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Excitation of torsional modes in guide vanes

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Excitation of torsional modes in guide vanes

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Abstract. Rotor stator interaction in high-head Francis turbines has led to several failures in recent years. Increasing efficiency demands require design optimization of the turbine components, which may lead to thinner profiles. Not only can component not withstand the given loads; quite often one or more of their natural frequencies coincide with that of the rotor-stator interaction. Most of the research published has been on runners, while other parts of the turbine are less studied. Even though guide vanes have torsional modes with frequencies which may be close to the exiting frequency from the rotor stator interaction with the runner, no significant failures due to resonance have been reported. This paper investigates some of the possible mechanisms which may negate resonance in the torsional modes of the guide vanes including; hydrodynamic damping from the flowing water and friction in the guide vane bearings. A case study is conducted on a guide vane where the calculated natural frequency is within 10% of the excitation frequency, while no significant vibrations have been reported. Further, the findings are generalized to Francis turbines of different specific speeds.

1. Introduction

In the last decade several large high head Francis runners have experienced cracks. Through the research from authors [10, 4, 3] the cause of the failure have been contributed to a resonance in the runner with the pressure field from the guide vanes. This interaction between the rotating runner and stationary guide vanes is called Rotor Stator Interaction (RSI). The guide vanes of the turbine will experience the same transient pressure field from RSI as the runner, only from the stationary domain. This pressure field will create a torque on the guide vane stem, which in theory could excite a resonance with the torsional mode of the guide vanes. However, very few cases have been reported. Some pump turbines have reported torsional vibration at small openings due to self excitation from the flow field. Nenneman and Parkinsons [7] showed using advanced CFD how this phenomena could be modeled. Predin et al. [8] found that a linear model for flow and the torsional movement of the guide vane was able to replicate measurements on a model pump turbine. Roth et al. [9] investigated the coupling of a bending mode in the guide vanes and the RSI pressure field. They showed how the RSI pressure amplitude decrease near the guide vane bending resonance frequency.

To estimate the risk of resonance the eigenfrequency of the torsional mode has to be calculated. The simplest way, and perhaps the common way, is to do a modal analysis where the guide vane is fixated at the arm, the bearings are modeled as friction less and the guide vane blade is submerged in water.

Using this method, we calculated the eigenfrequency of several old high head Francis turbine guide vanes in Norway. This study revealed that several of them had torsional frequencies within 10% of the exciting frequency from the runner. Even though such closeness between the forcing and eigenfrequency normally leads to large vibrations none was observed in any of the turbines. In this article we investigate what might be the cause to why no such vibrations have been observed. In particular, the effect of friction in the guide vane bearings have been investigated.

2. Theory
The vibrations of a complete regulating mechanism will be a set of complex and connected vibrations with several coupled modes. In this article we consider the torsional vibrations of a guide vane as a single degree of freedom system with a characteristic natural frequency ω_n and damping ζ.

$$\ddot{x} + 2\omega_n\zeta\dot{x} + \omega_n^2 x = F(t) \tag{1}$$

As the guide vane increases the angular momentum of the water flowing from the stay vanes to the runner it experiences a force from the water. This normal force F_0 is balanced in the guide vane bearings together with a frictional force. The force F_0 and friction force F_f will be in a stick condition when the frictional force is below the slip limit: $F_f = \mu \cdot F_0$. μ is the frictional coefficient between the bearing and guide vane.

At the same time the guide vanes will be subject to a time varying pressure field due to the passing of the runner vanes. This pressure field will oscillate with the runner passing frequency $f_r = {}^{n_{rpm}}/60 \cdot Z_r$ and create an oscillating torque M on the guide vane. For high head Francis turbines, this will be the main excitation force of torsional movement of the guide vane. The guide vane is more or less fixated at the top. The dynamic torque on the blade will twist the guide vane stem, rotating it inside of the bearings.

This configuration results in three different physical conditions in the interaction between the guide vane stem and the bearing. These are presented below. Two of them are only briefly presented as the findings of this paper suggest that they are not likely to occur in Francis turbines.

