

Figure 2- Identification of the force application point

According to the theory, we will start from the following formula:

$$OB^2 = OA^2 + OC^2 - 2 \cdot OA \cdot OC \cdot \sin 60^\circ$$

In the two pictures, we have the following information:

$O'C' = OC = \bar{F}$ , where F is the applied force.

$$O'A' = OA$$

Replacing in formula 1. The variables according to formulas 2 and 6, we obtain:

$$OB^2 = (coef \cdot OC \cdot \sin 60^\circ)^2 + OC^2 - 2 \cdot OA \cdot OC \cdot \cos 60^\circ$$

$$OB^2 = (coef \cdot OC \cdot \sin 60^\circ)^2 + OC^2 - 2 \cdot coef \cdot OC \cdot \sin 60^\circ \cdot OC \cdot \cos 60^\circ$$

$$OB^2 = coef^2 \cdot OC^2 \cdot \sin^2 60^\circ + OC^2 - 2 \cdot coef \cdot OC^2 \cdot \sin 60^\circ \cdot \cos 60^\circ$$

$$OB^2 = OC^2 (coef^2 \cdot \sin^2 60^\circ + 1 - 2 \cdot coef \cdot \sin 60^\circ \cdot \cos 60^\circ)$$

$$OB = OC \sqrt{0,2^2 \cdot 0,87^2 + 1 - 2 \cdot 0,2 \cdot 0,87 \cdot 0,5}$$

Base formula:

$$OB = OC \cdot 0,925,$$

We can conclude that the module of the resultant force represents 92,5 % of the module of the applied force.

Next we will study the decomposition of the resultant force into two components, one vertical and one horizontal, to determine the module of the force that acts directly on the dental slope (vertical component). From figure 1 we identify the following relation:

$$\frac{OV}{\sin \alpha} = OB, \Rightarrow$$

$$OV = OB \cdot \sin \alpha$$

In order to find the value of  $\alpha$ , we will find the value of  $\cos \alpha$ . In the BOC triangle:

$$\frac{BC}{\sin(90^\circ - \alpha)} = \frac{OB}{\sin 60^\circ}$$

We consider the friction coefficient  $coef = 0,2$ .

$$O'A' = coef \cdot O'B'$$

$$O'B' = O'C' \cdot \sin 60^\circ$$

Replacing in formula 4.  $O'B'$ .

According to the formula 5, we obtain:

$$O'A' = coef \cdot O'C' \cdot \sin 60^\circ,$$

and taking into consideration formula 3,

$$OA = coef \cdot OC \cdot \sin 60^\circ$$

$$\sin(90 - \alpha) = \frac{\sin 60 \cdot BC}{OB}$$

$$BC = OA$$

$$\sin(90 - \alpha) = \cos \alpha$$

$$\cos \alpha = \frac{\sin 60 \cdot OA}{OB}$$

$$\cos \alpha = \frac{\sin 60 \cdot coef \cdot O'C' \cdot \sin 60^\circ}{OC \cdot 0.925}$$

$$\cos \alpha = \frac{(\sin 60)^2 \cdot 0.2}{0.925} \Rightarrow \alpha = 80.67^\circ$$

$$\sin(80.67) = 0.98 \Rightarrow$$

$$OV = OB \cdot 0,98$$

The distribution of force on the support points of the deck will be inversely proportional to the distance between the point of its application and the extreme vicinity of the support.

To identify the point of application of force will study the figure 2 we have the following notations:

$l$  - distance between the tooth axis and the point of application of force

$a$  - length of the cusped slope

$$\frac{l}{\sin 60} = \frac{a/3}{\sin 90}$$

$$l = \frac{a}{3} \cdot \sin 60$$

## Results

Mean after which conducted the study are evaluated and accepted morphological measurements reported by specialty literature. The results are shown for each of the teeth engaged in the study.

