

# Unmanned surface vessel heading control of model-free adaptive method with variable integral separated and proportion control

Quanquan Jiang, Yulei Liao , Ye Li , Yugang Miao, Wen Jiang and Changsheng Cheng

## Abstract

Based on model-free adaptive control theory, the heading control problem of unmanned surface vessels under uncertain influence is explored. Firstly, the problems of compact form dynamic linearization model-free adaptive control method applied to unmanned surface vessel heading control are analyzed. Secondly, by introducing proportional control and variable integral separation factor, an variable integral separation model-free adaptive control algorithm with proportional control is proposed. The introduction of proportional control and variable integral separation factor solves the problems of oscillation, instability, and integral saturation when rudder angle is controlled directly to control the heading of unmanned surface vessel with compact form dynamic linearization model-free adaptive control method. Finally, the effectiveness of the method is verified by the simulation and field experiments results of heading control with model perturbation and system time delay in unmanned surface vessel heading subsystem.

## Keywords

Unmanned surface vehicles, heading control, model-free adaptive control, proportional control, variable integral separation factor

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## Introduction

Unmanned surface vessels (USVs) are attracting growing attention from researchers at home and abroad because of their extensive applications in environmental monitoring, marine survey, and port guards, coordinating work with autonomous underwater vehicles.<sup>1</sup> However, USV has the characteristics of nonlinear, uncertainty, time-varying, and time-delay, besides, it is susceptible to environment interference.<sup>2,3</sup> Hence, it is meaningful to study the motion control problems of USV with uncertainties. Aiming at model perturbation and time delay of heading subsystem, the heading control of USV is studied in this article.

At present, many scholars have carried out relevant research work on USV heading control and the control methods are mainly focused on sliding mode control,<sup>4,5</sup> adaptive control,<sup>6</sup> proportion, integral and derivative (PID) control,<sup>7,8</sup> intelligent control,<sup>9–12</sup> and so on. Miao et al.<sup>13</sup>

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by combining the expert control technology, S plane and PID control algorithms, an adaptive expert S-PID control algorithm was proposed for heading control of the micro-USV and field tests were conducted. However, the structure of the controller is complex, and the accurate acquisition of expert experience is difficult. Mu et al.<sup>14</sup> proposed an adaptive heading controller by trajectory linearization control technology, neural network minimum learning parameter method, disturbance observer and auxiliary design system, but the controller design needs precise mathematic models, which is very difficult in practice. Classic PID algorithm was used as the main heading control algorithm, and back-propagation neural network (BPNN) was also utilized to achieve more effective self-adaptive PID control.<sup>15</sup> At the same time, in order to improve the convergence speed and precision of BPNN, artificial bee colony algorithm was introduced to minimize the error of system and adjust the weight of BPNN.<sup>16</sup> However, BPNN structure selection is difficult to determine, generally based on experience, besides, BPNN has the problem of sample dependence: the approximation and generalization ability of network model is closely related to the typicality of learning samples, and it is difficult to select typical samples from the problem to form training set. Aiming at the problem of heading control of USV with variable mass and resistance, Wilhelm et al.<sup>16</sup> proposed a model reference adaptive backstepping method. Fan<sup>17</sup> proposed a fuzzy self-adaptive algorithm for USV heading control.

In the above method, the PID control algorithm has obtained the most extensive real ship application. However, USV is easily influenced by model perturbation and environmental disturbance force, which makes it difficult for the PID controller to maintain the consistent control performance; the parameters need to be adjusted again to stabilize the system.<sup>17</sup> It is difficult to establish accurate mathematical models of controlled systems, which makes it hard to achieve good control performance based on model-based control algorithms.<sup>18-20</sup> Therefore, it needs a model-free controller with good robustness and strong adaptability for USV heading control.

In recent years, data-driven control algorithms have attracted much attention.<sup>21</sup> Model-free adaptive control (MFAC) is one of data-driven control methods proposed by Hou Zhongsheng for a class of general single input and single output (SISO) discrete time nonlinear systems.<sup>22</sup> It does not consider the actual mathematical model of USV, instead, the controller design is based on the system input and output (Input/Output, I/O) data. It has been widely used in traffic, oil, refining, chemical, and other industrial control fields<sup>23</sup>; however, the research of this method in the field of motion control such as underwater vehicles and USV is relatively little, not to mention practical engineering application at present.

