

# Measurement of the distribution of event-by-event harmonic flow in Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV with the ATLAS detector

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**Abstract.** In recent years, the measurement of harmonic flow coefficients  $v_n$  has provided important insight into the hot and dense matter created in heavy ion collisions at RHIC and LHC. These coefficients are now understood to reflect the hydrodynamic response of the produced medium to the collision geometry. Due to finite number of nucleons in the system, the collision geometry can fluctuate from one event to another, and hence measuring the full distribution of the event-by-event  $v_n$  coefficients can provide better insights on the nature of these fluctuations and possible non-linear effects in the hydrodynamic response. This proceeding presents the first measurements of the event-by-event  $v_n$  distributions for  $n=2-4$  in Pb-Pb collisions at  $\sqrt{s_{NN}} = 2.76$  TeV with the ATLAS detector.

Relativistic heavy-ion collisions produce an extremely hot and dense medium commonly termed as the Quark Gluon Plasma. The produced medium expands anisotropically due to asymmetric pressure gradients with larger particle yields in the direction of the largest gradients. The azimuthal anisotropy can be expressed as a Fourier series:

$$\frac{dN}{d\phi} \propto 1 + 2 \sum_{n=1}^{\infty} v_n(p_T, \eta) \cos n(\phi - \Phi_n) \quad (1)$$

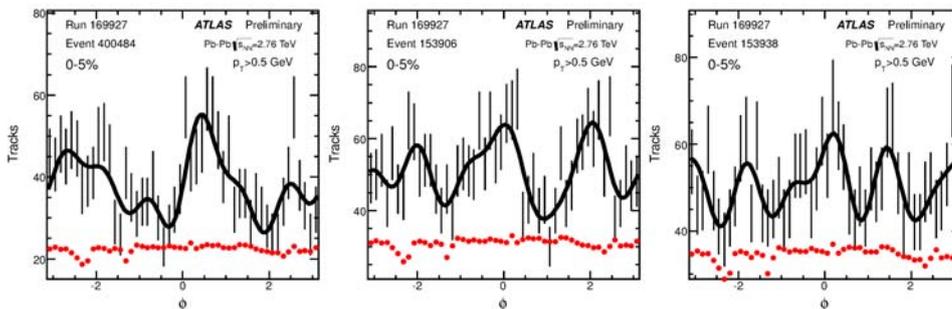
where,  $v_n$  and  $\Phi_n$  are the magnitude and phase of the  $n^{\text{th}}$  order harmonic flow [1]. Measurements of the  $p_T$ ,  $\eta$  and centrality dependence of the harmonics  $v_n$  have been done via the event-plane (EP) method [1] as well as by multi-particle correlation methods [1, 2]. In these methods, the  $v_n$  are obtained by averaging over a large number of events. Due to event by event fluctuations in the initial geometry, the  $v_n$  values vary event by event. Averaging over events, the EP and multi-particle correlation methods measure a mean response of the medium. For example, the EP method gives a value in between the mean and the RMS of the  $v_n$  distribution, i.e.  $\langle v_n \rangle < v_n^{EP} < \sqrt{\langle v_n^2 \rangle}$  [3]. A deeper understanding of the initial geometry and the expansion mechanism of the produced medium can be obtained by measuring the event-by-event (EbE)  $v_n$  distributions.

The large multiplicity in Pb-Pb collisions at the LHC as well as the large acceptance of the ATLAS inner detector [5] covering  $|\eta| < 2.5$  allow for the first measurements of the EbE  $v_n$  distributions in heavy-ion collisions. Figure 1 shows the azimuthal distribution (black points) of charged tracks with  $p_T > 0.5$  GeV for three individual events in the (0-5)% centrality class. The red points show the anisotropy in the detector acceptance (arbitrary normalization) obtained by



averaging over many events. It is clear that the EbE fluctuations in particle distributions are much larger than the detector acceptance effects.

The  $v_n$  measurements presented here were made using  $8 \mu b^{-1}$  of Minimum Bias Pb-Pb data at  $\sqrt{s_{NN}}$  of 2.76 TeV. Details of the results presented here are published in [6].