2.1. Guide Vane stem rolling in bearing
If the dynamic torque, M, is less than the frictional torque in the bearings ($M < r \cdot \mu \cdot F_0$), the guide vane stem will be stuck to the bearing and not be able to slide. Given that guide vane bearing has a radius R which is larger than the stem radius r, the guide vane stem will roll back and forth in the bearing. This is similar to a cylinder rolling back and forth in a valley under the force of gravity.

This case can be modeled as a cylinder rolling inside of a larger cylinder while being statically loaded with F_0. The setup can be seen in Figure 1.

In Figure 1 the guide vane stem has rotated an angle of ϕ. Since there is no sliding, the distance rolled on the bearing has to be the same as for the stem.

$$R \cdot \theta = r \cdot (\theta + \phi) \tag{2}$$

As the normal force F_0 now acts outside of the contact point P it will create a restoring torque M_r forcing the stem back to the equilibrium position. This torque is found by calculating F_0's torque around point P and linearising which gives:

$$M_r = \frac{F_0 \cdot r^2}{\Delta r} \cdot \phi \tag{3}$$
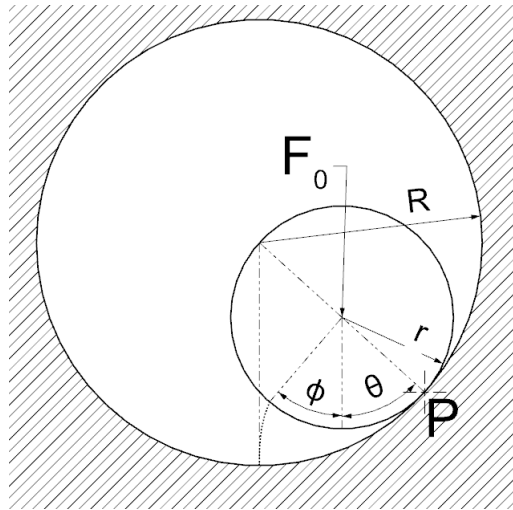
Figure 1. Sketch of the guide vane stem inside of the bearing. Shown in a pertubated position after rotating an angle ϕ. Difference in diameter is greatly exaggerated.

where Δr is the radial clearance in the bearing. This restoring torque is proportional to the angle θ and this represents an additional stiffness (in addition to the stem torsional stiffness) resisting the vane rotation. The formula reveals that the stiffness is inversely propositional to the clearance in the bearing. Given that such bearings often have tight clearances this spring constant may be significant.

It is worth noting that this calculation is done with the assumption of a perfectly circular stem and bearing. Wear and machining inaccuracies will change the shape which can affect the calculated stiffness.

2.2. Guide Vane stem sliding in bearing

If the dynamic torque is significantly larger than the frictional torque ($M >> r \cdot \mu \cdot F_0$) the guide vane stem will slide inside of the bearing. In this case the friction will act as damping. The amount of equivalent viscous damping (ζ_{eq-dry}) produced by such dry friction is dependent on both the excitation frequency (ω) and the amplitudes of the motion (A).

$$\zeta_{eq-dry} = \frac{2\mu F_0}{\pi m \omega \omega_n A} \tag{4}$$

As the vibration amplitude is in the denominator of the equation, the equivalent damping will diminish as the amplitudes grow.

2.3. Guide Vane stem rolling and sliding in bearing

If the dynamic torque is above the frictional torque, but still in the same order of magnitude ($M > r \cdot \mu \cdot F_0$), the resulting motion will be a combination of sliding and rolling. When the dynamic torque is below the frictional stick limit, the guide vane will roll, but as soon as the torque increases above the frictional stick limit, the guide vane will slide back with the friction acting as a damper.

2.4. Hydrodynamic damping

Research by Carl et al. [1] and Cotou et al. [2] has shown that the hydrodynamic damping for a vibrating foil may be significant at high water velocities. As the velocity of the water may reach

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60 to $70\,{}^m/s$ at the trailing edge of the guide vane this phenomenon must be accounted for to predict the guide vane motion.

