

## *Full Length Research Paper*

# **An efficient quantum-dot cellular automata full-adder**

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**The most important mathematical operation is addition. Other operations such as subtraction, multiplication and division are usually implemented by adders. An efficient adder can be of great assistance in designing arithmetic circuits. QCA is a promising technology which seems to be a good candidate for the next generation of digital systems. So, an efficient QCA full-adder will facilitate creating QCA computational and arithmetic systems. In this paper, two high performances QCA full-adders are presented. They have a very dense structure and constructed using new kinds of five-input majority gates. One of the proposed designs has a robust structure. In this design the presented design rules for constructing a robust QCA circuit have been considered. In contrast to the previous designs constructed using a five-input majority gate, in the proposed QCA full-adders the outputs come out from the same side of the circuit. Also, the input and output signals are not surrounded by the other cells and can easily be accessed. The proposed robust QCA full-adder dominates all the previous robust designs in terms of area, delay and complexity. Using this design, ripple carry adders with different word sizes (that is, 4, 8 and 16) are constructed. In this paper, QCA designer, a common QCA layout design and verification tool is employed to verify and simulate the proposed five-input majority gates and QCA full-adders.**

**Key words:** Quantum-dot cellular automata, full-adder, five-input majority gate, robustness, ripple carry adder.

## **INTRODUCTION**

The technology of semiconductor fabrication has been changed rapidly in the last decades but some applications require less power and more speed. There is a paradox in CMOS technology: the speed is not gained unless more power is consumed and if the power is reduced to save energy it results in speed reduction. Therefore, the designers prefer to use new technologies based on nanoelectronics instead of CMOS such as carbon nanotube field effect transistors (CNFET) and quantum-dot cellular automata (QCA). With these new technologies more integration and speed as well as less power consumption are achieved. Carbon nanotube field effect transistor (CNFET) (Dresselhaus et al., 2001) is same as CMOS in many aspects and could be replaced in most applications. CNFET has more compaction and consumes less power, but a quantum-dot cellular

automata is completely different from conventional CMOS technology. It consumes less power due to its specification which is hidden in a QCA cell structure.

QCA cells as well as, the circuits utilizing them have been fully fabricated and tested by researchers (Kummamuru et al., 2003; Orlov et al., 2003; Timler and Lent, 2003). Several studies have been performed towards implementation of molecular QCA structures which can operate at room temperature (Hu et al., 2005; Lent et al., 2003; Srivastava and Bhanja, 2007). Some of the other researchers such as (Bonyadi et al., 2007; Cho and Swartzlander, 2007, 2009; Cho, 2006; Hänninen and Takala, 2010; Hashemi et al., 2008; Kim et al., 2005, 2007; Navi et al., 2010a, b; Rahimi et al., 2007; Sayedsalehi et al., 2010; Tougaw and Lent, 1994; Vankamamidi et al., 2005; Vassilios and Ioannis, 2010; Vetteth et al., 2002; Wang et al., 2003; Zhang et al., 2004, 2005) have focused on designing efficient QCA circuits. In (Hashemi et al., 2008; Vassilios and Ioannis, 2010) efficient designs for QCA multiplexers have been presented. (Hashemi et al., 2008) introduces an efficient

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and robust 2:1 QCA multiplexer layout. This layout is implemented using the multilayer QCA wire crossing scheme. In (Vassilios and Ioannis, 2010) a 2:1 QCA multiplexer constructed using the coplanar wire crossing scheme is introduced which can be a useful component in designing  $2^n$  to 1 QCA multiplexers. Designing efficient QCA memory cells is one of the attractive fields in QCA. Line based and loop based structures generally are used to design a QCA memory cell. In (Vankamamidi et al., 2005) a novel QCA line based parallel memory has been introduced. Some of the other previous researches (Kim et al., 2005, 2007) have been focused on designing robust QCA circuits. In (Kim et al., 2005, 2007) some design rules for constructing a robust majority gate and coplanar wire crossing scheme against sneak noise paths have been introduced. Reduction of the number of QCA majority gates and optimization of QCA circuits is another attractive field in QCA. In some of the previous studies (Bonyadi et al., 2007; Zhang et al., 2004) required methods for QCA circuit optimization are investigated.

Adders are one of the basic components in designing arithmetic circuits like residue number systems and alike (Mollahosseini et al., 2010; Timarchi and Navi, 2009), therefore designing a robust, dense and simple full-adder is of great importance (Navi et al., 2009a, b). To date, several studies have been done on QCA adder designs (Cho and Swartzlander, 2007, 2009; Cho, 2006; Hänninen and Takala, 2010; Kim et al., 2007; Navi et al., 2010a, b; Rahimi et al., 2007; Sayedsalehi et al., 2010; Tougaw and Lent, 1994; Vetteth et al., 2002; Wang et al., 2003; Zhang et al., 2005). The first QCA full-adder design was presented in (Tougaw and Lent, 1994). This design is constructed using five three-input majority gates and three inverters. Another QCA full-adder using the same logical structure was introduced in (Vetteth et al., 2002). This design in contrast to the first design incorporates QCA clocking scheme. A simpler QCA full-adder was presented in (Wang et al., 2003). This full-adder is composed of three three-input majority gates and two inverters. Using this design, different layouts for a QCA full-adder have been presented to date (Cho and Swartzlander, 2007, 2009; Cho, 2006; Hänninen and Takala, 2010; Kim et al., 2007; Zhang et al., 2005). These layouts are different in terms of area, delay and number of QCA cells (complexity). In (Hänninen and Takala, 2010; Kim et al., 2007) robust QCA full-adders have been introduced. These designs have a more robust structure against sneak noise paths. Recently, a novel QCA full-adder design was introduced (Rahimi et al., 2007). This design is composed of one three-input majority gate, one inverter and a new kind of majority gates: a five-input voter. This study also presents an unconventional form of QCA cells. Based on the presented design in (Rahimi et al., 2007) different QCA full-adders have been introduced (Sayedsalehi et al., 2010, Navi et al., 2010 a, b). These designs are different in terms of area, number of QCA cells (complexity) and

delay.

As mentioned earlier, some of the previous studies have been performed towards implementation of QCA cells, while some have been done on designing efficient QCA circuits. In this study, two new efficient QCA full-adders are presented. The manufacturing concepts are out of scope of this paper. In order to design efficient QCA full-adders, two new five-input majority gates constructed using ordinary QCA cells are introduced. It is worth mentioning that, one of the proposed five-input majority gates and QCA full-adder constructed using this component have a robust structure. In these structures, the presented design rules for constructing a robust QCA circuit have been considered (Kim et al., 2005, 2007). Simulation results reveal that the proposed QCA full-adders have a very dense structure. In these designs, the input and output signals are not surrounded by the other cells. The outputs come out from the same side of the circuit and can easily be accessed. Regarding the reliable structure of the robust QCA full-adder, it is used to design ripple carry adders with different word sizes (that is, 4, 8 and 16). Simulation results show that these designs lead to significant improvements in terms of area; delay and complexity in comparison to the constructed ripple carry adders with the previous best design (Hänninen and Takala, 2010).

