q$  region, one small inelastic peak was observed around  $\sim 80$  meV at 6.5 K as denoted by the arrow in Fig. 3. The peak almost disappears at high  $Q$  region, indicating its magnetic origin. Except for this small peak around  $\sim 80$  meV, no clear difference between the data at 6.5 K and 280 K was seen. If the small peak corresponds to the intermultiplet transition between the ground  $J = 5/2$  multiplet and the excited  $J = 7/2$  multiplet in  $\text{Sm}^{3+}$  ion, interestingly, the energy is much smaller than the free  $\text{Sm}^{3+}$  ion value  $\sim 130$  meV [11] and the reported values



**Figure 3.** Energy spectra of neutrons scattered from  $\text{SmFe}_4\text{P}_{12}$  measured with  $E_i = 514.1$  meV at lowest temperature 6.5 K and 280 K for (a)  $2 \text{ \AA}^{-1} \leq Q \leq 6 \text{ \AA}^{-1}$  and (b)  $6 \text{ \AA}^{-1} \leq Q \leq 10 \text{ \AA}^{-1}$ . The arrow denotes the small inelastic peak at 6.5 K. The insets show the data below 50 meV.

in usual trivalent Sm compounds, for example, 131.5 meV in  $\text{Sm}^{3+}$  ion doped in  $\text{LaF}_3$  [16] and 129 meV in  $\text{SmPd}_3$  [17]. The small energy is comparable with the  $\Delta$  value estimated by the fit of  $1/\chi(T)$ . We also confirmed the existence of the small excitation below  $\sim 100$  meV and the absence of the excitation around  $\sim 130$  meV at low  $Q$  and low temperatures by a tentative INS experiment with the incident energy  $E_i = 300$  meV.

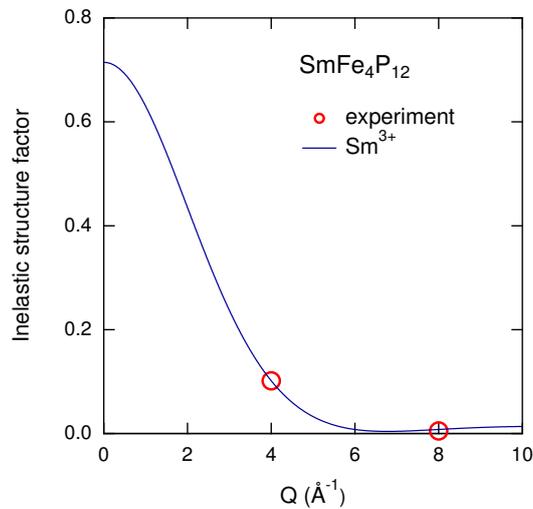
The INS intensity for the intermultiplet transitions from the  $J$  multiplet to the  $J+1$  multiplet is proportional to the inelastic structure factor

$$G(Q; J, J+1) = \sum_{k,l} C^{k,l} \langle j_k(Q) \rangle \langle j_l(Q) \rangle \quad (2)$$

where  $C^{k,l}$  are constants, which tabulated in appendix of [18], and  $\langle j_k(Q) \rangle$  are averages of spherical Bessel functions. The inelastic structure factor  $G(Q; \frac{5}{2}, \frac{7}{2})$  of  $\text{Sm}^{3+}$  monotonically decreases with increasing  $Q$ , in contrast to the elastic magnetic form factor which has a maximum at finite  $Q$ . Figure 4 shows the  $Q$  dependence of the integrated intensity of the small peak, which is the sum of the difference between the data at 6.5 K and 280 K in Fig. 3, and the inelastic structure factor  $G(Q; \frac{5}{2}, \frac{7}{2})$  expressed by Eq. (2), where the integrated intensity is normalized in a way that the intensity at  $Q = 4 \text{ \AA}^{-1}$  corresponds to  $G(4 \text{ \AA}^{-1}; \frac{5}{2}, \frac{7}{2})$ . The observed rapid decrease of the intensity with increasing  $Q$  agrees with the theoretical inelastic structure factor of  $\text{Sm}^{3+}$ .