Based on compact form dynamic linearization model-free adaptive control (CFDL\_MFAC) algorithm, this article discuss heading control problem of USV under

uncertain influence. Firstly, the problems of CFDL\_MFAC applied to USV heading control are analyzed. Secondly, introducing proportional control and variable integral separation factor solves the problems of oscillation, instability, and saturation when applying CFDL\_MFAC method to USV heading control directly; finally, the robust and adaptive performance of the variable integral separation model-free adaptive control algorithm with proportional control (VIS\_MFAC\_PC) method is verified by the simulation and outfield experiments results of heading control with model perturbation and system time lag in USV heading subsystem.

## Analysis of MFAC method and USV heading control application

Generally, SISO discrete time nonlinear systems can be expressed as<sup>23</sup>

$$y(k+1) = f(y(k), \dots, y(k-n_y), u_m(k), \dots, u_m(k-n_u)) \quad (1)$$

where  $y(k) \in R$ ,  $u_m(k) \in R$  respectively represent the input and output of the system at time  $k$ ;  $n_y$  and  $n_u$  are the order of the system. Obviously, USV heading subsystem is one of the nonlinear SISO systems, which can be expressed by equation (1).

The following assumptions are made for system (1):

**Assumption 1.** Except for finite moments, the partial derivatives of the  $(n_y + 2)$ th variables of  $f(\dots)$  exist and are continuous.<sup>23</sup>

**Assumption 2.** Except for finite moments, the system of equation (1) satisfies the generalized Lipschitz condition, that is, with any  $k_1 \neq k_2$ ,  $k_1, k_2 \geq 0$ , and  $u_m(k_1) \neq u_m(k_2)$

$$|y(k_1+1) - y(k_2+1)| \leq b|u_m(k_1) - u_m(k_2)| \quad (2)$$

where  $b > 0$  is a constant.<sup>23</sup>

In the point of practical view, above assumptions on control objects are reasonable and acceptable. Hypothesis 1 is a typical constraint on general nonlinear systems in control system design. Assumption 2 is the upper bound limitation of the change rate of system's output, that is, bounded-input makes bounded-output. The heading control subsystems of marine vehicles (ships, submarines, USV, offshore platforms, etc.) meet the above assumptions, obviously.

**Theorem 1.** If a nonlinear system satisfies Assumptions 1 and 2, when  $|\Delta u_m(k)| \neq 0$ , there must exist a time-varying parameter  $\phi_c(k) \in R$  named pseudo partial derivative (PPD) which makes the system of equation (1) transform into the CFDL model of equation (3)<sup>23</sup>:

$$\Delta y(k+1) = \phi_c(k) \Delta u_m(k) \quad (3)$$

where  $\phi_c(k)$  is bounded at any time. In equation (3),  $\Delta y(k+1) = y(k+1) - y(k)$ ,  $\Delta u_m(k) = u_m(k) - u_m(k-1)$ .

The CFDL\_MFAC algorithm is as follows<sup>23</sup>

$$u_m(k) = u_m(k-1) + \frac{\rho \hat{\phi}_c(k)}{\lambda + |\hat{\phi}_c(k)|^2} (y^*(k+1) - y(k)) \quad (4)$$

$$\hat{\phi}_c(k) = \hat{\phi}_c(k-1) + \frac{\eta \Delta u_m(k-1)}{\mu + \Delta u_m(k-1)^2} \times (\Delta y(k) - \hat{\phi}_c(k-1) \Delta u_m(k-1)) \quad (5)$$

$$\hat{\phi}_c(k) = \hat{\phi}_c(1), \text{ if } |\hat{\phi}_c(k)| \leq \varepsilon \text{ or } |\Delta u_m(k-1)| \leq \varepsilon \text{ or } \text{sign}(\hat{\phi}_c(k)) \neq \text{sign}(\hat{\phi}_c(1)) \quad (6)$$

where  $\phi_c(k)$  is the PPD;  $\hat{\phi}_c(k)$  is the estimation of the PPD;  $u_m(k)$  and  $u_m(k-1)$  denote the output of the CFDL\_MFAC controller at time  $k$  and  $k-1$  separately;  $\hat{\phi}_c(1)$  is the initial value of the PPD;  $\varepsilon$  is a sufficiently small positive number;  $\text{sign}(\bullet)$  is the symbolic function;  $\mu > 0$  and  $\lambda > 0$  are weight coefficients to adjust the change rate of PPD and controller output;  $\rho \in (0, 1]$  and  $\eta \in (0, 1]$  are the step factors.