## QUANTUM-DOT CELLULAR AUTOMATA

Quantum-dot is a potential hole which can arrest electrons, because electrons are unable to overcome their barrier and jump out side of the dot. The diameter of each dot is small enough to make its charging energy greater than  $k_B T$ , where  $k_B$  indicates the Boltzmann's constant and  $T$  is the operating temperature (Niemier, 2004). A QCA cell can be realized with semiconductor, metal, magnets and molecules. At first the metal-island implementation was used to demonstrate the concept of QCA (Amlani et al., 2000; Orlov et al., 1998; Toth and Lent, 1999). In this method, quantum dots are implemented using aluminum islands. In the semi conductor (or solid state) QCA implementation, (Single et al., 2000) QCA devices can potentially be implemented with the same highly advanced semiconductor fabrication processes which are used to implement CMOS devices (Smith et al., 2003). In this implementation, quantum dots are created from standard semi conductive materials such as InAs/GaAs (Suraprapapich et al., 2007) and GaAs/AlGaAs (Gardelis et al., 2003; Perez-Martinez et al., 2007). In molecular QCA (Lent et al., 2003; Li et al., 2001; Lieberman et al., 2002; Lu et al., 2007), the basic cell is a pair of identical molecules (Lent et al., 2003). The molecular devices can operate at room temperature and have a very high density. In magnetic QCA, a nano magnet is the basic cell (Haque et al., 2004). Cowburn and Wellands nanodot QCA Automata (Cowburn and

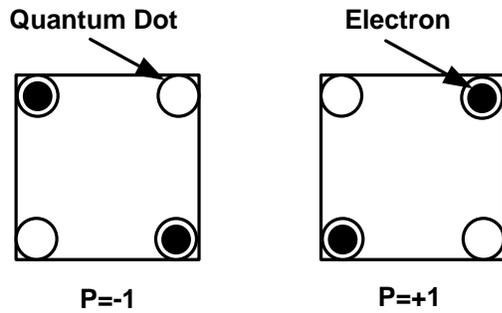


Figure 1. Illustration of a QCA cell's logic states.

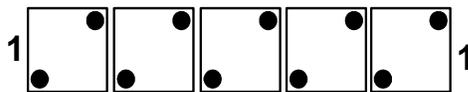


Figure 2. Signal propagation in a QCA Wire.

Welland, 2000), Parish and Forshaws Bi-stable Magnetic QCA (Parish and Forshaw, 2003, 2004) and field couple nanomagnets (Csaba et al., 2002, 2004) are the popular schemes of the magnetic QCA. The advantages and disadvantages of the presented materials (semiconductor, metal, magnets and molecules) have been investigated in (Srivastava, 2007).

In this study, a four-dot cell model is considered and a set of four quantum-dots in a square shaped arrangement is called a QCA cell, where there are only two excess electrons. In a QCA cell, the most important force which affects the electrons is coulumbic repulsion. So, the electrons always pose diagonally in the square to increase their distance and take the farthest position from each other to minimize the total system's energy. It is obvious that the electrons never stay on the same side of the square since they cannot maximize their distance. A QCA cell has two diagonal states: when the electrons are on the cell's main diagonal, they represent the logic "1" and the other diagonal shows the logic "0" (Figure 1).

A QCA wire could be made by arranging some QCA cells in a line. When two cells are close together, their electrons force each other and try to get minimum energy. The system energy would be minimized only when the cells' states are the same. In other words, when the first cell has a specific value, it copies its value to the neighbor cell and so on. Hence the signal could propagate through the line of cells and they work like a wire as shown in Figure 2.

Basic logic elements in QCA are inverters and three-input majority gates. A three-input majority gate has three inputs, one voter cell and one output. The voter state is determined according to the input cells' states. If most of them have status "1", the voter takes "1" and if the most inputs have "0", voter sends "0" to the output (Figure 3a).

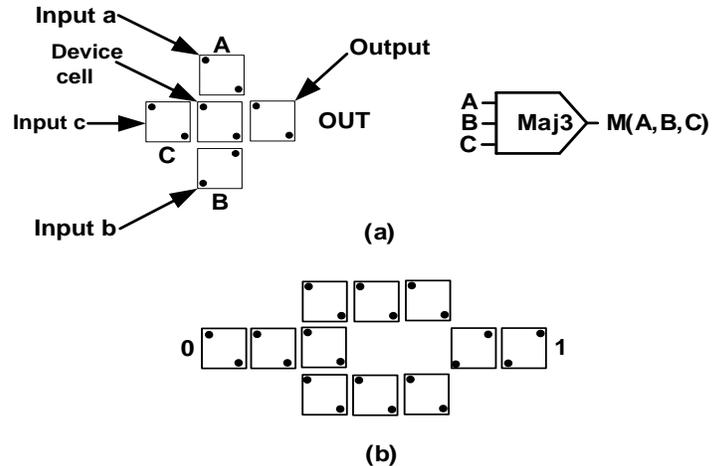


Figure 3. (a) A QCA majority gate (b) Illustration of a QCA inverter.

When an input of a majority gate is always "1", an "OR" gate is made (Equation 1). An "AND" gate is also made when an input is stuck at "0" as shown in Equation 2. The inverter has a very simple structure. As shown in Figure 3 (b) it can be implemented using 11 QCA cells:

$$Maj(A, B, 1) = A + B \quad (1)$$

$$Maj(A, B, 0) = A \cdot B \quad (2)$$

A QCA clocking zone is a group of QCA cells which are controlled by a same QCA clock. In QCA, four clocking zones are considered. The schematic of a QCA wire constructed using four clocking zones are shown in Figure 4a. It is worth mentioning that there is a  $90^\circ$  phase delay from one clocking zone to the next one as shown in Figure 4b. In (Kim et al., 2005, 2007), suitable QCA clock assignments to make a functional QCA three-input majority gate and coplanar wire crossing scheme are introduced. Using these clocking rules, a more reliable QCA circuit against sneak noise paths is achieved. The schematics of a robust majority gate and coplanar wire crossing scheme is shown in Figure 5a and b. As shown in Figure 5a, three different clocking zones are required to make a functional majority gate. Based on this figure, it is clear that in a robust majority gate, the input signals are positioned at the first clocking zone. In order to synchronize the affect of the input signals on the device cell, the middle QCA cells are positioned at the second clocking zone. Finally, the result is transmitted using QCA cells which are positioned at the third clocking zone. Based on Figure 5b, it is clear that two QCA clocking zones with  $90^\circ$  phase delay are required to implement a robust coplanar wire crossing scheme.

## MATERIALS AND METHODS

Here, previous QCA five-input majority gates as well as two new

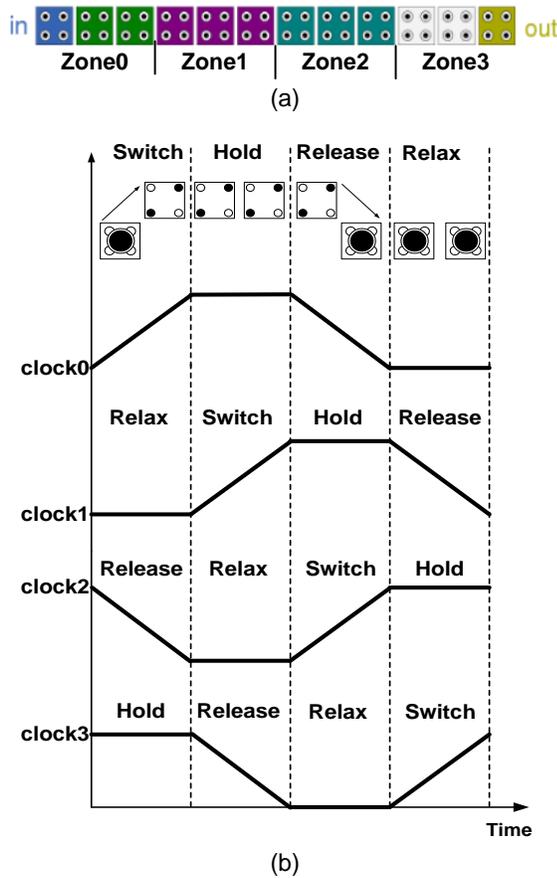


Figure 4. (a) A QCA wire with four clocking zones (b) QCA clocks wave forms.