**Figure 1.** Single track  $\phi$  distributions for three events (from left to right) in the (0-5)% centrality interval. The bars indicate the foreground distributions, the solid curves indicate a Fourier parameterization including first six harmonics and the red points indicate the detector acceptance functions. Charged tracks with  $p_T > 0.5$  GeV are used. Figure taken from [6].

The azimuthal distribution of charged tracks in an event can be expanded in a Fourier series to obtain the *observed* flow-vector  $(v_{n,x}^{obs}, v_{n,y}^{obs})$  as:

$$\frac{dN}{d\phi} \propto 1 + 2 \sum_{n=1}^{\infty} v_n^{obs} \cos n(\phi - \Phi_n^{obs}) = 1 + 2 \sum_{n=1}^{\infty} (v_{n,x}^{obs} \cos n(\phi) + v_{n,y}^{obs} \sin n(\phi)) \quad (2)$$

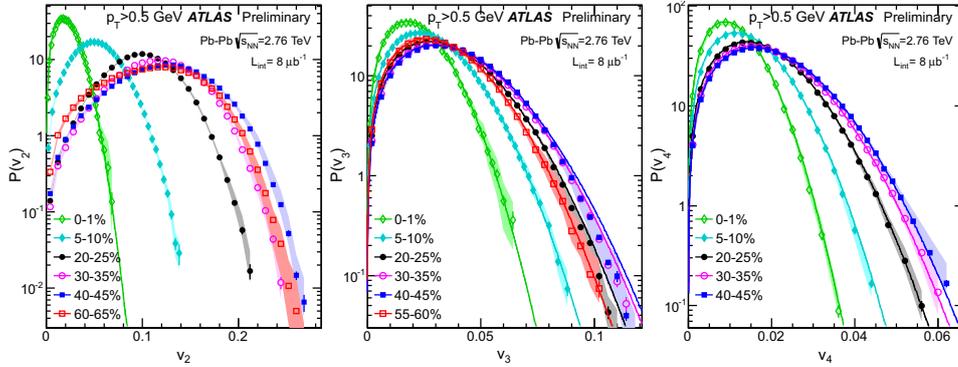
To account for the detector efficiency effects, each track is weighted by the the inverse of the tracking efficiency. The  $v_n^{obs}$  in an event is obtained as  $\sqrt{(v_{n,x}^{obs})^2 + (v_{n,y}^{obs})^2}$ . Due to the finite number of tracks in the event, the  $v_{n,x}^{obs}$  and  $v_{n,y}^{obs}$  and hence the  $v_n^{obs}$  fluctuate about the true values. The  $v_n^{obs}$  distribution needs to be corrected for this smearing using the response function, which gives the probability distribution of  $v_n^{obs}$  for a given true  $v_n$ . To obtain the response function, each event is divided into two sub-events containing tracks with  $\eta > 0$  and  $\eta < 0$  respectively. Taking the difference of the flow-vector between the two sub-events, the physical signal cancels out and the resulting distribution  $(v_{n,x}^{obs,1} - v_{n,x}^{obs,2}, v_{n,y}^{obs,1} - v_{n,y}^{obs,2})$  is consistent with a 2D Gaussian with identical widths  $\delta_{2SE}$  in the x and y directions. The response function can be obtained by shifting this 2D distribution to  $(v_{n,x}, v_{n,y})$  and then projecting it along the radial direction [6]:

$$p(v_n^{obs} | v_n) \propto v_n^{obs} e^{-\frac{(v_n^{obs})^2 + v_n^2}{2\delta^2}} I_0\left(\frac{(v_n^{obs})^2 + v_n^2}{\delta^2}\right), \delta = \delta_{2SE}/2 \quad (3)$$

where,  $I_0$  is the modified Bessel function of the second kind. This response function is used along with the Bayesian unfolding procedure [4] to calculate the unfolded  $v_n$  distributions. Note that this procedure implicitly assumes that the physical flow signal is rapidity independent, which is true when averaged over many events [1], but might not hold event by event.