CFDL\_MFAC algorithm only uses online input and output data of closed loop system to design controller, besides, the controller does not contain any explicit or implicit information of controlled system's dynamic model.<sup>23</sup> PPD is insensitive to time-varying parameter, time-varying structures, time-varying phases and even delay, thus CFDL\_MFAC has strong robustness and adaptability.

However, the algorithm cannot be directly applied to the heading control of USV. By analogizing the control structure of PID algorithm, it is known from formulation (5) that the CFDL\_MFAC algorithm belongs to incremental integral control structure. The heading of USV will produce overshoot and oscillation, when rudder angle is controlled directly to control the heading of USV with CFDL\_MFAC method. Besides, in the initial stage of USV heading control, or when the desired heading is changed greatly, the actual heading and expected heading of USV will have a great deviation in a short time. The existence of integral term results in integration accumulation of CFDL\_MFAC algorithm, which makes USV heading control system produce large overshoot, even oscillation, and increases regulation time-consuming. Therefore, for USV heading control system, the CFDL\_MFAC algorithm need to be improved.

### Variable integral separation model-free control adaptive method with proportional control

In the view of inevitable oscillation and instability of CFDL\_MFAC algorithm applied to heading control of USV, the control algorithm (5) is improved as follows

$$u_{m,p}(k) = u_{m,p}(k-1) + \frac{\rho \hat{\phi}_c(k)}{\lambda + |\hat{\phi}_c(k)|^2} (y^*(k+1) - y(k)) + k_p(e(k) - e(k-1)) \quad (7)$$

The algorithm consisting of formulas (5), (6), and (7) is called CFDL\_MFAC method with proportional control (hereafter referred as MFAC\_PC).

where  $k_p$  is the ratio coefficient;  $e(k)$  and  $e(k-1)$  denote heading deviation of time  $k$  and  $k-1$ , respectively;  $u_{m,p}(k)$  and  $u_{m,p}(k-1)$  denote the output of the MFAC\_PC method at time  $k$  and  $k-1$  separately;  $y^*(k+1)$  and  $y(k)$  represent reference heading and actual heading of  $k+1$  and  $k$ , respectively.

In the MFAC\_PC algorithm, the existence of integral terms  $\frac{\rho \hat{\phi}_c(k)}{\lambda + |\hat{\phi}_c(k)|^2} (y^*(k+1) - y(k))$  can eliminate static errors and improve control accuracy. However, in the initial stage of USV heading control, or when the desired heading is changed greatly, the actual heading and expected heading of USV will have a great deviation in a short time. The existence of integral term results in integration accumulation of MFAC\_PC algorithm, which makes USV heading control system produce large overshoot, even oscillation.

The MFAC\_PC algorithm is improved as follows: when controlled variable (USV heading angle) deviates greatly from set value, the integral term is reduced to avoid system stability reduction and overshoot increases due to the integral effect, at the same time, the control algorithm should still have stronger adaptability and faster response speed. When controlled variable approaches set value, the integral control is retained to eliminate static error and improve control accuracy. The improved algorithm is called variable integral separation model-free adaptive control algorithm with proportional control (VIS\_MFAC\_PC).