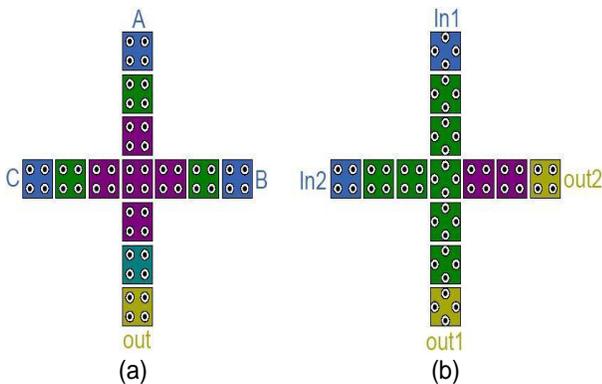


Figure 5. (a) A robust QCA majority gate (b) a robust coplanar crossing scheme constructed using the presented design rules in (Kim et al., 2005; Kim et al., 2007).

designs are introduced. Previous QCA full-adder designs are presented subsequently. Using the new five-input majority gates, two new QCA full-adders are introduced. The robust QCA full-adder will be used to construct ripple carry adders with different word sizes.

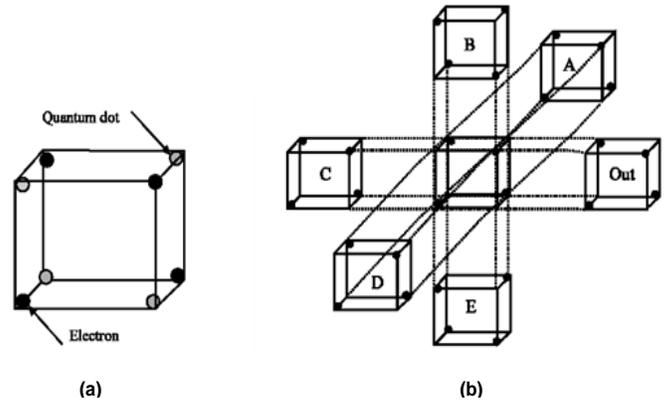


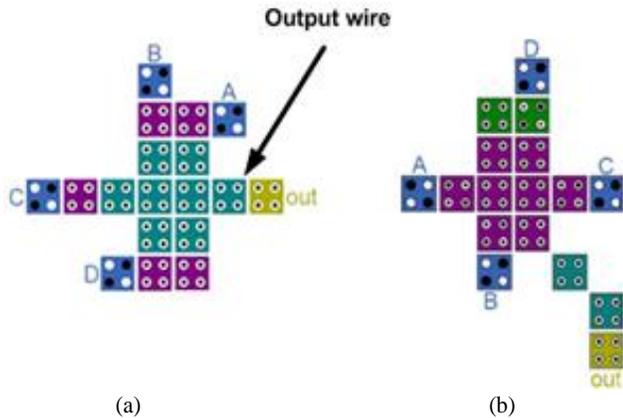
Figure 6. (a) a 3D QCA cell (b) a five-input majority gate presented in (Rahimi et al., 2007).

### FIVE-INPUT MAJORITY GATES

A three-input majority gate was introduced previously. Only one implementation has been presented for a three-input majority gate to date, but a five-input majority gate can be implemented using several designs. The first design for a five-input majority gate was introduced in Rahimi et al. (2007). This design is based on a three dimensional (3D) QCA cell. A 3D QCA cell is like a cube which has eight quantum dots on its corners where four surplus electrons are trapped (Figure 6a). The schematic of the presented five-input majority gate (Rahimi et al., 2007) is shown in Figure 6b. However, owing to some problems in simulation and physical implementation of 3D QCA cells in comparison to the classic ones, this design seemed not to be appropriate, at least at present.

Another QCA five-input majority gate was introduced in (Navi et al., 2010a). In contrast to the previous structure (presented in Figure 6), this design is implemented using ordinary QCA cells. In this design, the inputs do not have the same effect on the output. One of the inputs affects the output from one path but the other inputs affect the output in two ways. Also, in this design the output is surrounded by the input QCA cells and it cannot easily be accessed. Regarding the position of the output signal, this design is not so practical to implement larger QCA circuits. Navi et al. (2010b) presents another QCA five-input majority gate. This design is same as the previous structure (Navi et al., 2010a) is constructed using ordinary QCA cells. In this design, in contrast to the previous design (Navi et al., 2010a), the output is not surrounded by the other cells and therefore, it can easily be accessed. In other words, this structure does not need any wire crossover to transmit the output signal. Therefore the output signal can easily be used as the input of the other QCA circuits. Using this five-input majority gate a QCA full-adder is presented in (Navi et al., 2010b).

Subsequently, two QCA five-input majority gates are introduced. In one of these designs, the presented QCA clocking rules for constructing a robust majority gate (Figure 5a) have been considered and it has a robust structure. These designs are shown in Figure 7a and b. In the proposed designs, the inputs are shown by A, B, C and D. Based on Figure 7, it is clear that the value of the input D has been used as the two inputs of the proposed five-input majority gates. Therefore, these designs are suitable for implementing QCA full-adders which are constructed using three and five-input majority gates and inverters. In these full-adders the inversion of the carry value is used as the two inputs of the five-input majority gate (Rahimi et al., 2007). The first design is shown in Figure 7a. As shown in this figure, the output signal is not



**Figure 7.** Illustration of the proposed five-input majority gates (a) the first design (b) The second design with considering the design rules presented in (Kim et al., 2005, 2007).

surrounded by other cells. Therefore, this structure doesn't need any QCA wire crossover to transmit the output signal and this value can easily be used as the input of the other QCA circuits. In this structure, the seven middle QCA cells are device cells which produce the output. As shown in Figure 7a, the input QCA cells are positioned at the first clocking zone, while the middle QCA cells and the output wire is positioned at the second clocking zone. It is clear that there is a  $90^\circ$  phase delay between these clocking zones. The second design is shown in Figure 7b. In this design, the presented design rules for constructing a robust majority gate (Kim et al., 2005, 2007) have been considered. As shown in this figure, the inputs are positioned at the first clocking zone. The eight middle QCA cells (device cells) which make the five-input majority gate value are positioned at the second clocking zone and the output is transmitted using QCA cells which are positioned at the third clocking zone. Based on this figure, it is clear that there is a  $90^\circ$  phase delay between one clocking zones to the next one. Also, in this design two diagonally positioned QCA cells are used in the output. The first one transmits the inversion value of the five-input majority gate. This QCA cell is positioned diagonally to maximize the distance between the input and output QCA cells. Simulation results demonstrate that this reduces the noise effect and produces the inversion of the five-input majority gate. As shown in Figure 7b, the final value is produced using the second diagonally positioned QCA cell.

In this study, the proposed five-input majority gates were simulated using QCA Designer (Walus et al., 2004) version 2.0.3. In these simulations, both bi-stable and coherence vector engines (QCA designer documentation) were used to simulate the proposed designs. It is worth mentioning that these simulations were done using the default parameters of both simulation engines (QCA designer documentation) and using both engines, same results were achieved which shows the accuracy of the proposed designs. The simulation result of the proposed designs is shown in Figure 8. As shown in this figure, the output is valid after the first falling edge of the clock2.

