

# Theoretical Investigations of the Effect of N-Doping on Growth and Field Emission Properties of Carbon Nanotubes (CNTs)

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**Abstract.** In this work, we investigate effects of doping of hetero-atoms such as Nitrogen (N) on the growth and field emission properties of Carbon Nanotubes (CNTs) in low temperature plasma. A theoretical model is developed to incorporate kinetics of electron, ions and neutral atoms with N as doping elements in complex and low temperature plasma. Results of numerical calculations of the radius of N-doped CNT are presented for typical glow discharge plasma parameters. It is found that the radius of CNT is reduced with N-doping. The field enhancement factor of CNT is also estimated from the obtained results.

## 1. Introduction

The effect of the experimental parameters on the structure of nitrogen containing Multi-Wall Nanotubes (MWNTs) produced by an aerosol assisted Chemical Vapor Deposition (CVD) method has been studied by Koos *et al.* [1] previously. Ayala *et al.* [2] have demonstrated the effect of doping of carbon nanotubes with nitrogen. Kim *et al.* [3] have shown in their investigations that enhanced CNT growth in an N<sub>2</sub> or NH<sub>3</sub> environment is due to nitrogen incorporation into the CNT wall. Sharma and Tewari [4] have investigated the effect of plasma parameters on the growth and field emission properties of Carbon Nanotubes. The variation of field enhancement factor has been experimentally verified by Srivastava *et al.* [5] who also studied the enhanced field emission characteristics of nitrogen-doped carbon nanotube films showing field emissions at a level of 2.65–3.55 V/μm.

## 2. Model

Plasma containing electrons, positively charged ions of type A, B, and C, and neutral atoms of type A, B, and C, is considered. Here A corresponds to carbon, B to neon, and C to nitrogen as doping material. The initial radius of spherical CNT tip,  $r_0$ , can be estimated by evaluating the accumulation of electrons and positively charged ions on the CNT,

$$n_e \left( \frac{T_e}{m_e} \right)^{\frac{1}{2}} \exp \left( - \frac{e^2}{r_0 k_B T_e} \right) = \left( 1 + \frac{e^2}{r_0 k_B T_i} \right) \left[ n_{iA} \left( \frac{T_i}{m_{iA}} \right)^{\frac{1}{2}} + n_{iB} \left( \frac{T_i}{m_{iB}} \right)^{\frac{1}{2}} + n_{iC} \left( \frac{T_i}{m_{iC}} \right)^{\frac{1}{2}} \right], \quad (1)$$



with  $n_e$  and  $T_e$  the electron density and temperature, respectively. The ion temperature is denoted by  $T_i$ , the Boltzmann constant by  $k_B$ , and the electron charge by  $e$ . The densities of the ions are indicated by  $n_{iA}$ ,  $n_{iB}$  and  $n_{iC}$  with masses  $m_{iA}$ ,  $m_{iB}$  and  $m_{iC}$ , respectively.

### 2.1 Growth rate equation for the mass of CNT

The growth rate is evaluated using

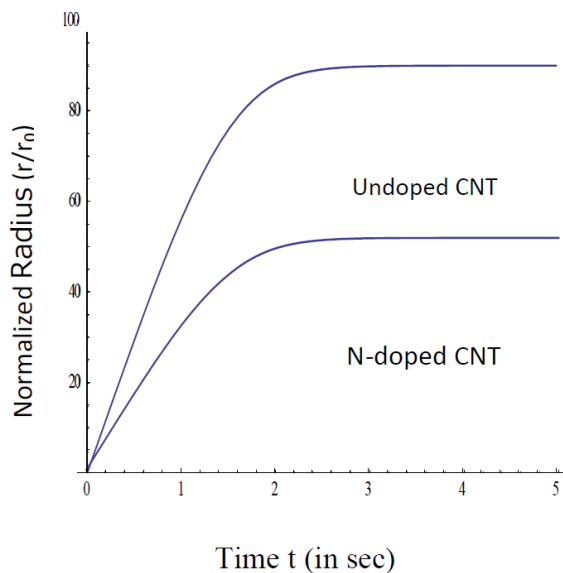
$$\frac{d}{d\tau} m_{ct} = (m_A \gamma_A n_{Act} + m_{iA} \gamma_{iA} n_{iAct} + m_C \gamma_C n_{Cct} + m_{iC} \gamma_{iC} n_{iCct}), \quad (2)$$