For first premolar

Mesial-distal distance of 7 mm

Cusped slope of 3.25mm

The amount of force applied to the teeth is 15 kgf

The angle  $\alpha = 60$

$$OB_{pm1} = OC_{pm1} \cdot 0,925$$

$$\Rightarrow OB_{pm1} = 13,875$$

$$F_{pm1} = OB_{pm1} \cdot 0.98$$

$$\Rightarrow F_{pm1} = 13.59$$

$$l_{pm1} = \frac{3.25}{3} \cdot \sin 60$$

$$\Rightarrow l_{pm1} = 0.94$$

For second premolars

Mesial-distal distance of 7mm

Cusped slope of 4 mm

The amount of force applied to the teeth is 15 kgf

The angle  $\alpha = 60$

$$OB_{pm2} = OC_{pm2} \cdot 0,925$$

$$\Rightarrow OB_{pm2} = 13,875$$

$$F_{pm2} = OB_{pm2} \cdot 0.98$$

$$\Rightarrow F_{pm2} = 13.59$$

$$l_{pm2} = \frac{4}{3} \cdot \sin 60$$

$$\Rightarrow l_{pm2} = 1.15$$

For first molar

Mesial-distal distance of 9mm

Cusped slope of 4.5 mm

The amount of force applied to the teeth is 19 kgf

The angle  $\alpha = 60$

$$OB_{m1} = OC_{m1} \cdot 0,925$$

$$\Rightarrow OB_{m1} = 17.575$$

$$F_{m1} = OB_{m1} \cdot 0.98$$

$$\Rightarrow F_{m1} = 17.22$$

$$l_{m1} = \frac{4.5}{3} \cdot \sin 60$$

$$\Rightarrow l_{m1} = 1.29$$

For second molar

Mesial-distal distance of 10.5mm

Cusped slope 5mm

The amount of force applied to the teeth is 19 kgf.

The angle  $\alpha = 60^0$

$$OB_{m2} = OC_{m2} \cdot 0,925$$

$$\Rightarrow OB_{m2} = 17.575$$

$$F_{m2} = OB_{m2} \cdot 0.98$$

$$\Rightarrow F_{m2} = 17.22$$

$$l_{m2} = \frac{5}{3} \cdot \sin 60$$

$$\Rightarrow l_{m2} = 1.44$$

For third molar

Mesial-distal distance of 10mm

Cusped slope of 4.5 mm

The amount of force applied to the teeth is 21 kgf

$$OB_{m3} = OC_{m3} \cdot 0,925$$

$$\Rightarrow OB_{m3} = 19.425$$

$$F_{m3} = OB_{m3} \cdot 0.98 \Rightarrow F_{m3} = 19.03$$

$$l_{m3} = \frac{4.5}{3} \cdot \sin 60 \Rightarrow l_{m3} = 1.29$$

The study of the established clinical situations by the original protocol are shown in Figure 3.

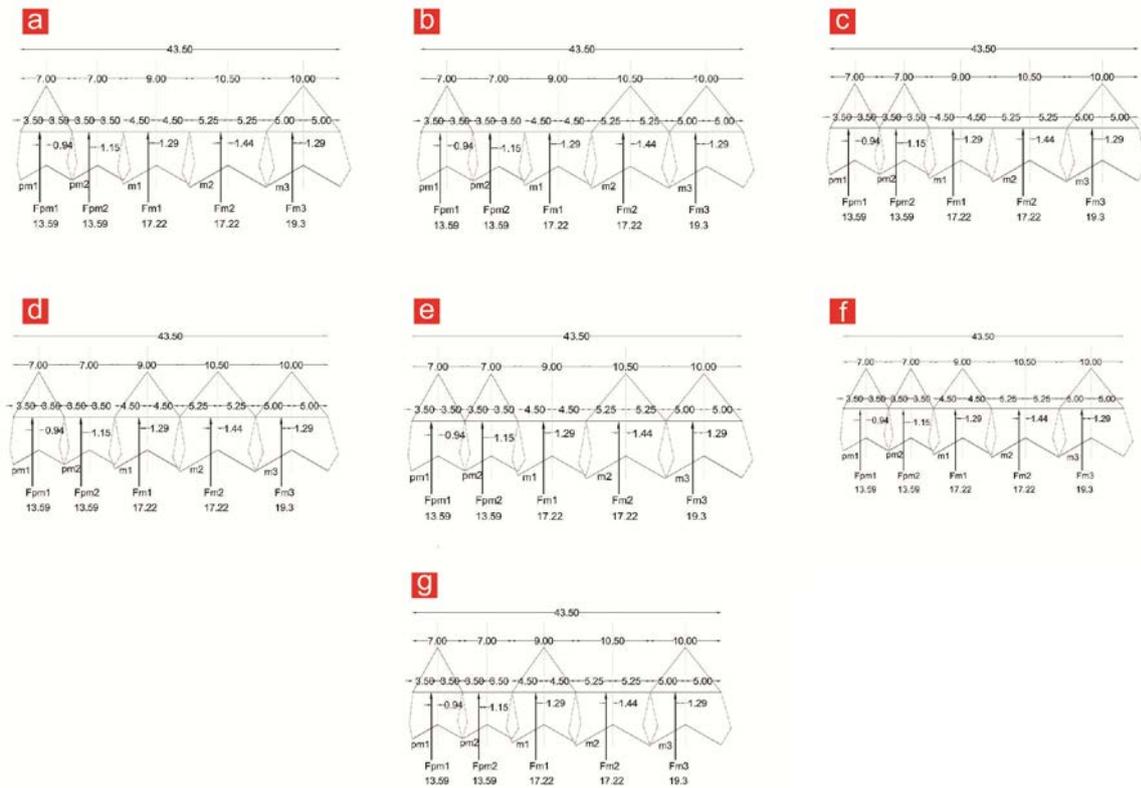


Figure 3- Edentulous interlaced versions accepted in the study

Situation 1.