## PREVIOUS QCA FULL-ADDER DESIGNS

Various QCA full-adders have been presented to date. The first one (presented in 1994) is composed of five three-input majority gates and three inverters (Tougaw and Lent, 1994). The schematic of this design is shown in Figure 9. This full-adder uses QCA coplanar wire

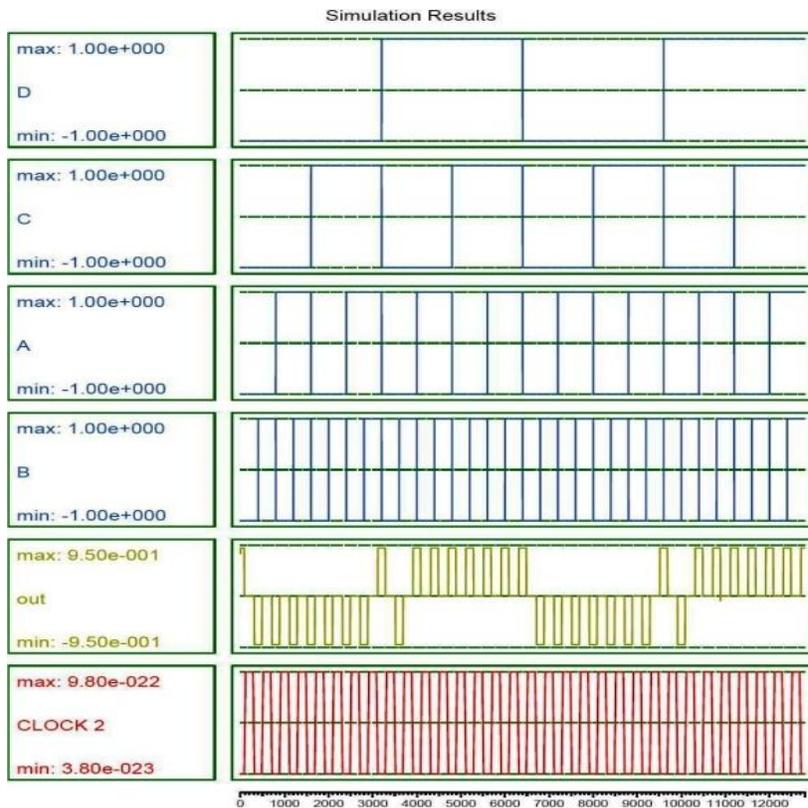
crossing scheme. It is implemented in one layer using 192 QCA cells. In this design QCA clocking concepts are not considered. In Vetteth et al. (2002) another QCA full-adder using the same logical structure and coplanar wire crossing scheme is presented. In contrast to the previous design, this full-adder incorporates QCA clocking scheme and takes 14 clock phases (3.5 clock cycles) to generate outputs. This full-adder was used in designing a 4-bit CLA (Vetteth et al., 2002).

A simpler QCA full-adder is presented in (Wang et al., 2003). This full-adder is composed of three three-input majority gates and two inverters (Wang et al., 2003). It uses QCA coplanar wire crossing scheme and takes 5 clock phases (1.25 clock cycles) to produce outputs. Hence, it is faster than presented design in (Vetteth et al., 2002). The schematic of this full-adder is shown in Figure 10. Different layouts for this schematic have been presented to date (Cho and Swartzlander, 2007, 2009; Cho, 2006; Hänninen and Takala, 2010; Kim et al., 2007; Zhang et al., 2005). The presented QCA full-adder in (Zhang et al., 2005) utilizes QCA multilayer wire crossing scheme and is simpler than previous design (Wang et al., 2003) in terms of cell count. It produces outputs in 4 clock phases (1 clock cycles); hence, it is faster than the previous designs. In the study of Cho and Swartzlander (2007) another QCA full-adder using the same logical structure and multilayer wire crossing scheme is presented. It takes 5 clock phases (1.25 clock cycles) to produce outputs. This full-adder was used to implement three kinds of adders (Ripple carry adder, carry look ahead adder and conditional sum adder) with large word sizes (Cho and Swartzlander, 2007). These adders were compared in terms of area, complexity (cell count) and delay (Cho and Swartzlander, 2007). Two other QCA full-adders (presented as Type I and II) using five gates (three majority gates and two inverters) are introduced in (Cho, 2006). These designs utilize QCA multilayer wire crossing scheme. The presented adder as Type II is more efficient in designing large adder circuits (Cho and Swartzlander, 2009; Cho, 2006). It is constructed using 86 QCA cells and takes only 3 clock phases (0.75 clock cycles) to produce outputs. This full-adder dominates all the previous designs in terms of area, complexity (cell count) and delay. In Hänninen and Takala (2010); Kim et al. (2007) robust QCA full-adders are presented. These designs use the coplanar wire crossing scheme for crossover wires. The presented design in (Hänninen and Takala, 2010) surpasses the presented design in (Kim et al., 2007) in terms of area, delay and complexity (cell count).

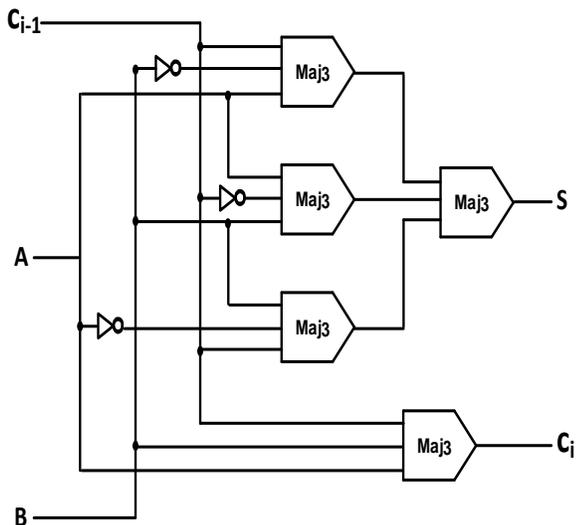
Another QCA full-adder design is presented in (Rahimi et al., 2007). This adder is constructed using unconventional form of QCA cells. It is composed of two majority gates and one inverter. In this design in contrast to the previous structures, implemented using three-input majority gates, one of the majority gates is a five-input voter. The schematic of this full-adder is shown in Figure 11. In order to implement this schematic, a cubic design for QCA cells is presented in (Rahimi et al., 2007). This cubic cell has six sides and can be used to implement a five-input majority gate (Rahimi et al., 2007).

Other QCA full-adders based on the presented schematic in Figure 11 have been introduced to date (Navi et al., 2010a, b; Sayedsalehi et al., 2010). These designs in contrast to the presented design in (Rahimi et al., 2007) are implemented using ordinary QCA cells. The layouts of the proposed designs are slightly different from the basic design (Rahimi et al., 2007). These designs use the multilayer wire crossing scheme for crossover wires and are implemented in three layers.

