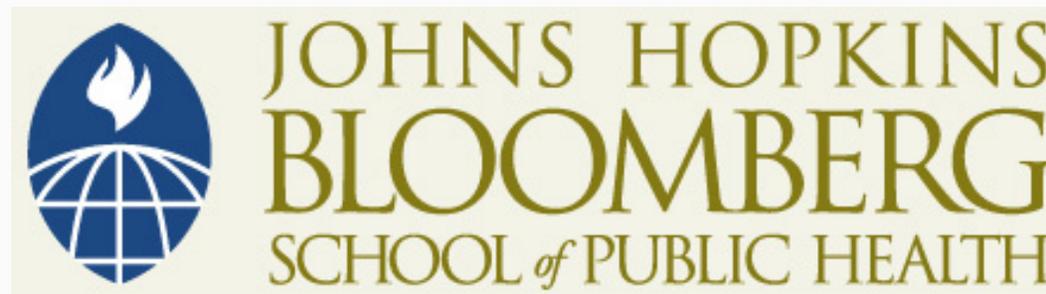


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Section D

Two Sample t-test, Two Choices

FYI: Equal Variances Assumption

- The “traditional” t-test assumes equal variances in the two groups
 - This can be formally tested with another hypothesis test!
 - But why not just compare observed values of s_1 to s_2 ?
- There is a slight modification to allow for unequal variances—this modification adjusts the degrees of freedom for the test, using slightly different SE computation (the formula I give you)
- If you want to be truly “safe” (desert island choice of t-test)
 - More conservative to use test that allows for unequal variance
- Makes little to no difference in large sample

FYI: Equal Variances Assumption

- Actually, the following occurs:
 - If underlying population level standard deviations are equal:
 - ▶ Both approaches give valid confidence intervals but intervals by approach assuming unequal standard deviations slightly wider (and p-values slightly larger)
 - If underlying population level standard deviations are not equal:
 - ▶ The approach assuming equal variances does not give valid confidence intervals and can severely under-cover the goal of 95%

Unequal SD Approach: Diet Type/ Weight Loss Example

- Command syntax:

- `ttesti n_1 \bar{x}_1 s_1 n_2 \bar{x}_2 s_2 , unequal`

```
. ttesti 64 -5.7 8.6 68 -1.8 3.9, unequal
```

Two-sample t test with unequal variances

	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf. Interval]
x	64	-5.7	1.075	8.6	-7.848216 -3.551784
y	68	-1.8	.4729445	3.9	-2.744001 -.8559989
combined	132	-3.690909	.5978226	6.868458	-4.873545 -2.508273
diff		-3.9	1.174437		-6.234436 -1.565564

diff = mean(x) - mean(y) t = -3.3207
Ho: diff = 0 Satterthwaite's degrees of freedom = 86.6941

Ha: diff < 0	Ha: diff != 0	Ha: diff > 0
Pr(T < t) = 0.0007	Pr(T > t) = 0.0013	Pr(T > t) = 0.9993

Equal SD Approach: Diet Type/ Weight Loss Example

- Command syntax:

- `ttesti n_1 \bar{x}_1 s_1 n_2 \bar{x}_2 s_2`

```
. ttesti 64 -5.7 8.6 68 -1.8 3.9
```

Two-sample t test with equal variances

```
-----+-----  
      |      Obs      Mean   Std. Err.   Std. Dev.   [ 95% Conf. Interval]  
-----+-----  
      x |      64      -5.7     1.075     8.6   -7.848216   -3.551784  
      y |      68      -1.8     .4729445     3.9   -2.744001   -.8559989  
-----+-----  
combined |     132   -3.690909   .5978226   6.868458   -4.873545   -2.508273  
-----+-----  
      diff |           -3.9   1.151038           -6.177191   -1.622809  
-----+-----  
      diff = mean(x) - mean(y)                                t = -3.3882  
Ho: diff = 0                                                degrees of freedom = 130  
  
      Ha: diff < 0                Ha: diff != 0                Ha: diff > 0  
Pr(T < t) = 0.0005              Pr(|T| > |t|) = 0.0009              Pr(T > t) = 0.9995
```

Unequal SD Approach: LDL/ Treatment Example

- Command syntax:

- `ttesti n_1 \bar{x}_1 s_1 n_2 \bar{x}_2 s_2 , unequal`

```
. ttesti 11 -1.41 .55 12 -.32 .65, unequal
```

Two-sample t test with unequal variances

	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf. Interval]	
x	11	-1.41	.1658312	.55	-1.779495	-1.040505
y	12	-.32	.1876388	.65	-.7329903	.0929903
combined	23	-.8413043	.1692296	.8115967	-1.192265	-.4903436
diff		-1.09	.2504163		-1.61095	-.5690505

diff = mean(x) - mean(y) t = -4.3528

Ho: diff = 0 Satterthwaite's degrees of freedom = 20.8813

Ha: diff < 0
Pr(T < t) = 0.0001

Ha: diff != 0
Pr(|T| > |t|) = 0.0003

Ha: diff > 0
Pr(T > t) = 0.9999

Equal SD Approach: LDL/Treatment Example

- Command syntax:
 - `ttesti n_1 \bar{x}_1 s_1 n_2 \bar{x}_2 s_2 , unequal`

```
. ttesti 11 -1.41 .55 12 -.32 .65
```

Two-sample t test with equal variances

	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf. Interval]	
x	11	-1.41	.1658312	.55	-1.779495	-1.040505
y	12	-.32	.1876388	.65	-.7329903	.0929903
combined	23	-.8413043	.1692296	.8115967	-1.192265	-.4903436
diff		-1.09	.2523107		-1.614709	-.5652911

```
diff = mean(x) - mean(y)                                t = -4.3201
Ho: diff = 0                                             degrees of freedom = 21
```

```
Ha: diff < 0
Pr(T < t) = 0.0002
```

```
Ha: diff != 0
Pr(|T| > |t|) = 0.0003
```

```
Ha: diff > 0
Pr(T > t) = 0.9998
```