

## B. Baumeister

### *Do finite Bruck loops behave like groups?*

Comment.Math.Univ.Carolin. 53,3 (2012) 337–346.

**Abstract:** This note contains Sylow's theorem, Lagrange's theorem and Hall's theorem for finite Bruck loops. Moreover, we explore the subloop structure of finite Bruck loops.

**Keywords:** finite loops, finite Bruck loops, finite Bol loops, finite  $A_r$ -loops, classical theorems for finite loops

**AMS Subject Classification:** 20N05, 20B05

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