The bridge has as a pillar teeth the premolar 1 and molar 3

The toothless gap is given by the premolar 2, molar 1 and molar 2:

The force supported by premolar 1 is equal to:  $FT_{pm1}=43,43$

The force supported by molar 3 is equal to:  $FT_{m3}=37,48$

b.Situation 2

The bridge has as a pillar teeth the premolar 1 and molar 2

The toothless gap is given by the premolar 2 and molar 1:

The force supported by premolar 1 is equal to:  $FT_{pm1} = 31,41$

The force supported by molar 2 is equal to:  $FT_{m2}= 30,21$

c. Situation 3

The bridge has as a pillar teeth the premolar 2 and molar 3

The toothless gap is given by the molar 1 and molar 2

The force supported by premolar 2 is equal to:  $FT_{pm2} = 33,87$

The force supported by molar 3 is equal to:  $FT_{m3}= 33,46$

d. Situation 4

The bridge has as a pillar teeth the premolar 1 and molar 1

The toothless gap is given by the premolar 2

The force supported by premolar 1 is equal to:  $FT_{pm1} = 22,86$

The force supported by molar 1 is equal to:  $FT_{m1}= 21,54$

e. Situation 5

The bridge has as a pillar teeth the premolar 2 and molar 2  
 The toothless gap is given by the molar 1

The force supported by premolar 2 is equal to:  $FT_{pm2} = 24,66$   
 The force supported by molar 2 is equal to:  $FT_{m2} = 23,37$

f. Situation 6

The bridge has as a pillar teeth the molar 1 and molar 3  
 The toothless gap is given by molar 2

The force supported by molar 1 is equal to:  $FT_{m1} = 28,19$   
 The force supported by molar 3 is equal to:  $FT_{m3} = 25,55$

g. Situation 7

The bridge has as a pillar teeth the premolar 1, molar 1 and molar 3  
 The toothless gap is given by the premolar 2 and molar 2

The force supported by molar 1 is equal to:  $FT_{m1} = 22,86$   
 The force supported by molar 1 is equal to:  $FT_{m1} = 32,75$   
 The force supported by molar 3 is equal to:  $FT_{m3} = 25,55$

Based on the maximum values of the vertical pressure supported by the teeth and periodontal (premolar I - 44 kg, premolar II - 44 kg, mol I - 45-70 kg, molar II - 45-70 kg, molar III - 64 kg) and taking into account that in chewing there are commonly used about 1/3 of the maximum force values we calculated the vertical forces supported by pillar teeth in the possible situations of conjunct restoration for maxillary lateral area.