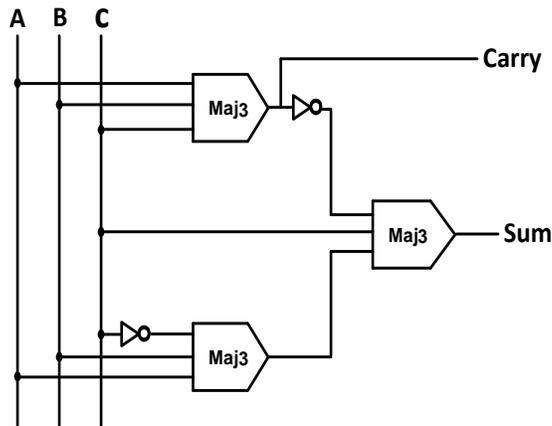
Although, the proposed designs in (Navi et al., 2010a, b) dominate the previous QCA full-adders in terms of area and complexity (cell count) and have an equal latency with the best previous designs (the QCA full-adders presented in (Cho and Swartzlander, 2009; Cho, 2006)) they are not suitable components for implementing larger QCA circuits. In these designs, the sum value comes out from the right while the carry out value comes out



**Figure 8.** The simulation results of the proposed five-input majority gates in Figure 7.



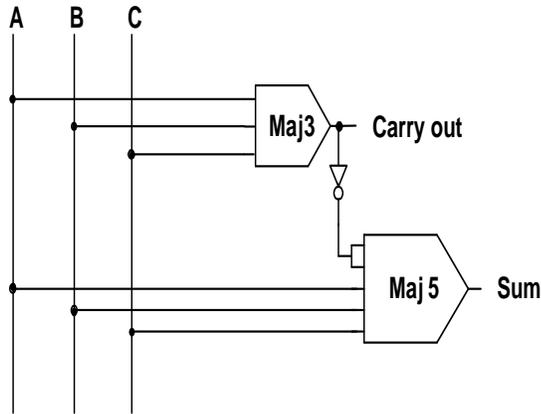
**Figure 9.** The QCA full-adder schematic presented in (Tougaw and Lent, 1994).



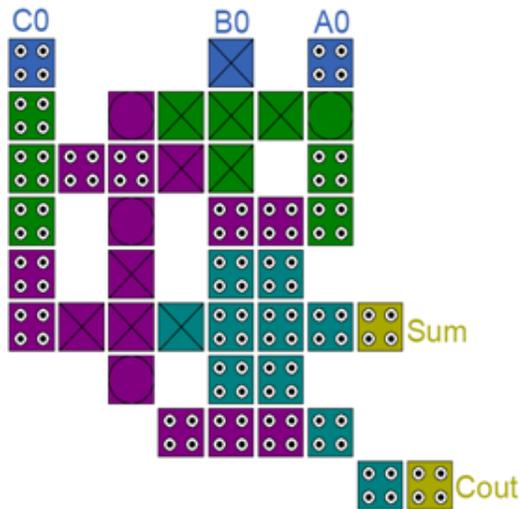
**Figure 10.** The QCA full-adder schematic presented in (Wang et al., 2003).

from the left side of the QCA full-adder. Therefore, if the outputs of the proposed full-adders are used as the inputs of the other circuits, some extra wiring will be required, which increases the area and complexity (cell count) of the total design. Also, in the proposed

designs (Navi et al., 2010a, b) the input signals are positioned in the middle of the QCA full-adder layout and cannot easily be accessed. In the presented design in (Navi et al., 2010a) the output of the full-adder is also surrounded by the other cells. Regarding these constraints, the proposed designs (Navi et al., 2010a, b) are not so practical to implement larger QCA circuits. Recently, using the five-input majority gates presented in (Navi et al., 2010a, b) two other QCA full-adders have been introduced (Sayedsalehi et al.,



**Figure 11.** The QCA full-adder schematic presented in (Rahimi et al., 2007).



**Figure 12.** The corresponding layout of the first QCA full-adder.

2010). These full-adders dominate all the previous designs in terms of cell count, area and delay. They use the multilayer wire crossing scheme to crossover wires. However, in these designs in contrast to the previous designs, QCA cells are distributed in the three layers of the circuit. Therefore they have a complex structure and are not so efficient to implement larger QCA circuits.

Subsequently, two QCA full-adders constructed using the new five-input majority gates are presented. In these designs, the input and output signals are not surrounded by the other cells and the outputs (*sum* and *carry* value) come out from the same side of the circuit. The first QCA full-adder (without considering QCA design rules in (Kim et al., 2005, 2007)) has a simple and dense structure and dominates the previous designs (Cho and Swartzlander, 2007, 2009; Cho, 2006; Tougaw and Lent, 1994; Vetteth et al., 2002; Wang et al., 2003; Zhang et al., 2005) in terms of area and complexity (cell count). Also, it has an equal latency with the previous best ones. The proposed robust QCA full-adder surpasses all the previous robust designs (Hänninen and Takala, 2010; Kim et al., 2007) in terms of area, complexity and latency. Using this

component, ripple carry adders with different word sizes (that is, 4, 8 and 16) are constructed. Simulation results demonstrate that these designs, in comparison to the previous robust structures, lead to significant improvements in terms of area, delay and complexity.

### THE NEW QCA FULL-ADDERS

By means of the new five-input majority gates presented in Figure 7a and b, efficient QCA full-adders can easily be implemented. The proposed layouts are slightly different from the basic QCA full-adder schematic presented in Figure 11. In these designs, the multilayer wire crossing scheme is used to crossing wires. The layout of the first design is shown in Figure 12. This full-adder has a simple structure and is constructed using the proposed QCA five-input majority gate presented in Figure 7a. In this design, at first the inversion of the carry value is calculated and then is used as the two inputs of the five-input majority gate. In contrast to the basic design (Figure 11) this value is inverted using a diagonally positioned QCA cell and the final carry value is obtained. The QCA full-adder related logic is presented in Equation (3):

$$\begin{aligned} \text{Sum} &= \text{Maj5}(\text{Carry}', \text{Carry}', A_0, B_0, C_0) \\ \text{Carry} &= \text{Maj3}(A_0, B_0, C_0) \end{aligned} \quad (3)$$

Figure 13 demonstrates the three layers of the proposed QCA full-adder. The first layer (as shown in Figure 13a, is composed of one three-input majority gate, one five-input majority gate and two diagonally positioned cells which act as inverters. As shown in this figure one of these cells inverts the carry value ( $\text{Maj3}(A_0, B_0, C_0)$ ) and the other makes  $C_{out}$ . The inversion of the carry value is used as the two inputs of the five-input majority gate. The second layer (presented in Figure 13b), consists of only four circular-shaped QCA cells for transferring  $A_0$  and carry values. The third layer (Figure 13c) comprises of two crossover wires (X-shape cell lines). These wires are used to complete multilayer crossover scheme in the proposed design. As shown in Figure 12, these lines are used to transfer  $A_0$  and carry values: (a) The first layer; (b) The second layer; (c) The third layer.