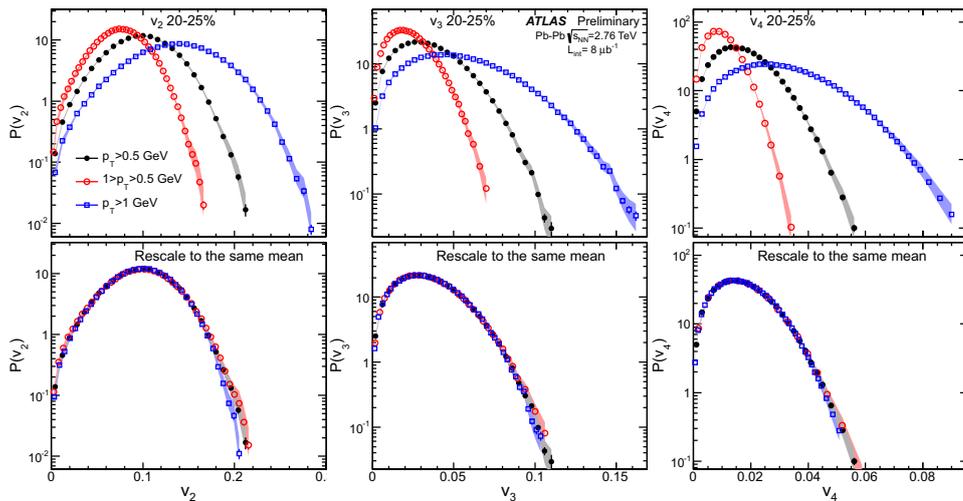
Figure 2 shows the final probability distributions for  $v_2 - v_4$  for several different centrality classes. The shape of the  $v_2$  distribution changes considerably from central to peripheral events while for  $v_3$  and  $v_4$  the change is relatively small. This is expected as the higher order harmonics  $v_3$  and  $v_4$  are produced due to fluctuations in the collision geometry, however  $v_2$  is also driven by the average second order eccentricity, which increases from central to peripheral events. The  $v_3$  and  $v_4$  distributions are well described by radial projections of 2D Gaussian distributions in

$\vec{v}_n$  with  $P(|\vec{v}_n|) = (|\vec{v}_n|/\sigma)e^{-|\vec{v}_n|^2/\sigma^2}$ ,  $\sigma = \sqrt{2/\pi}\langle v_n \rangle$  (solid lines) across all centralities. For the  $v_2$  distribution this only works for the (0-1)% central events.



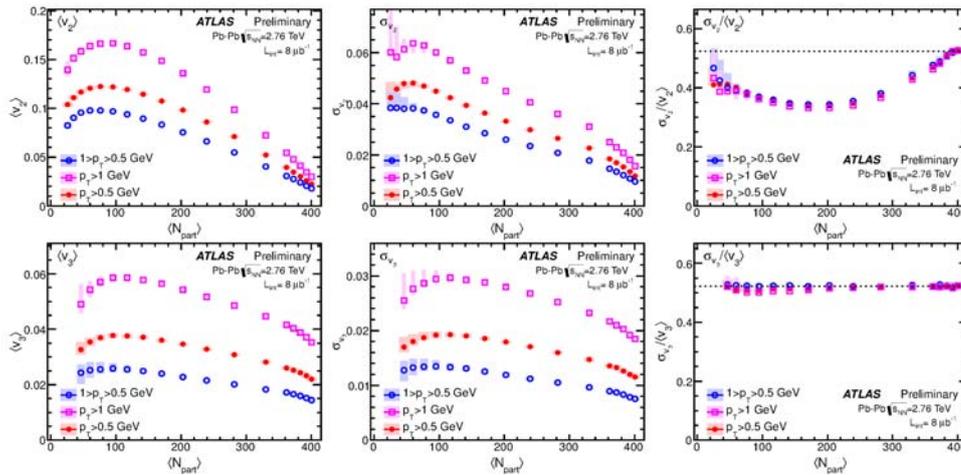
**Figure 2.** The probability distribution of the EbE  $v_n$  in several centrality intervals for  $n=2, 3$  and  $n=4$ . The error bars are statistical uncertainties, and the shaded bands are uncertainties on the  $v_n$  shape. The solid curves are distributions calculated assuming the  $v_n$  are radial projections of 2D Gaussian distributions; they are shown for 0-1% centrality interval for  $v_2$  and all centrality intervals for  $v_3$  and  $v_4$ . Figure taken from [6].