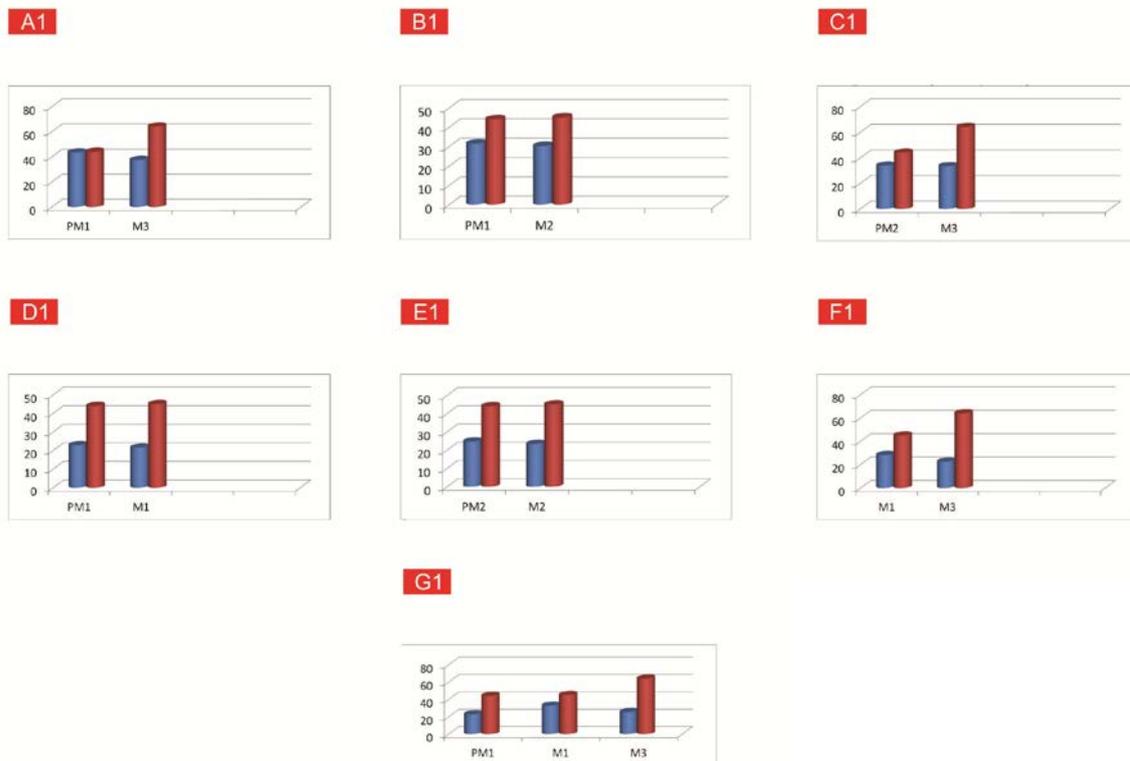


Figure 4- The forces exerted on the bridge abutments in clinical situations set to be studied

A1. In situation 1 when we have 14 X X X 18 - The force supported by the premolar 1 is 43,43 kgf, lower than the maximum support capacity of the tooth =44 kgf and the force supported by the molar 3 is equal to 37.48 kgf when the maximum support capacity of the tooth is = 64 kgf.

B1. In situation 2 when we have 14 X X 17 18 - The force supported by the premolar 1 is 31,41 kgf, lower than the maximum support capacity of the tooth = 44 kgf and the force supported by the molar 2 is equal to molar 3 equal to 37,48 kgf when the maximum support capacity of the tooth is 64 kgf.

C1. In situation 3 when we have 14 15 X X 18 - The force supported by the premolar 2 is 33,87 kgf, lower than the maximum support capacity of the tooth =44 kgf and the force supported by the molar 3 is equal to 33,46 kgf when the maximum support capacity of the tooth is 64 kgf.

D1. In situation 4 when we have 14 X 16 17 18 - The force supported by the premolar 1 =22,86 kgf lower than the maximum support of the tooth =44 kgf and force supported by molar 3 is equal to 21,54 kgf when the maximum support capacity of the tooth is 45-70 kgf.

E1. In situation 5 when we have 14 15 X 17 18 - The force supported by the premolar 2 = 24,66 kgf is lower than the maximum support capacity of the tooth= 44 kgf and the force supported by the molar 2 is equal to 23,37 kgf when the maximum support capacity of the tooth is 45-70 kgf.

F1. In situation 6 when we have 14 15 16 X 18 - The force supported by the molar 1 de 28,19 kgf is lower than the maximum support capacity of the tooth =45-70 kgf and the force supported by molar 3 is equal to 25,55 kgf when the maximum support capacity of the tooth is 64 kgf.

G1. In situation 7 when we have 14 X 16 X 18 - The force supported by the premolar 1 = 22, 86 kgf is lower than the maximum support capacity of the tooth =44 kgf, the force supported by the molar 1 is equal to 32,75 kgf when the force supported by the molar 3 is equal to 45-70 kgf and the force supported by the molar 3 is equal to 25,55 kgf when the

maximum support capacity of the tooth is 64 kgf.

## Discussions

In a normal mastication in all the cases of conjoint prosthetic the cumulative values of the vertical forces given by the artificial teeth can be supported by the pillar teeth [5,6].

In situation number 1 in a normal mastication when we as pillars the premolar1 and the molar 3, and toothless gap is given by premolar 2, molar 1 and molar 2, vertical forces given by toothless gap that are transmitted in the long axis of the premolar1(one pillar tooth) are very close to its maximum capacity support (43,43 kgf capacity calculated  $\leq$  44 kgf maximum capacity)which leads to the idea that the treatment option is a mistake. Since the study was done in the case of medium mastication in a clinical situation the possibility of adding another pillar tooth is taken into consideration. Morphology prosthesis also requires a reduction in the height and slope inclination cuspidiene while shaping a body of deck width buccolingually reduced. Occlusal rebalancing is a mandatory step that contributes to integration biological dental bridge.

The other situations may represent prosthetic solutions with the condition that the occlusal morphology allow the dispers of the horizontal, vertical and oblique components given by a force acting on this surface [7,8].

## Conclusion

The understanding of the occlusal morphology as a variable and ready to be improved support in making prosthesis can balance and harmonize the forces that can act at this level.

## Acknowledgements

All authors contributed equally to this study.

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