The layout of the robust QCA full-adder is shown in Figure 14. As shown in this figure, in the proposed design, the presented QCA design rules for constructing a robust QCA circuit (Figure 5a) have been considered. This design is implemented using the proposed five-input majority gate presented in Figure 7b. In this layout, the carry value is calculated using  $\text{Maj3}(A_0, B_0, C_0)$  and directly is transmitted to the output. Based on Figure 14, it is clear that in the proposed design as same the previous structure (Figure 12),  $A_0$ ,  $B_0$ ,  $C_0$ ,  $\text{Carry}'$  and  $\text{Carry}$  are the five inputs of the five-input majority gate. In this layout in contrast to the basic design (Figure 11) two diagonally positioned cells which act as inverters produce the final sum value. Subsequently, the first QCA cell has been positioned diagonally to maximize the distance between the input and output QCA cells. Simulation results show that this reduces the noise effect. Using the second diagonally positioned QCA cell, the final sum value is transmitted to the output. Figure 15 demonstrates the three layers of the proposed design. The first layer (as shown in Figure 15a) is composed of one three-input majority gate, one five-input majority gate and three diagonally positioned cells which act as inverters. One of these cells makes carry not value ( $\text{Maj3}(A_0, B_0, C_0)$ ) and two other QCA cells are used to produce the sum value. The second layer (presented in Figure 15b)), consists of only four circular-shaped QCA cells for transmitting  $C_0$  and carry values. The third layer (Figure 15c) comprises of two crossover wires (X-shape cell lines). These wires are used to complete multilayer crossover scheme in the proposed

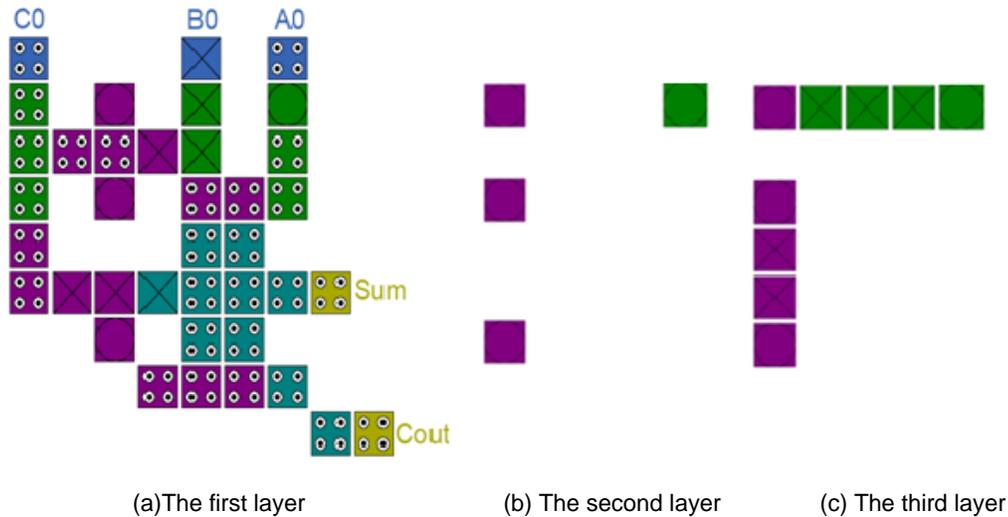


Figure 13. Three different layers of the first QCA full-adder.

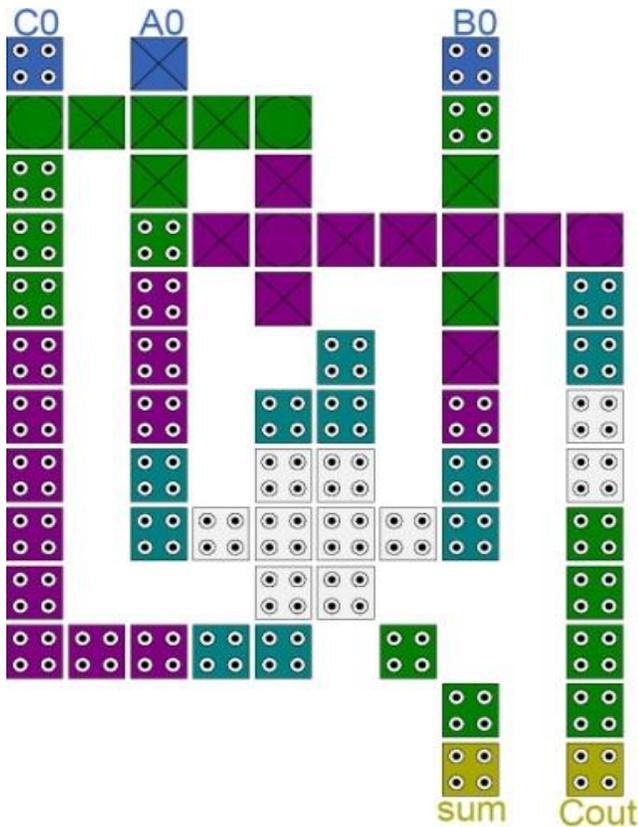


Figure 14. The corresponding layout of the proposed robust QCA full-adder.

design. As shown in Figure 14, these lines are used to transfer  $C_0$  and carry values: (a) The first layer; (b) The second layer; (c) The third layer.

As previously mentioned, in this study QCA circuits are implemented and simulated using QCA Designer (Walus et al., 2004) version 2.0.3. Simulation results show that in a bi-stable

simulation, both of the proposed QCA full-adders produce accurate results. In a coherence vector simulation, the robust design in comparison to the proposed design in Figure 12 has a more reliable operation. The simulation results of the robust QCA full-adder are shown in Figure 16. In these simulations, using the default parameters of both engines (QCA designer Documentation) same results were achieved. As shown in Figure 16, the outputs (presented as  $Sum$  and  $C_{out}$ ) are valid after the second falling edge of the clock0.

Using a QCA full-adder, ripple carry adders with different word sizes can easily be implemented. The layout of a four bit ripple carry adder constructed using the proposed robust QCA full-adder is shown in Figure 17. This structure has been constructed using four QCA full-adders. In this layout, the inputs are shown by  $c_0$ ,  $a_0$ - $a_3$  and  $b_0$ - $b_3$ . The  $s_0$ - $s_3$  and  $carry$  indicate the output values of the proposed design. As shown in this figure, the carry input value of a QCA full-adder is the carry output value of the previous QCA full-adder. Regarding this structure, larger QCA ripple carry adders can easily be implemented. In this study, in addition to the proposed design in Figures 17, 8 and 16 bit ripple carry adders have been constructed and will be used to comparison with the previous best designs in the next section. Due to the lack of space, the layout of the 8 and 16 bit ripple carry adders have not been reported here.

Figure 18 shows the simulation results of the proposed ripple carry adder in Figure 17. It is worth mentioning that in this simulation the default parameters of both engines were used and same results were achieved which show the accuracy of the proposed design. In this figure, the input  $A$  indicates the four inputs  $a_0$ - $a_3$ ,  $B$  indicates the four inputs  $b_0$ - $b_3$  and  $C$  shows the input  $c_0$ . The  $output$  is composed of  $carry$  and  $s_0$ - $s_3$ . The results are valid after the second falling edge of the clock3.