The intermultiplet transitions in many Sm-based compounds have been studied by INS experiments. Especially, large changes of INS spectra are reported in intermediate valence compounds such as  $\text{Sm}_{1-x}\text{Y}_x\text{S}$  [12, 19, 20]. If the valence of Sm ions in  $\text{SmFe}_4\text{P}_{12}$  deviates from trivalent slightly, the  $J = 0$  to  $J = 1$  excitation around 36 meV for  $\text{Sm}^{2+}$ , which has the largest inelastic structure factor in the rare-earth ions, may be expected. However no significant difference between the data at 6.5 K and 280 K around 36 meV was observed as shown in the inset of Fig. 3. This is consistent with the results of the magnetic susceptibility [2] and the X-ray absorption spectra [10].

The observed large reduction of the energy splitting between the  $J$  multiplets has not been reported so far. Here we discuss the origin of the small energy splitting. Firstly, we consider



**Figure 4.** The scattering vector dependence of the integrated intensity of the small peak around 80 meV. The line denotes the theoretical inelastic structure factor of  $\text{Sm}^{3+}$  expressed by Eq. (2).

the effects of the CF on the excited  $J = 7/2$  multiplet. Under the CF with  $T_h$  symmetry, the  $J = 7/2$  multiplet splits into two doublets and one quartet, where the 6th-order term in CF Hamiltonian also contributes to the splitting. Since the  $\Gamma_5 - \Gamma_{67}$  energy splitting in the ground  $J = 5/2$  multiplet is about 6 meV, the overall energy splitting in the  $J = 7/2$  multiplet due to the CF effects is estimated to be the same order of magnitude, as reported by INS experiments on some Sm-based compounds [21, 22]. This means that the energy reduction due to the CF effects may be at most  $\sim 20$  meV. Therefore the CF effects alone cannot explain the observed large reduction of the energy. Secondly, we might need to think the effect of the ferromagnetic interaction in  $\text{SmFe}_4\text{P}_{12}$ . It shifts the energy of excitations, for example, as reported in the permanent magnet  $\text{Sm}_2\text{Fe}_{17}$  [23]. However, the ferromagnetic interaction in  $\text{SmFe}_4\text{P}_{12}$  is very weak compared to the energy between the  $J$  multiplets and shifts rather higher energy. Thus, this interaction cannot explain the small energy splitting. Finally, we consider the strong mixing between  $4f$  electrons and conduction electrons and the rattling motion of Sm ions, resulting from the characteristic cage structure in filled skutterudites. Since the cage formed by the pnictogen X in  $\text{RT}_4\text{X}_{12}$  becomes smaller as changing  $\text{X} = \text{Sb} \rightarrow \text{As} \rightarrow \text{P}$ , the effects of the former may be more important in  $\text{SmFe}_4\text{P}_{12}$ . In fact, the band calculation shows that  $\text{RFe}_4\text{P}_{12}$  systems have the strongest  $c - f$  mixing [24]. On the other hand, the latter was not seen in  $\text{SmFe}_4\text{P}_{12}$  [25, 26], in contrast to  $\text{SmOs}_4\text{Sb}_{12}$  [26, 27, 28]. Therefore, this strong  $c - f$  mixing might renormalize the spin-orbit transition between the  $J$  multiplets.

In summary, we have performed magnetization measurement and INS experiments on filled skutterudite  $\text{SmFe}_4\text{P}_{12}$  by using high energy neutrons. The results indicate that the energy splitting between the ground  $J = 5/2$  multiplet and the excited  $J = 7/2$  multiplet is very small compared to usual Sm-based compounds. This large reduction of the energy might originate from the strong  $c - f$  mixing in  $\text{SmFe}_4\text{P}_{12}$ . The present study suggests that the contribution of the excited  $J = 7/2$  multiplet should be taken into account for understanding the electronic states in the Sm-based filled skutterudites.

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