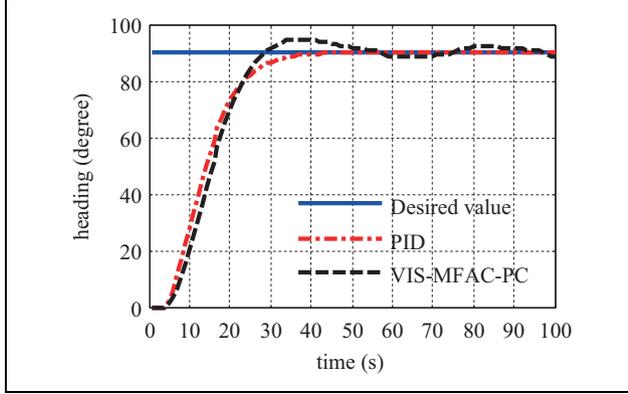
The VIS\_MFAC\_PC algorithm can be expressed as follows

$$u_{v,m,p}(k) = u_{v,m,p}(k-1) + \frac{\gamma \rho \hat{\phi}_c(k)}{\lambda + |\hat{\phi}_c(k)|^2} (y^*(k+1) - y(k)) + k_p(e(k) - e(k-1)) \quad (8)$$

$$\gamma = \begin{cases} 1, & |e(k)| \leq e_0 \\ \frac{\bar{e} - x}{\bar{e} - e_0}, & e_0 < |e(k)| < \bar{e} \\ 0, & |e(k)| \geq \bar{e} \end{cases} \quad (9)$$

$$\hat{\phi}_c(k) = \hat{\phi}_c(k-1) + \frac{\eta \Delta u_{v,m,p}(k-1)}{\mu + \Delta u_{v,m,p}(k-1)^2} \times (\Delta y(k) - \hat{\phi}_c(k-1) \Delta u_{v,m,p}(k-1)) \quad (10)$$





**Figure 3.** Heading response without uncertain influence.

parameters of VIS\_MFAC\_PC is  $\lambda = 0.1, \mu = 100, \eta = 1, \rho = 0.5, k_p = 3, e_0 = 1, \bar{e} = 20$ . The heading is expected to be  $90^\circ$ . Heading response results of the two controllers are shown in Figure 3.

For the sake of the fairness of subsequent comparison, both controller parameters have been manually adjusted to better. It can be seen from Figure 3 that the response curves of PID and MFAC almost coincide with each other. The response time is about 30 s of the two controllers. The root mean square (RMS) from 30 s to 100 s of VIS\_MFAC\_PC method response error is  $0.86^\circ$  and the RMS of PID controller is  $0.56^\circ$ . The experimental results show that the two controllers have more consistent control performance without any disturbance.

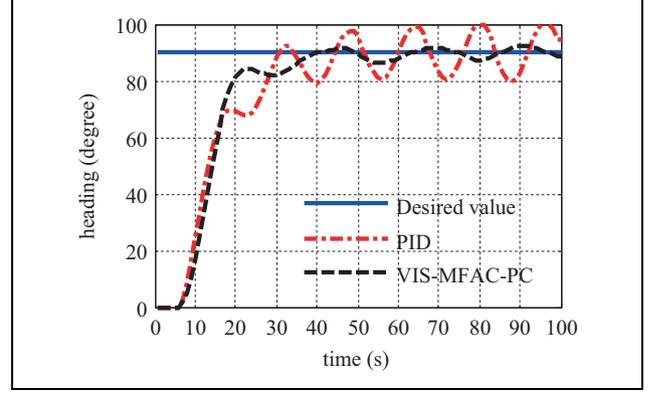
### Comparison experiments under uncertain influence

According to the theory of ship maneuverability, at the same time, the time delay characteristics of USV heading subsystem are also considered, the discrete mathematical motion model of the heading subsystem of USV can be expressed as

$$\begin{cases} \psi(k) = \psi(k-1) + \dot{\psi}(k) \times T_s \\ \dot{\psi}(k) = \dot{\psi}(k-1) + \ddot{\psi}(k) \times T_s \\ \ddot{\psi}(k) = (Ku(k-\tau) - \dot{\psi}(k))/T \end{cases} \quad (12)$$

where  $K$  and  $T$  are maneuver coefficients;  $T_s$  is sampling time;  $\tau$  is time delay constant for heading subsystem; and  $\psi(k)$ ,  $\dot{\psi}(k)$ , and  $\ddot{\psi}(k)$  represent heading angle, angular velocity, and angular acceleration of the system at the moment  $k$ , respectively.