## RESULTS

Using QCA designer, complexity, delay and area consumption of QCA circuits can easily be obtained (Walus et al., 2004). Table 1 demonstrates a detailed comparison between the proposed QCA full-adders and the previous designs (Cho and Swartzlander, 2007, 2009; Cho, 2006; Hänninen and Takala, 2010; Kim et al., 2007;

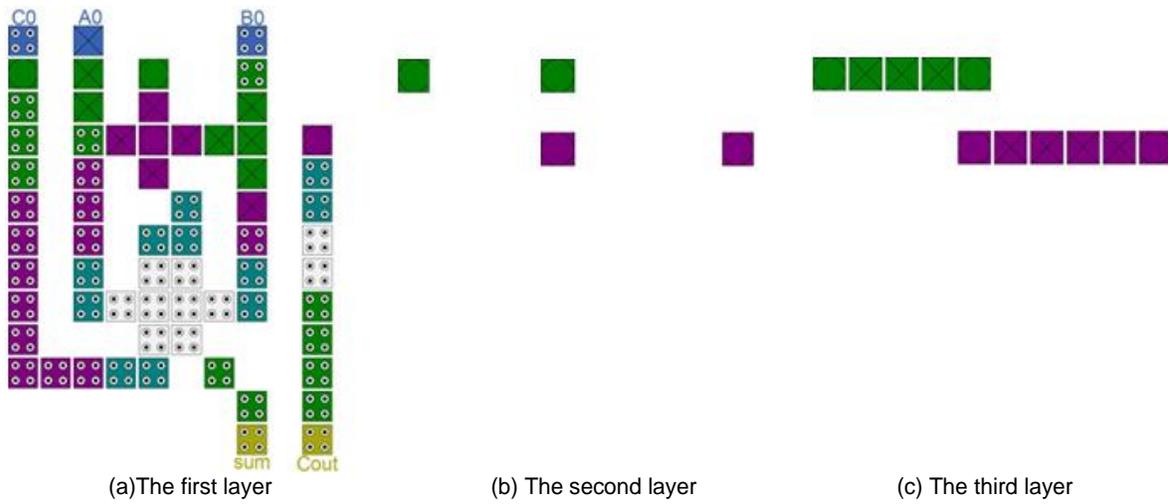


Figure 15. Three different layers of the proposed robust QCA full-adder in Figure 14.

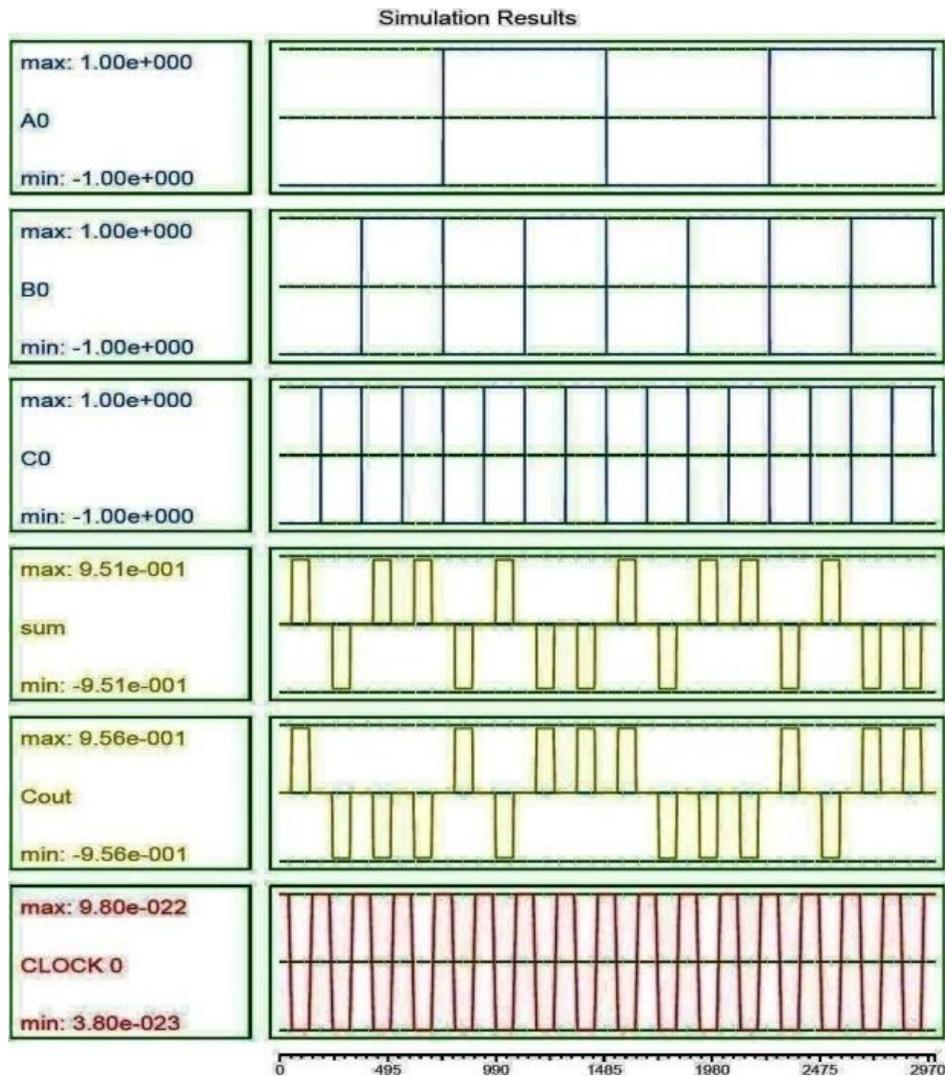


Figure 16. The Simulation results of the proposed full-adder presented in Figure 14.

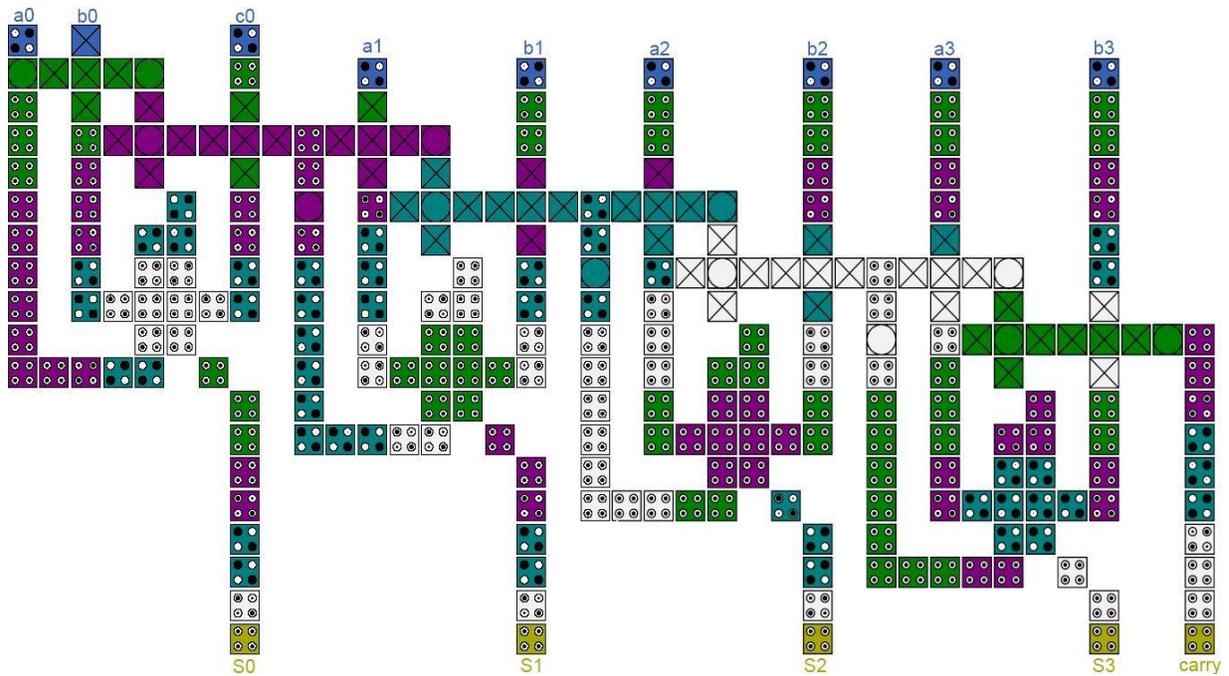


Figure 17. The layout of a four bit ripple carry adder constructed using the proposed robust QCA full-adder in Figure 14.