Using the modal work method developed for a hydrofoil by Monette et al. [5], and adapted for guide vanes by Myrvold [6], the damping can be expressed as in equation (5). It takes the work (W_f) done by the water through a vibration cycle and scales it based on the frequency (ω_n), mass(m) and amplitude(A) of the eigenmode in question.

$$\zeta = \frac{W_f}{2\pi \cdot m \cdot \omega_n^2 \cdot A^2} \tag{5}$$

2.5. Hydrodynamic stiffness

Monette et al. [5] provides compelling arguments that the added stiffness from the water flow is insignificant and the analytical formulas to calculate this effect is quite complicated. However, in the case of torsional movement of the guide vane it is easily available.

When dimensioning the guide vane apparatus, it is important to know the relation between the hydraulic torque and guide vane opening. As the torsional motion of the guide vane blade is the same as changing the guide vane opening, the hydrodynamic stiffness can be read directly from the M_{hydro}-θ diagram.

$$k_{hydro} = \frac{dM_{hydro}}{d\theta} \tag{6}$$

3. Case study

To investigate the effect of the bearing on the natural frequency of a guide vane a case study was conducted on a high head Francis turbine. This particular turbine was chosen as the calculated natural frequency of the torsional mode of the guide vane is near the runner passing frequency (when assuming only stem torsional stiffness). As it is a high head Francis the dynamic torque applied to the guide vanes are estimated to be higher than on a low head turbine. The main data of the turbine is shown in Table 1.

Table 1. Turbine Data.

Rated Head	:	395	m
Speed	:	500	rpm
Number of Runner Vanes	:	32	pc
Speed Number	:	0.063	n_{QE}
Runner Passing Frequency	:	267	Hz

The guide vane stem is long and slender with three bearings. A sketch of the geometry is shown in Figure 2. The bearing/stem have a h8/E7 fit which give a radial clearance of $0.036 < \Delta r < 0.08$. A CFD calculation of the turbine in question reveals a static force F_0 on the guide vanes vary from $99kN$ at speed no load to $58kN$ at full load. The dynamic torque amplitude is calculated to be about $M = 48Nm$ for all loads. Using a lower bound estimation of the friction coefficient, $\mu = 0.05$, gives a minimum frictional torque of $F_f = 130Nm$. As the dynamic torque is significantly less the frictional torque the guide vane stem should thus roll in the bearing.

Using equation (3) we can now calculate the possible range of stiffness from the bearings. Comparing this to the torsional stiffness of the stem, equation (7), gives an estimate of the importance of the bearing stiffness. Here the Young Modulus (E), diameter of the stem (D), lengh (L) and poisson factor (ν) are the important parameters.

$$k_{\theta\,stem} = \frac{dM}{d\theta} = \frac{GI_p}{L} = \frac{E \cdot \pi \cdot D^4}{2(1+\nu) \cdot 64 \cdot L} \tag{7}$$
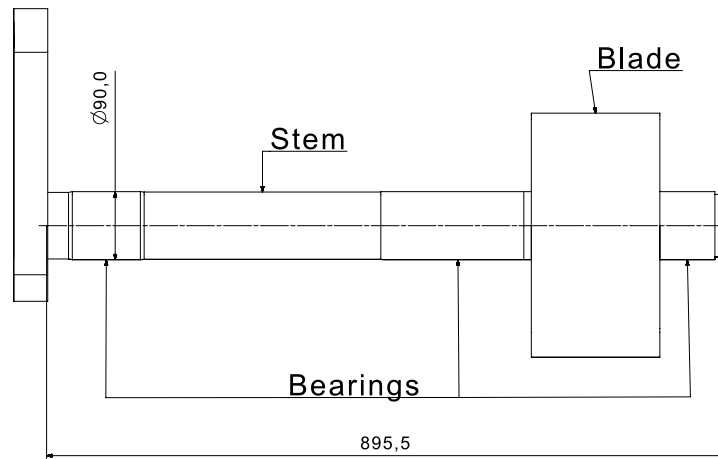
Figure 2. Guide vane geometry.

Table 2. Torsional stiffness k_θ.