Figure 3 compares the EbE distributions for the  $v_n$  for three different  $p_T$  ranges:  $0.5 < p_T < 1.0$  GeV,  $p_T > 1.0$  GeV and  $p_T > 0.5$  GeV for the (20-25)% centrality class. The  $v_n$  distributions for tracks with  $p_T > 1.0$  GeV are much broader than the ones for  $p_T < 1.0$  GeV reflecting the fact that the  $v_n$  increase with  $p_T$ . However, once the three distributions are scaled to the same mean value, their reduced shapes are almost identical as shown in the lower panels. This indicates that the hydrodynamic response to the initial geometry scales linearly with  $p_T$ .



**Figure 3.** Top panels: The unfolded distributions for  $v_n$  in the (20-25)% centrality interval for charged particles in  $p_T > 0.5$  GeV,  $0.5 < p_T < 1.0$  GeV and  $p_T > 1$  GeV. Bottom panels: same distributions but rescaled horizontally so the  $v_n$  values match that for  $p_T > 0.5$  GeV. The shaded bands represent the systematic uncertainties on the  $v_n$  shape. Figure taken from [6].

Figure 4 shows the mean values ( $\langle v_n \rangle$ ) and RMS widths ( $\sigma_{v_n}$ ) of the  $v_n$  distributions as well as the ratio of  $\sigma_{v_n}/\langle v_n \rangle$  as a function of the number of participating nucleons  $\langle N_{\text{part}} \rangle$ . While the  $\langle v_n \rangle$  and  $\sigma_{v_n}$  change with  $p_T$  the ratio is independent for all three harmonics. The ratio  $\sigma_{v_3}/\langle v_3 \rangle$  is independent of  $\langle N_{\text{part}} \rangle$  and consistent with the value of  $\sqrt{4/\pi - 1} = 0.52$  expected from 2D-Gaussian distributions,  $v_4$  shows a similar behavior as well (not shown). For  $v_2$  the Gaussian limit is reached only in most central events and shows a considerable deviation for mid-central and peripheral events, where the average collision geometry has a large second-order eccentricity. For all cases, the  $v_n$  measured via the EP method are found to lie in between  $\langle v_n \rangle$  and  $\sqrt{\langle v_n^2 \rangle}$  within statistical and systematic errors [6].



**Figure 4.** The  $\langle N_{\text{part}} \rangle$  dependence of  $\langle v_n \rangle$  (left column),  $\sigma_{v_n}$  (middle column) and  $\sigma_{v_n}/\langle v_n \rangle$  (right column) for  $n=2$  (top row) and  $n=3$  (bottom row). Each panel shows the results for three  $p_T$  ranges together with the total systematic uncertainties. The dotted lines in the right column indicate the value 0.52 expected for the radial projection of a 2-D Gaussian distribution. Figure taken from [6].

ATLAS has measured the event-by-event distribution of harmonic flow coefficients  $v_2 - v_4$  in various centrality bins. The  $v_2$  distribution is consistent with radial projection of 2D Gaussian distributions in most central events, but shows significant deviation for  $>5\%$  centrality. For  $v_3$  and  $v_4$  the distributions are consistent with 2D Gaussian for all centralities. The reduced shape of the  $v_n$  distributions has no  $p_T$  dependence showing that the hydrodynamic response to the initial geometry is independent of  $p_T$  up to an overall normalization. These measurements are the first of their kind and provide constraints on the hydrodynamic response as well as initial geometry fluctuations of the produced medium [6].

## References

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