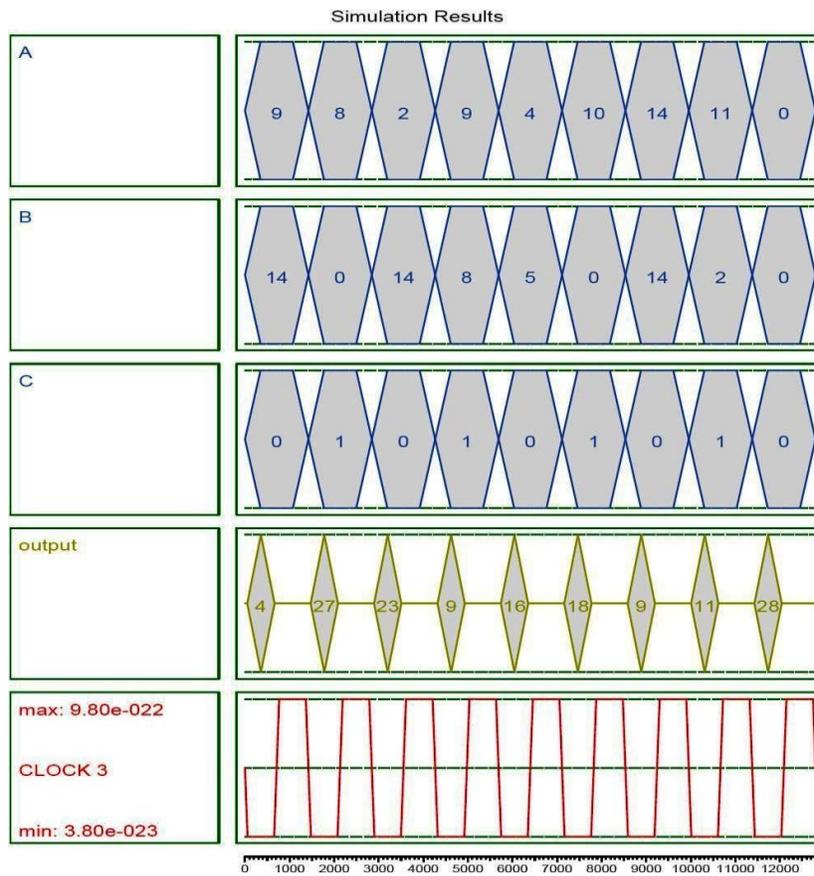


Figure 18. The Simulation results of the proposed four bit ripple carry adder presented in Figure 17.

**Table 1.** Detailed QCA full-adders comparison.

QCA full adder		Complexity (cells)	Area ( $\mu\text{m}^2$ )	Latency (clk cycle)
Non robust QCA full adders	QCA FA of (Tougaw and Lent, 1994)	192	0.20**	NA
	Coplanar QCA FA of (Vetteth et al., 2002)	292	0.62	3.5
	Coplanar QCA FA of (Wang et al., 2003)	145	0.17	1.25
	Multilayer QCA FA of (Zhang et al., 2005)	108	0.10	1
	Multilayer QCA FA of (Cho and Swartzlander, 2007)	135	0.14	1.25
	Type-II FA of (Cho and Swartzlander, 2009; Cho, 2006)	86	0.10	0.75
	Type-I FA of (Cho, 2006)	82	0.09	0.75
Proposed QCA FA in Figure 12	51	0.03	0.75	
Robust QCA full adders	The Robust QCA FA in (Kim et al., 2007)	220	0.36	3
	The Robust QCA FA in (Hänninen and Takala, 2010)	102	0.1	2
	Proposed QCA FA in Figure 14	79	0.05	1.25

\* NA = Not Applicable; \*\* This area is measured based on the prepared scheme in the related article.

**Table 2.** Detailed comparison of the robust ripple carry adders.

QCA ripple carry adders		Complexity (cells)	Area ( $\mu\text{m}^2$ )	Latency (clk cycle)
Ripple carry adders constructed using the presented design in (Hänninen and Takala, 2010)	4 bit	558	0.85	5
	8 bit	1528	2.93	9
	16 bit	4652	10.85	17
Ripple carry adders constructed using the proposed robust QCA full-adder	4 bit	308	0.29	2
	8 bit	695	0.79	3
	16 bit	1759	2.51	5

Tougaw and Lent, 1994; Vetteth et al., 2002; Wang et al., 2003; Zhang et al., 2005) in terms of area, complexity and delay. In this table, QCA full-adders have been divided in two main groups: robust and non robust QCA full-adders. In the robust QCA full-adders, the presented QCA design rules (Kim et al., 2005, 2007) for constructing a robust QCA circuit have been considered. Table 2 presents a detailed comparison between the proposed robust ripple carry adders and the ripple carry adders constructed using the best robust design (Hänninen and Takala, 2010).

## DISCUSSION

As shown in Table 1, the new non robust QCA full-adder (Figure 12) dominates all the previous designs (Cho and Swartzlander, 2007, 2009; Cho, 2006; Tougaw and Lent, 1994; Vetteth et al., 2002; Wang et al., 2003; Zhang et

al., 2005) in terms of area and complexity. It leads to a very dense structure and has an equal latency with the previous best designs. This design leads to around 66.66 percent improvement in area and 37.80 percent improvement in complexity in comparison to the best presented QCA full-adder constructed using three-input majority gates and inverters (Cho, 2006). Also, it is clear that the robust design surpasses all the previous robust QCA full-adders in terms of area, delay and complexity. Based on the proposed results in Table 2, it is clear that the new ripple carry adders lead to significant improvements in terms of area, delay and complexity in comparison to the best previous designs. For example, as shown in this table, the new robust 16 bit ripple carry adder lead to around 62.18, 76.27 and 70.58 percent improvements in terms of complexity, area and delay in comparison to the robust 16 bit ripple carry adder constructed using the presented design in (Hänninen and Takala, 2010).

As mentioned earlier, in the proposed designs in contrast to the previous QCA full-adders presented in (Navi et al., 2010 a, b), the outputs are obtained from the same side of the circuit. In these new designs the input and output signals are not surrounded by the other cells and can easily be accessed. Also in contrast to the presented QCA full-adders in (Sayedsalehi et al., 2010), the QCA cells are not distributed in the three layers of the QCA circuit and the new designs are simpler for implementation. Regarding the suitable position of the input and output signals in the proposed QCA full-adders and comparison results presented in Tables 1 and 2, these designs are useful components in designing QCA based arithmetic circuits.

## CONCLUSION

As mentioned earlier, the QCA technology provides us with an enormous speed and ultra low power consumption. In this paper, two new QCA full-adders using ordinary QCA cells were introduced. These designs have a simple structure and are constructed using two new five-input majority gates. One of the proposed designs has a robust structure. In this layout, presented design rules for constructing robust QCA circuits have been considered. Using this component, ripple carry adders with different word sizes (that is, 4, 8 and 16) are constructed. In the proposed QCA full-adders, in contrast to the previous QCA full-adders constructed, using a five-input majority gate, the input and output signals (*sum* and *carryout*) are not surrounded by the other cells. They come out from the same side of the circuit and can easily be accessed. Simulation results demonstrate that the first QCA full-adder has a very dense structure. It has an equal latency with the best previous designs. The second QCA full-adder (robust design) surpasses all the previous robust designs in terms of area, delay and complexity. Regarding the proposed results, the new designs are suitable components for constructing arithmetic QCA circuits.

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