where  $m_{ct}$  is the mass of the CNT of radius  $a$ . With the density of the CNT,  $\rho_{ct}$ , the mass of the CNT can be expressed in terms of the density  $m_{ct} = 4/3 \pi r^3 \rho_{ct}$ . The sticking coefficients for the atomic and ionic species are  $\gamma_A$ ,  $\gamma_{iA}$ ,  $\gamma_C$  and  $\gamma_{iC}$ , respectively. The two terms in Equation (2) correspond to gains in mass due to collection of atomic and ionic species A and C.

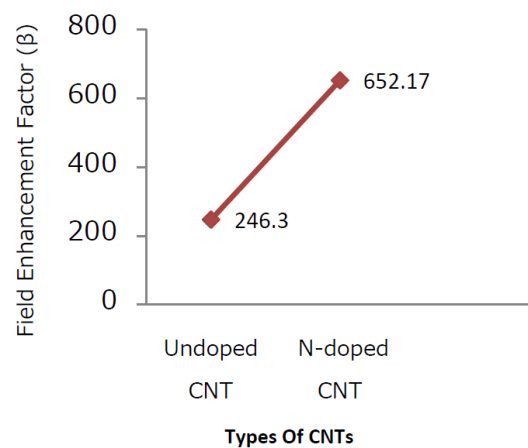
## 3. Results and discussion

For the developed model, calculations are carried out by taking the same parameters for the undoped spherical CNT tip as taken by Sharma and Tewari [4]. Calculations are for doped-nitrogen CNTs using boundary conditions and parameters at  $\tau=0$ ,  $n_{ct} = 10^6 \text{ cm}^{-3}$ ,  $n_{iA0}=n_{iB0}=n_{iC0}=10^9 \text{ cm}^{-3}$ ,  $n_{A0}=n_{B0}=5 \times 10^8 \text{ cm}^{-3}$ ,  $n_{C0}=5 \times 10^8 \text{ cm}^{-3}$ ,  $n_{e0}=10^9 \text{ cm}^{-3}$ ,  $T_{e0}=0.5 \text{ eV}$ ,  $T_{i0}=2500\text{K}$ ,  $T_{n0}=T_{ct}=2000\text{K}$ . Further,  $m_{iA} \approx m_A=12 \text{ amu}$  (carbon),  $m_{iB} \approx m_B=20 \text{ amu}$  (neon) and  $m_{iC} \approx m_C=14 \text{ amu}$  (nitrogen).

Figure 1 illustrates the variation of normalized radius  $r/r_0$  of spherical CNT tip with time for undoped CNTs and nitrogen-doped CNTs. The value of normalized radius is found to be more for undoped CNTs, and it reduces with N-doped CNTs. This confirms better field emission for N-doped CNTs. Fig. 2 illustrates the variation of field enhancement factor for undoped and N-doped CNTs. The field enhancement factor,  $\beta$ , for N-doped CNTs has been calculated. The results show higher value of  $\beta$  for N-doped CNTs.



**Figure 1.** Variation of the normalized radius  $r/r_0$  for undoped and N-doped CNTs.



**Figure 2.** Variation of the field enhancement factor for undoped and N-doped CNT's.

#### 4. Conclusions

The model developed for calculating the growth of spherical CNT tip with nitrogen as doping material predicts a diminished radius with nitrogen-doped as compared to undoped CNTs. Moreover, the computed field enhancement factors  $\beta$  for both doped and undoped CNTs show a maximum value on the order of 650 for nitrogen-doped CNTs. The obtained results have also been experimentally verified by Srivastava *et al.* [5].

#### References

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