Bearing$_\text{max}$	:	$5.6 \cdot 10^6$	Nm/rad
Bearing$_\text{min}$	:	$1.48 \cdot 10^6$	Nm/rad
Guide vane stem	:	$8 \cdot 10^5$	Nm/rad

As the stiffness from the bearings is of the same order of magnitude as the guide vane stem, their effect cannot be disregarded when calculating the natural frequency of the guide vanes.

3.1. Numerical investigation
To evaluate the guide vanes torsional response to the RSI pulsations from the runner a set of numerical calculations were conducted.

3.1.1. Eigenfrequency The eigenfrequency of the guide vane is calculated using the range of possible bearing stiffnesses. A water volume is placed around the guide vane profile to include the added mass effect of the water. Assuming that the static load F_0 mainly is carried by the two bearings closest to the blade, half of the bearing stiffness is distributed to each of those bearings.

With frictionless bearings the natural frequency of the guide vane is calculated to be 245 Hz, only 8% away from the exciting frequency. However, including the bearing stiffness significantly increases the natural frequency. This is shown in Figure 3 where the effect of bearing stiffness becomes evident. The torsional frequency increases 50% to 125% depending on operating point and clearance. This is less than what a direct comparison of the torsional stiffness would predict, which is likely due to the mode shape changing as with the introduced stiffness.

$$\Delta\omega_{n\,max\,theoretical} = \sqrt{\frac{8 \cdot 10^5 + 5.6 \cdot 10^6}{8 \cdot 10^5}} - 1 \approx 182\%$$

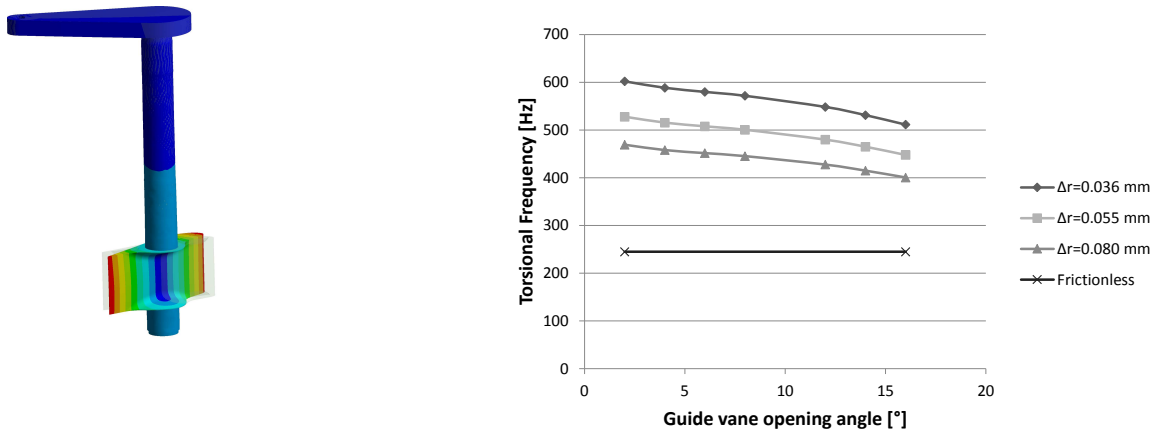$$\Delta\omega_{n\,min\,theoretical} = \sqrt{\frac{8\cdot10^5 + 1.48\cdot10^6}{8\cdot10^5}} - 1 \approx 69\%$$

Figure 3. Torsional frequency of guide vane with and without bearing stiffness for different bearing clearances Δr and different operating points.

3.1.2. Hydrodynamic damping Using a transient CFD calculation with imposed vibration of the guide vane blade according to the eigenmodes and frequencies found above, the damping was calculated using equation (5). Only the modes and frequencies with a radial clearance of 0.055mm was used. The guide vane was forced to oscillate with two different amplitudes, 0.1mm and 0.01mm.

As a simplification, all guide vanes were forced to oscillate in phase with the neighbour vane. This is not physically correct, but including the phase shift would significantly increase the computational requirements.

The resulting damping is almost constant at 3% with an increase at very small openings.