Based on the identification of field test data, the heading maneuverability parameters of “Dolphin-IB” can be obtained as  $K = 0.186, T = 1.068$ . The initial state of the heading control subsystem, the control parameters, the expected heading, and so on are consistent with the last section. Considering model perturbation and system delay, the simulation results are as follows.



**Figure 4.** Heading response comparison of  $K$  exists 50% perturbation and heading subsystem has 2 s time delay.

The model parameter  $K$  exists 50% perturbation, that is, let  $K$  increases 50%, besides, USV heading subsystem has 2 s time delay. The test results are shown in Figure 4.

It can be seen from Figure 4, when the model parameter  $K$  increases 50% and USV heading subsystem has 2 s time delay, the actual heading of USV is seriously oscillated under the action of PID controller and it cannot converge to the desired heading, and the heading system has become unstable. Using VIS\_MFAC\_PC algorithm, the actual heading of USV can converge rapidly to desired heading even though there is a small fluctuation at the beginning. The USV heading subsystem can still maintain stability with almost no overshoot and oscillation. The RMS from 40 s to 100 s of VIS\_MFAC\_PC method response error is  $2.46^\circ$  while the RMS of PID controller is  $6.54^\circ$ .

Simulation results show that VIS\_MFAC\_PC algorithm has better robustness and stronger adaptability than PID when USV heading subsystem has large model perturbation and time delay.

### Outfield test and analysis

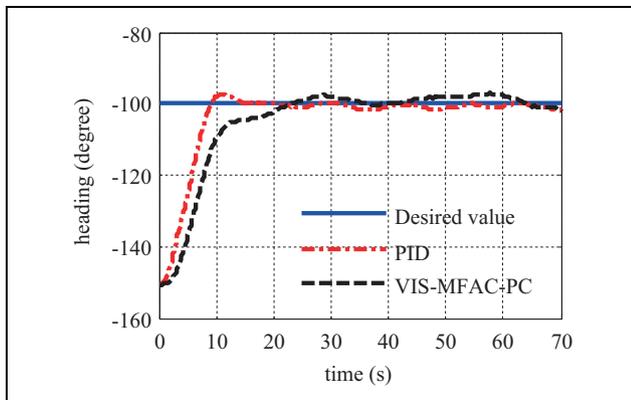
In order to further verify the robustness, adaptability, and practicability of the VIS\_MFAC\_PC method and promote engineering application, the proposed control method is applied to the USV of “Dolphin IB.” Experiments of USV heading control are shown in Figure 5.

Using VIS\_MFAC\_PC and PID algorithm to carry out field test, the USV speed is set 0.5 m/s at first. For the sake of the fairness of subsequent comparison, both controller parameters are manually adjusted to better. The controller parameters of VIS\_MFAC\_PC algorithm is  $\lambda = 3.0, \mu = 100, \eta = 1, \rho = 1, k_p = 1.2, e_0 = 5, \bar{e} = 30$ . The PID controller parameters is  $K_p = 3.0, K_I = 0.01, K_d = 1.4$  and expected heading is  $-100^\circ$ . The results of the experiments of the heading control under the action of the two controllers are shown in Figures 6 and 7.

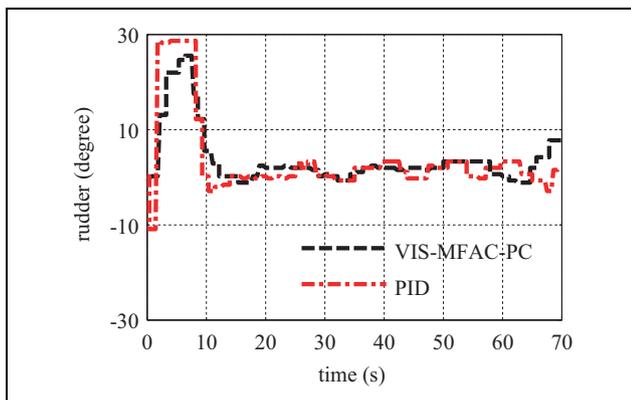
Keep the parameters of the two controllers unchanged, then set the USV speed at 1.2 m/s, and the desired heading



