

Systematic investigation of $E1$ strength for the isotopes from $Z = 28$ to 50

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Abstract. We carry out a systematic study of electric dipole mode ($E1$) for neutron-rich isotopes from nickel ($Z=28$) to tin ($Z=50$) using a time-dependent mean-field theory. Our time-dependent scheme is the canonical-basis time-dependent Hartree-Fock-Bogoliubov theory which can self-consistently describe nuclear dynamics with pairing correlation. We focus our discussion on the pygmy dipole resonance (PDR) and $E1$ polarizability (α_D). The correlation between neutron-skin thickness and PDR strongly depends on the neutron number, but the correlation between the skin thickness and α_D is much more stable.

1. Introduction

Recent progress in radioactive isotope facilities and experimental techniques allows us to generate and to study neutron-rich nuclei. In the neutron-rich region far from stability line, the neutron-skin and halo structures may appear in the ground state [1]. Due to their exotic structures in the ground state, new elementary modes are expected. The pygmy dipole resonance (PDR) is known as a candidate of such a characteristic excited state in the neutron-rich nuclei, which appears in low energy region, sometimes interpreted as a neutron-skin mode. Previous studies indicate that there is the linear relation between PDR and neutron-skin thickness [2, 3]. On the other hand, Ref.[4] indicates that the correlation between PDR and the skin is small from the covariance analysis, and that the electric dipole ($E1$) polarizability is much more correlated to the neutron skin than PDR [4]. Recently, the dipole polarizability has been measured for ^{206}Pb at RCNP, Osaka University [5].

In the present paper, the relation among neutron-skin, PDR and $E1$ polarizability, will be shown for over 350 isotopes, which is obtained by the linear response calculation using the time-dependent scheme.

2. Formulation

In order to study the dynamics of many nuclei including superfluid deformed nuclei, we proposed the canonical-basis time-dependent Hartree-Fock-Bogoliubov (Cb-TDHFB) theory. The Cb-TDHFB can be derived from the full TDHFB equation represented in the canonical basis and on the assumption that the pair potential can be approximated to be diagonal in the canonical basis [6].



Introducing the time-dependent canonical states $|\phi_k(t)\rangle$ and $|\phi_{\bar{k}}(t)\rangle$, we express the TDHFB state in the canonical (BCS) form as

$$|\Psi(t)\rangle = \prod_{k>0} \left\{ u_k(t) + v_k(t) c_k^\dagger(t) c_{\bar{k}}^\dagger(t) \right\} |0\rangle, \quad (1)$$

where $u_k(t), v_k(t)$ are time-dependent BCS factors. It should be noted that the pair of states, k and \bar{k} , are not necessarily related to each other by the time-reversal, $|\phi_{\bar{k}}(t)\rangle \neq T|\phi_k(t)\rangle$. The diagonal approximation of the pair potential leads to the following equations:

$$i \frac{\partial}{\partial t} |\phi_k(t)\rangle = (h(t) - \eta_k(t)) |\phi_k(t)\rangle, \quad i \frac{\partial}{\partial t} |\phi_{\bar{k}}(t)\rangle = (h(t) - \eta_{\bar{k}}(t)) |\phi_{\bar{k}}(t)\rangle, \quad (2a)$$

$$i \frac{d}{dt} \rho_k(t) = \kappa_k(t) \Delta_k^*(t) - \kappa_k^*(t) \Delta_k(t), \quad (2b)$$

$$i \frac{d}{dt} \kappa_k(t) = (\eta_k(t) + \eta_{\bar{k}}(t)) \kappa_k(t) + \Delta_k(t) (2\rho_k(t) - 1). \quad (2c)$$

These basic equations determine the time evolution of the canonical states, $|\phi_k(t)\rangle$ and $|\phi_{\bar{k}}(t)\rangle$, their occupation $\rho_k(t) = |v_k(t)|^2$, and pair probabilities $\kappa_k(t) = u_k(t)v_k(t)$. $\Delta_k(t)$ is the gap energy,

$$\Delta_k(t) = \sum_{l>0} G f(\varepsilon_k^0) f(\varepsilon_l^0) \kappa_l(t), \quad (3)$$

where G is a the pairing strength determined by the smoothed pairing method [7], and $f(\varepsilon)$ is a cutoff function which defines the number of canonical basis [6]. The cutoff function is time-independent with the single-particle energies ε_k^0 at the ground state.

We solve the Cb-TDHFB equations in real time and calculate the linear response of the nucleus. The numerical procedure of linear response is same as that of Ref.[6], we add an external field $\hat{V}_{\text{ext}}(\mathbf{r}, t) = -k\hat{F}_{E1}\delta(t)$ to the ground state of the nucleus, where $\hat{F}_{E1} = (N/A)\sum_p \hat{r}_p - (Z/A)\sum_n \hat{r}_n$, here $r = (x, y, z)$ and k is an arbitrary small parameter. Then, we compute the time-evolution of the nuclear density using the time-dependent scheme. We obtain the strength function $S(E1; E)$ through the Fourier transformation of the time-dependent expectation value of \hat{F}_{E1} [6]. To quantify the PDR, we use the ratio:

$$\frac{m_1(E_c)}{m_1} \equiv \frac{\int^{E_c} E \times S(E1; E) dE}{\int^{E_T} E \times S(E1; E) dE}, \quad (4)$$

where we adopt the cutoff energy $E_c = 10$ MeV and the total energy $E_T = 100$ MeV in the present calculation. The $E1$ polarizability α_D is defined using $E1$ strength function as,

$$\alpha_D \equiv 2 \int^{E_T} \frac{S(E1; E)}{E} dE. \quad (5)$$

In this work, we use the three-dimensional Cartesian coordinate for the canonical states, $\phi_k(\mathbf{r}, \sigma; t) = \langle \mathbf{r}, \sigma | \phi_k(t) \rangle$ with $\sigma = \pm 1/2$. The coordinate space is discretized in the square mesh of $\Delta x = \Delta y = \Delta z = 1.0$ fm in a sphere with radius of 15 fm.