3.1.3. Hydrodynamic Stiffness Using the hydraulic torque diagram, the hydrodynamic stiffness was calculated with equation (6). The value ranges from $-2\cdot10^4 Nm/rad$ to $0 Nm/rad$. Even though the damping is negative at all openings, its value is insignificant compared to both the stem stiffness and bearing stiffness. It is thus not included in the model.

3.1.4. Harmonic Response To quantify the difference between guide vane bearings with and without friction a harmonic response analysis was conducted at the runner vane passing frequency ($266.67\,[Hz]$). A harmonic pressure field from a transient CFD analysis was used as the forcing field on the guide vane blade. A constant damping of 3% is used as calculated above.
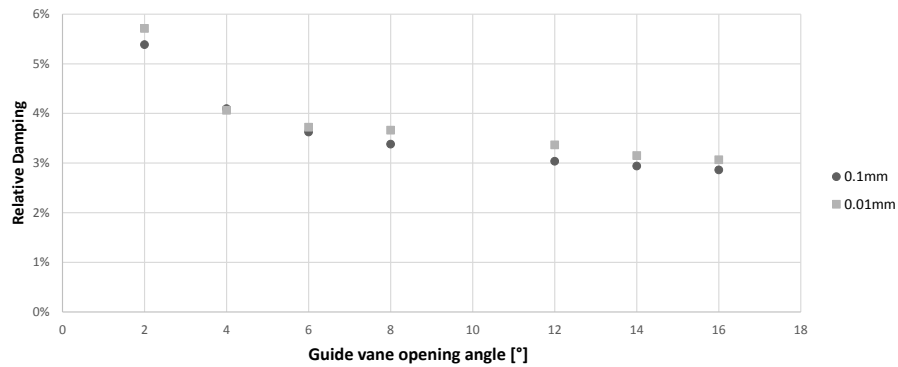
Figure 4. Relative Damping ($c/c_{critical}$) calculated for the torsional mode of the guide vane at different openings with two motion amplitudes.
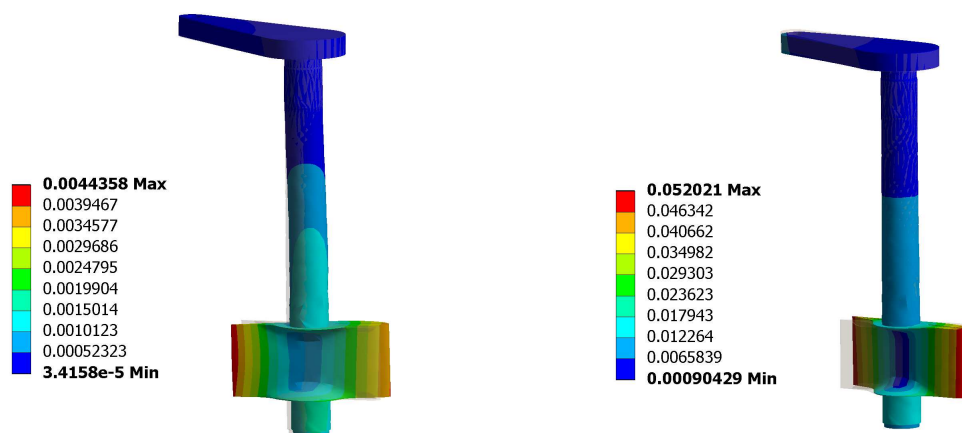

Figure 5. Vibration Amplitude with stem rolling in bearing (left) and frictionless sliding in bearing (Right).

Figure 5 shows the results where the stiffness from the bearings reduce the amplitudes by more than a decade.

3.2. Measurements
To investigate the dynamics of the guide vane a measurement series was conducted on the reference turbine. Ideally, one should either measured the stresses in the guide vane stem or the acceleration on the guide vane blade. These areas are however not available during operation. Two accelerometers was instead placed on the guide vane arm as shown in Figure 6. The vibration data was logged at $4800\,[Hz]$.