**Figure 5.** “Dolphin-IB” USV experiments. USV: unmanned surface vessel.



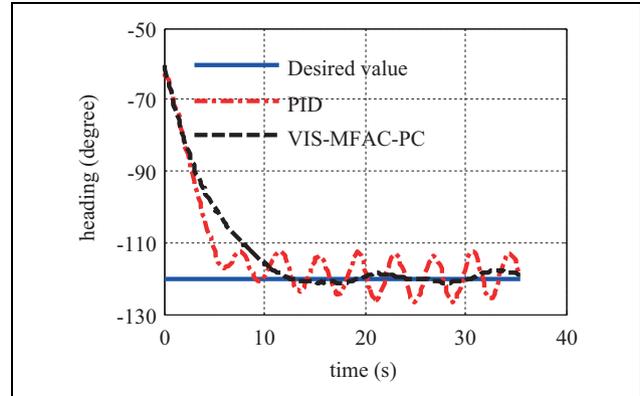
**Figure 6.** Heading response with USV speed is set at 0.5 m/s. USV: unmanned surface vessel.



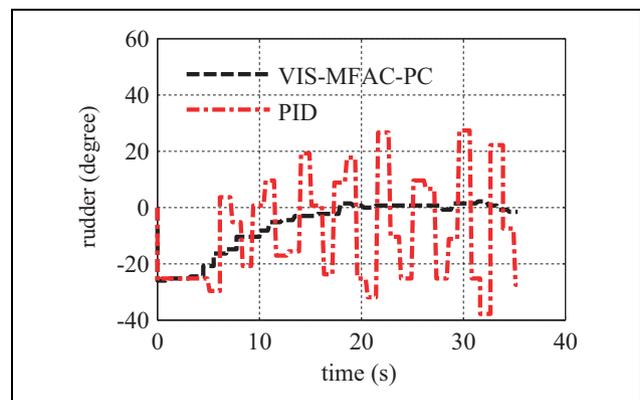
**Figure 7.** Rudder angle response with USV speed is set at 0.5 m/s. USV: unmanned surface vessel.

is  $-120^\circ$ . The results of the heading control test are shown in Figures 8 and 9.

As shown in Figures 6 and 7, when the USV speed is 0.5 m/s, the actual heading of “Dolphin IB” USV can converge to the desired heading under the action of the two controllers and almost no overshoot and concussion. The



**Figure 8.** Heading response with USV speed is set at 1.2 m/s. USV: unmanned surface vessel.



**Figure 9.** Rudder angle response with USV speed is set at 1.2 m/s. USV: unmanned surface vessel.

RMS from 20 s to 70 s of VIS\_MFAC\_PC controller response error is  $1.43^\circ$  while the RMS of PID controller is  $0.99^\circ$ .

According to Figures 8 and 9, after the USV speed is changed, the actual heading of USV is seriously oscillated under the action of PID controller and it cannot converge to the desired heading. The control performance is significantly deteriorated. In contrast, the VIS\_MFAC\_PC method ensures that the USV heading converges to the desired value without overshoot and no concussion, it still exhibits consistent dynamic performance. The RMS VIS\_MFAC\_PC controller response error is  $0.76^\circ$ , while the RMS of PID controller is  $4.57^\circ$ . Rudder angle error accumulation of PID and VIS\_MFAC\_PC controller from 10 s to 35 s is 2803 and  $163^\circ$ , respectively.

## Conclusion

Aiming at the USV heading control problem with uncertainties, proportional control and variable integral separation are combined with CFDL\_MFAC theory in the article. The following conclusions are obtained.

- (1) Through the analysis of CFDL\_MFAC method, the heading subsystem of USV will inevitably appear oscillation and instability, when rudder angle is directly controlled by this method to control the heading of USV.
- (2) The VIS\_MFAC\_PC method is proposed, which solves the limitation of the basic CFDL-MFAC method that does not apply to the USV heading control directly.
- (3) Simulation and field experiments show that compared with PID controller, VIS\_MFAC\_PC method is insensitive to uncertain factors such as model perturbation and system time delay and shows better performance.

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