3. Results

Figure 1 shows the PDR ratio as a function of neutron-skin thickness which is defined by the difference between root mean square radii of neutrons and protons, from Ge to Sn isotopes. In

both panels, open circles and triangles indicate the isotopes with $N=50$ and 82 , respectively. We can see the linear relation between the PDR ratio and the neutron-skin thickness for each isotopic chain with $N=50 \rightarrow 58$. The slope of the linear correlation becomes small as the proton number approaches $Z=50$. The slope for Sn isotope from $N=50$ to 58 is about a half of that in Ge isotope. The PDR ratio strength jumps up again over $N=82$. The correlation between PDR and N -skin strongly depends on the neutron number.

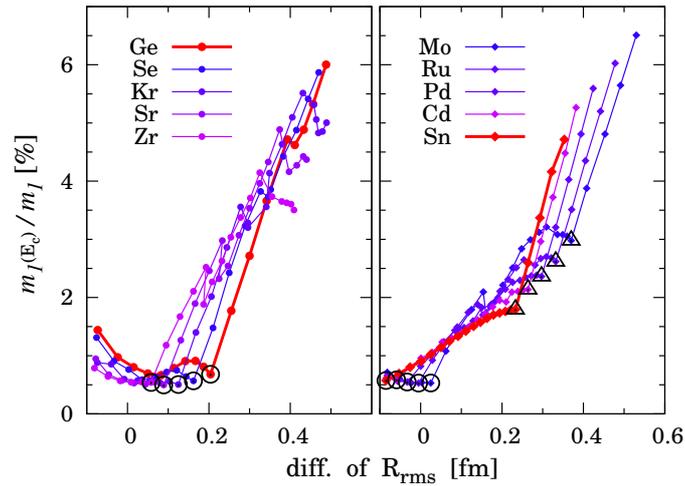


Figure 1. PDR ratio defined by Eq.(4), as a function of N -skin thickness from Ge to Sn isotopes. Open circle and triangle symbols indicate the isotope with $N=50$ and 82 , respectively.

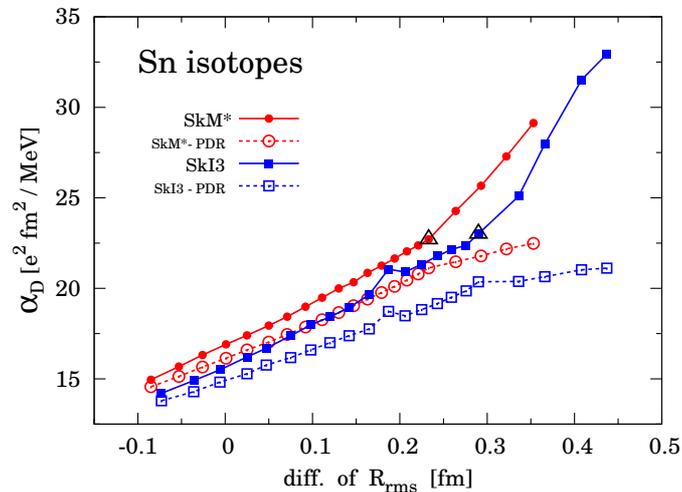


Figure 2. $E1$ polarizability α_D defined by Eq.(5), as a function of neutron-skin thickness for Sn isotopes with $N = 50 - 90$. Circles (squares) with solid lines indicate results with SkM* (SkI3) parameter set. Open symbols with dashed lines are defined by Eq.(6)

Figure 2 shows the $E1$ polarizability α_D as a function of N -skin thickness for Sn isotopes. Circles (squares) are obtained with the SkM* (SkI3) Skyrme energy functional. Open symbols in Fig.2 are computed from the $E1$ strength excluding the PDR part;

$$\tilde{\alpha}_D \equiv 2 \int_{E_c}^{E_T} \frac{S(E1; E)}{E} dE. \quad (6)$$

This can be regarded as the dipole polarizability associated with the giant dipole resonance. The SkI3 parameters are made so as to reproduce the ordering of single-particle levels in Pb isotopes obtained by the relativistic mean-field model. Especially, the part of the spin-orbit force is different from that of SkM*. The polarizability $\tilde{\alpha}_D$ is strongly correlated with the skin-thickness, although the contribution of the PDR becomes large in both results over $N=82$. In contrast to the relation between PDR and the skin, the correlation between α_D and the skin thickness is more stable with respect to change of the neutron number and the energy functional.

In summary, we found the linear correlation between the PDR and the neutron-skin thickness, however, the correlation rather strongly depends on the neutron number. The correlation between α_D and the neutron-skin thickness is more robust, especially if we remove the contribution from the PDR. This may suggest a better way to constrain the neutron-skin thickness by the observation of $E1$ strength function.

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