The overall measured vibration levels was small. By extracting the frequency component
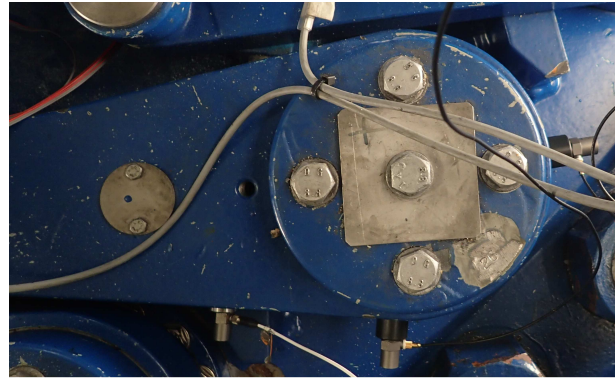
Figure 6. Accelerometer placement on the guide vane arm.

of each measurement at the runner vane passing frequency it is possible to compare the measurements to the Harmonic Response analysis. The results are shown in Figure 7. It clearly shows that the effect of the bearing stiffness due to friction has to be taken into account. With out this stiffness the the calculated vibration amplitudes become to high. Including the bearing stiffness gives a result very close to the measured values.
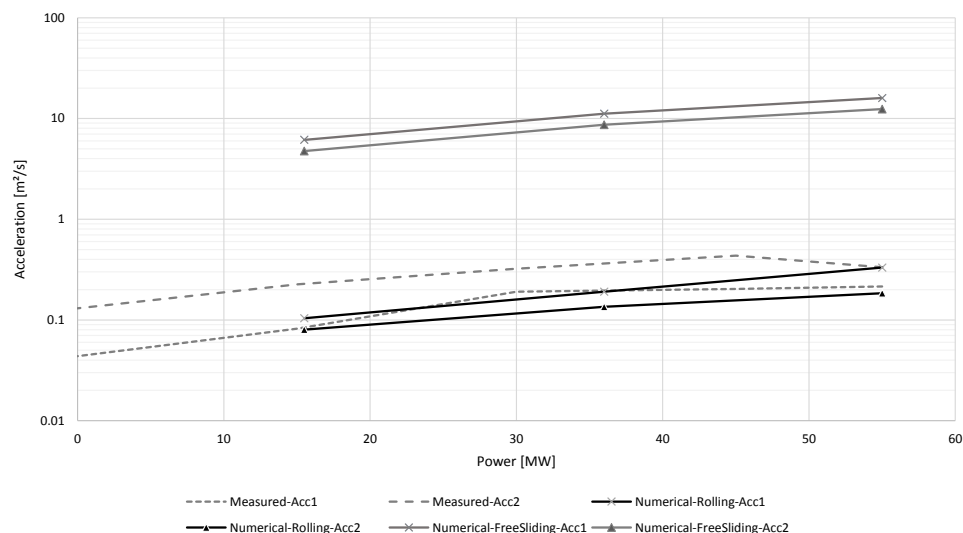

Figure 7. Measured accelerometer data vs calculated values for rolling bearing with friction and sliding frictionless bearings.

4. Applicability for other turbines
The case study showed that for a high head Francs turbine the guide vane will most likely roll in the bearings and the bearing stiffness is significant compared to the torsional stiffness of the guide vane.

Using data from numerical simulations of other Francis turbines, the required bearing friction coefficient which ensures rolling has been calculated. Nineteen different turbines was included in the set. Some with several operating points. The result is shown in Figure 8. In none of the cases examined does the required friction coefficient exceed 0.05. This seem to be independent

of the turbine head. This will of course be somewhat dependent on the design of the guide vane. However, this diagram contains data from both new and old designs.
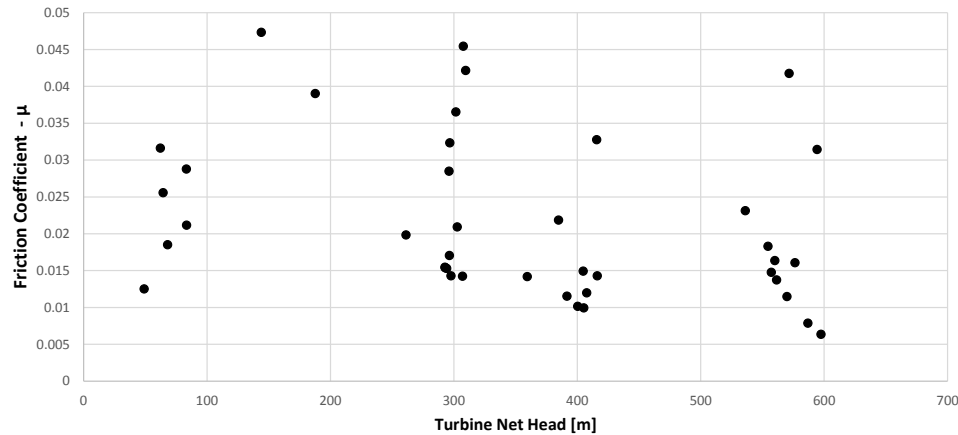

Figure 8. Required bearing friction coefficient to ensure rolling for different turbines.

The relative stem stiffness to the bearing stiffness is shown in Figure 9. It shows a clear trend where the bearing stiffness dominates at high heads while at low head turbines the stem stiffness is dominating.

Even though the effect of bearing stiffness is reduced at low head turbines, the effect is still significant enough to change the torsional frequency and it should thus be included in eigenfrequency calculations for all turbines.
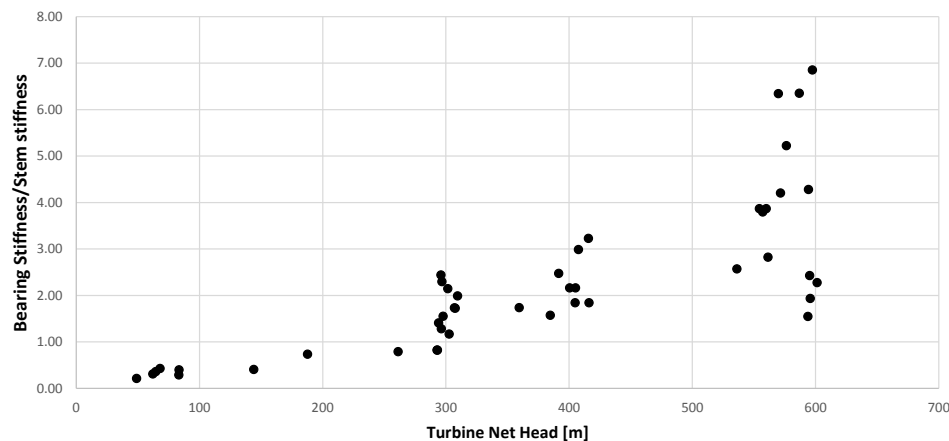

Figure 9. Bearing stiffness divided by stem stiffness assuming 0.1mm radial clearance for different turbines.

5. Conclusion

When estimating the harmonic response of the torsional eigenmode for Francis turbines, it is important to include the effect the bearings has on the relevant eigenfrequency. This was verified through on site measurements. For all 19 turbines investigated, the frictional torque in the bearing is significantly larger than the dynamic torque produced by the RSI forces, independent on turbine net head. With friction factors of $\mu > 0.05$ the friction is significant enough to stop

sliding. As there is a small clearance in the bearing, the bearing will have a torsion-spring like behavior forcing the guide vane back to its base position. This effect is very dependent on net head. For very high head units the spring coefficient of the bearing can be 2-10 times the torsional stiffness of the guide vane stem. For low head units the guide vane stem is significantly more torsional stiff than the bearings.

The added stiffness from the bearings increases the natural frequency of the torsional mode significantly compared to the estimated value using frictionless bearings. Due to the close relation between the bearings clearance and the stiffness, guide vanes with worn bearings will most likely have different torsional eigenfrequencies than new guide vanes.

The damping calculated is in the range of 3 to 6%. This, together with the added stiffness from the bearings, and overall robust designs, may be the reasons why so few problems have been reported for guide vane vibrations in high head Francis units.

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